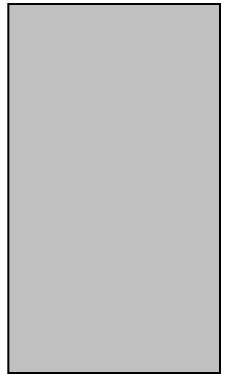


Powers of Two: Trace

Ex. Print powers of 2 that are $\leq 2^N$

- Increment i from 0 to N
- Double v each time

```
int i = 0;
int v = 1;
while (i <= N) {
    System.out.println(i + " " + v);
    i = i + 1;
    v = 2 * v;
}
```



N = 6

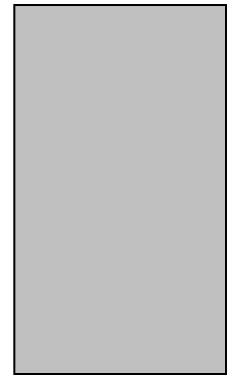
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    v = 2 * v;
}
```

i
0



$N = 6$

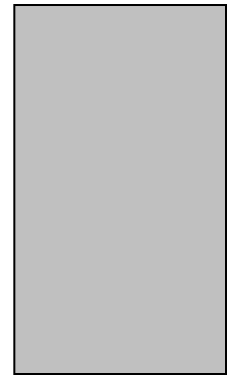
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}
```

i	v
0	1



$N = 6$

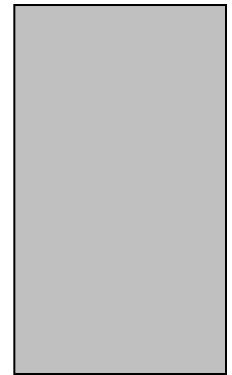
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}
```

i	v	$i \leq N$
0	1	true



$N = 6$

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```

i	v	$i \leq N$
0	1	true

0 1

$N = 6$

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    i = i + 1;
    v = 2 * v;
}
```

i	v	$i \leq N$
0	1	true
1		

0 1

$N = 6$

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    i = i + 1;
    v = 2 * v;
}
```

i	v	$i \leq N$
0	1	true
1	2	

```
0 1
```

$N = 6$

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    v = 2 * v;
}
```

i	v	$i \leq N$
0	1	true
1	2	true

```
0 1
```

$N = 6$

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    i = i + 1;
    v = 2 * v;
}
```

i	v	$i \leq N$
0	1	true
1	2	true

0	1
1	2

$N = 6$

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    System.out.println(i + " " + v);
    i = i + 1;
    v = 2 * v;
}
```

i	v	$i \leq N$
0	1	true
1	2	true
2		

0	1
1	2

$N = 6$

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int i = 0;
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    System.out.println(i + " " + v);
    i = i + 1;
    v = 2 * v;
}
```

i	v	$i \leq N$
0	1	true
1	2	true
2	4	

0	1
1	2

N = 6

Powers of Two: Trace

Ex. Print powers of 2 that are $\leq 2^N$

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- Double v each time

```
int i = 0;
int v = 1;
while (i <= N) {
    System.out.println(i + " " + v);
    i = i + 1;
    v = 2 * v;
}
```

i	v	$i \leq N$
0	1	true
1	2	true
2	4	true

0	1
1	2

$N = 6$

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    i = i + 1;
    v = 2 * v;
}
```

i	v	$i \leq N$
0	1	true
1	2	true
2	4	true

```
0 1
1 2
2 4
```

$N = 6$

Powers of Two: Trace

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    i = i + 1;
    v = 2 * v;
}
```

i	v	$i \leq N$
0	1	true
1	2	true
2	4	true
3		

0	1
1	2
2	4

$N = 6$

Powers of Two: Trace

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    i = i + 1;
    v = 2 * v;
}
```

i	v	$i \leq N$
0	1	true
1	2	true
2	4	true
3	8	

0	1
1	2
2	4

$N = 6$

Powers of Two: Trace

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}
```

i	v	$i \leq N$
0	1	true
1	2	true
2	4	true
3	8	true

0	1
1	2
2	4

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}
```

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0	1	true
1	2	true
2	4	true
3	8	true

```
0 1
1 2
2 4
3 8
```

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}
```

i	v	$i \leq N$
0	1	true
1	2	true
2	4	true
3	8	true
4		

0	1
1	2
2	4
3	8

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    i = i + 1;
    v = 2 * v;
}
```

i	v	$i \leq N$
0	1	true
1	2	true
2	4	true
3	8	true
4	16	

0	1
1	2
2	4
3	8

$N = 6$

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    i = i + 1;
    v = 2 * v;
}
```

i	v	$i \leq N$
0	1	true
1	2	true
2	4	true
3	8	true
4	16	true

```
0 1
1 2
2 4
3 8
```

$N = 6$

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- Double v each time

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    v = 2 * v;
}
```

i	v	$i \leq N$
0	1	true
1	2	true
2	4	true
3	8	true
4	16	true

```
0 1
1 2
2 4
3 8
4 16
```

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    v = 2 * v;
}
```

i	v	$i \leq N$
0	1	true
1	2	true
2	4	true
3	8	true
4	16	true
5		

```
0 1
1 2
2 4
3 8
4 16
```

$N = 6$

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- Double v each time

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    System.out.println(i + " " + v);
    i = i + 1;
    v = 2 * v;
}
```

i	v	$i \leq N$
0	1	true
1	2	true
2	4	true
3	8	true
4	16	true
5	32	

```
0 1
1 2
2 4
3 8
4 16
```

N = 6

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}
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0	1	true
1	2	true
2	4	true
3	8	true
4	16	true
5	32	true

```
0 1
1 2
2 4
3 8
4 16
```

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i	v	$i \leq N$
0	1	true
1	2	true
2	4	true
3	8	true
4	16	true
5	32	true

```
0 1
1 2
2 4
3 8
4 16
5 32
```

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    v = 2 * v;
}
```

i	v	$i \leq N$
0	1	true
1	2	true
2	4	true
3	8	true
4	16	true
5	32	true
6		

0	1
1	2
2	4
3	8
4	16
5	32

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    i = i + 1;
    v = 2 * v;
}
```

i	v	$i \leq N$
0	1	true
1	2	true
2	4	true
3	8	true
4	16	true
5	32	true
6	64	

0	1
1	2
2	4
3	8
4	16
5	32

$N = 6$

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    v = 2 * v;
}
```

i	v	$i \leq N$
0	1	true
1	2	true
2	4	true
3	8	true
4	16	true
5	32	true
6	64	true

```
0 1
1 2
2 4
3 8
4 16
5 32
```

$N = 6$

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i	v	$i \leq N$
0	1	true
1	2	true
2	4	true
3	8	true
4	16	true
5	32	true
6	64	true

0	1
1	2
2	4
3	8
4	16
5	32
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}
```

i	v	$i \leq N$
0	1	true
1	2	true
2	4	true
3	8	true
4	16	true
5	32	true
6	64	true
7		

0	1
1	2
2	4
3	8
4	16
5	32
6	64

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}
```

i	v	$i \leq N$
0	1	true
1	2	true
2	4	true
3	8	true
4	16	true
5	32	true
6	64	true
7	128	

0	1
1	2
2	4
3	8
4	16
5	32
6	64

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    i = i + 1;
    v = 2 * v;
}
```

i	v	$i \leq N$
0	1	true
1	2	true
2	4	true
3	8	true
4	16	true
5	32	true
6	64	true
7	128	false

0	1
1	2
2	4
3	8
4	16
5	32
6	64

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}
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i	v	$i \leq N$
0	1	true
1	2	true
2	4	true
3	8	true
4	16	true
5	32	true
6	64	true
7	128	false

0	1
1	2
2	4
3	8
4	16
5	32
6	64

N = 6