

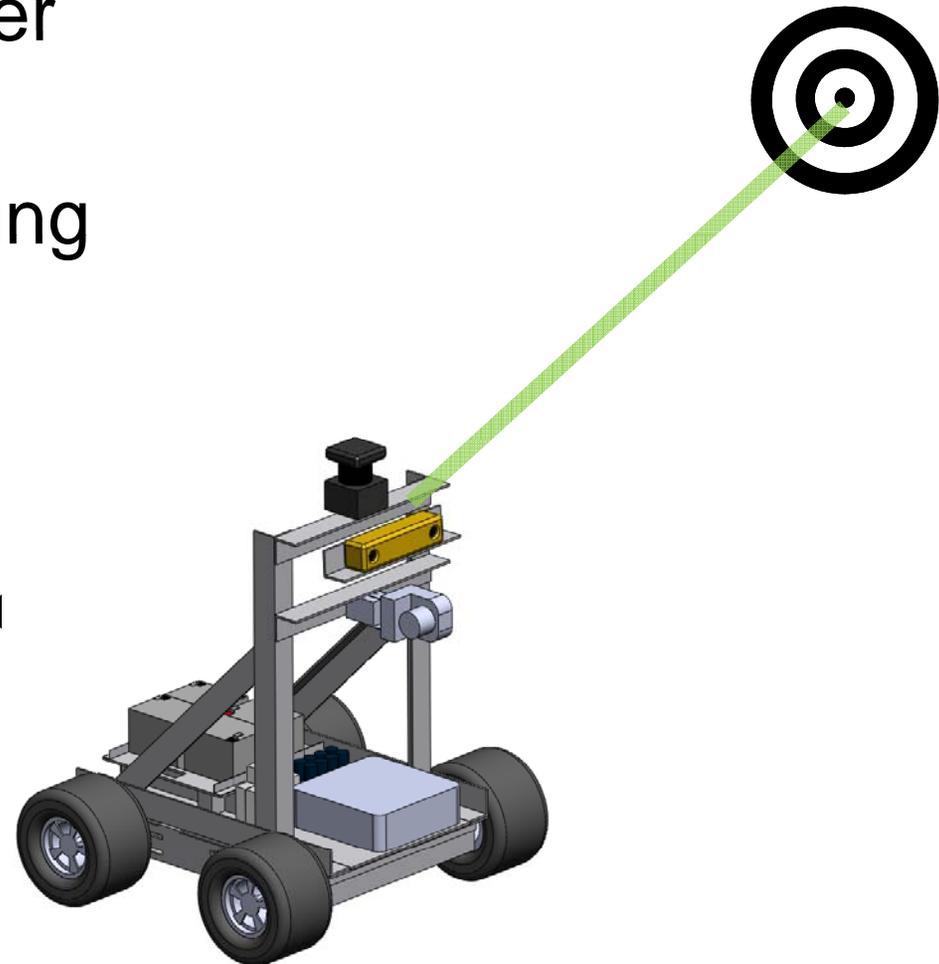
AUTONOMOUS LASER LOCKING SYSTEM

Sunfest 2010
NSF REU program

By Brett Kuprel
Advised by Professor Daniel Lee and Alex Kushleyev

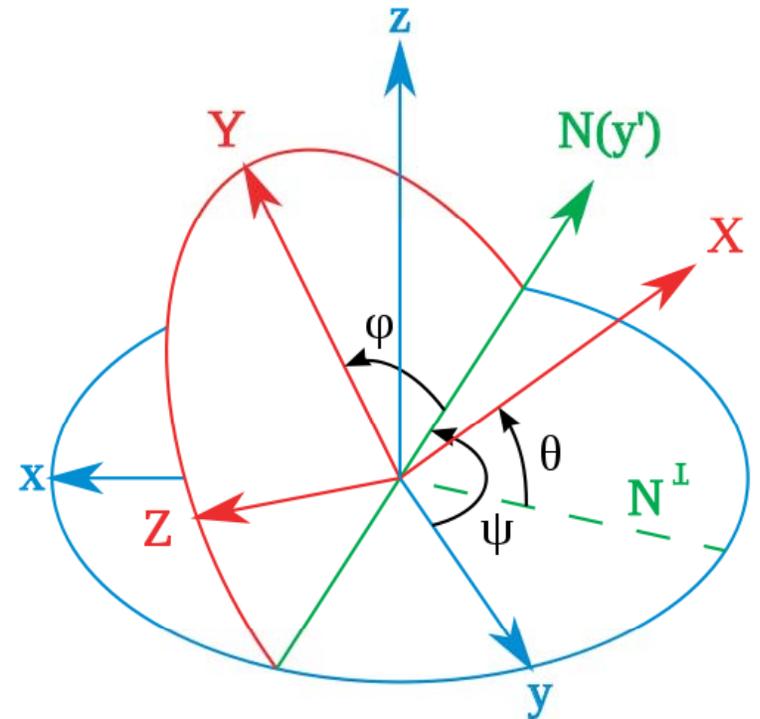
Overview

- Goal is to keep laser pointed at target
- Target can be moving relative to robot
- To be used in the MAGIC 2010 autonomous robotics competition



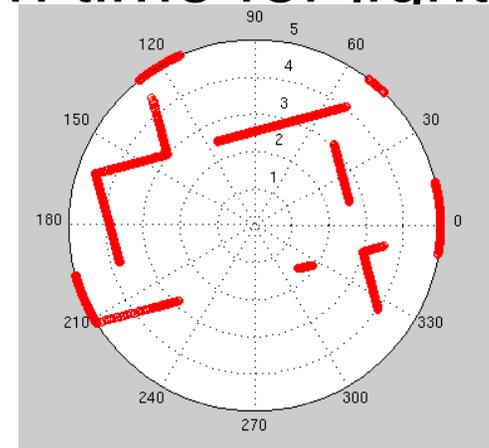
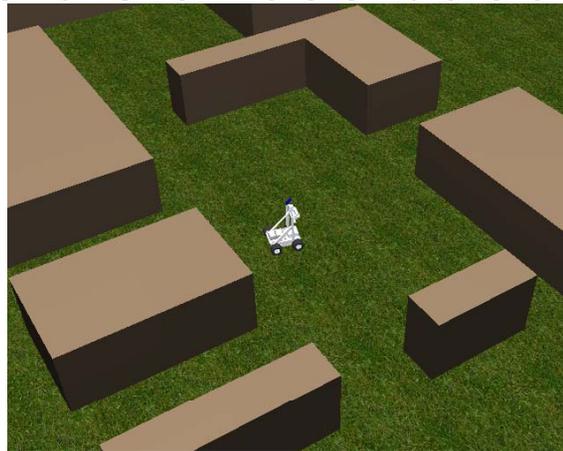
Position and Rotation Estimation

- Required for robot to know where to point laser
- GPS not precise enough, inaccurate around buildings
- Better method is to map the environment with sensors and localize the robot within the map, aka Simultaneous Localization and Mapping (SLAM)
- SLAM analyzes information from LIDAR, gyroscopes, and odometry



LIDAR

- Like RADAR, but different wavelength
- Emits and receives light at 1080 different angles spread over 270 degrees at a rate of 40 Hz
- Calculates distances based on time for light to return



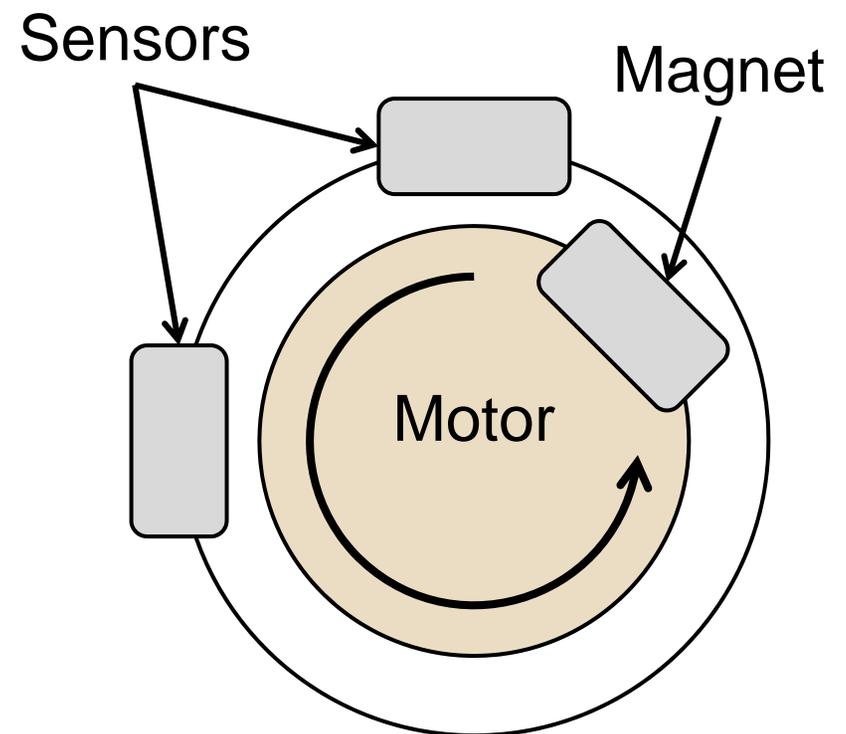
Gyroscopes

- ❑ Measures angular velocity
- ❑ Integrate to get angular displacement
- ❑ $d\theta = \int w dt$
- ❑ 3 required to measure rotation around any axis in space



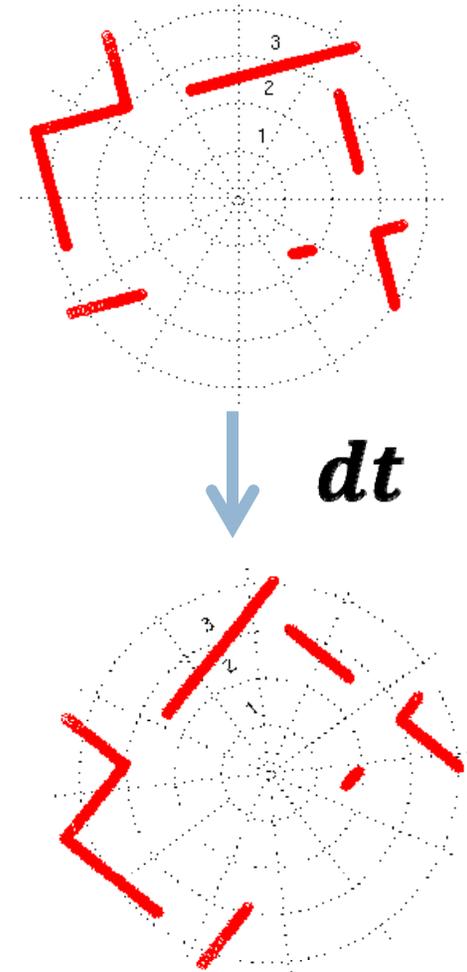
Odometry

- As motor spins, magnets from motor and cage interact causing voltage spikes
- 2 magnets to determine direction (CW or CCW)
- Resulting measurement is angle per time
- When used with wheel radius, distance traveled can be calculated



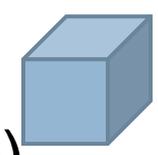
Sensor Synthesis - SLAM

- Together the sensors can be used to create a map of the environment
- Main idea: consecutive lidar maps are pieced together
- Piecing together requires translating and rotating depending on how the robot moved between lidar maps
- Robot motion can be determined by odometry and gyroscopes



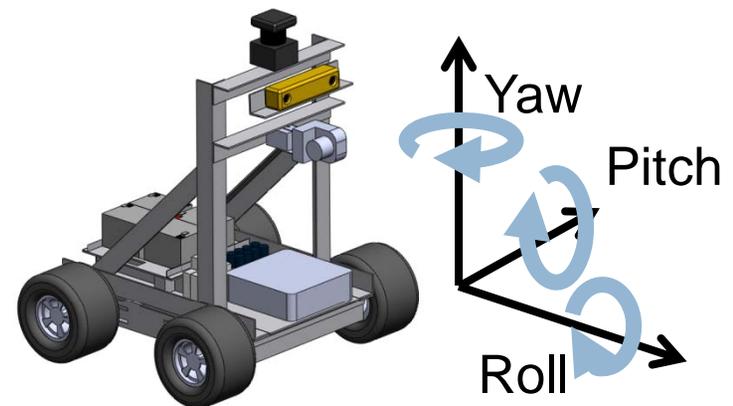
Rotational Freedom

- Position and rotation of robot can be estimated
- Need to be able to point laser at target
- Requires 2 degrees of rotational freedom
 - 0 degrees = line of sight
 - 1 degree = plane of sight (rotated line)
 - 2 degrees = volume of sight (rotated plane)



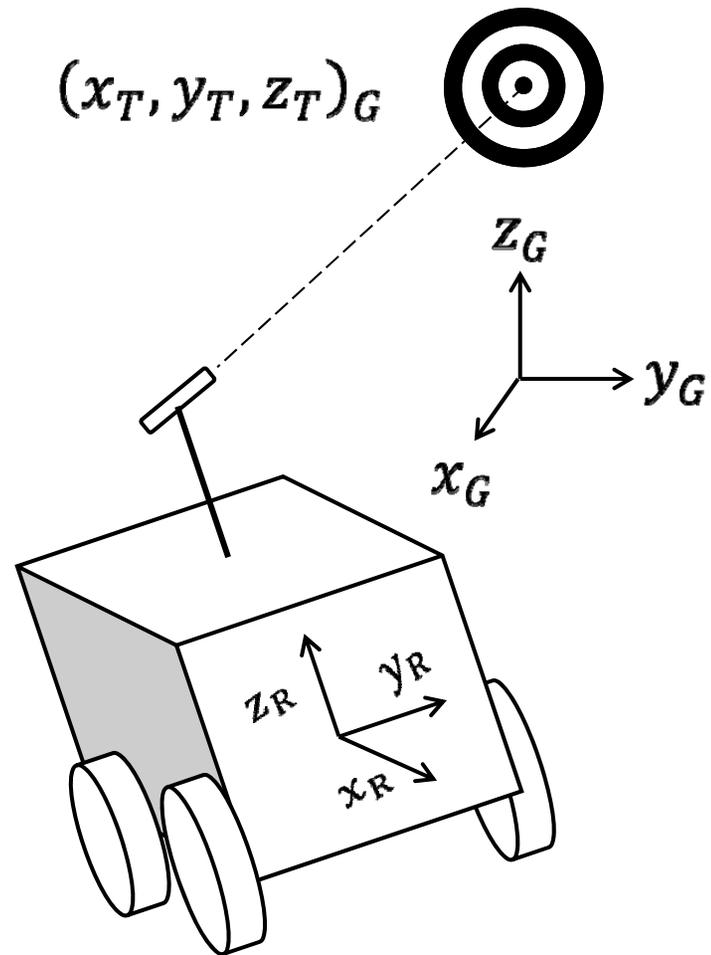
Rotational Freedom

- 2 perpendicular servos
- Each servo has 300 degrees of freedom
- Servos control pitch and yaw
- Resulting field of view is all points in space except a 60 degree pyramid



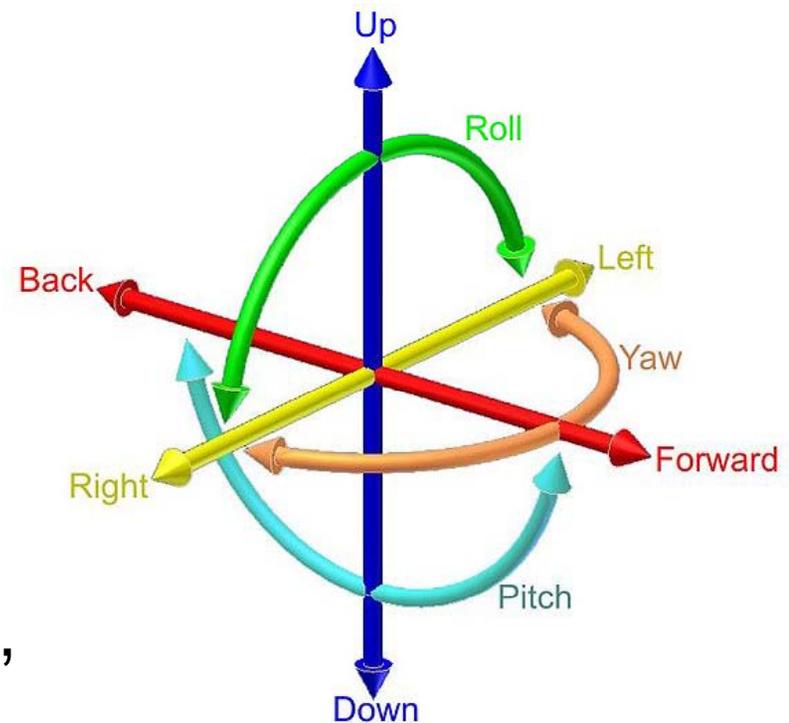
Robot Coordinate System

- Target given in global coordinates
- Use homogenous transformation matrix to convert global coordinates into robot coordinates



Required for Transformation Matrix

- Finding robot coordinates requires robot's position and rotation in 6 degrees of freedom to be known
- 6 degrees of freedom:
 - ▣ Translation in 3 perpendicular axes (eg x, y, z)
 - ▣ Rotation around 3 perpendicular axes (eg roll, pitch, yaw)



Using Transformation Matrix

- Robot coordinates can be found by simply multiplying by transformation matrix
- $(x_T, y_T, z_T)_R = T_{G \rightarrow R} * (x_T, y_T, z_T)_G$

$$\square T_{G \rightarrow R} = \begin{bmatrix} \text{Trans(RobotPosition)} * \dots \\ \text{Rot}_z(\text{yaw}) * \dots \\ \text{Rot}_y(\text{pitch}) * \dots \\ \text{Rot}_x(\text{roll}) * \dots \\ \text{Trans(LaserOffset)} \end{bmatrix}^{-1} = \dots$$

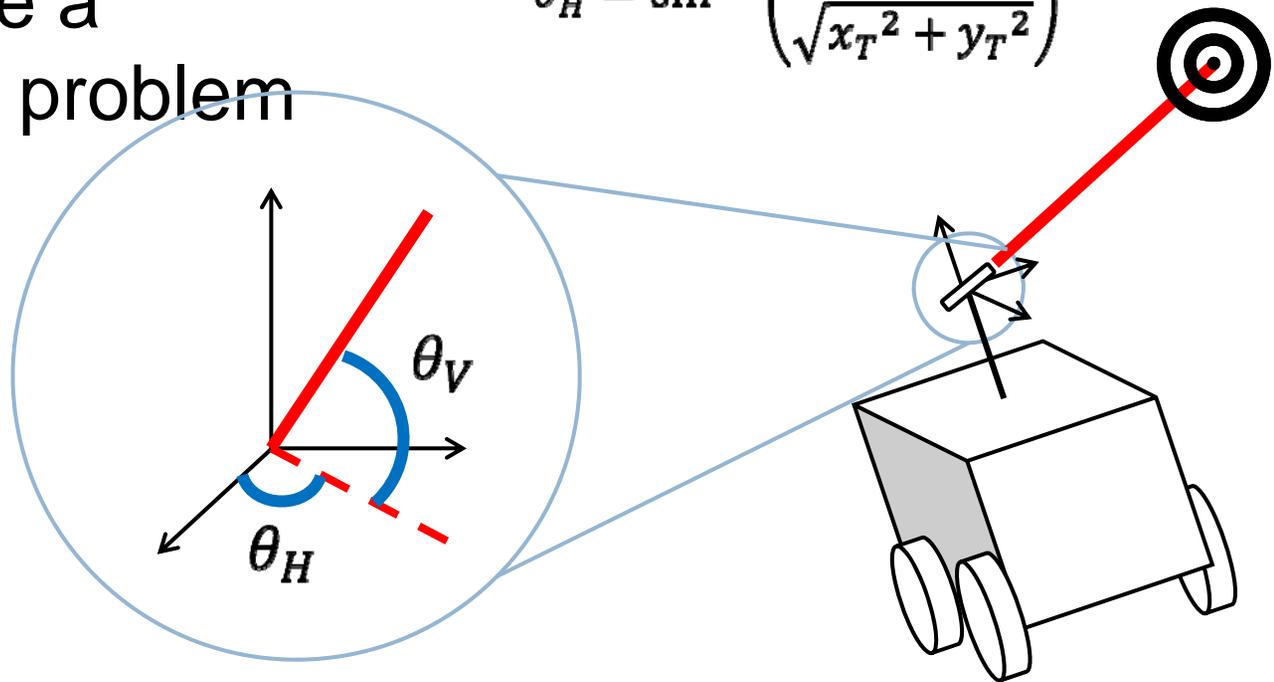
$$\left(\begin{bmatrix} 1 & 0 & 0 & x_R \\ 0 & 1 & 0 & y_R \\ 0 & 0 & 1 & z_R \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} \cos(\text{yaw}) & -\sin(\text{yaw}) & 0 & 0 \\ \sin(\text{yaw}) & \cos(\text{yaw}) & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} \cos(\text{pitch}) & 0 & \sin(\text{pitch}) & 0 \\ 0 & 1 & 0 & 0 \\ -\sin(\text{pitch}) & 0 & \cos(\text{pitch}) & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos(\text{roll}) & -\sin(\text{roll}) & 0 \\ 0 & \sin(\text{roll}) & \cos(\text{roll}) & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & 0 & x_L \\ 0 & 1 & 0 & y_L \\ 0 & 0 & 1 & z_L \\ 0 & 0 & 0 & 1 \end{bmatrix} \right)^{-1}$$

Calculating Angles of Servos

- Once target is known in robot coordinates, servo angles are a geometry problem

$$\theta_V = \sin^{-1} \left(\frac{-z_T}{\sqrt{x_T^2 + y_T^2 + z_T^2}} \right)$$

$$\theta_H = \sin^{-1} \left(\frac{y_T}{\sqrt{x_T^2 + y_T^2}} \right)$$

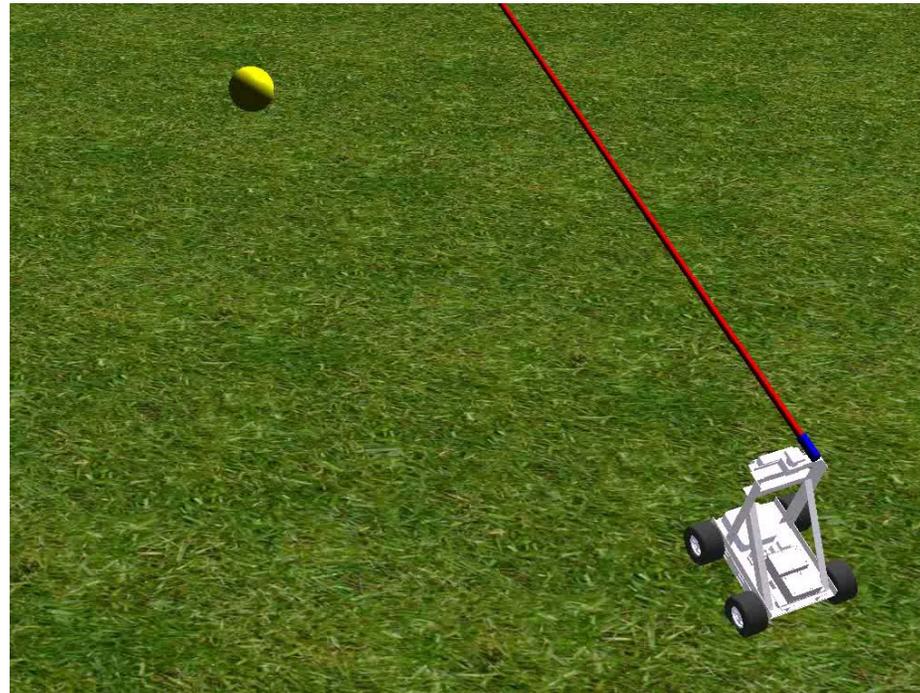


Continuous Servo Motion

- Sending target angle commands at discrete time intervals results in unsteady rotation of the servos
- Solution is to send angular velocity commands instead
- Used a PID controller to determine desired angular velocity
 - ▣ Velocity = sum of proportional, integral, and derivative of error
 - ▣ Error is difference between current angle and desired angle



Simulation



Actual Robot



Acknowledgements



- Professor Daniel Lee
- Alex Kushleyev
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