Programming Languages and Techniques

Lecture Notes for CIS 120

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April 23, 2014

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Chapter 1

Overview and Program Design

1.1 Introduction and Prerequisites

CIS 120 is an introductory computer science course taught at the University of Pennsylvania.

Entering students should have some previous exposure to programming and the ability to write small programs (10-100 lines) in some imperative or object-oriented language. Because of CIS 110 and AP Computer Science, the majority of entering students are familiar with Java. However, students with experience in languages such as Python, C, C++, Matlab, or Scheme have taken this course and done well.

In particular, the skills that we look for in entering CIS 120 students are familiarity with the basic *tools* of programming, including editing, compiling and running code, and familiarity with the basic *concepts* of programming languages, such as variables, assignment, conditionals, objects, methods, arrays, and various types of loops.

1.2 Course Philosophy

The core of CIS 120 is *programming*. The skill of writing computer programs is fun, useful and rewarding in its own right. By the end of the semester, students should be able to design and implement—from scratch—sophisticated applications involving graphical user interfaces, nontrivial data structures, mutable state, and complex control. In fact, the

final homework assignment for the course is a playable game, chosen and designed by the student.

More importantly, programming is a conceptual foundation for the study of computation. This course is a prerequisite for almost every other course in the computer science program at Penn, both those that themselves have major programming components and those of a more theoretical nature. The science of computing can be thought of as a modern day version of logic and critical thinking. However, this is a more concrete, more potent form of logic: logic grounded in computation.

Like any other skill, learning to program takes plenty of practice to master. The tools involved—languages, compilers, IDEs, libraries, and frameworks—are large and complex. Furthermore, many of these tools are tuned for the demands of rigorous software engineering, including extensibility, efficiency and security.

The general philosophy for introductory computer science at Penn is to develop programming skills in stages. We start with basic skills of "algorithmic thinking" in our intro CIS 110 course, though students enter Penn already with this ability through exposure to AP Computer Science classes in high school, through summer camps and courses on programming, or independent study. At this stage, students can write short programs, but may have less fluency with putting them together to form larger applications. The first part of CIS 120 continues this process by developing design and analysis skills in the context of larger and more challenging problems. In particular, we teach a systematic process for program design, a rigorous model for thinking about computation, and a rich vocabulary of computational structures. The last stage (the second part of CIS 120 and beyond) is to translate those design skills to the context of industrial-strength tools and design processes.

This philosophy influences our choice of tools. To facilitate practice, we prefer mature platforms that have demonstrated their utility and stability. For the first part of CIS 120, where the goal is to develop design and analysis skills, we use the OCaml programming language. In the second half of the semester, we switch to the Java language. This dual language approach allows us to teach program design in a relatively simple environment, make comparisons between different programming paradigms, and motivate sophisticated features such as objects and classes.

OCaml is the most-widely used dialect of the ML family of languages. Such languages are not new—the first version of ML, was designed by

Robin Milner in the 1970s; the first version of OCaml was released in 1996. The OCaml implementation is a free, open source project developed and maintained by researchers at INRIA, the French national laboratory for computing research. Although OCaml has its origins as a research language, it has also attracted significant attention in industry. For example, Microsoft's F# language is strongly inspired by OCaml and other ML variants. Scala and Haskell, two other strongly typed functional programming languages, also share many common traits with OCaml.

Java is currently one of the most popularly used languages in the software industry and representative of software object-oriented development. It was originally developed by James Gosling and others at Sun Microsystems in the early nineties and first released in 1995. Like OCaml, Java was released as free, open source software and all of the core code is still available for free. Popular languages related to Java include C# and, to a lesser extent, C++.

Goals

There are four main, interdependent goals for CIS 120.

Increased independence in programming While we expect some familiarity with programming, we don't expect entering students to be full-blown programmers. The first goal of 120 is to extend their programming skills, going from the ability to write program that are 10s of lines long to programs that are 1000s of lines long. Furthermore, as the semester progresses, the assignments become less constrained, starting from the application of simple recipes, to independent problem decomposition.

Fluency in program design The ability to write longer programs is founded on the process of program design. We teach necessary skills, such as test-driven development, interface specification, modular decomposition, and multiple programming idioms that extend individual problem solving skills to system development.

Firm grasp of fundamental principles CIS 120 is not just an introductory programming course; it is primarily an introductory computer *science* course. It covers fundamental principles of computing, such as recursion,

lists and trees, interfaces, semantic models, mutable data structures, references, invariants, objects, and types.

Fluency in core Java We aim to provide CIS 120 students with sufficient core skills in a popular programming language to enable further development in a variety of contexts, including: advanced CIS core courses and electives, summer internships, start-up companies, contributions to open-source projects and individual exploration. The Java development environment, including the availability of libraries, tools, communities, and job opportunities, satisfies this requirement. CIS 120 includes enough details about the core Java languages and common libraries for this purpose, though is not an exhaustive overview to Java or object-oriented software engineering. There are many details about the Java language that CIS 120 does not cover; the goal is to provide enough information for future self study.

Why OCaml?

The first half of CIS 120 is taught in the context of the OCaml programming language. In the second half of the semester, we switch to Java for lectures and assignments. If the goal is fluency in core Java, why use OCaml at all? We use OCaml in CIS 120 for several reasons.

"[The OCaml part of the class] was very essential to getting fundamental ideas of comp sci across. Without the second language it is easy to fall into routine and syntax lock where you don't really understand the bigger picture."

—CIS 120 Student

It's not Java. By far, the majority of students entering CIS 120 know only the Java programming language. Different programming languages foster different programming paradigms. Only knowing one language leads to a myopic view of programming, being unable to separate "that is how it is done" from "that is how it is done in Java". By switching languages, we provide perspective about language-independent concepts, introducing other ways of decomposing and expressing computation that are not as well supported by Java.

Furthermore, not all students have this background in Java, nor do they have the same degree of experience. We start with OCaml to level the playing field and give students with alternative backgrounds a chance to develop sophistication in programming and review the syntax of Java on their own. (For those that need more assistance with the basics, we offer CIS 110.)

Finally, learning a new programming language to competence in six weeks builds confidence. A student's first language is difficult, because it involves learning the concepts of programming at the same time. The second comes much easier, once the basic concepts are in place, and the second is understood more deeply because the first provides a point of reference.

Rich, orthogonal vocabulary.

We specifically choose OCaml as an alternative language because of several properties of the language itself. The OCaml language provides features of Java that native features for many of the topics that we would like to study: including lists and tree-like data structures, interfaces, and first-class computation. These features can be can be studied in isolation as there are few abstractions and intricate interactions with the rest of the language.

Functional programming. OCaml is a functional programming language, programmer."—CIS which encourages the use of "persistent" (immutable) data structures. In 120 Student contrast, every data structure in Java is mutable by default. Although CIS 120 is not a functional programming course, we find that the study of persistent data structures is a useful introduction to programming. In particular, persistence leads to a simpler, more mathematical programming model. Programs can be thought of in terms of "transformations" of data instead of "modifications," leading to simpler, more explicit interfaces.

How the different parts of CIS 120 fit to-1.3 gether

Homework assignments provide the core learning experience for CIS 120. Programming is a skill, one that is developed through practice. The homework assignments themselves include both "etudes", which cover basic concepts directly and "applications" which develop those concepts in the context of a larger purpose. The homework assignments take time.

"[OCaml] made me better understand seemed innate to programming, which were merely assumptions that Java made. It made me a better Iava

Lectures Lectures serve many roles: they *introduce*, *motivate* and *contextualize* concepts, they *demonstrate* code development, they *personalize* learning, and *moderate* the speed of information acquisition.

To augment your learning, we make lecture slides, demonstration code and lecture notes available on the course website. Given the availability of these resources, why come to class at all?

- To see code development in action. Many lectures include live demonstrations of code design, and only the resulting code is posted on the website. That means the thought process of code development is lost: your instructors will show some typical wrong turns, discuss various design trade-offs and demonstrate debugging strategies. Things will not always go according to plan, and observing what to do when this happens is also a valuable lesson.
- To interact with the new material as it is presented, by asking questions. Sometimes asking a question right at the beginning can save a lot of later confusion. Also to hear the questions that your classmates have about the new material. Sometimes it is difficult to realize that you don't fully understand something until someone else raises a subtle point.
- To regulate the timing of information flow for difficult concepts. Sure, you can read the lecture notes in less than fifty minutes. However, sometimes slowing down, working through examples, and thinking deeply is required to internalize a topic. You may have more patience for this during lecture than while reading lecture notes on your own.
- For completeness. We cannot promise to include everything in the lectures in the lecture notes. Instructors are only human, with limited time to prepare lecture notes, particularly at the end of the semester.

Labs The labs (or "recitations") provide a small-group setting for coding practice and individual attention from the course staff.

The lab grade comes primarily from lab participation. The reason is that the lab is there to get you to write code in a low-stress environment. In this environment, we use pair programming, teaming you up with your classmates to find the solutions to the lab problems together. The purpose

of the teams is not to divide the work—in fact, we expect that in many cases it will take longer to complete the lab work using a team than by doing it yourself! The benefit of team work lies in discussing the entire exercise with your partner—often you will find that you and your partner have different ideas about how to solve the problem and find different aspects difficult.

Furthermore, labs are another avenue for coding practice, adding to the quantity of code that you write during the semester. The following parable illustrates the value of this:

The ceramics teacher announced he was dividing his class into two groups. All those on the left side of the studio would be graded solely on the quantity of work they produced, all those on the right graded solely on its quality.

His procedure was simple: on the final day of class he would weigh the work of the quantity group: 50 pounds of pots rated an A, 40 pounds a B, and so on. Those being graded on quality, however, needed to produce only one pot — albeit a perfect one — to get an A.

Well, come grading time and a curious fact emerged: the works of highest quality were all produced by the group being graded for quantity!

It seems that while the quantity group was busily churning out piles of work — and learning from their mistakes — the quality group had sat theorizing about perfection, and in the end had little more to show for their efforts than grandiose theories and a pile of dead clay.

David Bayles and Ted Orland, from "Art and Fear" [1].

Exams The exams provide the fundamental assessment of course concepts, including both knowledge and application. Some students have difficulty seeing how pencil-and-paper problems relate to writing computer programs. Indeed, when completing homework assignments, powerful tools such as IDEs, type checkers, compilers, top-levels, and online documentation are available. None of these may be used in exams. Rather, the purpose of exams is to assess both your understanding of these tools and, more importantly, the way you *think* about programming problems.

1.4 Course History

The CIS 120 course material, including slides, lectures, exams, examples, homeworks and labs were all developed by faculty members at the University of Pennsylvania, including Steve Zdancewic, Benjamin Pierce, Stephanie Weirich, Fernando Pereira, and Mitch Marcus. From Fall 2002 to Fall 2010, the course was taught primarily using the Java programming language, with excursions into Python. In Fall 2010, the course instructors radically revised the material in an experimental section, introducing the OCaml language as a precursor to Java. Spring 2011, the dual-language course has been used for all CIS 120 students. In some ways, the use of OCaml as an introductory language can be seen as CIS 120 "returning to its roots." In the 1990s the course was taught only in functional languages: a mix of OCaml and Scheme. The last major revision of the course replaced these wholesale with Java. Joel Spolsky lamented this switch in a 2005 blog post entitled "The Perils of JavaSchools", available at http://www.joelonsoftware.com/ articles/ThePerilsofJavaSchools.html.

1.5 Program Design

Program design is the *process* of translating informal specifications ("word problems") into running code. Learning how to design programs involves decomposing problems into a set of simpler steps.¹

The program design recipe comprises four steps:

- 1. **Understand the problem.** What are the relevant concepts in the informal description? How do the concepts relate to each other?
- 2. **Formalize the interface.** How should the program interact with its environment? What types of input does it require? Why type of output should it produce? What additional information does it need? What properties about its input may it assume? What is true about the result?

¹The material in this section is adapted from the excellent introductory textbook, *How to Design Programs* [3].

- 3. **Write test cases.** How does the program behave on typical inputs? On unusual inputs? On erroneous ones?
- 4. **Implement the required behavior.** Only after the first three steps have been addressed is it time to write code. Often, the implementation will require decomposing the problem into simpler ones and applying the design recipe again.

We will demonstrate this process by considering the following design problem:

Imagine an owner of a movie theater who wants to know how much he should charge for tickets. The more he charges, the fewer people can afford tickets. After some experiments, the owner has determined a precise relationship between the price of a ticket and average attendance. At a price of \$5.00 per ticket, 120 people attend a performance. Decreasing the price by a dime (\$.10) increases attendance by 15. However, the increased attendance also comes at an increased cost: Each attendee costs another four cents (\$0.04), on top of the fixed per-performance cost of \$180. The owner would like to be able to calculate, for any given ticket price, exactly how much profit he will make.

We will develop a solution to this problem by following the design recipe in the context of the OCaml programming language. In the process, we'll introduce OCaml by example. In the next chapter, we give a more systematic overview of its syntax and semantics.

Step 1: Understand the problem. In the scenario above, there are five relevant concepts: the ticket *price*, (number of) *attendees, revenue, cost* and *profit*. Among these entities, we can define several relationships.

From basic economics we know the basic relationships between profit, cost and revenue. In other words, we have

$$profit = revenue - cost$$

and

$$revenue = price \times attendees$$

Also, the scenario tells us how to compute the cost of a performance

```
cost = \$180 + attendees \times \$0.04
```

but does not directly specify how the ticket price determines the number of attendees. However, because revenue and cost (and profit, indirectly) depend on the number of attendees, they are also determined by the ticket price.

Our goal is to determine the precise relationship between ticket price and profit. In programming terms, we would like to define a *function* that, given the ticket price, calculates the expected profit.

Step 2: Formalize the Interface. Most of the relevant concepts—cost, ticket price, revenue and profit—are dollar amounts. That raises a design choice about how to represent *money*. Like most programming languages, OCaml can calculate with integer and floating point values, and both are attractive for this problem, as we need to represent fractional dollars. However, the binary representation of floating point values makes it a poor choice for money, since some numeric values—such as 0.1—cannot be represented exactly, leading to rounding errors. (This "feature" is not unique to OCaml—try calculating 0.1 + 0.1 + 0.1 in your favorite programming language.) So let's represent money in cents and use integer arithmetic for calculations.

Our goal is to define a function that computes the profit given the ticket price, so let us begin by writing down a skeleton for this function—let's call it profit—and noting that it takes a single input, called price. Note that the first line of this definition uses type annotations to enforce that the input and and output of the function are both integers.²

```
let profit (price:int) : int =
...
```

Step 3: Write test cases. The next step is to write test cases. Writing test cases *before* writing any of the interesting code—the fundamental rule of

²OCaml will let you omit these type annotations, but including them is mandatory for CIS120. Using type annotations is good documentation; they also improve the error messages you get from the compiler. When you get a type error message, the first thing you should do is check that your type annotations correct.

test-driven program development—has several benefits. First, it ensures that you understand the problem—if you cannot determine the answer for one specific case, you will find it difficult to solve the more general problem. Thinking about tests also influences the code that you will write later. In particular, thinking about the behavior of the program on a range of inputs will help ensure that the implementation does the right thing for each of them. Finally having test cases around is a way of "futureproofing" your code. It allows you to make changes to the code later and automatically check that they have not broken the existing functionality.

In the situation at hand, the informal specification suggests a couple of specific test cases: when the ticket price is either \$5.00 or \$4.90 (and the number of attendees is accordingly either 120 or 135). We can use OCaml itself to help compute what the expected values of these test cases should be.

The OCaml let-expression gives a name to values that we compute, and we can use these values to compute others with the let-in expression form.

Using these, we can write the test cases themselves:

```
let test () : bool =
    (profit 500) = profit_500
;; run_test "profit at $5.00" test

let test () : bool =
    (profit 490) = profit_490
;; run_test "profit at $4.90" test
```

The predefined function test (provided by the Assert module) takes

no input and returns the boolean value **true** only when the test succeeds.³ We then invoke the command run_test to execute each test case and give it a name, which is used to report failures in the printed output; if the test succeeds, nothing is printed. After invoking the first test case, we can define the test function to check the profit function's behavior at a different price point.

Step 4: Implement the behavior. The last step is to complete the implementation. First, the profit that will be earned for a given ticket price is the revenue minus the number of attendees. Since both revenue and attendees vary with to ticket price, we can define these as functions too.

```
let revenue (price:int) : int =
    ...

let cost (price:int) : int =
    ...

let profit (price:int) : int =
    (revenue price) - (cost price)
```

Next, we can fill these in, in terms of another function attendees that we will write in a minute.

```
let attendees (price:int) : int =
    ...

let revenue (price:int) : int =
    price * (attendees price)

let cost (price:int) : int =
    18000 + 4 * (attendees price)
```

For attendees, we can apply the design recipe again. We have the same concepts as before, and the interface for attendees is determined by the code above. Furthermore, we can define the test cases for attendees from the problem statement.

³Note that single =, compares two values for equality in OCaml.

To finish implementing attendees, we make the assumption that there is a linear relationship between the ticket price and the number of attendees. We can graph this relationship by drawing a line given the two points specified by the test cases in the problem statement.



We can determine what the function should be with a little high-school algebra. The equation for a line

$$y = mx + b$$

says that the number of attendees y, is equal to the slope of the line m, times the ticket price y, plus some constant value b. Furthermore, we can determine the slope of a line given two points:

$$m = \frac{\textit{difference in attendance}}{\textit{difference in price}} = \frac{-15}{10}$$

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Once we know the slope, we can determine the constant b by solving the equation for the line for b and plugging in the numbers from either test case. Therefore $b = 120 - (-15/10) \times 500 = 870$.

Putting these values together gives us a mathematical formula specifying attendees in terms of the ticket price.

```
attendees = (-15/10) \times price + 870
```

Translating that math into OCaml nearly completes the program design.

```
let attendees (price : int) : int =
  (-15 / 10) * price + 870
```

Unfortunately, this code is not quite correct (as suggested by the pink background). Fortunately, however, our tests detect the issue, failing when we try to run the program and giving us a chance to think a little more carefully.

The problem turns out to be our choice of integer arithmetic. Dividing the integer -15 by the integer 10 produces the integer 1, rather than the exact answer 1.5. If, instead, we multiply by the price before dividing we retain the precision needed for the problem.

```
let attendees (price : int) : int =
  (-15 * price) / 10 + 870
```

Finally, note that there are other ways to implement profit that return the correct answer and pass all of the tests, but that are inferior to the one we wrote. For example, we could have written:

```
let profit (price:int) : int =
  price * (-15 * price / 10 + 870) -
  (18000 + 4 * (-15 * price / 10 + 870))
```

However, this program hides the structure and concepts of the problem. It duplicates sub-computations that could be shared, and it does not record the thought process behind the calculation.

Of course, for such a simple problem, this four-step design methodology may seem like overkill. During the course, we'll use it to attack much larger and more complex design problems, where its benefits will be clearer.

Chapter 2

Introductory OCaml

2.1 OCaml in CIS 120

OCaml is a rich and expressive programming language, but, for the purposes of CIS 120, we need only a very minimal subset of its features. Moreover, we use OCaml in a very stylized way that is designed to make using it as simple as possible and reduce the kinds of errors that students might encounter while writing their first programs.

These notes summarize the OCaml features that are needed in the first few homework assignments for CIS 120. As the course progresses, we will explain more concepts and the associated syntax, *etc.*, as needed.

Note: Our intention is that these notes should be self contained: It should not be necessary to use any OCaml features not described here when completing the CIS 120 homework projects. If we've missed something, or if you find any of the explanations confusing, please post a question to the class discussion web site.

2.2 Primitive Types and Expressions

In programming, a *type* describes the structure of some form of data and specifies a collection of operations for manipulating and computing with data of this form.

OCaml, like any programming language, supports various *primitive* data types like integers, booleans, and strings, all of which are built into the language. Each of these primitive data types supports some specific

```
Integers:
                                             constants
                    \dots -2, -1, 0, 1, 2, \dots
             int
                                             addition
                    1 + 2
                    1 - 2
                                             subtraction
                    2 * 3
                                             multiplication
                    10 / 3
                                             integer division
                                             modulus (remainder)
                    10 mod 3
                    string_of_int 3
                                             convert int 3 to string "3"
Booleans: bool
                    true, false
                                             constants
                                             logical negation
                    not true
                    true && false
                                             and (conjunction)
                                             or (disjunction)
                    true || false
 Strings: string
                                             constants
                    "hello", "CIS 120",...
                    "\n"
                                             newline
                    "hello"^"world\n"
                                             concatenation (carat)
Generic comparisons (producing a bool):
                                             equality
                                             inequality
                    <>
                                             less-than
                                             less-than-or-equals
                    <=
                                             greater-than
                    >
                                             greater-than-or-equals
```

Figure 2.1: OCaml primitive data types and some operations on them.

operations; there are also a few generic operations that work on data of any type. Figure 2.1 gives a summary of a few basic OCaml types, some example constants of those types, and some of their operations.

Given these operations and constants, we can build more complex *expressions*, which are the basic unit of OCaml programs. For example, here are some simple expressions:

```
3 + 5
2 * (5 + 10)
"hello" ^ "world\n"
false && (true || false)
not ((string_of_int 42) = "forty two")
```

Parentheses are used to group expressions according to the usual laws of precedence. Note that different groupings may have different meanings (just as in math):

```
3 + (2 * 7) <> (3 + 2) * 7
```

2.3 Value-oriented programming

The way we run an OCaml program is to calculate it to a *value*, which is just the result of a computation. All of the constants of the primitive data types like 3, "hello", true, etc., are values.

We write $\langle exp \rangle \Longrightarrow \langle val \rangle'$ to mean that the expression $\langle exp \rangle$ computes to the value $\langle val \rangle$.

Note: The symbol '⇒' is not part of OCaml's syntax; it is notation that we use to talk about the OCaml language.

For example:

The value of an expression is computed by calculating. For values, there is no more calculation left to do—they are done. For expressions built out of operations, we first calculate the values of the subexpressions and then apply the operation to those results.

The operations on the primitive types int, string, and bool do the "expected thing" in one step of calculation, which we indicate by using the notation ' \longrightarrow '. We can then calculate via a series of steps like so:

```
(2 + 3) * (5 - 2)
\mapsto 5 * (5 - 2) \qquad because 2 + 3 \mapsto 5
\mapsto 5 * 3 \qquad because 5 - 2 \mapsto 3
\mapsto 15
```

We write $(2 + 3) * (5 - 2) \Longrightarrow 15$ when the expression calculates to a value in an arbitrary number of steps.

Here is another example, this time using boolean values:

if-then-else

OCaml's if-then-else construct provides a useful way to choose between two different result values based on a boolean condition. Importantly, OCaml's if is itself an expression, which means that parentheses can be used to group them just like any other expression. Here are some simple examples of conditional expressions:

```
if true then 3 else 4
(if 3 > 4 then 100 else 0) + 17
```

Because OCaml is value oriented, the way to think about if is that it chooses one of two expression to evaluate. We run an if expression by first running the boolean test expression (which must evaluate to either true or false). The value computed by the whole if-then-else is then either the

value of the then branch or the value of the else branch, depending on whether the test was true or false.

For example, we have:

```
(if (3 > 4) then 5 + 1 else 6 + 2) + 17

\mapsto (if false then 5 + 1 else 6 + 2) + 17

\mapsto (6 + 2) + 17

because the test was false

\mapsto 8 + 17

\mapsto 25
```

Note: Unlike C and Java, in which if is a statement form rather than an expression form, it does not make sense in OCaml to leave off the else clause of an if expression. (What would such an expression evaluate to in the case that the test was false?) Moreover, since either of the expressions in the branches of the if might be selected, they must both be of the same type.

Here are some erroneous uses of if:

Note that because **if-then-else** is an expression form, multiple **if-then-else**s can be nested together to create a "cascading" conditional:

```
if (3 > 4) then "abc"
else if (5 > 4) then "def"
else if (7 > 6) then "ghi"
else "klm"
```

This expression evaluates to "def".

2.4 let declarations

A complete OCaml program consists of a sequence of top-level *declarations* and *commands*. Declarations define constants and functions; commands (described in §2.9) are used to generate output and test the behavior of those functions.

Constant declarations use the **let** keyword to *name* the result of an expression.

```
let x = 3
```

This declaration *binds* the identifier \times to the number 3. The name \times is then available for use in the rest of the program. Informally, we sometimes call these identifiers "variables," but this usage is a bit confusing because, in languages like Java and C, a variable is something that can be modified over the course of a program. In OCaml, like in mathematics, once a variables value is determined, it can never be modified... As a reminder of this difference, for the purposes of OCaml we'll try to use the word "identifier" when talking about the name bound by a **let**.

A slightly more complex example is:

```
let y = 3 + 5 * 2
```

When this program is run, the identifier y will be bound to the result of evaluating the expression 3 + 5 * 2. Since $3 + 5 * 2 \implies 13$ we have:

```
let y = 3 + 5 * 2 \implies let y = 13
```

The general form of a **let** declaration is:

let
$$\langle id \rangle = \langle exp \rangle$$

If desired, **let** declarations can also be annotated with the type of the expression. This type annotation provides documentation about the identifier, but can be inferred by the compiler if it is absent.

let
$$\langle id \rangle$$
 : $\langle type \rangle = \langle exp \rangle$

To run a sequence of **let** declarations, you evaluate the first expression and then *substitute* the resulting value for the identifier in the subsequent declarations. Substitution just means to replace the occurrences of the identifier with the value. For example, consider:

```
let x = 3 + 2
let y = x + x
let z = x + y + 4
```

We first calculate 3 + 2 \Longrightarrow 5 and then substitute 5 for x in the rest of the program:

```
let x = 5
let y = 5 + 5
let z = 5 + y + 4
```

We then proceed with evaluating the next declaration (5 + 5 \Longrightarrow 10) so we have:

```
let x = 5
let y = 10
let z = 5 + 10 + 4
```

And finally, $5 + 10 + 4 \Longrightarrow 19$, which leads to the final "fully simplified" program:

```
let x = 5
let y = 10
let z = 19
```

Shadowing

What happens if we have two declarations binding the same identifier, as in the following example?

```
let x = 5
let x = 17
```

The right way to think about this is that there are unrelated declarations for two identifiers that both happened to be called \times . In particular, we don't substitute the value 5 for the second \times above—the let declaration needs an *identifier* and 5 is not an identifier. We say that \times is *bound* by a let, and we do not substitute for such binding occurrences.

Now consider how to run this example:

```
let x = 5
let y = x + 1
let x = 17
let z = x + 1
```

The occurrence of \times in the definition of z refers to the one bound to 17. In OCaml identifiers refer to the *nearest enclosing declaration*. In these examples the second occurrence of the identifier \times is said to *shadow* the first occurrence—subsequent uses of \times will find the second binding, not the first. So the values computed by running this sequence of declarations is:

Since identifiers are just names for expressions, we can make the fact that the two \times 's are independent by consistently renaming the latter one, for example:

```
let x = 5
let y = x + 1
let x2 = 17
let z = x2 + 1
```

Then there is no possibility of ambiguity.

Note: Identifiers in OCaml are not like variables in C or Java. In particular, once a value has been bound to a an identifier using **let**, the association between the name and the value never changes. There is no possibility of changing a variable once it is bound, although, as we saw above, one can introduce a new identifier whose definition shadows the old one. Identifiers are more like variables in math—they are placeholders for which values can be "plugged in."

2.5 Local 1et declarations

So far we have seen that let can be used to introduce a top-level binding for an identifier. In OCaml, we can use let as an expression by following it with the in keyword. Consider this simple example:

```
let x = 3 in x + 1
```

Unlike the top-level **let** declarations we saw above, this is a *local* declaration. To run it, we first see that $3 \Longrightarrow 3$ and then we substitute 3 for x in the expression following the **in** keyword. Since this is a local use of x, we don't keep around the **let**. Thus we have:

```
let x = 3 in x + 1 \Longrightarrow 4
```

More generally, the syntax for local lets is:

```
\mathbf{let} \ \langle id \rangle : \langle type \rangle = \langle exp \rangle \ \mathbf{in} \ \langle exp \rangle
```

Here, the identifier bound by the let is in available only in the expression after the in keyword—when we run the whole thing, we substitute for the identifier only there (and not elsewhere in the program). The identifier x is said to be in scope in the expression after in.

Since the let-in form is itself an expression, it can appear anywhere an expression is expected. In particular, we can write sequences of let-in expressions, where what follows the in of one let is itself another let:

```
let price = 500 in
let attendees = 120 in
let revenue = price * attendees in
let cost = 18000 + 4 * attendees in
revenue - cost
```

Also, the expression on the right-hand side of a top-level let declaration can itself be a let-in:

We follow the usual rules for computing the answer for this program: evaluate the right-hand-side of each **let** binding to a value and substitute it in its scope. This yields the following sequence of steps:

Non-trivial scopes

It may seem like there is not much difference between redeclaring a variable via shadowing and the kind of assignment that updates the contents of a variable in a language like Java or C. The real difference becomes apparent when you use local **let** declarations to create non-trivial scoping for the shadowed identifiers.

Here's a simple example:

```
(* inner let shadows the outer one *)
let x = 1 in
x + (let x = 20 in x + x) + x
```

Because identifiers refer the their *nearest enclosing* **let** *binding*, this program will calculate to a value like this:

Note that in the first step, we substitute 1 for the outer \times in its scope, which doesn't include those occurrences of \times that are shadowed by the inner let.

Local **let** definitions are particularly useful when used in combination with functions, as we'll see next.

2.6 Function Declarations

So far we have seen how to use let to name the results of intermediate computations. The let declarations we've seen so far introduce an identifier that stands for one particular expression. To do more, we need to be

able to define *functions*, which you can think of as *parameterized expressions*. Functions are useful for capturing similarity between related calculations.

In mathematical notation, you might write a function using notation like:

$$f(x) = x + 1$$

In OCaml, top-level function declarations are introduced using let notation, just as we saw above. The difference is that function identifiers take parameters. The function above is written in OCaml like this:

```
let f (x:int) : int =
  x + 1
```

Here, f is an identifier that names the function and x is the identifier for the function's input parameter. The notation (x:int) indicates that this input is supposed to be an integer. The subsequent type annotation indicates that f produces an integer value as its result.

Functions can have more than one parameter, for example here is a function that adds its two inputs:

```
let sum (x:int) (y:int) :int =
  x + y
```

Note: Unlike Java or C, each argument to a function in OCaml is written in its own set of parentheses. In OCaml you write this

```
let f (x:int) (y:int) : int = ...
rather than this:
   let f (x:int, y:int) : int = ... (* BAD *)
```

In general, the form of a top level function declaration is:

```
\mathbf{let} \ \langle id \rangle \ (\langle id \rangle : \langle type \rangle) \dots (\langle id \rangle : \langle type \rangle) : \ \langle type \rangle = \langle exp \rangle
```

Calling functions

To call a function in OCaml, you simply write it next to its arguments—this is called *function application*. For example, given the function f declared above, we can write the following expressions:

```
f 3
(f 4) + 17
(f 5) + (f 6)
f (5 + 6)
f (f (5 + 6))
```

As before, we use parentheses to group together a function with its arguments in case there is ambiguity about what order to do the calculations.

To run an expression given by a function call, you first run each of its arguments to obtain values and then calculate the value of the function's body after substituting the arguments for the function parameters. For example:

```
f (5 + 6)
\mapsto f 11
\mapsto 11 + 1 \quad substitute \ 11 \text{ for } x \text{ in } x + 1 \text{ (the body of } f)
\mapsto 12
Similarly we have:
\sup (f 3) (5 + 2)
\mapsto \sup (3 + 1) (5 + 2) \quad substitute \ 3 \text{ for } x \text{ in } x+1
\mapsto \sup 4 (5 + 2)
\mapsto \sup 4 7 \quad sum \ 4 7
\mapsto 4 + 7 \quad substitute \ 4 \text{ for } x \text{ and } 7 \text{ for } y \text{ in } x + y
\mapsto 11
```

Functions and scoping

Function bodies can of course refer to any identifiers in scope, including constants...

```
let one = 1

let increment (x:int) : int =
   x + one
```

... and other functions that have been defined earlier:

Given the above declarations, we can calculate as follows:

```
quadruple 2 \mapsto double (double 2) substitute 2 for x in the body of quadruple \mapsto double (2 + 2) substitute 2 for x in the body of double \mapsto double 4 \mapsto 4 + 4 substitute 4 for x in the body of double \mapsto 8
```

Local **let** declarations are particularly useful inside of function bodies, allowing us to name the intermediate steps of a computation. For example:

```
let sum_of_squares (a:int) (b:int) (c:int) : int =
  let a2 = a * a in
  let b2 = b * b in
  let c2 = c * c in
  a2 + b2 + c2
```

2.7 Types

OCaml (like Java but unlike, for example C) is a *strongly typed* programming language. This means that the world of OCaml expressions is divided up into different types with strict rules about how they can be combined. We have already seen the primitive types int, string, and bool, and we will see many other types throughout the course.

Clearly, an integer like 3 has type int. We express this fact by writing "3: int", or, more generally $\langle exp \rangle$: $\langle type \rangle$. We have already seen this notation in use in **let** declarations and in function parameters, where (x : int) means that x is a parameter of type int.

In a well-formed OCaml program, every expression has a type. Moreover, this type can be determined "compositionally" from the operations used in the expression. An expression is *well-typed* if it has at least one type. Here are some examples of well-typed expressions and their types:

Before you run your OCaml program, the compiler will *typecheck* your program for you. This process makes sure that your use of expressions

in the program is consistent, which rules out many common errors that programmers make as they write their programs.

For example, the expression 3 + "hello" is *ill typed* and will cause the OCaml compiler to complain that "hello" has type string but was expected to have type int. Such error checking is good, because there is no sensible way for this program to compute to a value—OCaml's type checking rules out mistakes of this form. It is better to reject this program while it is still under development than to allow it to be distributed to end users, where such mistakes can cause serious reliability problems.

All of the built in operators like +, *, &&, etc.. have types as you would expect. The arithmetic operators take and produce int's; the logical operators take and produce bool's. The comparison operators = and <> take two arguments of any type (they must both be of the *same* type) and return a bool. This means that, 3 = "hello" will produce an error message, for example, while 3 = 4 and "hello" <> "goodbye" are both well typed.

The type annotations on user-defined functions tell you about the types of their inputs and result. For example, the function <code>quadruple</code> declared above expects an <code>int</code> input and produces an <code>int</code> output. We abbreviate this using the notation <code>int -> int</code>, the type of "functions that take one <code>int</code> as input and produce an <code>int</code> as output."

```
quadruple : int -> int
```

Because double also expects an int and produces an int, it also has the type int -> int.

On the other hand, the function <code>sum_of_squares</code> takes three arguments (each of type <code>int</code>) and produces an <code>int</code>. Its type is written as follows:

```
sum_of_squares : int -> int -> int -> int
```

Each of the functions in OCaml's libraries has a type, and these types can often give a strong hint about the behavior of the function. One example that we have seen so far is string_of_int, which has the type int -> string.

Common typechecking errors

OCaml's type checker uses these function types to make sure that your program is consistent. For example, the expression double "hello" is ill-

typed because double expects an int but the argument "hello" has type string. If you try to compile a program that contains such an ill-typed expression, the compiler will give you an error and point you to the offending expression of the program.

Another common error in OCaml programming is to omit one or more of the arguments to a function. Suppose you meant to increment a sum of squares $2^2 + 3^2 + 4^2$ by 1, and you wrote the expression below, accidentally leaving off the third argument:

```
(sum_of_squares 2 3) + 1  (* missing argument *)
```

In this case, OCaml will complain that the expression on the left of the + should be of type int but instead has type int -> int. That is because you have supplied two out of the three arguments to <code>sum_of_squares</code>; the resulting expression is still a function of the third parameter, that is, if you give the missing argument 4, the resulting expression will have the expected type <code>int</code>. The OCaml error messages take some getting used to, but they can be very informative.

Conversely, another frequent mistake is to provide too many arguments to a function. For example, suppose you meant to perform the calculation described above, but accidentally left out the + operator. In that case, you have:

```
(sum_of_squares 2 3 4) 1 (* extra argument, missing + *)
```

OCaml interprets this as trying to pass an extra argument, but since the expression in parentheses isn't a function, the compiler will complain that you have tried to apply an expression that isn't of function type.

2.8 Failwith

OCaml provides a special expression, written failwith "error string", that, when run, instead of calculating a value, immediately terminates the program execution and prints the associated error message. Such failwith expressions can appear *anywhere* that an expression can (but don't forget the error message string!).

Why is this useful? When developing a program it is often helpful to "stub out" unimplemented parts of the program that have yet to be filled

in. For example, suppose you know that you want to write two functions f and g and that g calls f. You might want to develop g *first*, and then go back to work on f later. failwith can be used as a placeholder for the unimplemented (parts of) f, as shown here:

```
let f (x:int) : int =
  if (x < 0)
    then (failwith "case x= 0 unimplemented")
    else x * 17 - 3

let g (y:int) : int =
  f (y * 10)</pre>
```

In CIS 120, the homework assignments use failwith to indicate which parts of the program should be completed by you. Don't forget to remove the failwith's from the program as you complete the assignment.

Note that using failwith at the top level is allowed, but will cause your program to terminate early, potentially without executing later parts of the code:

2.9 Commands

So far, we have seen how to use top-level declarations to write programs and functions that can perform calculations, but we haven't yet seen how to generate output or otherwise interact with the world outside of the OCaml program. OCaml programs can, of course, do I/O, graphics, write to files, and communicate over the network, but for the time being we will stick with three simple ways of interacting with the external world: printing to the screen, importing other OCaml modules and libraries, and running program test cases.

We call these actions *commands*. Commands differ from expressions or top-level declarations in that they don't calculate any useful value. Instead, they have some *side effect* on the state of the world. For example, the print_string command causes a string to be displayed on the terminal, but doesn't yield a value. Note that, because commands don't calculate

to any useful value, it doesn't make sense for them to appear within an expression of the program.

Commands (for now) may appear only at the top level of your OCaml programs. Syntactically, commands look like function call expressions, but we prefix them with ;; to distinguish them from other function calls that yield values. This notation emphasizes the fact that commands don't do anything except interact with the external world.

Displaying Output

The simplest command is print_string, which causes its argument (which should have type string) to be printed on the terminal:

```
;; print_string "Hello, world!"
```

If you want your printed output to look nice, you probably want to include an "end-of-line" character, written "\n", so that subsequent output begins on the next line.

```
;; print_string "Hello, world!\n"
```

OCaml also provides a command called print_endline that is just like print_string except it automatically supplies the "\n" at the end:

```
;; print_endline "Hello, world!"
```

There is also a command called print_int, which prints integers to the terminal:

The arguments to commands can be expressions whose values depend on other identifiers that are in scope, which lets you print out the results of calculations:

```
let volume (x:int) (y:int) (z:int) : int =
    x * y * z

let side : int = 17

;; print_int (volume side side side) (* prints "4913" *)
```

The function <code>string_of_int</code> and the string concatenation operator ^ are often useful when constructing messages to print. We might rewrite the example above to be more informative:

Importing Modules: the Assert library

OCaml provides several libraries, and programmers can develop their own libraries of code. The command open takes a (capitalized) module name as an argument and imports the functions of that module so that they can be used in the subsequent program.

For the time being, the only external module we need to worry about is the one that provides the testing infrastructure for CIS 120 projects. This module is called Assert, and one of the commands it provides is the run test command described next.

All of our homework projects and labs already include the following line, which ensures that run_test is available:

```
(* Import the CIS 120 testing infrastructure library *)
;; open Assert
```

The run_test Command

The last command needed for the homework assignments (at least for now), is run_test, which, as described above is provided by the Assert library.

The run_test command takes two arguments: (1) a string that serves as a label for the test and is used when printing the results of the test, and (2) a function identifier that names the test to be run.

Here is an example use of run_test:

```
let test () : bool =
  (1 + 2 + 3) = 7
;; run_test "1 + 2 + 3" test
```

The test function declared just above run_test takes no arguments, as indicated by the () parameter, and returns a bool result. A test succeeds if it returns the value true and fails otherwise (note that a test might fail by calling failwith, in which case no answer is actually returned).

The effect of the run_test command is to execute the test function and, if the test fails, print an error message to the terminal that indicates which test failed. In the example above, it is easy to see that this test fails, since $1 + 2 + 3 \implies 6$, which is not equal to 7.

To run multiple tests in one program, we simply use shadowing so that we can re-use the identifier test for all the test functions. Here's an example:

```
let f (x:int) : int = (x + 1) / 2

(* This test succeeds *)
let test () : bool =
    (f 7) = 4
;; run_test "f 7" test

(* This test function shadows the one above; it fails *)
let test () : bool =
    (f 0) = 1
;; run_test "f 0" test
```

2.10 A complete example

Putting it all together, we can implement a program that solves the simple design problem posed in lecture.

```
(* Import the CIS 120 testing framework *)
;; open Assert
(* Using OCaml as a simple calculator *)
let profit_five_dollars : int =
 let price = 500 in
 let attendees = 120 in
 let revenue = price * attendees in
  let cost = 18000 + 4 * attendees in
 revenue - cost
(* Generate output useful for debugging, understanding *)
;; print_endline ("profit $5.00 = " ^
                    (string_of_int profit_five_dollars))
(* Assumes a linear relationship between attendees and price *)
let attendees (price:int) : int =
       (-15 * price) / 10 + 870
(* Tests for attendees, generated from the problem description *)
let test () : bool =
        (attendees 500) = 120
;; run_test "attendees @ $5.00" test
let test () : bool =
       (attendees 490) = 135
;; run_test "attendees @ $4.90" test
let revenue (price:int) : int =
      price * (attendees price)
let cost (price:int) : int =
        18000 + 4 * (attendees price)
let profit (price : int) : int =
        (revenue price) - (cost price)
(* A test case generated from the problem description *)
let test () : bool =
        (profit 500) = profit_five_dollars
;; run_test "profit $5.00" test
let test () : bool =
       (profit 490) = 47610
;; run_test "profit $4.90" test
```

2.11 Notes

Parts of this Chapter were adapted from lecture notes by Dan Licata written for CMU's course 15-150 Fall 2011, Lecture 2.

Chapter 3

Lists and Recursion

So far we have seen how to create OCaml programs that compute with *atomic* or *primitive* values—integers, strings, and booleans. A few real world problems can be solved with this just these abstractions, but most problems require computing with collections of data—sets, lists, tables, or databases.

In this chapter, we'll study one of the simplest forms of collections: *lists*, which are just ordered sequences of data values. Many of you will have seen list data structures from your previous experience with programming. OCaml's approach to list processing emphasizes that computing with lists closely follows the *structure* of the datatype. This will be a recurring theme throughout the course: the structure of the data tells you how you should compute with it.

3.1 Lists

What is a list? It's just a sequence of zero or more values. That is, a list is either

```
the empty list, sometimes called nil, or v::tail a value v followed by tail, a list of the remaining elements.
```

There is no other way of creating a list: all lists have one of these two forms. The double-colon operator '::' constructs a non-empty list—it takes as inputs the head of the new list, v, and a (previously constructed) list, tail. This operator is sometimes pronounced "cons" (short for "construction")

tor"). Note that :: is just a binary operator like + or ^, but, unlike those, it happens to take arguments of two different types—its left argument is an element and its right argument is a *list* of elements.

Here are some examples of lists built from [] and :::

```
[]
3::[]
1::2::3::[]
true::false::true::[]
"do"::"re"::"mi"::"fa"::"so"::"la"::"ti"::[]
```

The examples above can also be written more explicitly using parentheses to show how :: associates. For example, we can equivalently write 1::(2::(3::[])) instead of 1::2::3::[]. We usually leave out these parentheses because they aren't needed: the OCaml compiler fills them in automatically. Note that if you were to write (1::2)::3::[] you will get a type error—2 by itself isn't a list.

You can, however have lists of lists—i.e., the elements of the outer list can themselves be lists:

```
(1::2::[])::(3::4::[])::[]
```

Writing out long lists using :: over and over can get a little tedious, so OCaml provides some syntactic sugar to make things shorter. You can write a list of values by enclosing the elements in [and] brackets and separating them with semicolons. Rewriting some of the examples we have seen so far using this more convenient notation, we have:

```
3::[] = [3]

1::2::3::[] = [1;2;3]

true::false::true::[] = [true;false;true]

(1::2::[])::(3::4::[])::[] = [[1;2];[3;4]]
```

Calculating With Lists

As with the primitive operators discussed in §2, the arguments to :: can themselves be complex expressions. To simplify such an expression, we calculate the head element down to a value and then calculate the tail list down to a value. A list is a value just when all of its elements are values.

For example, we might calculate like this:

```
(1 + 2) :: ((2 + 3) :: [])
\longrightarrow 3 :: (2+3) :: [] \qquad because 1+2 \longmapsto 3
\longmapsto 3 :: 5 :: [] \qquad because 2+3 \longmapsto 5
```

And then we're done because the entire list consists of values. Equivalently, we could have used the more compact notation:

```
[(1 + 2); ((2 + 3)])
\longmapsto [3; (2+3)] \qquad because 1+2 \longmapsto 3
\longmapsto [3; 5] \qquad because 2+3 \longmapsto 5
```

All of the rules for calculation that we've already seen carry through here as well. We can use **let** to bind list expressions and name intermediate computations, and we use substitution just as before:

```
let square (x:int) : int = x * x
let l : int list = [square 1; square 2; square 3]
let k : int list = 0::l

let square (x:int) : int = x * x
let l : int list = [1;4;9]
let k : int list = [0;1;4;9]
```

List types

The example just above uses the type annotation 1: int list to indicate that 1 is a list of int values. Similarly, we can have a list of strings whose type is string list or a list of bool lists, whose type is (bool list) list.

All of the elements of a list must be of the *same* type: OCaml supports only "homogeneous" lists. If you try to create a list of mixed element types, such as 3::"hello"::[], you will get a type error. While this may seem limiting, it is actually quite useful; knowing that you have a list of ints, for example, means that you can perform arithmetic operations on all of those elements without worrying about what might happen if some non-integer element is encountered.

Simple pattern matching on lists

We have seen how to construct lists by using ::. How do we take a list value apart? Well, there are only two cases to consider: either a list is

empty, or it has some head element followed by some tail list. In OCaml we can express this kind of case analysis using *pattern matching*. Here is a simple example that uses case analysis to determine whether the list 1 is empty:

The begin match $\langle exp \rangle$ with ... end expression compares the shape of the value computed by $\langle exp \rangle$ against a series of pattern cases. In this example, the first case is | [] -> true, which says that, if the list being analyzed is empty, then the result of the match should be true.

The second case is | x::tl -> false, which specifies what happens if the the list being analyzed matches the pattern x::tl. If that happens, then the expression to the right of the -> in this branch will be the result of the whole match.

Note that the *patterns* [] and x::tl look exactly like the two possible ways of constructing a list! This is no accident: since all lists are built from these constructors, these are exactly the cases that we have to handle—no more, and no less. The difference between the pattern x::tl and a list value is that in the pattern, x and tl are *identifiers* (i.e. place holders), similar to the identifiers bound by let. When the match is evaluated, they are *bound* to the corresponding components of the list, so that they are available for use in the expression following the pattern's ->.

To see how this works, let's look at some examples. First, let's see how to evaluate the example above, which doesn't actually use the identifiers bound by the pattern:

 \longmapsto (by substituting [1;2;3] for 1)

At this point, we match the list [1;2;3] against the first pattern, which is []. Since they don't agree—[] doesn't have the same shape as [1;2;3]—we continue to the next case of the pattern. Now we try to match the pattern x::t1 against [1;2;3]. Remember that [1;2;3] is just syntactic sugar for 1::2::3::[], which, if we parenthesize explicitly, is just 1::(2::(3::[])). This value *does* match the pattern x::t1, letting x be 1 and t1 be 2::3::[]. Therefore, the result of this pattern match is the right-hand side of the ->, which in this example is just **false**. The entire program thus steps to:

```
let 1 : int list = [1;2;3]
let is_l_empty : bool = false
```

In more interesting examples, the identifiers like \times and t1 that are used in a cons-pattern will also appear in the right-hand side of the match case. For example, here is a function that returns the square of the first element of an int list, or -1 if the list is empty:

Let's see how a call to this function evaluates:

Now we test the branches in order. The first branch's pattern ([]) doesn't match, but the second branch's pattern does, with \times bound to 3 and t1 bound to [2;1], so we substitute 3 for \times and [2;1] for t1 in the

right-hand side of that branch, i.e.:

3.2 Recursion

The definition of lists that we gave at the start of this chapter said that a list is either

```
the empty list, sometimes called nil, or v::tail a value v followed by tail, a list of the remaining elements.
```

Note that this description of lists is *self referential*: we're defining what lists are, but the second clause uses the word "list"! How can such a "definition" make sense? The trick is that the above definition tells us how to build a list of length 0 (i.e. the empty list []), or, given a list of length n, how to construct a list of length n + 1. The phrase "list of the remaining elements" is really only talking about strictly *shorter* lists.

This is the hallmark of an *inductive data type*: such data types tell you how to build "atomic" instances (here, []) and, given some smaller values, how to construct a bigger value out of them. Here, :: tells us how to construct a bigger list out of a new head element and a shorter tail.

This pattern in the structure of the data also suggests how we should compute over it: using *structural recursion*. Structural recursion is a fundamental concept in computer science, and we will see many instances of it throughout the rest of the course.

The basic idea is simple: to create a function that works for *all* lists, it is sufficient to say what that function should compute for the empty list, and, assuming that you already have the value of the function for the tail of the list, how to compute the function given the value at the head. Like the definition of the list data type, functions that compute via structural

recursion are themselves self referential—the function is defined in terms of itself, but only on smaller inputs!

Calculating the length of a list

Here is an example of how to use structural recursion to compute the length of a list of integers:

Note that we use the keyword rec to explicitly mark this function as being recursive. If we omit the 'rec', OCaml will complain if we try to use the function identifier inside its own body. Also, note that this function does case analysis on the structure of 1 and that the body of the second branch calls length recursively on the tail—this is an example of structural recursion, since the tail is always smaller than the original list.

The first branch tells us how to compute the length of the empty list, which is just 0. The second branch tells us how to compute the length of a list whose head is \times and whose tail is t1. Assuming that we can calculate the length of t1 (which is the result of length t1 obtained by the recursive call), we can compute the length of the whole list by adding one.

Let us see how these calculations play out when we run the program:

More int list examples

By slightly modifying the length function from above, we can obtain a function that sums all of the integers in a list.

Again we apply the design pattern for recursive functions. The sum of all elements of the empty list is just 0, since there are no elements. If $sum\ tail$ is the sum of all the elements in the tail of a list whose first element is n, then we obtain the total sum by simply calculating $n + (sum\ tail)$.

Here's the code, along with a couple test cases:

```
let rec sum (l:int list) : int =
  begin match l with
  | [] -> 0
  | n::tail -> n + (sum tail)
  end

let test () : bool =
    (sum []) = 0
;; run_test "sum []" test

let test () : bool =
    (sum [1;2;3]) = 6
;; run_test "sum [1;2;3]" test
```

Now let's look at a slightly more complex example. Suppose we want to write a function that takes a list of integers and filters out all the even integers—that is, our function should return a list that contains just the even elements of the original list.

Filtering the even numbers out of the empty list yields the empty list. And if filter_out_evens tail is the result of filtering the tail of the original list, we just need to check whether the head of the list is even to know whether it belongs in the output:

For a third example, suppose we want to write a function that determines whether a list *contains* a given integer. The solution again uses structural recursion over the list parameter, but also takes as input the int to

search for:

Finally, suppose we want to compute the list of *all suffixes* of a given list, that is:

```
suffixes [1;2;3] \Longrightarrow [[1;2;3]; [2;3]; [3]; []]
```

We can easily compute this by observing that at every call to <code>suffixes</code> we simply need to cons the list itself onto the list of its own suffixes. Note that this observation holds true even for the empty list!

The list structural recursion pattern

All of the example list functions we have seen so far follow the same pattern. To define a function f over a list, we to case analysis to determine whether the list is empty or not. If it is empty, we can calculate the result of f [] directly, without any recursive calls to f. If the list is *not* empty, we compute the answer for a list whose head is hd using the result of the recursive call (f rest). In code:

This pattern is extremely general: many, many useful functions can be written easily by following this recipe. Here is a (very partial) list of such functions, with brief descriptions. It is a good exercise to figure out how to implement all these functions using structural recursion.

- all_even determines whether all elements of an int list are even
- append takes two lists and "glues them together", for example append [1;2;3] [4;5] ⇒ [1;2;3;4;5]
- intersection takes two lists and returns the list of all those elements that appear in both lists; for example:
 intersection [1;2;2;3;4;4;3] [2;3] ⇒ [2;2;3;3]
- every_other computes the list obtained by dropping every second element from the input list, for example: every_other [1;2;3;4;5] ⇒ [1;3;5]

When designing tests for list processing functions, you should *always* consider at least two cases: a test case for the empty list, and a case for non-empty lists. Other kinds of test cases to consider might have to do with whether the list is even or odd, or whether the function has special behavior when the list has just one element.

Note: For those of you who have taken or are taking CIS 160, it is also worth noticing that writing a program by structural induction over lists follows the same pattern as proving a property by induction on the list. There is a base case (i.e. the case for []) and an inductive case (i.e. the recursive case). It is no accident that lists are called inductive data structures.

Using helper functions

Sometimes the list function we are trying to implement isn't trivial to compute, even given the value of the recursive call. An example of such a

function is prefixes, which is like the suffixes example above, but instead calculates the list of prefixes of the input list. For example, we want to have:

```
prefixes [1;2;3] \Longrightarrow [[]; [1]; [1;2]; [1;2;3]]
```

Why is this not so direct to implement as suffixes was? Suppose we're trying to calculate prefixes [1;2;3]. Following the structural recursion pattern, we would expect to call prefixes on the tail of this list, which is:

```
prefixes [2;3] \Longrightarrow [[]; [2]; [2;3]]
```

Given this result for the recursive call to prefixes, and the head 1, we need to compute prefixes for the entire list [1;2;3]. Looking for a pattern, it seems that we need to put 1 at the head of *each* of the prefixes of [2;3]. Since this functionality isn't given to us directly by prefixes, we need to define an auxiliary function to help out. Let's call it prepend. As usual, we document our examples as test cases.

Now, using prepend, it becomes much simpler to define prefixes:

For another example where a helper function is needed, consider trying to compute a function rotations that, given a list of integers, computes the list of all "circular rotations" of that list. For example:

```
rotations [1;2;3;4] \Longrightarrow [[1;2;3;4]; [2;3;4;1]; [3;4;1;2]; [4;1;2;3]].
```

Here again, thinking about how rotations would work on the result of

a recursive call illustrates why there might be a need for a helper function. When we use rotations on the tail of the list [1;2;3;4], we get:

```
rotations [2;3;4] \Longrightarrow [2;3;4]; [3;4;2]; [4;2;3]
```

The relationship between rotations [2;3;4] and rotations [1;2;3;4] seems very nontrivial—it seems like we have to intersperse the head 1 at various points (in the last spot, the second-to-last spot, the third-to-last spot, etc.) in the prefixes of the tail. We could perhaps write an auxiliary function that does this, but that still seems complicated.

Here's another approach that simplifies the solution. Consider what information from the original list that we have at each recursive call to some function ${\tt f}$

If each such recursive call to f were to calculate one of the rotations of the original list, what information would f be missing? Each call is missing a prefix of the original list!

```
(*missing prefix*)

f [1;2;3;4] []

f [2;3;4] [1]

f [3;4] [1;2]

f [4] [1;2;3]

f [] [1;2;3;4]
```

If we append the two lists in each row above, we obtain one of the desired permutations of the *original* list. (One of the permutations, [1;2;3;4], appears twice—we'll have to be careful to leave one of them out of the result.)

This suggests that we can solve the rotations problem by creating a helper function that takes an extra parameter—namely, the missing prefix needed to compute one permutation of the original list.

If we were to accumulate these lists together into a list of lists, we would be done. That is, we want a function f that works like:

```
f [1;2;3;4] [] \Longrightarrow [[1;2;3;4]; [2;3;4;1]; [3;4;1;2]; [4;1;2;3]]
```

What should f do on a tail of the original, assuming we provide the missing prefix?:

```
f[2;3;4][1] \Longrightarrow [[2;3;4;1]; [3;4;1;2]; [4;1;2;3]]
```

Do you see the pattern? Each call to the helper function f computes some (but not all) of the rotations of the original list. Which ones? The ones beginning with each of the elements of the first input to f. Observe that at each call f suffix prefix we have that prefix @ suffix is the original list and suffix @ prefix is the next rotation to generate.

Function f should therefore simply recurse down the suffix list; but at each call it needs to rotate its own head element to the end of the prefix list, to maintain the relationship described above.

We already know how to put an element at the *front* of a list—we use :.. How do we put one at the tail? Well, we simply write a second helper function that does the job. We call it snoc (because it is the opposite of cons):

Putting it all together, we can write rotations like so:

Infinite loops: Non-structural recursion

All of the examples list processing functions described above are guaranteed to terminate. Why? Because every list is contains only finitely many elements and each of the recursive calls in a structurally recursive function is invoked on a *strictly shorter* list (the tail). This means that at some point the chain of recursion will bottom out at the empty list.

OCaml does not strictly enforce that all list functions be structurally recursive. Consider the following example, in which the loop function calls itself "recursively" on the *entire* list, rather than just on the tail:

```
let loop (l:int list) : int =
 begin match 1 with
   [] -> 0
   | h::tl -> 1 + (loop l)
```

Watch what happens when we run this program on the list [1]:

```
loop [1]
\longmapsto (substitute [1] for l in the body of loop)
      begin match [1] with
        | [] -> 0
        | h::tl -> 1 + (loop 1)
\mapsto (the second case matches)
   1 + (loop 1)
                    (* uh oh! *)
\longmapsto \ldots \longmapsto
   1 + (1 + (1 + (1 + (loop 1))))
\mapsto (the program keeps running forever)
```

If you find one of your programs mysteriously looping, a non-structural recursive call may be the culprit.

Chapter 4

Tuples and Nested Patterns

4.1 Tuples

Lists are good data structures for storing arbitrarily long sequences of homogeneous data, but sometimes it is convenient to bundle together two or more values of *different* types. OCaml provides *tuples* for this purpose. A tuple is a fixed-length sequence of values, enclosed in parentheses and separated by commas. Here are some examples:

Note that, unlike lists, the elements of a tuple need not have the same types.

We write tuple types using infix * notation, so for the three examples above, we have:

Of course, the elements of a tuple expression can themselves be complex expressions (including lists). OCaml evaluates a tuple expression by evaluating each of the components of the tuple. For example, $(1+2+3, true | | false) \implies (6, true)$ because $1+2+3 \implies 6$ and true $| | false \implies true$.

Lists and tuples can easily be combined to create more interesting data

structures. Here are a couple of examples and their types:

```
[(1, "uno"); (2, "dos"); (3, "tres")]
          : (int * string) list
([1; 2; 3], ["uno"; "dos"; "tres"])
          : (int list) * (string list)
```

Pattern matching on tuples

Like lists, tuples can be "inspected" by pattern matching. Also as for lists, the patterns themselves mimic the form of tuple values. For example:

Note that, since there's only one way to construct a tuple (using parens and commas), we only need *one* case when pattern matching against a tuple.

A more lightweight way to give names to the components of a tuple is to use a generalization of **let** binding that we have already seen. The idea is that, since there is only ever one case when matching against a tuple, we can abbreviate that case using the syntax **let** $(x,y) = \ldots$ For example, we can rewrite first and second above using **let**-tuple notation like this:

```
let first (x:int * string) : int =
  let (left, right) = x in left

let second (x:int*string) : string =
  let (left, right) = x in right
```

We omit the type annotation from the let binding because OCaml can infer it from the type of the tuple to the right of the = (e.g. by looking at the type of x above, it is easy to figure out that left should have type int and right should have type string).

The "empty" tuple, unit:

There's one special case of tuples to explain—the tuple of *no* elements. This is written in OCaml as (), and its type is called unit. There is only one value, namely (), of type unit, so not much information is conveyed by a unit value.

We have already seen () mentioned in our test functions: since they take no meaningful inputs, they have the type unit -> bool. We could write our test functions like

```
let test (x:unit) : bool =
...
```

(where we give an explicit name, x, to the unit parameter), but there is not much point in doing this, since the parameter is not used in the function's body. So we write () instead of (x:unit), emphasizes that the parameter is trivial.

The other place in OCaml where unit is often used is as the return type of *commands* such as print_string. For example, print_string takes a string input and produces a unit output: its type is string -> unit. (Here, unit functioning like a void return type in C or Java.) Since there is only one value of type unit, such functions cannot return meaningful results: they are executed purely for their side effects on the machine's state (such as printing to the terminal). Whenever you see an OCaml function that return unit, you should take it as a strong hint that there will be some I/O or some kind of other effect when you call that function.

See §12 for a more in-depth discussion about the uses of the unit type.

4.2 Nested patterns

We saw in Chapter 3 that lists can be inspected by pattern matching. Lists values have two constructors, [], and ::, and list patterns analogously have two possible forms. Tuples, as we saw just above, are matched using (..., ...,) patterns. Furthermore, just as we can build complicated list and tuple *expressions* by nesting constructors, we can build complex list *patterns* by nesting too. Here are some examples of nested patterns:

As an example of how one might use nested patterns, the following match expression has three cases, one for when the list is empty, one for singleton lists, and one for when a list has two or more elements:

When OCaml processes a match expression, it checks the value being matched against each pattern *in the order they appear*. In the example above, the case for singletons must appear *before* the case for two or more, since the pattern x::tail can match a singleton list like 1::[] by binding tail to []. This means that if we were to reverse the order of the cases, then the third branch would never be reached:

```
begin match 1 with
    | [] -> ...
    | x::tail -> ...
    | x::[] -> ... (* this case is never reached! *)
end
```

If your cases are written so that one of them can never be executed, OCaml will warn you that the match case is unused. This is a good sign that there is a bug in your program logic!

4.3 Exhaustiveness

OCaml can determine whether you have covered all the possible cases when pattern matching against a datatype. For example, suppose you wrote the following:

```
begin match 1 with
    | [] -> ... (* case for empty *)
    | x::[] -> ... (* case for singleton *)
end
```

This match expression only handles lists of length 0 and 1. If 1 happens to evaluate to a longer list, then at run-time the program will terminate and OCaml will report a Match_failure error. To prevent such surprises at run time, OCaml will give you a helpful warning that you have missed a possible case ("this pattern-matching is not exhaustive") when you compile the program. Besides the warning, the compiler will provide an example that isn't handled by your branches.

4.4 Wildcard (underscore) patterns

Sometimes the particular value in a pattern doesn't matter. For example, recall that we wrote a length function like this:

```
let rec length (l:int list) : int =
  begin match l with
  | [] -> 0
  | x::tl -> 1 + (length tl) (* x not used *)
  end
```

Note that the second branch doesn't use x anywhere. We can emphasize that fact by using the special '_' pattern, which matches *any* value but doesn't give a name for it. So, for example, we could write:

A wildcard pattern can appear anywhere in a pattern. Here are some examples:

4.5 Examples

Here's an example function that uses lists, tuples, and nested pattern matching. The function is called <code>zip</code>; it takes as inputs two lists, and it returns a list of pairs, drawn "in lockstep" from the two lists. For example, we have:

(The last case is needed for exhaustive pattern matching.)

It is instructive to see how the same function would be written without the use of nested patterns or wildcards. It is considerably more verbose!

Chapter 5

User-defined Datatypes

5.1 Atomic datatypes: enumerations

We have seen that OCaml provides several means of creating and manipulating structured data. Our toolbox includes primitive datatypes int, string, and bool, immutable lists, and tuples, as well as the ability to write (potentially recursive) functions over such data.

Despite these many options, programs often need application-specific datatypes. For example, suppose you were building a calendar application, you might want to have a datatype for representing the days of the week. Or, if your program involved computing over DNA sequences, you might need a representation for the nucleotides (adenine, guanine, thymine, and cytosine) that make up a DNA strand.

One possibility would be to use the existing datatypes available to represent your program-specific data. For example, you might choose to use int values to represent days of the week, with some mapping like:

```
Sunday = 0
Monday = 1
Tuesday = 2
```

This could work¹, but it's not a very good idea for a few reasons. First, int values and days of the week support different operations—it makes

¹It's essentially what you do in a weakly-typed language like C

sense to subtract 1 - 2 to obtain the answer -1, but what would the subtraction Tuesday - Wednesday mean? There is no day of the week that is represented by -1. This may seem relatively innocuous, but it's a recipe for disaster. Consider writing a function that converts days of the week (represented as ints) into strings:

```
let string_of_weekday (wd:int) : string =
  if wd = 0 then "Sunday"
  else if wd = 1 then "Monday"
  else if wd = 2 then "Tuesday"
  ...
  else if wd = 6 then "Saturday"
  else failwith "not a valid weekday"
```

Everywhere you use such an encoding, you have to check to make sure (as in the last else clause above) to handle the case of an *invalid* encoding. Forgetting to check for such cases will lead to bugs and other unexpected failures in your code.

Another reason why such encodings are a bad idea is that it's also possible to accidentally confuse types—if you encode both weekdays and nucleotides as int values, it would be possible to pass an integer representing a nucleotide to the string_of_weekday function, which will likely yield nonsensical behavior.

For all of the reasons above, modern type-safe programming languages, including OCaml, Java, C#, Scala, Haskell, and others allow programmers to create *user-defined datatypes*, which effectively extend the programming language with new abstractions that can be manipulated just like any other values.

In OCaml, such datatypes are declared using the type keyword. For example, here is how the datatype for days-of-the-week can be defined:

```
type day =
| Sunday
| Monday
| Tuesday
| Wednesday
| Thursday
| Friday
| Saturday
```

This declaration defines a new type, named day, and seven *constructors* for that type, Sunday, Monday, *etc.* These constructors *are* the values

of the type day—they enumerate all the possible ways of creating a day. Moreover, there are *no other ways* to create a value of type day.

Note: In OCaml, user-defined types must be lowercase, and the constructors for such types must be uppercase identifiers.

After this top-level declaration, you can program with days of the week as a new type of value, for example, we could build a list of some days of the week like this:

```
let weekend_days : day list = [Saturday; Sunday]
```

So, we can put values of type day into data structures; how else can we compute with them?

If you think about it, the only fundamental operation needed on a datatype like <code>day</code> is the ability to distinguish one value (like <code>Monday</code>) from another value (like <code>Tuesday</code>). Given that operation, we can build up more complicated operations simply by programming new functions.

Just as OCaml uses pattern matching to allow functions to examine the structure of lists and tuples, we also use pattern matching to do case analysis on user-defined datatypes. The patterns *are* the constructors of the datatype. So, we can write a function that computes with days like this:

```
let is_weekend_day (d:day) : bool =
  begin match d with
  | Sunday -> true
  | Saturday -> true
  | _ -> false
  end
```

Here's another function that, given a day of the week, returns the day after it:

```
let day_after (d:day) : day =
  begin match d with

| Sunday -> Monday
| Monday -> Tuesday
| Tuesday -> Wednesday
| Wednesday -> Thursday
| Thursday -> Friday
| Friday -> Saturday
| Saturday -> Sunday
end
```

The fact that the seven constructors <code>Sunday</code>, <code>Monday</code>, <code>etc.</code>, are the <code>only</code> ways of creating a value of type <code>day</code> means that OCaml can automatically determine when you have covered all of the cases. For example, if you had left out the wildcard case <code>_</code> in <code>is_weekday</code> or if you had accidentally left out one of the days in <code>day_after</code>, the OCaml compiler will give you a warning that your pattern matching is not exhaustive.

5.2 Datatypes that carry more information

Although the simple *atomic* data values, like those used for the day type, are useful in many situations, it is often useful to associate extra information with a data constructor.

For example, suppose you are collaborating with a biologist who researches DNA and are writing a program to process DNA sequences in various ways. (See Homework 2.)

Recall that there are four basic nucleotides, and we can easily represent them using the atomic datatypes we have already seen:

Now consider the problem of how to represent data being produced by some potentially faulty sensor that is able to detect counts of nucleotides or triples of nucleotides that are bundled together into a codon. That is, the experiment can produce one of three possible measurements: the measurement can be *missing* (indicating a fault), the measurement can be a *nucleotide count* which consists of a particular nucleotide value along with an integer representing the count detected, or the measurement can be a *codon count* which consists of a triple of nucleotides along with a count.

In OCaml, we can use the **type** keyword to create a datatype whose values contain the information described above:

```
type experiment =
    | Missing
    | NucCount of nucleotide * int
    | CodonCount of (nucleotide * nucleotide * nucleotide) * int
```

This type declaration introduces the type <code>experiment</code> and three possible constructors. The <code>Missing</code> constructor is an atomic value—it doesn't depend on any more information. The other two constructors, <code>NucCount</code> and <code>CodonCount</code> each have some data associated with them. This is indicated syntactically by the <code>of</code> keyword followed by a type.

To build a NucCount value, for example, we simply provide the NucCount constructor with a pair consisting of a nucleotide and an int. Similarly, we can build a CodonCount by providing a triple of nucleotides and an int. Here are some examples values, all of which have type experiment:

```
Missing
NucCount (A, 17)
NucCount (G, 124)
CodonCount ((A,C,T), 0)
CodonCount ((G,A,C), 2512)
```

Just as we use pattern matching to do case analysis on the atomic values in the day type, we can also use pattern matching on these more complex data structures. The only difference is that since these constructors carry extra data, we can use nested patterns (see §4.2) to bind identifiers to the subcomponents of a value. Here, for example, is a function that extracts the numeric count information from each experiment:

```
let get_count (m:measurement) : int =
  begin match m with
  | Missing -> 0
  | NucCount(_,n) -> n
  | CodonCount(_,n) -> n
  end
```

Note that since the NucCount constructor takes a pair, we use a nested tuple pattern to bind its components in the branches. The CodonCount branch is similar. If we had instead been looking for a particular occurrence of a codon triple, we might have used a more explicit pattern instead. For example, suppose we are looking for the counts of experiments for which a codon whose first and last nucleotide is G. We could write such a function like this:

5.3 Type abbreviations

The examples above show the utility of defining *new* datatypes. The type structure defines both how we can create values of the type and how we inspect a value to determine its constituent parts. Sometimes, however, it is convenient to be able to name *existing* types, both to emphasize the abstraction and to make it simpler to work with.

Returning to the DNA example, we might find it useful to define a type for codons, which consist of a triple of nucleotides, and a type for helices, which are just lists of nucleotides. We do so in OCaml using *type abbreviations*, like this:

```
type codon = nucleotide * nucleotide * nucleotide
type helix = nucleotide list
```

These top-level declarations introduce new *names* for existing types. Note that, unlike the datatype definitions we saw above, these type declarations don't use a list of |-separated constructor names. OCaml can tell the difference because constructor names (A,C,Missing, NucCount) are always capitalized but type identifiers (day, nucleotide, codon) are always lowercase.

After having made these type abbreviations, we can use each name interchangeably with its definition throughout the remainder of the program, including subsequent type definitions. For example, if we have made these type abbreviations, we could shorten the type definition for experiment to this:

Since a type abbreviation is just a new name for an existing type, we can use whatever functions or pattern matching operations were available for the existing type to process data of the abbreviated type.

5.4 Recursive types: lists

There is one final wrinkle in understanding user-defined datatypes, and that is the idea that when creating a new type definition, we can define the type *recursively*. That is, the data associated with one of the type's constructors can mention the type being defined.

For example, we are already familiar with the type string list, which contains lists of strings and has two constructors: [] (nil) and :: (cons); for a refresher, see §3. We can define our own version of string lists by using a recursive type, like this:

```
type my_string_list =
    | Nil
    | Cons of string * my_string_list
```

Here, the constructor Nil plays the role of [], and a value like Cons(v,tl) plays the role of v::tl. We can program recursive functions over these lists just as we would the built-in ones. For example, here is the length function for the my_string_list type:

```
let rec my_length (l:my_string_list) : int =
  begin match l with
  | Nil -> 0
  | Cons(_, tail) -> 1 + (my_length tail)
end
```

We could even write functions that convert between my_string_list and the built-in string list type:

Chapter 6

Binary Trees

OCaml includes built-in syntax for lists, and we have already seen how we can create a user-defined datatype that has the same structure as those built-in lists. Lists are a very common pattern in programming because sequences of data occur naturally in many settings—the list of choices in a menu, the list of students taking a course, the list of results generated by a search engine, *etc.*.

In this chapter, we introduce another frequently occurring data structure—the *binary tree*. Sometimes, such trees arise naturally from the problem domain: for example the evolutionary tree that arises when a species evolves into two new species. Other times, computer scientists use trees because they let us exploit an ordering on data to efficiently search for the presence of an element in a large set of possible values, as we will see below.

For the purposes of this Chapter, we'll consider a simple example of binary trees. What is a binary tree? A binary tree is either <code>Empty</code> (meaning that it has no elements in it), or it is a <code>Node</code> consisting of a left subtree, an integer *label*, and a right subtree.

In OCaml, we can represent this datatype like so:

```
type tree =
    | Empty
    | Node of tree * int * tree
```

Figure 6.1 shows a picture of a typical binary tree. The *root* node is at the top of the tree. A *leaf* is a node both of who's children are Empty—they appear at the bottom of the tree in this picture.¹ Any node that is not a leaf

¹For some reason, trees in computer science have their roots at the top and their leaves

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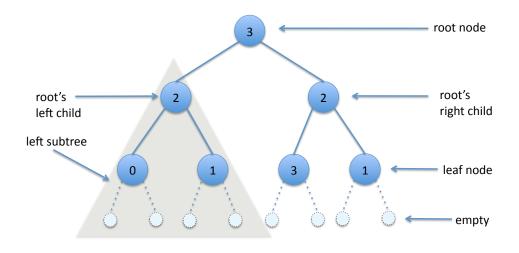


Figure 6.1: The parts of a binary tree.

is sometimes called an *internal* node of the tree.

The tree in Figure 6.1 is represented in OCaml by simply building up a value from the tree constructors. The serial nature of text isn't very good at representing the 2D picture, but you can still see how the picture corresponds to the OCaml value:

We can simplify the presentation a little bit be creating a helper function to make a leaf when given the int for its label:

at the bottom...unlike real trees.

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Note that the definition of the type tree is recursive, but, unlike the list datatype we saw previously, there are two occurrences of tree within a Node. This means that when we write a recursive function that computes with trees, it will in general have two recursive calls.

Here are some simple examples that compute basic properties about a tree:

```
(* counts the number of nodes in the tree *)
let rec size (t:tree) : int =
  begin match t with
  | Empty -> 0
  | Node(l,_,r) -> 1 + (size l) + (size r)
  end

(* counts the longest path from the root to a leaf *)
let rec height (t:tree) : int =
  begin match t with
  | Empty -> 0
  | Node(l,_,r) -> 1 + max (height l) (height r)
  end
```

The *size* of a tree is the total number of nodes in the tree (ignoring the labels of those nodes). A tree's *height* is the length of the longest path from the root to any leaf.

Different ways of processing a tree use can traverse the elements in different orders, depending on the desired goal. Three canonical ways of traversing the tree are *in order* (first the left child, then the node, then the right child), *pre order* (first the node, then the left child, then the right), and *post order* (first the left child, then the right child, then the node). We can write functions that enumerate the elements of a tree in these orders by serializing the tree into a list:

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```
(* returns the in order traversal of the tree *)
let rec inorder (t:tree) : int list =
 begin match t with
    | Empty -> []
    | Node (1, n, r) \rightarrow (inorder 1)@(n::(inorder r))
  end
(* returns the preorder traversal of the tree *)
let rec preorder (t:tree) : int list =
 begin match t with
    | Empty -> []
    | Node(l,n,r) -> n::(preorder l)@(preorder r)
  end
(* returns the post-order traversal of the tree *)
let rec postorder (t:tree) : int list =
 begin match t with
    | Empty -> []
    | Node(l,n,r) -> (postorder l)@(postorder r)@[n]
  end
```

For the example tree in Figure 6.1, we have:

```
inorder tree_fig_51 \Longrightarrow [0;2;1;3;3;2;1] preorder tree_fig_51 \Longrightarrow [3;2;0;1;2;3;1] postorder tree_fig_51 \Longrightarrow [0;1;2;3;1;2;3]
```

One use for such tree traversals is to *search* for a particular element. For example, we can use the following function to determine whether a tree has a node labeled by the given integer:

This function first checks the root node's value, x, to see if it is n. If so, the answer is **true** (recall that OCaml's boolean or operator $|\cdot|$ is short circuiting—if its left argument evaluates to **true** then the right-hand argument is never evaluated). In the case that x <> n, the search continues recursively into first the left sub tree and then the right subtree.

Chapter 7

Binary Search Trees

The function contains might, in the worst case, have to search through all the nodes of the tree. In particular, when looking for an element n that isn't in the tree, this search will continue until every node is examined. For a small tree, that isn't such a problem, but in the case that the tree contains tens of thousands or millions of elements, such a search can take a long time.

Can we do better? It depends on what the data in the tree is representing. If it is the *structure* of the tree that matters or if there are patterns in the data of the nodes of the tree, then we may not be able to improve the search process—for example, it might be important that a certain element appears many times at various points in the tree.

However, there is another common case: the nodes of the tree are intended to be distinct labels, and what matters is whether a given label is present or absent in the tree. In this case, we can think of the tree of nodes as representing the *set* of node labels and the contains function as determining whether a given label is in the set.

If we further assume that the labels can be *linearly ordered* (i.e. arranged on the number line), it is possible to *dramatically* improve the performance of searching the tree by exploiting that ordering. The basic idea is the same one underlying the telephone book or a dictionary—arranging the data in a known order, for example by alphabetical order, allows someone who is searching through the data to skip over large irrelevant parts.

For example, when looking up the telephone number for a taxi cab, I might flip open the phone book to the "L" section (probably in the "lawyers") section. Since I know that "taxi" comes after "lawyer" alpha-

betically, I don't even have to bother to look earlier in the phone book. Instead, I flip much later, perhaps to the "R" part, where I see "restaurant" listings. Since "taxi" is still later, I know I don't have to look at the intervening pages. Flipping once more to the "V" section of "veterinarians", I now know to flip just a bit earlier, where I finally hit the "T" for "taxi" part of the phone book.

The basic idea of a binary search tree is to arrange the data in the tree such that by looking at the label of the node being visited the algorithm knows whether to proceed into the left child or the right child, and, moreover, it knows that the unvisited child contains irrelevant nodes.

This leads us to the binary search tree invariant.

Definition 7.1 (Binary Search Tree Invariant).

- Empty is a binary search tree.
- A tree Node(lt,x,rt) is a binary search tree if lt and rt are both binary search trees, and every label of lt is less than x and every label of rt is greater than x.

Note that this definition, like the structure of a binary tree, is itself *recursive*—we define what it means to be a binary search tree in terms of binary search trees. Figure 7.1 shows an example binary search tree. The edges are marked with < and > to indicate the relationship between a node's label and its children.

What is the advantage of this invariant? Well, unlike the contains function defined above, which potentially has to look at every node of the tree to see if it contains a given element, we can write a lookup function that only searches the relevant parts of the tree.

```
(* ASSUMES: t is a binary search tree
   Determines whether t contains n *)
let rec lookup (t:tree) (n:int) : bool =
   begin match t with
   | Empty -> false
   | Node(lt, x, rt) ->
        if x = n then true
        else if n < x then lookup lt n
        else lookup rt n
end</pre>
```

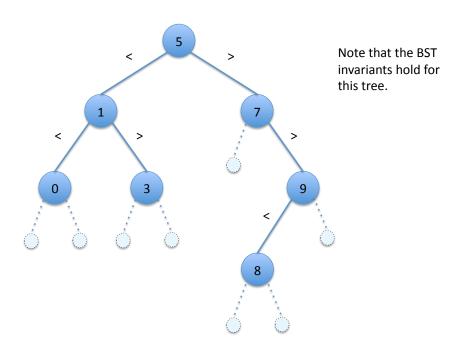


Figure 7.1: A binary search tree.

Note the difference: lookup will only ever take either the left branch (if n is less than the node's label) or the right branch (if n is greater than the node's label) when searching the tree.

How much difference could this make in practice? Consider the case of a binary search tree containing a million distinctly labeled nodes. Then the contains function will have to look at a million nodes to determine that an element is *not* in the tree. In contrast, if the lookup function takes time proportional to the *height* of the tree. In the good case when the tree is very full (i.e. almost all of the nodes have two children), then the height is roughly logarithmic in the size of the tree¹. In the case of a million nodes, this works out to approximately 20. Thus, doing a lookup in a binary search tree will be about 50,000 times faster than using contains.²

 $^{^{1}}$ A complete, balanced binary tree of height h has $2^{h}-1$ nodes, or, conversely if there are n nodes, then the tree height is $\log_{2} n$.

²The assumption that the tree is nearly full and balanced is a big one—to ensure that this is the case more sophisticated techniques (e.g. red–black trees) are needed. See CIS

7.1 Creating Binary Search Trees

We now know how to do efficient lookup in a binary search tree by exploiting the ordering of the labels and the invariants of the tree. How do we go about obtaining such a tree?

One possibility would be to simply check whether a given tree satisfies the binary search tree invariant. We can code up the invariant as a boolean valued-function that determines whether a given tree is a binary search tree or not.

To do so, we first create two helper functions that can determine whether all of the nodes of a tree are less than (or greater than) a particular int value:

```
(* helper functions for writing is_bst *)
(* (tree_less t n) is true when all nodes of t are
   strictly less than n
let rec tree_less (t:tree) (n:int) : bool =
 begin match t with
   | Empty -> true
    | Node(lt, x, rt) ->
       x < n && (tree_less lt n) && (tree_less rt n)
  end
(* (tree_gtr t n) is true when all nodes of t are
  strictly greater than n
let rec tree_gtr (t:tree) (n:int) : bool =
 begin match t with
   | Empty -> true
    | Node(lt, x, rt) ->
        x > n && (tree_gtr lt n) && (tree_gtr rt n)
  end
```

The is_bst function uses these two helpers to directly encode the binary search tree invariant as a program:

¹²¹ if you're interested in such datastructures.

```
(* determines whether t satisfies the bst invariant *)
let rec is_bst (t:tree) : bool =
  begin match t with
  | Empty -> true
  | Node(lt, x, rt) ->
        is_bst lt && is_bst rt &&
        (tree_less lt x) && (tree_gtr rt x)
end
```

This solution isn't very satisfactory, though. It is very unlikely that some tree we happen to obtain from somewhere actually satisfies the binary search tree invariant. Moreover, checking that the tree satisfies the invariant is pretty expensive.

A better way to construct a binary search tree, is to start with a simple binary search tree like Empty, which trivially satisfies the invariant, and then insert or delete nodes as desired to obtain a new binary search tree.

Each operation must *preserve* the binary search tree invariant: given a binary search tree t as input, insert t n should produce a new binary search tree that contains the same set of elements as t but additionally contains n. If t happens to already contain n, then the resulting tree is just t itself.

How can we implement such an insertion function? The key idea is that inserting a new element is just like searching for it—if we happen to find the element we're trying to insert, then the result is just the input tree. On the other hand, if the input tree does not already contain the element we're trying to insert, then the search will find a <code>Empty</code> tree, and we just need to replace that empty tree with a new leaf node containing the inserted element. In code:

The code for insert exactly mirrors that of lookup, except that it returns a tree at each stage rather than simply searching for the element. We have to check that the resulting tree maintains the binary search tree invariant, but this is easy to see, since we only ever insert a node n to the left of a node n when n is strictly less than n. (And similarly for insertion into the right subtree.)

Deletion is more complex, because there are several cases to consider. If the node we are trying to delete is not already in the tree, then <code>delete</code> can simply return the original tree. On the other hand, if the node is in the tree, there are three possibilities. First: the node to be deleted is a leaf. In that case, we simply remove the leaf node by replacing it with <code>Empty</code>. Second, the node to be deleted has exactly one child. This case too is easy to handle: we just replace the deleted node with its child tree. The last case is when the node to be deleted has two non-empty subtrees. The question is how delete the node while still maintaining the binary search tree invariant.

This requires a bit of cleverness. Observe that the left subtree must be non-empty, so it by definition contains a *maximal* element, call it m, that is still strictly less than n, the node to be deleted. Note also that m is *strictly less* than all of the nodes in the right subtree of n. Both of these properties follow from the binary search tree invariant. We can therefore *promote* m to replace n in the resulting tree, but we have to also remove m (which is guaranteed to be a leaf) at the same time.

Putting all of these observations together gives us the following code:

```
(* returns the maximum integer in a NONEMPTY bst t *)
let rec tree_max (t:tree) : int =
 begin match t with
   | Empty -> failwith "tree_max called on empty tree"
    | Node (_, x, Empty) -> x
   | Node (_,_,rt) -> tree_max rt
  end
(* returns a binary search tree that has the same set of
  nodes as t except with n removed (if it's there) *)
let rec delete (n:int) (t:tree) : tree =
 begin match t with
    | Empty -> Empty
    | Node(lt,x,rt) ->
        if x = n then
          begin match (lt,rt) with
            | (Empty, Empty) -> Empty
            | (Node _, Empty) -> lt
            | (Empty, Node _) -> rt
            | _ -> let m = tree_max lt in
                Node (delete m lt, m, rt)
          end
        else
          if n < x then Node(delete n lt, x, rt)</pre>
          else Node(lt, x, delete n rt)
  end
```

Chapter 8

Generic Functions and Datatypes

Consider these two functions that compute the lengths of either an int list (length1) or a string list (length2):

```
let rec length1 (l:int list) : int =
  begin match 1 with
  | [] -> 0
  | _::tl -> 1 + (length1 tl)
  end

let rec length2 (l:string list) : int =
  begin match 1 with
  | [] -> 0
  | _::tl -> 1 + (length2 tl)
  end
```

Other than the type annotation on the argument 1, both functions are *identical*—they follow exactly the same algorithm, independently of the kind of elements stored in the lists.

Computing a list length is an example of a *generic function*. In this case, the function is generic with respect to the type of list elements. Modern programming languages like OCaml (and also including Java and C#) provide support for writing such generic functions so that the same algorithm can be applied to many different input types.

For example, to write one length function that will work for *any* list, we can write:

```
(* a generic version of length *)
let rec length (l:'a list) : int =
  begin match l with
  | [] -> 0
  | _::tl -> 1 + (length tl)
  end
```

The only difference between this generic version and the two above, is that the type of the argument 1 is 'a list. Here the 'a is a *type variable*; a place holder for types. The type of length says that it works for an input of type 'a list where 'a can be instantiated to *any* type.

For example, given the definition above, we can pass length a list of integers or a list of strings:

OCaml uses the type of the list passed in to length to figure out what the 'a should be. In the first case, the type 'a is instantiated to int, in the second, 'a is instantiated to string.

The length function doesn't need to do anything with the elements of the list, but there are generic functions that can manipulate the list elements. For example, here is how we can write a generic append function that will take two lists of the same element type and compute the result of appending them:

```
(* generic append *)
let rec append (l1:'a list) (l2:'a list) : 'a list =
  begin match l1 with
  [] -> 12
  [ h::tl -> h::(append tl l2)
  end
```

Here there are a couple of observations to make. First, the type variable 'a appears in the types of two different inputs (11 and 12); this means that whenever OCaml figures out what type 'a stands for, it must agree with both list arguments—it is not possible to call append with a int list as the first argument and a string list as the second argument. Second, the result type of the function also mentions 'a, which means that the element type of the resulting list is the same as the element types of both the input lists. Finally, note that we can still use pattern matching to manipulate generic data: since 11 has type 'a list we know that inside the case for

cons h must be of type 'a and tl itself has type 'a list.

Functions may be generic with respect to more than one type of value. For example, below is a generic version of the zip function that we saw in $\S4.5$ (the version there worked only with inputs of type int list and string list):

```
let rec zip (l1:'a list) (l2:'b list) : ('a*'b) list =
  begin match (l1,l2) with
  | ([], []) -> []
  | (h1::tl1, h2::tl2) -> (h1,h2)::(zip tl1 tl2)
  | _ -> failwith "zip called on unequal length lists"
  end
```

Some examples of using zip show how it behaves "the same" no matter which types the 'a and 'b variables are instantiated to:

```
'a = int and 'b = string:
    zip [1;2;3] ["uno", "dos", "tres"] =>
    [(1,"uno"); (2,"dos"); (3,"tres")]
'a = int and 'b = int:
    zip [1;2;3] [4;5;6] => [(1,4); (2,5); (3,6)]
'a = bool and 'b = int:
    zip [true; false] [1;2] => [(true,1); (false,2)]
```

8.1 User-defined generic datatypes

We saw in §5 how programmers can define their own datatypes in OCaml, but we haven't yet seen how to define a generic datatype like OCaml's built in list. The idea is straightforward: we create a generic datatype by parameterizing the type by type variables ('a, 'b, etc.) just like the ones used to write down the types in a generic function.

Recall the definition of int-labeled binary trees that we worked with in $\S 6$:

```
(* non-generic binary trees with int labels *)
type tree =
    | Empty
    | Node of tree * int * tree
```

We can make this into a generic binary tree type by adding a type parameter like so:

```
(* generic binary trees labeled by 'a values *)
type 'a tree =
    | Empty
    | Node of ('a tree) * 'a * ('a tree)
```

Note the differences: we have generic type 'a tree that represents binary trees all of whose nodes are contain values of type 'a. Different concrete instances of such trees may instantiate the 'a variable differently. The type variable 'a is a type, so it can be used as part of a tuple, as shown in the case for the Node constructor. The recursive occurrences of tree must also be parameterized by the same 'a—this ensures that all of the subtrees of an 'a tree have nodes consistently labeled by 'a values.

Here are some examples:

```
Node (Empty, 3, Empty) : int tree

Node (Empty, "abc", Empty) : string tree

Node (Node (Empty, (true, 3), Empty),

(false, 4), Empty) : (bool * int) tree

Node (Node (Empty, 3, Empty), "abc", Empty) 

Error! ill-typed
```

Such generic datatypes can be computed with by pattern matching, just as we saw earlier. In particular, the constructors of the datatype form the patterns, and those patterns bind identifiers of the appropriate types within the branches. For example, we can write a generic function that "mirrors" (i.e. recursively swaps left and right subtrees) like this:

```
let rec mirror (t:'a tree) : 'a tree =
  begin match t with
  | Empty -> Empty
  | Node(lt, x, rt) -> Node(mirror rt, x, mirror lt)
  end
```

In the branch for the Node constructor, the identifiers lt and rt have type 'a tree and identifier x has type 'a. Since this function doesn't depend on any particular properties of 'a it is truly generic.

8.2 Why use generics?

Why are generic functions and datatypes valuable? They allow programmers to re-use algorithms in many contexts. For example, we can define lots of different list functions generically and then re-use them for any particular kind of list we happen to need. In particular, the designers of the generic list functions don't have to be aware of what particular kind of list elements some future program might happen to use. A programmer may find herself needing a widget list in a graphics program, but if she needs to know its length, then the generic list length will do the trick. Importantly, generic functions work even for types not yet defined when the generic function or datatype was created.

This flexible re-use of code has another benefit: it means less work debugging lots of specialized versions of the same thing. If we had to write a list length function for every type of list element, then we would have to have many copies of essentially the same program. Such code duplication becomes a nightmare to maintain in larger-scale software systems. Imagine needing to keep twenty "almost identical but not quite" versions of the same function in sync—if you find a bug in one instance of the code, you have to patch it the same way in all nineteen other instances.

Chapter 9

Modularity and Abstraction

In this chapter we consider another mechanism for re-using code in different contexts: abstract types and modules. The key idea of an abstract type is to bundle together the name of a fresh type together with operations for working with that new type. This interface specifies all of the ways that values of the new type can be created and used. The type is considered to be abstract because the interface does not reveal details about how the type is implemented "behind the scenes". Instead, various code modules can each provide different implementations of the same interface, perhaps with different performance characteristics.

9.1 A motivating example: finite sets

Recall from your mathematics courses the notion of a *set*. A set is an un-ordered collection of distinct elements. In mathematical notation, sets are usually written by writing down elements inside of $\{$ and $\}$ brackets, though sometimes the empty set is written \emptyset . Here are some examples:

$$\begin{cases}
 1, 2, 3, 4 \\
 a, b, c \\
 \{(1, 2), (3, 4), (5, 6)\}
 \end{cases}$$

Even though these sets are written using a list-like notation, the order of the elements doesn't matter. That is, according to mathematics:

$$\{1,2,3\} = \{3,2,1\} = \{2,1,3\}$$

Given a set S, we use the mathematical notation $x \in S$ to indicate the proposition that x is an element of the set S. Therefore, we have, for example:

$$1 \in \{1, 2, 3\}$$

In math, we have various operations that operate on sets. For example, we can combine two sets by taking their *union*, written $S_1 \cup S_2$, which is the set containing exactly the elements found in either S_1 or S_2 :

$$\{1,2,3\} \cup \{2,3,4,5\} = \{1,2,3,4,5\}$$

Similarly, set *intersection* $S_1 \cap S_2$ is the set containing exactly the elements found in both S_1 and S_2 :

$$\{1,2,3\} \cap \{2,3,4,5\} = \{2,3\}$$

Just as the list abstraction occurs naturally in many problem domains, so too does the notion of *set*: the set of students in a class, the set of coordinates that make up a picture, the set of answers to a survey, the set of data samples from an experiment, *etc.*. That's why the idea of a "set" occurs so frequently in math and computer science—it's a really fundamental concept that appears just about everywhere.

The difference for programming is that OCaml already provides a built-in notion of lists, but the programmer has to implement the set abstraction herself.¹

9.2 Abstract types and modularity

Suppose we want to implement a type of sets in OCaml. How do we go about that process? The first step of design, as always, is to understand the problem—what concepts are involved and how do they relate to one another. Clearly, sets contain elements, but, just as we can have a list of integers and a list of strings, the element type can vary from set to set. Thus, we expect the set type to be generic over its element type:

¹Actually OCaml's libraries do provide an implementation of sets in the set module; here we'll see how one could write this library oneself.

```
type 'a set = ... (* 'a is the type of elements *)
```

How do we create a set and how do we manipulate the sets once we have them? Here there are many possible design alternatives: we are looking for a simple list of operations that will allow us to create and use sets flexibly. We certainly need a way of creating an empty set, and it seems reasonable to be able to add an element to or remove an element from an existing set. Taking a cue from mathematics, we might also consider adding a union operation. It is also worth thinking about how sets relate to other datatypes like lists: for example, we might want to be able to create a set out of a list of elements. Putting all of these considerations together, we arrive at the following operations for creating sets:

```
let empty : 'a set = ...
let add (x:'a) (s:'a set) : 'a set = ...
let remove (x:'a) (s:'a set) : 'a set = ...
let union (s1:'a set) (s2:'a set) : 'a set = ...
let list_to_set (l:'a list) : 'a set = ...
```

We also need a way of examining the contents of a set, determining whether a given set is empty, or whether it is equal to another set. It might also be useful to be able to enumerate the elements of a set as a list. This yields these further operations:

```
let is_empty (x:'a set) : bool = ...
let member (x:'a) (s:'a set) : bool = ...
let equal (s1:|a set) (s2:|a set) : bool = ...
let elements (s:'a set) : 'a list = ...
```

Interfaces: .mli files and signatures

Having understood the concepts related to the set datatype and identified the operations that connect them, we can now proceed to the second step of the design process: formalizing the interface. To do so, we need to understand a bit about how programming languages package together code as re-usable components.

In programming languages jargon, a *module* is an independently-compilable collection of code that (typically) provides a few data types and their associated operations. Modules provide a way of decomposing large software projects into several different pieces, each of which can be de-

veloped in isolation. Modules that are intended to provide common and widely-used implementations of datastructures, algorithms, or other operations, are often called *libraries*.

A key feature of modules is that they provide boundaries between different parts of a program. Modules separate code at *interfaces*, which specify the ways in which external code (outside the module) can legally interact with the module's *implementation*, which is the code inside the module that determines the behavior of the module's operations.

The point of the interface is that code outside the module can be written only with reference to the interface—the external code can't (and shouldn't) depend on the particular details of how the operations supported by the interface are implemented.

Different programming languages provide different mechanisms for specifying module interfaces—C uses "header" files and Java uses the interface keyword, for example. As we shall see, OCaml uses either a .mli file or a "module type signature". The commonality among these approaches is the ability to write down a specification using the types of the operations in the module.

For the 'a set example above, if we look at only the types of each of the operations, we are left with this type signature:

Note that we are using the "arrow" notation to specify function types (see §2.7), so we can read the type of add, for example, as a function that takes a value of type 'a and and 'a set and returns an 'a set. Also note that, unlike an implementation, we use the keyword val (instead of let) to say that any module that satisfies this interface will provide a named value of the appropriate type. So any implementation of the set module must provide an add function with the type mentioned above.

OCaml provides two ways of defining module interfaces. The first way is to use OCaml modules corresponding to file names. In this style, we put the above interface code in a file ending with the <code>.mli</code> extension, for example <code>ListSet.mli</code>, and the implementation in a similarly-named <code>.ml</code> file, for example <code>ListSet.ml</code>. The "i" part of the file extension stands for "interface", and each OCaml <code>.ml</code> file is, by default, associated with the correspondingly named <code>.mli</code> file.²

The second way to define an interface is to use an explicitly named module type signature. For example, we might put the following type signature in a file called MySet.ml:

This program gives the name <code>Set</code> to the interface (a.k.a. module type) defined by the signature between the <code>sig</code> and <code>end</code> keywords. Other code can appear before or after this declaration, but it won't be considered part of the <code>Set</code> signature.

We can also create an explicitly-named module with a given interface using a similar notation. Rather than put the code implementing each set operation in a .ml file, we do this:

²In fact, if you don't create a .mli file for a given .ml file, the OCaml compiler will create one for you by figuring out the most liberal interface it can for the given implementation. You may have noticed these files appearing when you work with OCaml projects in Eclipse.

```
module LSet : Set = struct
    type 'a set = ...

let empty : 'a set = ...
let add (x:'a) (s:'a set) : 'a set = ...
let remove (x:'a) (s:'a set) : 'a set = ...
let union (s1:'a set) (s2:'a set) : 'a set = ...
let list_to_set (l:'a list) : 'a set = ...

let is_empty (x:'a set) : bool = ...
let member (x:'a) (s:'a set) : bool = ...
let equal (s1:|a set) (s2:|a set) : bool = ...
let elements (s:'a set) : 'a list = ...
end
```

Here the keywords **struct** and **end** delineate the code that is considered to be part of the LSet module. The advantage of having a named interface is that we can re-use it in other contexts. For example, we might create a second, more efficient, implementation of sets in a new module:

```
module BSet : Set = struct
    ... (* a different implementation of sets *)
end
```

Regardless of whether we choose to use .mli files or explicitly-named interfaces, OCaml will check to make sure that the implementation actually complies with the interface. This means that every operation, type, or value declared in the interface must have an identically-named, but fully realized, implementation in the module. Moreover, OCaml will check that the implementation and the interface agree with respect to the types they use. The implementation may include more than necessary to meet the interface—it can contain extra types, helper functions, or auxiliary values that aren't revealed by the interface.

Because each file of an OCaml program corresponds to a module, if we want to access components of one file from another file, we have to either use the module "dot" notation or open the module to expose the identifiers it defines. For example, if we have defined the set module in ListSet.ml (whose interface is given by ListSet.mli), and we want to use those operations in a different module found in Foo.ml, we write ListSet.<identifier> inside of Foo.ml. For example, we might write:

```
let add_to_set (s:int ListSet.set) : int ListSet.set =
  ListSet.add 1 (ListSet.add 2 s)
```

This can become burdensome, so OCaml also provides the open command, which reveals all of the operations defined in a module's interface without the need to use the ListSet. prefix. The following is equivalent to the above:

```
;; open ListSet

let add_to_set (s:int set) : int set =
   add 1 (add 2 s)
```

There is one gotcha—if we use explicitly named modules, we still need to either explicitly use dot notation for the implicitly defined module corresponding to the filename. For example, if the <code>Set</code> interface and the two modules <code>LSet</code> and <code>BSet</code> were all defined in the <code>MySet.ml</code> file, we could write:

```
;; open MySet          (* reveal the LSet and BSet modules *)

(* work with LSet values *)
let add_to_lset (s:int LSet.set) : int LSet =
    LSet.add 1 (LSet.add 2 s)

(* work with BSet values *)
let add_to_bset (s:int BSet.set) : int BSet =
    BSet.add 1 (BSet.add 2 s)
```

Implementations and Invariants

The power of abstract ypes as embodied by modules and interfaces is that the interface can *hide* representation details from clients of the module. In particular, the interface can *omit* the definition of how a particular type is implemented internally to the module.

Consider the Set module, for example. There are many possible ways we could imagine implementing a datastructure for sets. Since sets are similar to lists, except that sets contain no duplicates and are considered to be unordered, we might choose to *represent* a set by a list subject to an *invariant* that is enforced by the implementing module.

As specific examples, here are just a few of the many possible represen-

tations for the abstract type 'a set, along with an invariant that might be useful for implementing the set:

```
Representation Type Invariant
```

- 'a list no duplicate elements
- 'a list no duplicates, in sorted order
- 'a tree no duplicate elements
- 'a tree binary-search-tree invariants

Inside a module implementing the <code>Set</code> interface, we are free to choose any suitable type and invariants for concretely representing the abstract type 'a <code>set</code>. Inside the module, we can then implement the set operations in terms of that representation type. Crucially, if we are careful to ensure that any value of the abstract type produced by the module satisfies the representation invariants, we can assume that any such values passed in to the functions of the module will already satisfy the invariants—external code cannot violate the representation invariants.

Let us see how this is helpful by example. Suppose that we choose to implement the <code>Set</code> interface using <code>'a list</code> as the representation type and "no duplicates" as the invariant. We can proceed to implement the functions of the <code>Set</code> interface like so:

```
module LSet : Set = struct
  (* inside the module we represent sets as lists *)
  (* INVARIANT: the list contains no duplicates *)
  type 'a set = 'a list
  (* the empty set is just the empty list *)
  let empty : 'a set =
    []
  (* tests whether x is contained in the set s *)
  let rec member (x:'a) (s:'a set) : bool =
    begin match s with    (* use the fact that s is a list *)
    | [] -> false
    | y::rest \rightarrow x = y | | member x rest
    end
  (* add the element x to the set s *)
  (* NOTE: add produces a set, so it must maintain
   * the no duplicates invariant *)
  let add (x:'a) (s:'a set) : 'a set =
    if (member x s) then s (* x is already in the set *)
                 (* add x to the set *)
    else x::s
  (* remove the element x from the set s *)
  let rec remove (x:'a) (s:'a set) : 'a set =
    begin match s with
    [] -> []
    | y::rest ->
         if x = y then rest
                              (* x can't occur in rest
                                  because of the invariant *)
         else y::(remove x rest)
    end
   ... (* implement the rest of the operations *)
end
```

The choice of which invariants to maintain can impact the implementation of various operations. For example, to implement the equals operation on sets when representing them as lists with the "no duplicates" invariant, we must check that each element of the first list is a member of the second, and vice-versa. This expensive equality check is necessary because the invariant doesn't say anything about the ordering of elements

in the list, and sets are supposed to be unordered.

On the other hand, if we had chosen a stronger invariant, such as representing a set as a sorted list of elements (with no duplicates), then testing for equality simply amounts to checking that each list contains the same elements in order. The tradeoff is that with this stronger invariant, the add function becomes more expensive—we have to insert the newly added element at the appropriate location to maintain the sorting invariant.

9.3 Another example: Finite Maps

As another example of an abstract type, consider the problem of implementing a *finite map*, which is a data structure that keeps track of a finite set of *keys*, each of which is associated with a particular *value*. These kinds of datastructures are useful for representing things like dictionaries—here the keys are words and the values are their definitions. We could also use a finite map to capture the relationship between a collection of students and their majors in college.

Using an informal notation, we might write down a finite map from students to their majors like this:

```
\begin{array}{ccc} \text{Alice} & \mapsto & \text{CSCI} \\ \text{Bob} & \mapsto & \text{ESE} \\ \text{Chuck} & \mapsto & \text{FNCE} \\ \text{Don} & \mapsto & \text{BIOL} \end{array}
```

As with the sets, we can then think about which operations are needed to work with finite maps. Clearly we need ways of creating finite maps, adding key–value bindings to an existing map, looking up the value that corresponds to a key, *etc.*.

After some thought, we might arrive at an interface for finite maps that looks like this:

```
module type Map = sig
  (* a finite map from keys of type 'k to values of type 'v *)
  type ('k,'v) map

  (* ways to create and manipulate finite maps *)
  val empty : ('k,'v) map
  val add : 'k -> 'v -> ('k,'v) map -> ('k,'v) map
  val remove : 'k -> ('k,'v) map -> ('k,'v) map

  (* ways to ask about the contents of a finite map *)
  val is_empty : ('k,'v) map -> bool
  val mem : 'k -> ('k,'v) map -> bool
  val find : 'k -> ('k,'v) map -> 'v
  val keys : ('k,'v) map -> 'k list
  val values : ('k,'v) map -> 'v list
  val bindings : ('k,'v) map -> ('k*'v) list
end
```

Also as with sets, we can imagine many ways of concretely implementing such a finite map interface. For example, we can represent the type ('k,'v) map as a list of 'k*'v pairs, perhaps with an invariant that requires each key appearing in the list to be unique. We could also choose to implement finite maps using binary search trees, where we index the nodes by the key component and also store a value with each key.

If we follow the first approach, we might end up with this implementation of the interface above:

```
module ListMap : Map = struct

(* INVARIANT: each key occurs at most once in the list *)
type ('k,'v) map = ('k * 'v) list

let empty : ('k,'v) map = []

let is_empty (m:('k,'v) map) =
    m = []

let rec mem (k:'k) (m:('k,'v) map) : bool =
    begin match m with
    | [] -> false
    | (k1,_)::rest -> k1=k || mem k rest
end
```

```
let rec find (k:'k) (m:('k,'v) map) : 'v =
   begin match m with
     | [] -> failwith "Not found"
      (k1,v)::rest -> if k1=k then v else find k rest
    end
  let rec remove (k:'k) (m:('k,'v) map) : ('k,'v) map =
   begin match m with
      | [] -> []
      | (k1,v1)::rest ->
       if k1=k then rest
        else (k1, v1)::(remove k rest)
    end
  let add (k:'k) (v:'v) (m:('k,'v) map) : ('k,'v) map =
    (k,v)::(remove k m)
  let rec keys (m:('k,'v) map) : 'k list =
   begin match m with
      | [] -> []
      | (k, v)::rest -> k::(keys rest)
   end
  let rec values (m:('k,'v) map) : 'v list =
   begin match m with
     [] -> []
      | (k, v) :: rest -> v:: (values rest)
    end
  let bindings (m: ('k, 'v) map) : ('k*'v) list =
end
```

Chapter 10

First-class Functions

In this chapter, conclude our tour of value-oriented (or "declarative") programming by studying the ramifications of a beautiful and amazing fact: functions are values!

What do I mean by that? Well, just as the number 3 is an int that can be used as an argument to a function or as a value computed by a function, functions themselves can be used both as arguments to other functions and as the result of a computation.

For example, consider the following function called twice:

```
let twice (f:int -> int) (x:int) : int =
  f (f x)
```

twice itself takes an input f of function type! In this case, f should be an int -> int function. What can twice do with f? It can only *call* the function or pass it to some other function. Here, twice calls f on the result of calling f on the argument x.

How do we use such a function? We can call twice by passing it an argument of type int -> int. For example, suppose we define an add_one function:

```
let add_one (z:int) : int = z + 1
```

Then we can write the expression twice add_one 3, which will evaluate to the value 5. To see why, we just follow the familiar rules of substitution:

```
twice add_one 3

Add_one (add_one 3) substitute add_one for f and 3 for x in twice

Add_one (3 + 1) substitute 3 for z in add_one

Add_one 4 because 3+1 \implies 4

Add_one 5 substitute 4 for z in add_one

Because 4+1 \implies 5

Similarly if we have the first time.
```

Similarly, if we have the function square:

```
let square (z:int) : int = z * z
```

Then we have twice square 3 \Longrightarrow 81 because calling square twice computes the z to the 4th power.

10.1 Partial Application and Anonymous Functions

How do we return a function as the result of another function? Consider this example:

```
let make_incrementor (n:int) : int -> int =
  let helper (x:int) = n + x in
  helper
```

This function takes an int as input and *returns* a function of type int \rightarrow int. What does that function do? When it is called on some value x, it will compute the result n + x.

How does this function evaluate? If we apply make_incrementor to 3, we can compute as follows:

```
make_incrementor 3

→ let helper (x:int) = 3 + x in helper substitute 3 for n
```

At this point, we seem to get stuck: what value is computed for helper? More puzzling is how to think about a function that takes more than one argument. Suppose we apply the function to only one input—what happens then? Here's an example:

```
let sum (x:int) (y:int) : int = x + y   (* has two arguments *)
let sum_applied (x:int) : int -> int =
    sum x
```

The function sum has type int -> int -> int. If we partially apply it—give it only *some* of its inputs—then we can treat that partial application as a function! In this case, since we partially apply sum to an integer x, we are left with a function that expects only one input, namely y.

To explain how to compute with such partially applied functions and functions as results, we need to introduce one new concept: the *anonymous* function. An anonymous function is exactly what the term implies—it is a function without a name. Using OCaml syntax, we can write an anonymous function like this:

```
fun (x:int) \rightarrow x + 1
```

Here, the keyword **fun** indicates that we are creating a value of function type. In this case, the function takes one input called (x:int), and the body of the function is the expression x+1.

We can write an anonymous version of the sum function above like this:

```
fun (x:int) (y:int) \rightarrow x + y
```

These anonymous functions *are* values. If we want to give such a function a name, we can do so using the regular **let** notation. For example, the following definition is equivalent to the "named" version of sum given above:

```
let sum : int \rightarrow int \rightarrow int = fun (x:int) (y:int) \rightarrow x + y
```

Note: The syntax for anonymous functions, unlike named functions, does not have a place to write the return type. This is just an oddity of OCaml syntax; in practice OCaml can always figure out what the return type should be anyway.

We can apply an anonymous function just like any other function, by writing it next to its inputs and using parentheses to ensure proper grouping. We evaluate anonymous function applications by substituting argument value for the parameter name in the body of the function. In the case that there is more than one parameter, we simply keep around the <code>fun ... -> ...</code> parts until the function as been fully applied (i.e. it has been applied to enough parameters.

For example, let's see how the anonymous version of sum evaluates when applied to just a single input:

```
(fun (x:int) (y:int) → x + y) 3

→ (fun (y:int) → 3 + y) substitute 3 for x
```

The resulting anonymous function *is* the answer of such a computation. Having around anonymous functions means we can name such intermediate computations that result in functions. The fact that "named" definitions are just shorthand for the **let**-named anonymous functions, means we can now see all of the steps in a computation as simple substitution and primitive operations:

```
let sum (x:int) (y:int) : int = x + y
let add_three = sum 3
let answer = add_three 39
\mapsto (by equivalence of named an let-bound anonymous forms)
let sum = fun (x:int) (y:int) \rightarrow x + y
let add_three = sum 3
let answer = add_three 39
\longmapsto (substituting the definition of sum)
let sum = fun (x:int) (y:int) \rightarrow x + y
let add_three = (fun (x:int) (y:int) -> x + y) 3
let answer = add_three 39
\longmapsto (substituting 3 for x)
let sum = fun (x:int) (y:int) \rightarrow x + y
let add_three = (fun (y:int) -> 3 + y)
let answer = add_three 39
→ (substituting the definition of add_three)
let sum = fun (x:int) (y:int) \rightarrow x + y
let add_three = (fun (y:int) -> 3 + y)
let answer = (fun (y:int) \rightarrow 3 + y) 39
\longrightarrow (substituting 39 for y)
let sum = fun (x:int) (y:int) \rightarrow x + y
let add_three = (fun (y:int) -> 3 + y)
let answer = 3 + 39
\longrightarrow (because 3+39 \Longrightarrow 42)
let sum = fun (x:int) (y:int) \rightarrow x + y
let add_three = (fun (y:int) -> 3 + y)
let answer = 42
```

10.2 List transformation

What can we do with first-class functions? They provide a powerful way to share the common features of many algorithms. As a simple example, consider these two list operations that we saw in the list implementation of finite maps (§9.3):

These functions are nearly identical—each one processes the elements of the input list of key–value pairs in turn, projecting out either the key component or the value component as appropriate.

We can reorganize this program to exploit that common structure by creating a helper function parameterized by a function that says what to do with the key-value pair:

After factoring out this common algorithm, we can then express keys and values in terms of this helper by remember that the fst function returns the first element of a pair and the snd function returns the second element.

Now observe that the helper function doesn't really depend on the fact that it is processing key-value pairs. We can further generalize by observing that the helper can be made to work over *all* lists, regardless of their element types, by simply giving f the right type. This leads to to the following function, called transform:¹

This list transformer applies the function f to each element of the input list and returns the resulting list—it transforms a list of 'a values into a list of 'b values. Such transformations are extremely fundamental to any list-processing programs, so this operation is very useful in practice. It also combines well with anonymous functions, since you can pass an anonymous function as the argument f.

Let's look at some examples:

```
transform String.uppercase ["abc"; "dog"; "cat"]

\Rightarrow ["ABC"; "DOG"; "CAT"]

transform (fun (x:int) -> x+1) [1;2;3;4]

\Rightarrow [2;3;4;5]

transform (fun (x:int) -> x * x) [1;2;3;4]

\Rightarrow [1;4;9;16]

transform string_of_int [1;2;3]

\Rightarrow ["1"; "2"; "3"]

transform (fun (x:(int*int)) -> (fst x) + (snd x)) [(1,2); (3,4); (5,6)]

\Rightarrow [3; 7; 11]
```

¹In an unfortunate accident of fate, the transform function is also often called map—the intuition is that the function *maps* a given function across each element of the list. This use of the word "map" is not to be confused with the abstract type of finite maps we saw in §9.3.

10.3 List fold

The list transformation function captures one common idiom of list processing, but it is possible to generalize even further. Consider these three functions that are defined using the standard list recursion pattern:

The comments in the code above indicate the common features of these functions. For *any* function defined by structural recursion over lists, there are two things to consider: First, what should the function return in the case that the list is empty? This is called the *base* case of the recursion because it is where the chain of recursive calls "bottoms out." Second, assuming that you know the value computed by the recursive call on the tail of the list, how do you *combine* that result with the head of the list to compute the answer for the whole list?

In the case of the the list length function, for example, the base case says that the empty list has length 0. The recursive case combines the value of the recursive call length tl with the head of the list (which happens to be ignored) to compute 1 + (length tl).

For the exists function, which determines whether a list of bool values contains true, the base case indicates that the empty list does not contain true (i.e. the result is false). The recursive case computes the answer for the whole list with head x and tail tl by simply returning true either when x is true or when exists tl evaluates to true—combining the head with the recursive call is just taking their logical "or".

For reverse, the base case says that reversing the empty list is just the empty list, and the recursive case says that we can combine the reversal of the tail with x to obtain a completely reversed list by just appending [x] at then end of the reversed tail.

So what? All three functions follow the same recursive pattern. We can expose this common structure by creating a *single* function that is parameterized by the base value and the combine operation—those are the only places where our three examples differ.

Let's call this function <code>fold</code>—it "folds up" a list into an answer by following structural recursion. To make <code>fold</code> as generic as possible, let's consider implementing it for an arbitrary list of type 'a list. The result type of a structurally recursive function varies from application to application, so we expect the result type of <code>fold</code> to be generic, and, as shown by the <code>length</code> and <code>exists</code> examples, it could be different from the element type of the list we're folding over. So, the return type of <code>fold</code> should be some type 'b. Those choices dictate the type of <code>base</code> and <code>combine</code>: <code>base</code> must have type 'b since it is the "answer" for the empty list. Similarly, <code>combine</code> takes the head element of the list, which has type 'a, and the answer obtained from the recursive call on the tail of the list, which has type 'b, and produces an answer, which must also be of type 'b.

These considerations lead us to this definition of fold:

This recursive function is embodies the *essence* of structural recursion over lists—it is parameterized exactly where there can be some choice about what to do. Note that the first argument passed to combine is x and that the second argument is the result of recursively folding (with the same combine and base) over the t1.

What is fold useful for? Well, we can easily re-implement the three examples above like this:

```
let length2 (l:'a list) : int =
  fold (fun (x:'a) (length_tl:int) -> 1 + length_tl) 0 l

let exists2 (l:bool list) : bool =
  fold (fun (x:bool) (exists_tl:bool) -> x || exists_tl) false l

let reverse2 (l:'a list) : 'a list =
  fold (fun (x:'a) (reverse_tl:'a list) -> reverse_tl @ [x]) [] l
```

I've named the second parameter of the anonymous functions that get passed as fold's combine operation to remind us how that parameter is related to the recursive call—there is no other particular significance to the choice of length_tl, for example. We could equally well have written length2 like this:

```
let length2 (l:'a list) : int =
  fold (fun (x:'a) (y:int) -> 1 + y) 0 l
```

Any function that you can write by by structural recursion can be expressed using fold. Here, for example, is how to reimplement the transform function:

```
let transform (f:'a -> 'b) (l:'a list) : 'b list =
  fold (fun (x:'a) (trans_tl:'b list) -> (f x)::trans_tl) [] l
```

Chapter 11

Partial Functions: option types

Consider the problem of computing the maximum integer from a list of integers. At first sight, such a problem seems simple—we simply look at each element of the list and retain the maximum. We can start to program this functionality very straightforwardly by using the by-now-familiar list recursion pattern:

Unfortunately, this program doesn't have a good answer in the case that the list is empty—there is no "maximum" element of the empty list.

What can we do? One possibility is to simply have the <code>list_max</code> function fail whenever it is called on an empty list. This solution requires that we handle three separate cases, as shown below:

```
let rec list_max (l:int list) : int =
  begin match l with
    | [] -> failwith "list_max called on []"
    | x::[] -> x
    | x::tl -> max x (list_max tl)
    end
```

The cases cover the empty list, the singleton list, and a list of two-or more elements. We have to separate out the singleton list as a special case because it is the first length for which the <code>list_max</code> function is well defined.

This solution is OK, and can be very appropriate if we happen to know by external reasoning that <code>list_max</code> will never be called on an empty lists. We saw such use of failure in the <code>tree_max</code> function used to find the maximal element of a *nonempty* binary search tree in §6. However, what if we can't guarantee that the <code>list_max</code> function won't be called on an empty list? How else could we handle this possibility without failing, and thereby aborting the program¹

The problem is that <code>list_max</code> is an example of a partial function—it isn't well-defined for all possible inputs. Other examples of partial functions that you have encountered are the integer division operation, which isn't defined when dividing by <code>0</code>, and the <code>Map.find</code> function, which can't return a good value in the case that a key isn't in its set of key–value bindings.

It turns out that we can do better than failing, and, moreover, we already have all the tools needed. The idea is to create a datatype that explicitly represents the absence of a value. We call this datatype the 'a option datatype, and it is defined like this:

```
type 'a option =
    None
    Some of 'a
```

There are only two cases: either the value is missing, represented by the constructor None, or the value is present, represented by Some v. As with any other datatype, we use pattern matching to determine which case occurs.

Option types are very useful for representing the lack of a particular value. For a partial function like <code>list_max</code>, we can alter the return type to specify that the result is optional. Doing so leads to an implementation like this:

¹OCaml, like Java and other modern languages, supports *exceptions* that can be caught and handled to prevent the program from aborting in the case of a failure. Exceptions are another way of dealing with partiality; we will cover them later in the course.

As you can see, this implementation handles the same three cases as in the one that uses failwith; the difference is that after the recursive call we must explicitly check (by pattern matching against the result) whether list_max tl is well defined.

At first blush, this seems like a rather awkward programming style, and the need to explicitly check for None versus Some v onerous. However, it is often possible to write the program in such a way such checks can be avoided. For example, here is a cleaner way to write the same list_max function by using fold:

```
let rec list_max (l:int list) : int option =
  begin match l with
  [] -> None
  | x::tl -> Some (fold max x tl)
  end
```

The expression fold $\max \times \text{tl}$ takes the maximum element from among those in tl and x, which is always well-defined.

It is also worth pointing out that because the type 'a option is distinct from the type 'a, it is never possible to introduce a bug by confusing them—OCaml will force the programmer to do a pattern match before being able to get at the 'a value in an 'a option.

For example, suppose we wanted to find the sum of the maximum values of each of two lists. We can write this program as:

```
let sum_two_maxes (l1:int list) (l2:int list) : int option =
  begin match (list_max l1, list_max l2) with
  | (None, None) -> None
  | (Some m1, None) -> Some m1
  | (None, Some m2) -> Some m2
  | (Some m1, Some m2) -> Some (m1 + m2)
  end
```

Here we are forced to explicitly think about what to do in the case that both lists are empty—here we make the choice to make <code>sum_two_maxes</code> itself return an <code>int option</code>. The option types prevent us from mistakenly trying to naively do (<code>list_max 11</code>) + (<code>list_max 12</code>), which would result in a program crash (or worse) if permitted.

In languages like C, C++, and Java that have a null value which can be given *any* type, it is an extremely common mistake to conflate null, which should mean "the lack of a value," with "an empty value" of some type. For example, one might try to represent the empty list as null. However, such conflation very often leads to so-called "null pointer exceptions" that arise because some part of the program treats a null as though it has type 'a, when it is really meant to be the None of an 'a option.

There is a big difference between "the absence of a list" and "an empty list"—it makes sense to insert an element into the empty list, for example, but it never makes sense to insert an element into "the absence of a list."

Sir Tony Hoare, Turing-award winner and a researcher scientist at Microsoft, invented the idea of null in 1965 for a language called ALGOL W. He calls it his "billion-dollar mistake" because of the amount of money the software industry has spent fixing bugs that arise due to unfortunate confusion of the 'a and 'a option types. Option datatypes provide a simple solution to this problem.

We will see that option types also play a crucial role when we study linked, mutable datastructures in §16.

Chapter 12

Unit and Sequencing Commands

This Chapter studies a very uninteresting datatype: unit. This datatype is uninteresting because it contains exactly one value, called the unit value and written (). However, although unit itself is uninteresting, it is still *useful*. Here we will see why.

We have already seen unit in action in a couple of places. First, in OCaml, every function takes exactly one argument—we can use the *unit* type to indicate that the argument is uninteresting:

```
let f (x:unit) : int = 3
```

Since there is only one value of type unit, we can omit the x:unit in the definition above, to obtain the equivalent:

```
let f () : int = 3
```

This function takes the unit argument and produces the value 3; it has type unit \rightarrow int. We call it, as usual, by function application to the (only!) value of type unit, like this: f ().

The unit value is first class, and we can use it in **let** bindings and pattern matching like this:

As with tuples (and other datatypes that require only one branch when

pattern matching), we can also pattern match in let and fun bindings:

```
let () = print_string "hello"
let g : unit -> int = fun () -> 3
```

We have been using functions that take unit inputs to write the test predicates of the homework assignments, typically something like:

```
let test () : bool =
  length [1;2;3] = 3
```

Here, test: unit -> bool is a function.

We have also seen functions that *return* unit values: these are the *commands*. Since commands don't return any interesting data, the only reason to run them is for their *side effects* on the state of the computer. Here are some commands that we have seen, and their types:

```
print_string : string -> unit
print_endline : string -> unit
    print_int : int -> unit
    run_test : string -> (unit -> bool) -> unit
```

So far, we have seen how to run these commands at the program's top level, using the ;; notation:

```
;; print_string "this prints a string"
```

We can also embed commands within expressions using a binary operator called ';'. The idea is that e1; e2 first runs e1, which must be an expression of type unit, which may have side effects. The resulting () value is discarded and then e2 is evaluated. Thus, the ; operator lets us sequence commands.

```
let ans : int =
  print_string "printing is a side effect";
17
```

This program prints the string as a side effect and then binds the identifier ans to the value 17. Note that ; is an infix operator—you will get error messages if you write a ; after the second expression.

```
let ans : int =
   print_string "printing is a side effect";
   17;  (* <-- don't put a semicolon after the second expression! *)</pre>
```

As usual, we can nest expressions, and use them inside of local lets.

This is very useful for printing out information inside a function body, for example:

```
let f (x:int) : int =
  print_string "x is ";
  print_int x;
  print_string "\n";
  x + x
```

12.1 The use of ';'

We have now seen several places where the symbol ';' appears in OCaml programs (and we'll see one more in the next section).

Unfortunately, ; in OCaml means different things depending on how it is used. Also unfortunately, none of those usages corresponds exactly to how ; is used in "usual" imperative programming as in C or Java.

In OCaml programs (but not the Toplevel loop), ; is always a *separator*, not a *terminator*. The list below collects together all the syntax combinations that use ;

```
i; open Assert open a module at the top-level of a program
i; print_int 3 run a command at the top-level of a program
i[1; 2; 3] separate the elements of a list
sequence a command elements of a list
sequence a command elements of a record type (see §13)
if x=3; y=4}
```

We have also seen that, when executing OCaml expressions in the toplevel interactive loop, we use ;; as a terminator to let OCaml know when to run a given expression.

Chapter 13

Records of Named Fields

13.1 Immutable Records

Tuples are a light-weight way to collect together a small number of data values into a coherent package. Sometimes, though, it is nice to give *names* to the different components of such a package so that we can easily remember what the different parts are, and access them.

OCaml, like most other languages, provides a datatype of *records* that are designed specifically for this purpose. As we shall see in the upcoming course material, the humble record plays an important role in both imperative and object-oriented programming. Here we study the basics.

Record types are like tuples with named fields. The type is written as a list of $\langle id \rangle$: $\langle type \rangle$ pairs between $\{\ \}$ brackets. For example, suppose we wanted to create a program for manipulating color data as part of an image-manipulation package. The color data comes as red, green, and blue components. We could define a suitable type like this:

```
type rgb = {r:int; g:int; b:int} (* a type for colors *)
```

The values of the rgb type are records written using similar syntax:

```
(* Some rgb values *)
let red : rgb = {r=255; g=0; b=0;}
let blue : rgb = {r=0; g=0; b=255;}
let green : rgb = {r=0; g=255; b=0;}
let black : rgb = {r=0; g=0; b=0;}
let white : rgb = {r=255; g=255; b=255;}
```

Given one of these rgb values, we can access each field of the record using "dot" notation: value.field. For example, to write a function that averages each component of a record, we would write:

```
(* using 'dot' notation to project out components *)
(* calculate the average of two colors *)
let average_rgb (c1:rgb) (c2:rgb) : rgb =
    {r = (c1.r + c2.r) / 2;
    g = (c1.g + c2.g) / 2;
    b = (c1.b + c2.b) / 2;}
```

For example, we can calculate that:

```
average_rgb red blue \Longrightarrow {r=127; g=0; b=127}
```

Because records often contain many fields, it is useful to be able to create a copy of the record that differs from the original in only a few places. The with notation for records does exactly that. It is used as follows:

```
(* using 'with' notation to copy a
   record but change one (or more) fields *)
let cyan = {blue with g=255}
let magenta = {red with b=255}
let yellow = {green with r=255}
```

For example, we have cyan \Longrightarrow {r=0; g=255; b=255}, namely a copy of the blue value where the g field has been replaced by 255. Note that the with notation encloses a record expression (like blue) inside curly-braces. We can create a copy with more than one field replaced by listing each changed field: {blue with g=17; r=17}.

In this color example, each field has the same type, but that doesn't have to be the case. For example, we might create a record of employee data by doing something like:

```
type employee = {
  name : string;
  age : int;
  salary : int;
  division : string
}
```

Chapter 14

Mutable State and Aliasing

Up to this point, we have studied programming in a style that is mostly *pure*—we have worked with tree structured data that can be defined by recursive datatypes, and we have seen how recursive functions that follow that structure can be used to compute new values from old ones. This style of programming is called *pure* because we model computation as simply producing new values from old, proceeding by *substituting* values for the identifiers that name the results of intermediate computations. We can think of substitution as simply *copying* data (though efficient implementations won't do that, of course).

Pure programs work with *immutable* values—once a value has been named, the association between the identifier and its value is never altered thereafter. Pure programs are easy to reason about, since all computation can be explained by local reasoning with simple computation steps. This use of *persistent* data structures (ones that give don't change) can simplify many programming tasks, since you never have to worry about possibly destroying an old value when computing a new one. Moreover, since pure programs only *read* the data from existing values and never *modify* that data, it is easier to perform tasks in parallel—two computations running simultaneously on immutable data structures will never interfere with each other.

In contrast, most programming languages support a more *imperative* programming style, in which the program state is *mutable*, meaning that it

¹Of course we can *shadow* an existing occurrence of a name with a new binding, but that doesn't change the old value.

can be modified *in place*. Imperative programming is extremely useful in many situations, and it can simplify code that would otherwise be difficult to implement in a pure way.

Mutable state lets us write programs that exhibit "action at a distance"—in which two remote parts of the program interact with one another by modifying a shared piece of state. Such sharing can also be used to create non-tree-like data structures that have cycles or explicitly shared subcomponents. Mutable state also allows the possibility of efficient re-use of the computer's memory, since modifying a value in place doesn't require any copying or extra space. These features combine to make it possible to implement algorithms that have strictly better space requirements or performance characteristics than their pure, immutable counterparts.

However, although mutable state is powerful, it also requires us to radically modify the model of computation that we use to reason about our programs' behaviors. Since mutable state requires us to "update a value in place" we have to explain where the "place" is that is being updated. This seemingly simple change necessitates a much more complex view of the computer's memory, and we can no longer use the simple substitution model to understand how our programs evaluate.

The new computation model, called the *abstract stack machine*, accounts for all of the new behaviors introduced by adding mutable state. These include *aliasing*, which lies at the heart of shared memory, and the non-local memory effects, which make it harder to reason about programs.

14.1 Mutable Records

To see how the "action at a distance" provided by mutable state can simplify some programming problems, let's consider a simple task. Suppose we wanted to do a performance analysis of the delete operation for the binary search trees we saw in §7. In particular, suppose that we want to count the number of times that the helper function tree_max is called, either by delete or via recursion.

First, let's recall the definition of these functions:

```
(* returns the maximum integer in a NONEMPTY BST t *)
let rec tree_max (t:tree) : int =
 begin match t with
    | Empty -> failwith "tree_max called on empty tree"
    Node (\_, x, Empty) \rightarrow x
    | Node (_,_,rt) -> tree_max rt
  end
(* returns a binary search tree that has the same set of
   nodes as t except with n removed (if it's there)
let rec delete (n:'a) (t:'a tree) : 'a tree =
  begin match t with
    | Empty -> Empty
    | Node(lt,x,rt) ->
        if x = n then
          begin match (lt,rt) with
            | (Empty, Empty) -> Empty
            | (Node _, Empty) -> lt
            | (Empty, Node _) -> rt
            | _ -> let m = tree_max lt in
                Node (delete m lt, m, rt)
          end
        else
          if n < x then Node (delete n lt, x, rt)
          else Node(lt, x, delete n rt)
  end
```

It isn't too hard to modify the tree_max function to return both the maximum value in the tree and a count of the number of times that it is called (including by itself, recursively):

```
let rec tree_max2 (t:'a tree) : 'a * int =
  begin match t with
  | Empty -> failwith "tree_max called on empty tree"
  | Node(_,x,Empty) -> (x, 1)
  | Node(_,,rt) -> let (m, cnt) = tree_max2 rt in (m, cnt+1)
  end
```

Now to modify the delete function itself, we have to "thread through" this extra information about the count:

```
let rec delete2 (n:'a) (t:'a tree) : 'a tree * int =
 begin match t with
    | Empty -> (Empty, 0)
    | Node(lt,x,rt) ->
        if x = n then
          begin match (lt,rt) with
            | (Empty, Empty) -> (Empty, 0)
            | (Node _, Empty) -> (lt, 0)
            | (Empty, Node _) -> (rt, 0)
            _ -> let (m, cnt1) = tree_max2 lt in
                     let (lt2, cnt2) = delete2 m lt in
                         (Node (1t2, m, rt), cnt1 + cnt2)
          end
        else
          if n < x then
            let (lt2, cnt) = delete2 n lt in
            (Node(lt2, x, rt), cnt)
          else
            let (rt2, cnt) = delete2 n rt in
            (Node(lt, x, rt2), cnt)
  end
```

This is a bit clunky, but it gets even worse if we consider that code that uses the <code>delete2</code> method will have to be modified to keep track of the count too. For example, before these modifications, we could have written a function that removes *all* of the elements in a list from a tree very elegantly by using <code>fold</code> like this:

```
let delete_all (1: 'a list) (t: 'a tree) : 'a tree =
  fold delete t 1
```

After modifying delete to count the calls to tree_max, we now have the much more verbose:

```
let delete_all2 (1: 'a list) (t: 'a tree) : 'a tree * int =
  let combine (n:'a) (x:'a tree*int) : 'a tree * int =
    let (delete_all_tl, cnt1) = x in
    let (ans_t, cnt2) = delete2 n delete_all_tl in
        (ans_t, cnt1+cnt2)
in
fold combine (t,0) 1
```

Ugh!

Mutable state lets us sidestep having to change delete and the all of the code that uses it. Instead, we can declare a global *mutable* counter, which only needs to be incremented whenever tree_max is invoked. Let's see how to do this in OCaml:

```
type state = {mutable count : int}

let global : state = {count = 0}

let rec tree_max3 (t:'a tree) : 'a =
   globals.count <- globals.count + 1;  (* update the count *)
   begin match t with
   | Empty -> failwith "tree_max called on empty tree"
   | Node(_,x,Empty) -> x
   | Node(_,,rt) -> tree_max3 rt
   end
```

Here, the type state is a record containing a single field called count. This field is marked with the keyword mutable, which indicates that the value of this field may be updated in place. We then create an instance of this record type—I have chosen to call it global as a reminder that this state is available to be modified or read anywhere in the remainder of the program. (We'll see how to avoid such use of global state below, see §17.)

The only change to the program we need to make is to update the <code>global.count</code> at the beginning of the <code>tree_max</code> function. OCaml uses the notation <code>record.field <- value</code> to mean that the (mutable) <code>field</code> component of the given <code>record</code> should be updated to contain <code>value</code>. Such expressions are <code>commands</code>—they return a <code>unit</code> value, so the sequencing operator ';' (see §12) is useful when working with imperative updates.

Neither the delete nor the delete_all functions need to be modified. At any point later in the program, we can find out how many times the tree_max function has been called by by simply doing global.count. We can reset the count at any time by simply doing global.count <- 0.

14.2 Aliasing: The Blessing and Curse of Mutable State

As illustrated by the example above, mutable state can drastically simplify certain programming tasks by allowing one part of the program to interact with a remove part of the program. However, this power is a double-edged sword: mutable state makes it potentially much more diffi-

cult to reason about the behavior of a program, and requires a much more sophisticated model of the computer's state to properly explain.

To illustrate the fundamental issue, consider the following example. Suppose we wanted to implement a type for tracking the coordinates of points in a 2D space. We might create a mutable datatype of points, and couple useful operations on them like this:

```
type point = {mutable x:int; mutable y:int}

(* shift a points coordinates *)
let shift (p:point) (dx:int) (dy:int) : unit =
  p.x <- p.x + dx;
  p.y <- p.y + dy

let string_of_point (p:point) : string =
  "{x=" ^ (string_of_int p.x) ^ "}"
  "; y=" ^ (string_of_int p.y) ^ "}"</pre>
```

We can now easily create some points and move them around:

```
let p1 = {x=0;y=0}
let p2 = {x=17;y=17}

;; shift p1 12 13
;; shift p2 2 4
;; print_string (string_of_point p1) (* prints {x=12; y=13} *)
;; print_string (string_of_point p2) (* prints {x=19; y=21} *)
```

So far, so good.

Now consider this function, which simply sets the x coordinates of two points and then returns the new coordinate of the first point:

```
let f (p1:point) (p2:point) : int =
  p1.x <- 17;
  p2.x <- 42;
  p1.x</pre>
```

What will this function return? The "obvious" answer is that since p1.x was set to 17, the result of this function will always be 17. But that's *wrong!* Sometimes this function can return 42. To see why, consider this example:

```
let p = {x=0;y=0} in
  f p p (* f called with the same point for both arguments! *)
```

Calling f on the same point twice causes the identifiers p1 and p2 men-

tioned in the body of f to be *aliases*—these two identifiers are *different names* for the *same* mutable record.

A more explicit way of showing the same thing is to consider the difference between these two tests:

```
(* p1 and p2 are not aliases *)
let p1 = \{x=0; y=0\}
let p2 = \{x=0; y=0\}
;; shift p2 3 4
(* this test will PASS *)
let test () : bool =
 p1.x = 0 \&\& p1.y == 0
;; run_test "p1's coordinates haven't changed" test
(* p1 and p2 are aliases *)
let p1 = \{x=0; y=0\}
let p2 = p1
;; shift p2 3 4
(* this test will FAIL *)
let test () : bool =
 p1.x = 0 \&\& p1.y == 0
;; run_test "p1's coordinates haven't changed" test
```

Aliasing like that illustrated above shows how programs with mutable state can be subtle to reason about—in general the programmer has to know something about which identifiers might be aliases in order to understand the behavior of the program. For small examples like those above, this isn't too difficult, but the problem becomes much harder as the size of the program grows. The two points passed to a function like f might themselves have been obtained by some complicated computation, the outcome of which might determine whether or not aliases are provided as inputs.

Such examples also motivate the need for a different model of computation, one that takes into account the "places" affected by mutable updates. If we blindly follow the substitution model that has served us so well thus far, we obtain the wrong answer! Here is an example:

```
let p1 = {x=0;y=0}
let p2 = p1          (* create an alias! *)
let ans = p2.x <- 17; p1.x</pre>
```

```
\longrightarrow (by substituting the value for p1)
```

 \longmapsto (by substituting the value for p2)

```
let p1 = {x=0;y=0}
let p2 = {x=0;y=0}
let ans = {x=0;y=0}.x <- 17; {x=0;y=0}.x</pre>
```

 \longmapsto update the x field "in place", but we need to discard the result

```
let p1 = {x=0; y=0}
let p2 = {x=0; y=0}
let ans = ignore({x=17; y=0}); {x=0; y=0}.x
```

```
let p1 = {x=0; y=0}
let p2 = {x=0; y=0}
let ans =(); {x=0; y=0}.x
```

 \mapsto throw away the unit answer

```
let p1 = {x=0;y=0}
let p2 = {x=0;y=0}
let ans = {x=0;y=0}.x
```

```
\mapsto project the x field
```

The next chapter develops a computation model, called the *abstract stack machine*, suitable for explaining the correct behavior of this and all other examples.

Chapter 15

The Abstract Stack Machine

We saw in the last chapter that the simple substitution model of computation breaks down in the presence of mutable state. This chapter presents a more detailed model of computation, called the *abstract stack machine* that lets us faithfully model programs even in the presence of mutable state. While we develop this model in the context of explaining OCaml programs, small variants of it can be used to understand the behaviors of programs written in almost any other modern programming language, including Java, C, C++, or C#. The abstract stack machine (abbreviated ASM) is therefore an important tool for thinking about software behavior.

The crucial distinction between the ASM and the simple substitution model presented earlier is that the ASM properly accounts for the *locations* of data in the computer's memory. Modeling such spatial locality is essential, precisely because mutable update modifies some part of the computer's memory in place—the notion of "where" an update occurs is therefore necessary. As we shall see, the ASM gives an accurate picture of how OCaml (and other type-safe, garbage-collected languages like Java and C#) represents data structures internally, which helps us predict how much space a program will need and how fast it will run.

Despite this added realism, the ASM is still *abstract*—it hides many of the details of the computer's actual memory structure and representation of data. The level of detail present in the ASM is chosen so that we can understand the behavior of programs in a way that doesn't depend on the underlying computer hardware, operating system, or other low-level details about memory. Such details might be needed to understand C or C++ programs for example, which aren't type-safe and require programmers to

manually manage memory allocation.

15.1 Parts of the ASM

Recall that the substitution model of computation had two basic notions:

- *values*, which are "finished" results such as integers (*e.g.* 0,1, ...), tuples of values (*e.g.* (1, (2,3))), records (*e.g.* $\{x=0; y=1\}$), functions (*e.g.* (fun (x:int) -> x + 1)), or constructors applied to values (*e.g.* Cons (3, Nil)).
- *expressions*, which are "computations in progress", like 1+2*3, (f x), p.x, begin match ... with ... end, etc..

The substitution model computes by simplifying an expression—that is, repeatedly substituting values for identifiers, and performing simple calculations—until no more simplification can be done.

For programs that don't use mutable state, the abstract stack machine will achieve the same net results. That is, for *pure* programs, the ASM can be thought of as a (complicated) way of implementing substitution and simplification. We didn't previously specify precisely what was meant by "substitution"; instead we relied on your intuitions about what it means to replace an identifier with a value, and just left it at that. The ASM gives an explicit algorithm for implementing substitution using a *stack*, and further refines the notion of value and computation model to keep track of where in memory the data structures reside.

There are three basic parts of the abstract stack machine model:

- The *workspace* keeps track of the expression or command that the computer is currently simplifying. As the program evaluates, the contents of the workspace change to reflect the progress being made by the computation.
- The stack keeps track of a sequence of bindings that map identifiers to their values. New bindings are added to the stack when the let expression is simplified. Later, when an identifier is encountered during simplification, its associated value can be found by looking in the stack. The stack also keeps track of partially simplified expressions that are waiting for the results of function calls to be computed.

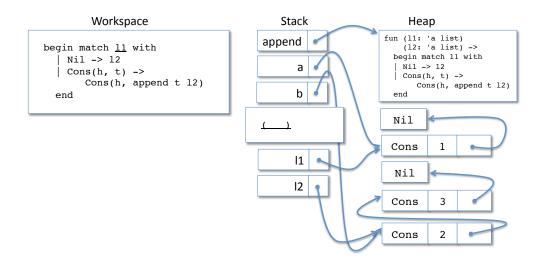


Figure 15.1: A picture of an Abstract Stack Machine in mid evaluation of a list operation <code>append a b</code>. The code in the workspace is preparing to look up the value of the local identifier <code>ll</code> in the stack (as indicated by the underline) before proceeding on to do a pattern match. The stack contains bindings for all of the identifiers introduced to this point, including <code>append</code> and the two lists <code>a</code> and <code>b</code>. It also has a saved workspace, which is there because <code>append</code> is recursive, and bindings for <code>ll</code> and <code>ll</code>. The stack values are themselves references into the heap, which stores both code (for the body of the <code>append</code> function itself), and the list structures built from <code>Cons</code> and <code>Nil</code> cells. The arrows are references, as explained in §15.2.

• The *heap* models the computer's memory, which is used for storage of non-primitive data values. It specifies (abstractly) where data structures reside, and shows how they reference one another.

Figure 15.1 shows these three parts of an ASM in action. The sections below explain each of these pieces in more detail and explains how they work together. First, however, we need to understand how the ASM represents its values.

15.2 Values and References to the Heap

The ASM makes a distinction between two kinds of values. *Primitive values* are integers, booleans, characters, and other "small" pieces of data

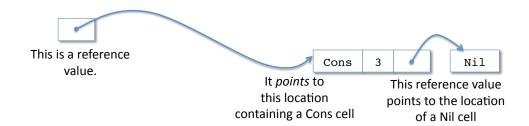


Figure 15.2: A pictorial representation of reference values.

for which the computer provides basic operations such as addition or the boolean logic operations.

All other values are references to structured data stored in the heap. A *reference* is the *address* (or *location*) of a piece of data in the heap. Pictorially, we draw a reference as an "arrow"—the start of the arrow is the reference itself (*i.e.* the address). The arrow "points" to a piece of data in the heap, which is located at the reference address. Figure 15.2 shows how we visualize reference values in the ASM.

The heap itself contains three different kinds of data:

- A *cell* is labeled by a datatype constructor (such as cons or Nil) and contains a sequence of constructor arguments. Figure 15.2 shows two different heap cells. One is labeled with constructor name Cons, which has two arguments, namely 3 and a reference to the second heap cell, which is labeled Nil (and has no arguments). The arguments to a constructor are themselves just values (either primitive values or references.) Note that, conceptually, the constructor names like Cons take up some amount of space in the heap.
- A *record* contains a value for each of its fields. Unlike constructor cells, the field names of a record don't actually take up space in the heap, but we mark them anyway to help us do book keeping. We mark mutable record fields using a "doubled" box, as shown, for example, by the record of type point in Figure 15.3. Such a mutable field is the "place" where an "in-place" update occurs, as we shall see below.
- A *function*, which is just an anonymous function value of the form (**fun** (x1:t1) ... (xn:tn) -> e). Figure 15.1 shows that the stack

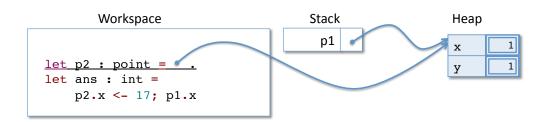


Figure 15.3: The state of the ASM just before it creates the stack binding for p2. Note that p2 is an alias of p1—they both point to the *same* record of the heap.

binding for append is a reference to the code for the append function itself.¹

References as Abstract Locations

What, exactly is a reference value, like the one shown in Figure 15.2? A reference is an abstract representation of a location in the heap—references are abstract because it doesn't matter exactly "where" the location being pointed to is. For the purposes of understanding aliasing and the other aspects of sharing among data structures, it is enough to know whether two references point to the same location.

We can peel back the abstraction just a bit to see how references work in the internals of the computer. Figure 15.4 shows two different views of the same situation. The right side of the figure depicts a reference value that points to a Cons cell containing the value 3 and a reference to Nil, exactly the same configuration as shown in Figure 15.1. The left-hand side gives a lower-level explanation in terms of the computer's memory.

On a 32-bit machine, we can think of the computer's memory as being a giant array of 32-bit words, where the array is indexed by numbers in the range 0 to $2^{32}-1$ (which happens to be 4,294,967,295). In this low-level view, an address is simply a number, and we have to encode heap cells and other data structures by choosing some particular representation by using patterns of of 32-bit words. Such decisions are made during compilation. For example, the compiler might decide that the constag of a memory cell should be represented using the number 120120120 and that Nil should

¹We will have to refine this notion of heap-allocated functions slightly to account for *local* functions. See 17.1 for details.

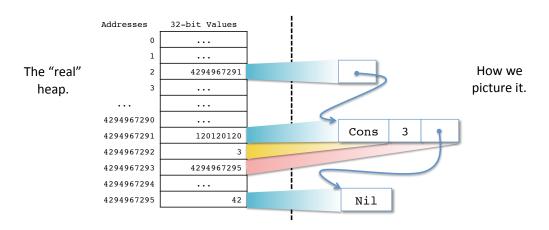


Figure 15.4: The "real" computer memory (left) is just an array of 32-bit words, each of which has an address given by the index into the array. The ASM provides an abstract view of this memory (right) in which the exact address of a piece of heap-allocated data is hidden. Constructor tags are just arbitrary 32-bit integers chosen by the compiler—in this example, the tag for <code>cons</code> is 120120120 and the tag for <code>Nil</code> is 42. Constructor data is laid out contiguously in memory, and a reference is just the address of some other word of memory. Again, the ASM hides these representation details.

be represented by the tag 42, as depicted in Figure 15.4. The ASM hides these insignificant details, so we don't have to worry about them as we try to explain the behavior of our programs.²

Some languages, like C or C++, use the low-level, numeric view of memory references, in which case they are usually called *pointers*. The distinction is that references are *abstract*—the only operations supported by references are reference creation, dereferencing (that is, getting the value referred to by the reference), and determining whether two references point to the same heap location (reference equality). In contrast, pointers correspond directly to machine addresses, which are just numbers (as shown in Figure 15.4). Therefore, in languages like C or C++ you can do "pointer arithmetic" to, for example, calculate an offset from a pointer. This can be very useful for low-level programming, but can also lead to a lot of serious bugs if you have errors in your arithmetic calculations. In the general computer science vernacular, the terms "reference" and "pointer"

 $^{^2}$ Even this low-level explanation sweeps a lot of details under the rug—the operating system and hardware collaborate to provide the illusion that there are $2^{32} - 1$ words of memory available to a given process, though, strictly speaking, not all of it is immediately available. Also portions of the memory space are reserved for OS-related tasks, I/O, etc.

```
Workspace Stack Heap

let x = 10 + 12 in

let y = 2 + x in

if x > 23 then 3 else 4
```

Figure 15.5: The initial state of the ASM starts with the workspace containing the entire program, and the stack and heap both empty.

are often used interchangeably, with some potential for confusion.

15.3 Simplification in the ASM

The abstract state machine processes a program by repeatedly simplifying the contents of the workspace until the workspace contains only a value, which is the answer computed by the program. During this process, the ASM creates new bindings in the stack, allocates data structures in the heap, and, in the case of mutable update, modifies the contents of mutable record fields.

In the start configuration of the ASM, the workspace contains the entire program to be executed, and the stack and heap are both empty.

At each step of simplification, the ASM finds the first (left-most) "ready subexpression" and simplifies it according to computation rules determined by the program expression. The intuition is that the "ready" expression is the one that will be simplified next. In our pictures of the ASM, we <u>underline</u> the ready expression.

As an example, consider simulating the ASM on this program:

```
let x = 10 + 12 in
let y = 2 + x in
  if x > 23 then 3 else 4
```

Figure 15.5 shows the initial configuration of the ASM for this example.

The basic rules for simplification are:

• An expression involving a primitive operator (like +) is ready if all of its arguments are values. Primitive operations are simplified by

```
Workspace Stack Heap

let y = 2 + 22 in
 if x > 23 then 3 else 4
```

Figure 15.6: The example from Figure 15.5 after several steps of simplification. There is a binding of \times to 22 in the stack, and the expression 2 + 22 is ready to simplify next.

replacing the expression with its result. This is exactly as we have seen previously. For example, the expression 10 + 12 \Longrightarrow 22, so we replace 10 + 12 by 22.

- A let expression let x: t = e in body is ready if e is a value. It is simplified by adding (pushing) a new binding for the identifier x to e at the *end* of the stack, and leaving body in the workspace.
- A variable is always ready. It is simplified by looking up the binding
 associated with the variable in the stack and replacing the variable
 by the corresponding value. This lookup process proceeds by searching from the most recent bindings to the least recent—this algorithm
 guarantees that we find the newest definition for a given variable.

Figure 15.6 shows the example program after several steps of simplification according to these rules. Slides 15–31 from Lecture 12 show the full sequence of simplification steps for this example, which results in computing the value 4.

Shadowing and the Stack

The ASM stack properly accounts for shadowing variables (recall §2.4), as can be seen by using it to evaluate this program:

```
let x = 22 in
let x = 2 + x in
  if x > 23 then 3 else 4
```



Figure 15.7: An example of how proper shadowing is implemented in the ASM. The value of the ready variable x will be found by searching the stack from most recent (x maps to 24) to least recent (x maps to 22).

Figure 15.7 shows the state of the ASM when the variable \times of the conditional expression is ready to be looked up in the stack. There are two bindings for \times , but the most recent one (*i.e.* the one closest to the bottom) will be used, which is consistent with shadowing.

The sequence of bindings is called a *stack* because we only ever *push* elements on to the stack and then *pop* them off in a last-in-first-out (LIFO) manner. This is just like a stack of dinner plates—it's easy to put more on top or take away the last one put there, but it's hard to remove one in the middle. (For some reason, computer scientist's stacks are often drawn with their "top" toward the bottom of the page as we show in the ASM diagrams; this is bizarre, but at least consistent with trees having their leaves at the bottom and roots at the top.)

Treating let-bound identifiers using a stack discipline ensures that the most recently defined value for a given identifier name will be used during the computation. Below we will see how the ASM pops bindings as part of returning a value computed by a function call.

Simplifying Datatype Constructors and match

The simplification rules mentioned above don't yet involve the heap—they just implement substitution by explicitly using a stack of identifier bindings. Data constructors, like <code>cons</code> and <code>Nil</code>, on the other hand, do interact with the heap—simplifying a constructor allocates some space on the heap and creates a reference to the newly allocated space. The simplification rule is therefore quite simple:

• A constructor (like Cons or Nil) is ready if all of its arguments are values. A constructor expression is simplified by allocating a heap

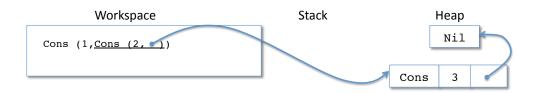


Figure 15.8: The ASM in the process of evaluating the expression 1::2::3::[], which we could rewrite equivalently as Cons(1, Cons(2, Cons(3, Nil))). Here, the Nil and $Cons(3, _)$ cells have already been allocated in the heap, and the ASM is ready to allocate the $Cons(2, _)$ cell.

cell with the constructor tag and its arguments as data and then replacing the constructor expression with this newly created reference.

Figure 15.8 shows the ASM part way through evaluating the list expression 1::2::3::[]. Each use of the :: operator causes the ASM to allocate a new cons cell in the heap. Slides 51–60 of Lecture 12 show the full animation of the ASM for this example.

Simplifying a match expression of the following shape is pretty straight forward:

• Such a match expression is ready to simplify if e is a value (which will typically be a reference to a cell in the heap). The match is simplified by finding the first pattern starting from pat1 and working toward patN that structurally matches the heap cell referred to by e. Once such a matching pattern, patX is found, the ASM adds new stack bindings for each identifier in the pattern—the values to which those identifiers are bound is determined by the shape of the heap structure. The workspace is then modified to contain branchX, the branch body corresponding to patX. If no such pattern matches, the ASM aborts the computation with a Match_failure error.

The append example from the Lecture 12 slides shows in detail the use of pattern match simplification.

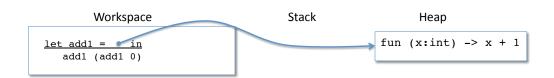


Figure 15.9: The ASM after moving a function value to the heap. It is ready to create a binding, named add1 to the reference.

Simplifying functions

There are three parts to simplifying functions: moving function values to the heap, *calling* a function, and *returning* a value computed by a function to some enclosing workspace.

The first of these steps is very straight forward. Recall from §10.1 that top-level function declarations are just short hand for naming an anonymous function. For example, the following are equivalent ways of defining add1:

```
let add1 (x:int) : int = x + 1 in
   add1 (add1 0)

and
let add1 = fun (x:int) : int -> x + 1 in
   add1 (add1 0)
```

The ASM therefore simplifies the first expression to the second before proceeding. Since anonymous functions like (fun (x:int) : int -> x + 1) are one of the three kinds of heap data (see §15.2), the ASM just moves the fun value to the heap and replaces the fun expression with the newly created reference. The ASM then follows the usual rules for let simplification to create a binding for the function name on the stack. Figure 15.9 shows how the example program above looks after following these simplification rules.

Simplifying function call expressions is more difficult. The issue is that, in general, the function call may itself be nested within a larger expression that will require further simplification after the function returns its computed value. To model this situation faithfully, the ASM must therefore keep track of where in the surrounding expression the value computed by a function call should be returned to once the function is done.

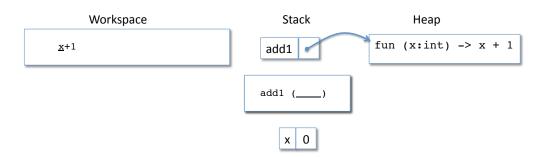


Figure 15.10: The ASM just after the call to the inner add1 has been simplified. The stack contains a saved workspace whose hole marks where the answer of this function call should be returned. It also contains a binding for the add1 function's argument x.

In the example program above, after creating a binding for add1 on the stack, we reach a situation in which the worskspace contains the expression add1 (add1 0). We can simplify the innermost add1 by looking up the reference in the stack as usual. Then we're ready to do the function call—in general, a function call is ready to simplify if the function is a reference and all of its arguments are values. Suppose that we magically knew that the answer computed by add1 0 was going to be a value ANSWER. Then the we should eventually simplify workspace by replacing inner function call, (add1 0), with ANSWER to obtain a new workspace add1 ANSWER.

To achieve that goal, the ASM simplifies a function call like this:

First it saves the current workspace to the stack, marking the spot where the ANSWER should go with a "hole". In our example, since the original workspace was ansi (ansi 0), the saved workspace when doing the inner call will be ansi (____), where the ___ marks the "hole" to which the answer will be returned.

Second, the ASM adds new stack bindings for each of the called function's parameters. Suppose that the function being called has the shape $fun(x1:t1) \dots (xN:tN) \rightarrow body$ in the heap and it is being called with the arguments $v1 \dots vK$. Then there will be stack bindings added for $x1 \mapsto v1 \dots xJ \mapsto vJ$. In our running example, the add1 function takes only one argument called x, so only one binding will be added to the stack.

Third, the workspace is replaced by the body of the function.⁴

³In general there can be *fewer* arguments than the function requires, which corresponds to the case of partial application.

⁴In the case of partial application, the workspace is replaced by a fun expression of the

Figure 15.10 shows the state of the ASM just after the inner call to add1 has been simplified.

Once the function call has been initiated and the function body is in the workspace, simplification continues as usual. This process may involve adding more bindings to the stack, doing yet more function calls, or allocating new data structures in the heap.

Assuming that the code of the function body eventually terminates with some value, the ASM is in a situation in which the result of the function should be returned as the ANSWER to the corresponding workspace that was saved on the stack at the time that the function was called. For example, after a few steps of simplification, the workspace in Figure 15.10 will contain only the value 1, which is the answer of the inner call to add1.

When this happens—that is, when the workspace contains a value and there is at least on saved workspace on the stack—the ASM returns the value to the old workspace. It does so by *popping* (*i.e.* removing) all of the stack bindings that have been introduced since the last workspace was saved on the stack. It then replaces the current workspace (which just contains some value v) with the last saved workspace (and also popping it from the stack), replacing the answer "hole" with the value v.

In our running example, after the workspace in Figure 15.10 simplifies to the value 1, the ASM will pop the binding for x from the stack, restore the workspace to add1 1 (where the hole has been replaced by 1), and then pop the saved workspace. Simplification then proceeds as usual.

Lecture 12 contains an extended animation of the ASM simplification for a more complex example, which shows how to run the following program:

```
let rec append (l1: 'a list) (l2: 'a list) : 'a list =
  begin match l1 with
  | Nil -> 12
  | Cons(h, t) -> Cons(h, append t l2)
  end in

let a = Cons(1, Nil) in
  let b = Cons(2, Cons(3, Nil)) in

append a b
```

form fun (xL:tL) .. (xN:tN) \rightarrow body, where L is J+1. To properly continue simplification will, in this case, require the use of a closure. See §17.1.

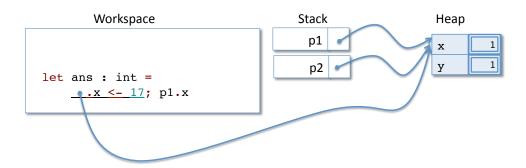


Figure 15.11: The state of the ASM just before doing the imperative update to the p2.x field. Note that p1 and p2 are aliases—they point to the same record in the heap.

Simplifying Mutable Record Operations

The whole purpose of the ASM is to allow us to explain the behavior of programs that use mutable state. We are finally to the point where we can make sense of "in place" updates to mutable record fields, and we can use the ASM to explain the behavior of programs that exhibit aliasing.

The rules for simplifying records, field projections, and mutable field updates are simple:

- A record expression is ready if each of its fields is a value. We simplify a record by allocating a record structure in the heap and replacing the record expression with a reference to that structure. Recall that we mark the mutable fields of a record using a double-lined box; this is simply to help us visualize which parts of the heap might be modified during a program's execution.
- A record field projection expression, like p.x is ready of p is a value. It is simplified by replacing the expression by the value stored in the x field of the record in the heap.
- A mutable field update expression, like p.x <- e is ready if both p and e are values. The expression is simplified by changing the x field of the record pointed to by p to contain the value e instead of whatever it contained before. The entire update expression is replaced by the unit value, ().

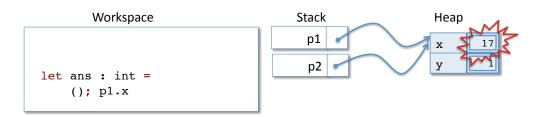


Figure 15.12: The ASM after doing the imperative update shown in Figure 15.11. It is clear that running p1.x from this state will yield 17.

We can now see how the ASM correct the deficiencies of the substitution model. Recall the following example, which computed to the incorrect answer 0 when we used the substitution model (see §14.2)

```
let p1 = {x=0;y=0}
let p2 = p1         (* create an alias! *)
let ans = p2.x <- 17; p1.x</pre>
```

After creating the stack bindings for p1 and p2, the resulting ASM configuration will be that shown in Figure 15.11. It is clear that p1 and p2 are aliases—they point to the same record in the heap. Modifying the x field via the p2 reference, therefore also modifies the x field of the p1 reference—they are the *same* field. Figure 15.12 shows the effect of doing the update; it is clear that the ASM will eventually compute 17 as the (correct) answer for this program.

Chapter 16

Linked Structures: Queues

In this chapter, we consider how to use mutable state to build "imperative linked" data structures in the heap. Why would we want to do that? The pure datatypes, like lists and trees, that we have studied so far all have a simple recursive structure: we build "bigger" structures out of already existing "smaller" structures. A consequence of that way of structuring data is that we can't easily modify "distant" parts of the data structure. For example, when we implement the <code>snoc</code> function, which adds an element to the end of a list, we were forced to do this:

If we examine the behavior of the function call <code>snoc v 1</code> using the ASM, we can see that <code>snoc copies</code> the entire list 1 (because it uses the :: operator) after creating a new list to hold the value v. This means that adding a single element to the tail of the list costs time proportional to the length of the list, and, since 1 is duplicated, twice as much heap space will be used.

Sometimes this persistent nature of pure lists is useful—for example, if we needed to use both 1 and the result of <code>snoc v 1</code>, we might have to create the copy anyway (which always takes time proportional to the length of 1). However, in many situations it would be more efficient and simpler to just be able to add an element to the tail of the list directly. We can do that by creating a data structure that is similar to a list, but that uses mu-

table references to link together nodes. By keeping *two* references, one to the head and one to the tail, we can then efficiently update the structure at either end.

The resulting structure is called a *queue* because one common mode of use is to *enqueue* (add) elements to the tail of the queue and *dequeue* (remove) them from the head. (Think of people waiting in line for concert tickets.) Queues are used in many situations where lists can be used, but they also serve as a key component in "work list" algorithms (where they keep track of tasks remaining to be done), networking applications (where they buffer requests to be handled on a first-come, first-served basis), and search algorithms (where they keep track of what part of some space to explore next).

The design criteria above suggest that we use the following interface for a queue module:

```
module type QUEUE = sig
  (* type of the data structure *)
  type 'a queue

  (* Make a new, empty queue *)
  val create : unit -> 'a queue

  (* Determine if the queue is empty *)
  val is_empty : 'a queue -> bool

  (* Add a value to the tail of the queue *)
  val enq : 'a -> 'a queue -> unit

  (* Remove the head value and return it (if any) *)
  val deq : 'a queue -> 'a
end
```

16.1 Representing Queues

How do we implement mutable queues? We need two data types—one to store the data of the "internal" nodes that form the list-like structure, and one containing the references to the head and tail of the queue. The nodes of the queue will be linked together via references, but since the last element of the queue isn't followed by a next element, those references should be optional. Similarly, in an empty queue, there are no nodes for

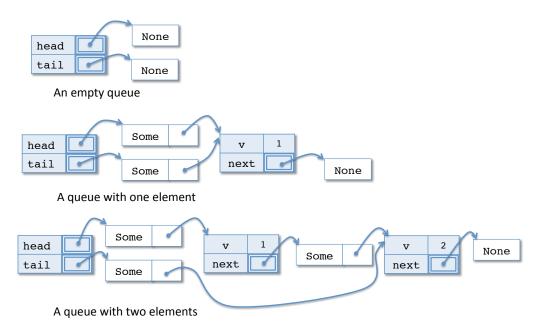


Figure 16.1: Several example queues as they would appear in the heap. Note that the frequent use of options motivates the need for some "visual" shorthand. See Figure 16.2 for a more compact way of drawing such linked structures.

the head and tail to refer to, so they must also be optional. These considerations lead us to define the queue representation types like this:

```
module Q : QUEUE = struct

type 'a qnode = {
    v : 'a;
    mutable next : 'a qnode option;
}

type 'a queue = {
    mutable head : 'a qnode option;
    mutable tail : 'a qnode option;
}

end
```

Figure 16.1 shows several examples of queue values as they would appear in the heap of the ASM. As shown in these examples, the proliferation

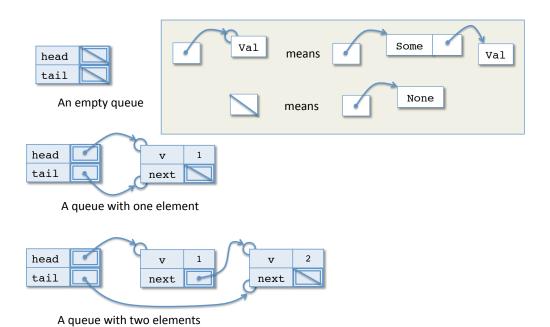


Figure 16.2: The queue structures from Figure 16.1 drawn using a visual short-hand in which references to None are represented by a slash and references to Some $\,_{\text{V}}$ are drawn as an arrow to a "some bubble", which gives a "handle" to the underlying value $\,_{\text{V}}$.

of some and None constructors in the heap creates a lot of visual clutter. Although it is necessary to acknowledge their existence (especially since the *type* of a reference to <code>some v</code> is different from that of a reference to just <code>v</code> itself), it is useful to present these drawings in a more compact way. Figure 16.2 shows the same three queue structures represented using "visual shorthand" for <code>None</code> and <code>Some</code> constructors in the heap.

As you can see, the basic structure of a queue is a linear sequence of qnodes, each of which has a next pointer to its successor. The tail element of the queue has its next field set to None. For the empty queue, both the head and tail are None, for a singleton queue, the head and tail both point to the same qnode, and for a queue with more than one element, the head and tail point to the first and last elements, respectively.

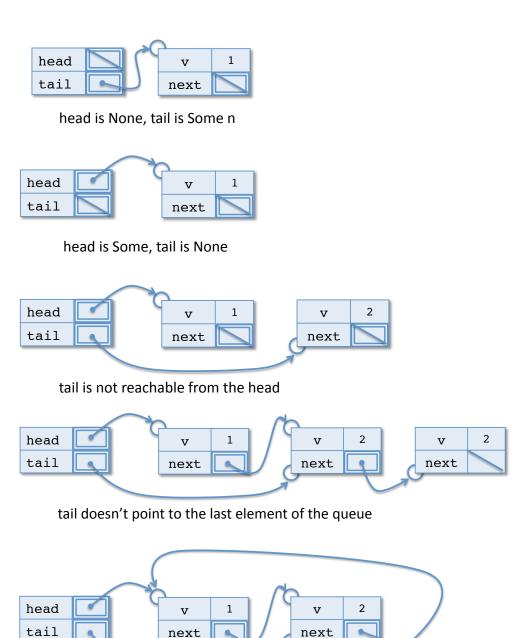


Figure 16.3: Several examples of bogus heap structures that conform to the queue datatypes. The queue invariants rule out all of these examples (and many more).

the links contain a cycle!

16.2 The Queue Invariants

Although the two types defined above provide enough structure to let us create heap values with the desired shapes, they are *too permissive*—there are many values that conform to these types that don't meet our expectations of what a proper queue should be. Figure 16.3 shows several examples of such bogus queue structures as they might appear in the heap.

This situation is similar to the one we encountered when studying binary search trees. There, the type of 'a trees was rich enough to contain trees with arbitrary nodes, but we found that by imposing additional structure in the form of the binary search tree invariant (see Definition 7.1), we could constrain the shape of trees in a way so that the natural ordering of its nodes' data can be exploited to drastically improve search.

For queues, we would therefore like to impose some restrictions that rule out the bogus values but preserve all of the "real" queues.

Definition 16.1 (Queue Invariant).

A data structure of type 'a queue satisfies the queue invariants if (and only if), either

- 1. both head and tail are None, or,
- 2. head is Some n1 and tail is Some n2, and
 - n2 is reachable by following next pointers from n1
 - n2.next *is* None

The first part of the invariant ensures that there is a unique way of representing the empty queue. The second part applies if the queue is non-empty. It says that tail actually points to the tail element, and that this n2 is reachable from the head. Together these latter invariants imply that there are no cycles in the link structure and that the queue itself is "connected" in the sense that all nodes are reachable from the head.

It is easy to verify that each of the bogus queue examples from Figure 16.3 can be ruled out by these invariants as ill-formed. Therefore, as long as we are careful that our queue manipulation functions establish these invariants when creating queues and preserve them when modifying an existing queue, we may also assume that any queues passed in to the Q module already conform to the invariants. As always, this reasoning

is justified because the type 'a queue is *abstract*—the type definition is not exported in the module interface (see §9).

16.3 Implementing the basic Queue operations

Now that we understand the 'a queue type and its invariants, it is not too difficult to implement the operations required by the QUEUE interface. Creating a fresh empty queue is easy, as is determining whether a given queue is empty:

```
(* create an empty queue *)
let create () : 'a queue =
    { head = None;
        tail = None }

(* determine whether a queue is empty *)
let is_empty (q:'a queue) : bool =
        q.head = None
```

Note that, due to the queue invariants, we could have equally well chosen to check whether q.tail = None in is_empty, and we never have to check both. By assumption, either both q.head and q.tail are None or neither is.

How do we add an element at the tail of the queue? If the queue is empty, we simple create a new internal queue node and then update both the head and tail pointers to refer to it. If the queue is non-empty, then we need to create a new queue node. By virtue of the fact that it will be the new tail, we know that its next pointer should be None. To maintain the queue invariants, we must also modify the old tail node's next field to point to the newly created node:

Note that <code>enq</code> returns <code>unit</code> as its result—this function is a command that imperatively (destructively) modifies an existing queue. After the update, the old queue is no longer available.

Removing an element from the front of the queue is almost as easy. If the queue is empty, the function simply fails. Otherwise, head is adjusted to point to the next node in the sequence. One might therefore think that the correct implementation of <code>deq</code> is:

```
(* BROKEN attempt to remove an element from the head
  of the queue *)
let deq (q: 'a queue) : 'a =
  begin match q.head with
  | None ->
      failwith "deq called on empty queue"
  | Some n ->
      q.head <- n.next;
      n.v
end</pre>
```

However, this implementation fails to re-establish the queue invariants: in the case that there is exactly one element in the queue, which gets removed, the tail pointer should be set to None—otherwise head will be None and the tail will still be Some. The correct implementation must therefore check for that possibility and adjust the tail accordingly:

```
(* remove an element from the head of the queue *)
let deq (q: 'a queue) : 'a =
  begin match q.head with
  | None ->
      failwith "deq called on empty queue"
  | Some n ->
      q.head <- n.next;
      if n.next = None then q.tail <- None;
      n.v
end</pre>
```

In general, when manipulating linked, heap-allocated data structures, it is important to keep in mind the invariants that make sense of the structure. Understanding the invariants can help you structure your programs in a way that helps you get them right.

16.4 Iteration and Tail Calls

Suppose that we want to extend the queue interface to include some operations that work with the queue as a whole, rather than just with one node at a time. A simple example of such a function is the length operation, which counts the number of elements in the queue:

```
module type QUEUE =
sig
  (* type of the data structure *)
  type 'a queue

  (* Get the length of the queue *)
  val length : 'a queue -> int
end
```

One simple way to implement this function is to directly translate the recursive definition of length that we are familiar with for immutable lists to the datatype of queues. Since the "linked" structure of the queues is given by the sequence of qnode values and the queue itself consists of just the head and tail pointers, we need to decompose the length operation into two pieces: one part that uses recursion as usual to process the qnodes and one part that deals with the actual queue type itself. (Note that this is

yet another place where the structure of the types guides the code that we write.)

We can therefore write length like this:

```
(* Calculate the length of the list using recursion *)
let length (q:'a queue) : int =
  let rec loop (no: 'a qnode option) : int =
    begin match no with
    | None -> 0
    | Some n -> 1 + (loop n.next)
    end
in
loop q.head
```

In this code, the helper function loop recursively follows the sequence of qnode values along their next pointers until the last node is found. Note that this function implicitly assumes that the queue invariants hold, since a cycle in the next pointers would cause the program to go into an infinite loop.

Although this program will compute the right answer, it is still somehow unsatisfactory: if we observe the behavior of a call to this version of length by using the ASM, we can see that the height of the stack portion of the ASM state is proportional to the length of the queue—each recursive call to loop will save a copy of the workspace consisting of $1 + (\underline{\hspace{1cm}})$ and create a new binding for the copy of no. The slides for Lecture 15 give a complete animation of the ASM for such an example.

It seems awfully wasteful to use up so much space just to count the number of elements in the queue—why not just talk down the queue, keeping a running total of the number of nodes we've seen so far? This version of length requires a slight modification to the loop helper function to allow it to keep track of the count:

¹To be fair, this *same* criticism applies to the recursive version of length for immutable lists that we studied earlier.

```
(* Calculate the length of the list using iteration *)
let length (q:'a queue) : int =
  let rec loop (no:'a qnode option) (len:int) : int =
    begin match no with
    | None -> len
    | Some n -> loop n.next (1+len)
    end
in
loop q.head 0
```

Why is this better? At first glance, it seems that we are stuck with the same problems as with the recursive version above. However, note that in this version of the code, the workspace pushed on to the stack at the recursive call to loop will always be of the form (_____). That is, after the call to loop in the Some n branch of the match, there is no more work left to be done (in contrast, the first version always pushed workspaces of the form 1 + (_____), which has a pending addition operation). If we watch the behavior of this program in the ASM, we see that the ASM will always perform a long series of stack pops, restoring these empty workspaces when loop finally returns the len value in the None branch.

The observation that we will always immediately pop the stack after restoring an empty workspace suggests a way to optimize the ASM behavior: there is no need to push an empty workspace when we do such a function call since it will be immediately popped anyway. Moreover, at the time when we would have pushed an empty workspace, we can also eagerly *pop* any stack bindings created since the last non-empty workspace was pushed. Why? Since the workspace is empty, we know that none of those stack bindings will be needed again.

We say that a function call that would result in pushing an empty workspace is in a *tail call*² position. The ASM optimizes such functions as described above—it doesn't push the (empty) workspace, and it eagerly pops off stack bindings. This process is called *tail call optimization*, and it is frequently used in functional programming.

Why is tail call optimization such a big deal? It effectively turns re-

 $^{^2}$ The word "tail" in this definition is not to be confused with the tail of a queue. The "tail" in tail call means that the function call occurs at the "end" of the function body. Note, however, that very often when writing loops over queues you will want a tail call whose argument is towards the tail of the queue, relative to the "current" node being visited.

cursion into iteration. Imperative programming languages include for and while loops that are used to iterate a fragment of code multiple times. The essence of such iteration is that only a constant amount of stack space is used and that parts of the program state are updated each time around the loop, both to accumulate an answer and to determine when the loop should finish.

In the iterative version of the queue <code>length</code> function shown above, the extra <code>len</code> argument is incremented at each call. If we see how the ASM stack behaves when using tail call optimizations, each such call to <code>loop</code> essentially *modifies* the stack bindings in place. That is, at every call to <code>loop</code>, there will be one stack binding for <code>no</code> and one stack binding for <code>len³</code>. Since, under tail call optimizations, those two old bindings will be popped and the two new bindings for <code>no</code> and <code>len</code> will be pushed each time <code>loop</code> is called, the net effect is the <code>same</code> as imperatively updating the stack. The Lecture 15 slides give a detailed animation of this behavior in the ASM.

The upshot is that writing a loop using tail calls is *exactly the same* as writing a while loop in a language like Java, C, or C++. Indeed, tail calls subsume even the break and continue keywords that are used to "jump out" of while loops—the break keyword corresponds to just returning an answer from the loop, and the continue keyword corresponds to calling loop in a tail-call position.

16.5 Loop-the-loop: Examples of Iteration

Let's see how we can use tail recursion to write several different functions that iterate over the queue structures.

First, let's just create a simple print operation that outputs the queue values on the terminal in a nicely formatted way:

³And, technically, one for the loop function itself, which is saved in the *closure* for the loop code when it is moved to the heap.

In this example, the loop doesn't produce any interesting output—it simply walks down the queue nodes, converts each value to a string, and prints out that string. Note that the call to loop in the Some n branch is in a tail-call position: the print_endline will be done before the loop. The print function enters the loop by calling loop q.head—this means that the loop will start traversing the queue from the head.

Next, let's try writing a function that converts a queue to a list. Here the loop function will return an 'a list, which is built up as the loop traverses over the sequence of nodes. Therefore the loop function itself needs an extra argument in which to "accumulate" this answer.

Our first instinct might be to do this:

```
(* Retrieve the list of values stored in the queue,
    ordered from head to tail. *)
let to_list (q: 'a queue) : 'a list =
    let rec loop (no: 'a qnode option) (l:'a list) : 'a list =
        begin match no with
        | None -> l
        | Some n -> loop n.next (l @ [n.v])
        end
    in loop q.head []
```

Since we are building up the accumulator list 1 from the head of the queue to the tail, we need to add each node's value to the *end* of 1 (as shown by the use of @ in the recursive call). When loop has reached the end of the sequence of nodes (the None case), it simply returns the resulting list. Note that we provide the empty list [] as the second argument when we start the loop—this says that the "initial value" of the accumulator list

is [].

However, this implementation isn't that great because, as we saw before the append operation takes time proportional to the length of 1. Since we use it on 1, which increases in length each time around the loop, this algorithm will end up taking roughly n^2 time, where n is the length of the queue.

A better way to structure this program is to build up the accumulator list in reverse order during the loop, and then reverse the entire thing only once at the end. This leads us to this variant, which will take time proportional to the length of the queue:

```
(* Retrieve the list of values stored in the queue,
    ordered from head to tail. *)
let to_list (q: 'a queue) : 'a list =
    let rec loop (no: 'a qnode option) (l:'a list) : 'a list =
        begin match no with
        | None -> List.rev l
        | Some n -> loop n.next (n.v::l)
        end
    in loop q.head []
```

Here we simply cons the node value to the front of the accumulator list 1, but then use the library call List.rev to reverse the list when the loop is done (in the None branch).

We can rewrite many of the list-processing functions that used recursion to take advantage of tail-recursive loops. For example, we can sum the elements of an int queue using this function:

```
(* Sum the elements of the queue *)
let sum (q: int queue) : int =
  let rec loop (no: int qnode option) (sum:int) : int =
    begin match no with
    | None -> sum
    | Some n -> loop n.next (sum + n.v)
    end
  in loop q.head 0
```

Again the accumulator that changes at each iteration of the loop is the running total, here called sum.⁴ When the loop terminates, we simply return the sum, at each iteration we increase the sum parameter by n.v. As

⁴In fact the term "accumulator" comes from thinking of the extra argument of the loop function as a "running total" begin "accumulated".

before, we have to initialize the value of sum to 0 by calling the loop on q.head and 0.

It is instructive to compare these iterative functions to the recursive ones we are already familiar with. For example, here is the recursive version of sum_list that we have seen previously, where I have used suggestive names for the head and tail of the list:

We can see that in the recursive solution the "base case" computes the length of the empty list, which is 0. In contrast, the iterative version initializes the "accumulator" to 0 in the call to 100p—the base case is analogous to the initial value of the accumulator. The recursive version does the addition *after* recursively computing the sum of the "next" part of the list, while the iterative version does the addition *before* it jumps back to the start of the loop.

16.6 Infinite Loops

When using iteration, it is possible to accidentally cause your program to go into an infinite loop. Unlike the case for recursion, however, an infinite loop may just "diverge silently"—since the loop doesn't consume any stack space, a loop might not exhaust all of the available memory. Infinite recursion usually causes OCaml to produce the error message:

```
Stack overflow during evaluation (looping recursion?)
```

This is possible because the operating system can detect that the program has used up all of its stack space and abort the program.

When using tail recursion, one could accidentally create an infinite loop by writing a program like this:

```
(* Accidentally go into an infinite loop *)
let accidental_infinite_loop (q:'a queue) : int =
   let rec loop (qn:'a qnode option) (len:int) : int =
        begin match qn with
        | None -> len
        | Some n -> loop qn (len + 1)
        end
   in loop q.head 0
```

This program mistakenly calls loop with the *same* qn each time in the body of the some branch. When we run it on a non-empty queue, the program will just hang, producing no output and no error message. This kind of error can be frustrating to recognize—make sure that your programs actually terminate when you run them.

A second way in which an iterative program can go into an infinite loop is if the link structure being traversed contains a cycle. This could occur, for example, if a value of type 'a queue that doesn't satisfy the queue invariants is passed to a function that expects the queue invariants to hold.

In some circumstances, we can plan for the possibility of cyclic data structures and check to see whether the function has detected a cycle. For example, suppose that you wanted to write a function that, given a possibly invalid queue (*i.e.* one that doesn't necessarily satisfy the queue invariant) returns the last node that can be reached by following next pointers from the head. (You might want to implement such a function to *check* whether a given queue satisfies the invariants—the last element reachable from the head should be pointed to by the tail.)

Here is a function that accomplishes this task:

This function relies on a helper function, called <code>contains_alias5</code>, which, given a value and a list determines whether the list contains any aliases of the value. The loop traverses nodes starting from the head and adds each one it passes to the <code>seen</code> accumulator—if it ever encounters the same node twice the queue structure must have contained a cycle, so the result is <code>None</code>. Otherwise, the traversal will eventually find a node whose <code>next</code> field is <code>None</code>, which is the last element reachable from the <code>head</code>.

If we tried to write this function in the naive way shown below, calling it with a invalid cyclic queue would cause the program to loop silently:

```
(* BROKEN: this version of get_tail could loop *)
let rec get_tail (q: 'a queue) : 'a qnode option =
   let rec loop (qn: 'a qnode) : 'a qnode option =
        begin match qn.next with
        | None -> Some qn
        | Some n -> loop n
        end
   in loop q.head
```

⁵See HW05.

Chapter 17

Local State

This Chapter explores some ways of packaging state with functions that operate on that state. Such encapsulation, or *local* state, provides a way to restrict some parts of the program from tampering with mutable values. By *sharing* a piece of local state among several functions, we can profitably exploit the "action at a distance" that mutable references provide.

Recall the motivating example from §14 in which a global identifier with the mutable field <code>count</code> let us neatly keep track of how many times the <code>tree_max</code> function had been called. There are several drawbacks of using a single, global reference. First, if we want to have multiple different counters, each of which is used to track the usage of a different function, we have to name each of the counters at the top level of the program. What's worse, each function that uses such a counter would need to have to be modified in a slightly different way—we might have to write <code>global1.count <- global1.count + 1</code> in one function and the nearly identical <code>global2.count <- global2.count + 1</code> in another function. Supposing that we might also sometimes want to decrement the counters, or reset them to 0 at various points throughout the program, keeping track of which <code>global</code> identifier to use can quickly become quite a hassle.

The key idea in solving this problem is to use first-class functions combined with *local* mutable state. As a first step, lets first isolate the main functionality of a counter. The code below shows an incr function, which (for now) increases the count of the global counter by 1 and then returns the new count:

```
type state = {mutable count : int}

let global = {count = 0}

let incr () : unit =
    global.count <- global.count + 1;
    global.count</pre>
```

How do first-class functions and local state apply here? The problem is that to have more than one counter, we need to generate a new mutable state record for each counter instance. We can do that by making a function that creates the state and then *returns* the incr function that updates the state:

```
type state = {mutable count : int}

let mk_incr () : unit -> int =
  let ctr = {count = 0} in
  let incr () =
    ctr.count <- ctr.count + 1;
    ctr.count
in
incr</pre>
```

Each time we call the mk_incr function, the result will be to create a new counter record ctr and then return a function for incrementing that counter. For example, if were to run the following program, we would get two incr functions, each with its own local counter:

```
let incr1 : unit -> int = mk_incr ()
let _ = incr1 ()
let incr2 : unit -> int = mk_incr ()
```

17.1 Closures

To understand how a call to the mk_incr function evaluates, we need to make one slight refinement to the ASM model of §15—the reason has to deal with returning a function that refers to locally-defined identifiers. In our particular example, the incr function returned by mk_incr refers to ctr, which is *local* to mk_incr. Therefore, the ctr binding will be created on the stack during the evaluation of a call to mk_incr, but that binding

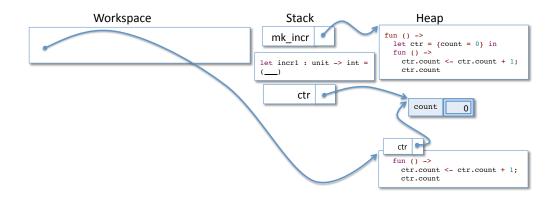


Figure 17.1: This ASM shows how the local function declared in mk_incr stores its own local copy of the stack bindings needed to evaluate its body. Here, since the incr function uses ctr, its *closure* contains a copy of that stack binding.

will be popped off at the point where mk_incr returns!

To remedy this problem, when the ASM stores a function value to the heap, it also stores any of the local stack bindings that might be needed during the evaluation of a call to that function. In this example, since the body of incr refers to ctr, the ASM stores a local copy of the stack binding for ctr with the function data itself. Figure 17.1 shows the state of the ASM at the point just after incr has been stored to the heap but before mk_incr returns. When ctr is popped off the stack, the function incr will still be able to access its value via the locally saved binding. This combination of a function with some local bindings is called a *closure*. As we shall see, closures are intimately related to *objects* of an object-oriented language like Java.

When do the bindings associated with a closure get used? They are needed to evaluate the body of the function, so, whenever a function invocation occurs, any local bindings stored in the function closure are copied back to the stack before the function's argument bindings are created.

Therefore, when we the program above calls <code>incr1</code> (), the <code>ctr</code> value will be copied back on to the stack before the body of the function is executed. This ensure that when the body mentions <code>ctr</code>, there is always the appropriate binding on the stack.

Moreover, since each copy of the function has its *own* closure bindings, multiple calls to mk_incr will result in distinct closures, each with different, local copies of their own counter records. We can see this by looking at the

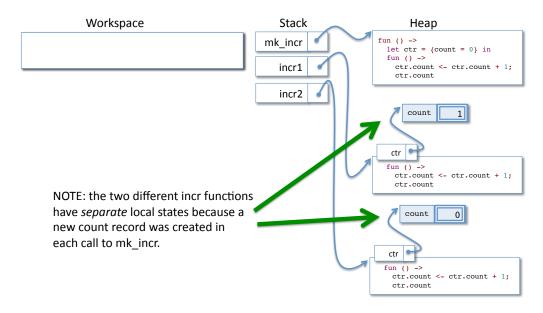


Figure 17.2: The resulting ASM configuration after two calls to mk_incr. Each closure has its own local copy of ctr. Note also that the *only* way to modify the state of the ctr record is to invoke the function—the state is effectively isolated from the rest of the program. This property is called *encapsulation* of state.

state of the ASM after running the second call to mk_incr. As Figure 17.2 shows, there are two closures, each with its own copy of ctr.

Another important aspect of using local state in this way is that the *only* way to access a ctr record is by invoking the corresponding incr function. This means that no other part of the program can accidentally tamper with the value stored in the counter. This kind of isolation of one part of the computer's state from other parts of the program is called *encapsulation*. If the state inside the counter object was more complex and required certain invariants to be maintained, restricting access to only a small number of functions means that we only have to ensure that they preserve the invariants.

17.2 Objects

A second step toward solving the problem of reusable counters is to define a better interface for counters. For example, we might want to decouple

incrementing the counter from reading its current value, or we might want to add the ability to decrement and reset the counter. This leads us to define incr, decr, get, and reset operations. It is straightforward to share a global reference among several functions in this way, as shown here:

```
type state = {mutable count : int}

let global = {count = 0}

let incr () : unit =
    global.count <- global.count + 1

let decr () : unit =
    global.count <- global.count - 1

let get () : int =
    global.count

let reset () : unit =
    global.count <- 0</pre>
```

This is a better interface—we now have a suite of operations that are suitable for manipulating one counter, but it still doesn't allow us to conveniently work with more than one such counter.

The solution to is to package these operations together in a record and, instead of using mk_incr to create one function, use a function called mk_counter that generates all of the functions in one go:

```
type counter = {
  incr : unit -> unit;
  decr : unit -> unit;
  get : unit -> int;
  reset : unit -> unit;
let mk_counter () : counter =
  let ctr : state = {count = 0} in
  {incr = (fun () -> ctr.state <- ctr.state + 1);</pre>
   decr = (fun () -> ctr.state <- ctr.state - 1);</pre>
   get = (fun () -> ctr.state);
   reset = (fun () -> ctr.state <- 0);
let ctr1 : counter = mk_counter () in
let ctr2 : counter = mk_counter () in
;; ctrl.incr ();
;; ctr2.incr ();
;; ctr1.incr ();
let ans : int = ctrl.get ()
```

17.3 The generic 'a ref type

Situations like the counter example above, in which only a single mutable field is needed, arise often in programming. For example, you might need a mutable bool flag that indicates whether some feature of your program should be enabled, or perhaps you need a mutable string to keep track of some data being entered by the user into a text box.

While we could define a new record type specifically for each of these situations (just as we defined the state) type for the counters example), that would quickly become tedious and difficult to work with.

Instead, we can simply define a generic type of "single field" mutable records like this:

```
type 'a ref = {mutable contents : 'a}
```

This type is pronounced "ref" (as in *reference*), and it comes built in to OCaml. Working with the 'a ref type is so common that OCaml also provides syntactic sugar for creating, updating, and getting the value stored

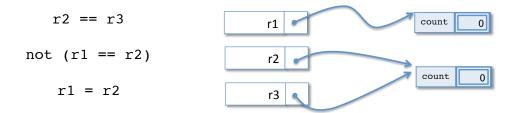


Figure 17.3: The difference between *reference* (==) and *structural* = equality. Reference equality simply checks whether two references point to the same heap location. Structural equality (recursively) compares the two values to see whether all of their contents are the same.

in the contents field of a 'a ref value. These syntactic abbreviations are:

As an example of using these syntactic abbreviations, we could have written the mk_counter function from above as the following, with equivalent results:

```
let mk_counter () : counter =
  let ctr : int ref = ref 0 in
  {incr = (fun () -> ctr := (!ctr) + 1);
  decr = (fun () -> ctr := (!ctr) - 1);
  get = (fun () -> !ctr);
  reset = (fun () -> ctr := 0);
}
```

17.4 Reference (==) vs. Structural Equality (=)

We have seen the importance of understanding aliasing when reasoning about heap-allocated mutable data structures. One natural problem is thus to determine whether two reference values are in fact aliases. OCaml, like all modern programming languages, provides an operation, written v1 == v2 that yields true when v1 and v2 are aliases and false if they are not. This kind of equality, for obvious reasons, is called *reference equality*.

In contrast, the expression v1 = v2 checks whether v1 and v2 are *structurally equal*. This means that = will, in general, traverse the two structures v1 and v2 comparing whether they agree on the values of their primitive

datatype consituent pieces *and* whether the contents of any references are (recursively) structurally equal. Figure 17.3 shows, pictorially, the difference between these two types of equality.

These two types of equality are useful in different circumstances. To summarize:

Structural equality:

- Recursively traverses the structure of the data, comparing the two values' components to make sure they contain the same data.
- May go into an infinite loop if the data structure contains cycles.
- Never considers one function value to be equal to another (even to *iself*).
- Is generally the right kind of equality to use for immutable data.

Reference equality:

- Determines whether two reference values are aliases, or whether primitive values are identical, and never traverses link structure.
- Will say that a function reference is equal only to itself.
- Otherwise equates strictly fewer things than structural equality.
- Is usually the right kind of equality to use for comparing mutable data.

Chapter 18

Wrapping up OCaml: Designing a GUI Library

18.1 Taking Stock

Thus far, we have studied program design "in the small", where the programs we have written are at most a couple of functions, and their use is relatively straightforward. We have studied a general design strategy for developing software, which starts with understanding the problem and then uses *types* and *tests* to further refine that understanding before we actually develop code.

Throughout our studies, we have used OCaml's features to explore different ways of structuring data. First we used pure representations like lists and trees, where the primary way of processing the data is via recursive functions. Then we looked at imperative data structures, such as the queues of the last chapter, where the primary modes of operation are iteration and imperative update. Along the way, we saw many other kinds of structured data: tuples, options, records, functions, *etc...*, which give us tools for thinking about how to decompose the data of a problem into an appropriate form for computing with it. We have also encountered several styles of abstraction—hiding of detail—that can help when structuring larger programs, including generic types and functions, the idea of an abstract type implemented in a module, and the use of hidden (or encapsulated) state of an object.

In subsequent chapters, we will explore these concepts again, this time

from the point of view of Java programming, where we will see that all of the same ideas apply. Here, however, we investigate how to put together all of the tools we developed in OCaml to produce a useful tool, namely a (rudimentary) paint program. Implementing such a paint program isn't that difficult, given the appropriate library for graphical user interface (GUI) design. We make this design process more interesting by developing the GUI library too—that is, we start from OCaml's native graphics library, which doesn't provide any of the familiar components (like buttons, text boxes, scroll bars, etc..) that are used to create a GUI application like the paint program. On top of that simple graphics library, we will build a useable GUI library, modeled after Java's Swing libraries.

"[The OCaml GUI/Paint project was my favorite because] I really enjoyed understanding how graphics works. I thought building up a graphics library from class lectures and on my own was both a very exciting and great learning experience. We don't usually get to see the inner working of libraries but this project afforded me the opportunity to understand what was going on lower level in the code with few abstractions." — Anonymous CIS 120 Student

There are several reasons for going through this design exercise:

- It demonstrates that, even with just the programming techniques we have studied so far, we can build a pretty serious application.
- It illustrates a more complex design process than what we have seen so far.
- As we shall see, that design process leads to the event-driven model of reactive programming, which can be applied in many different contexts.
- It motivates why there are features, such as classes and inheritance, in object-oriented languages like Java.
- It shows how a real GUI library, like Java's Swing, works.

18.2 The Paint Application

As a first step towards designing a GUI library, let us consider an example application that might be built using such a library.

Figure 18.1 shows an example of the kind of paint program that we are aiming to build with the techniques presented in this Chapter.¹ We are

¹We will get started with the design, and leave the rest up to the project associated with this part of the course.

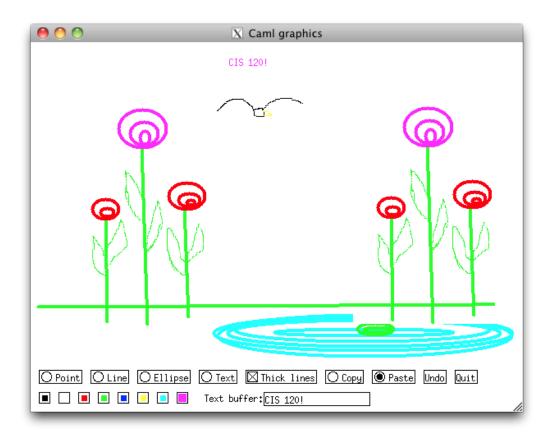


Figure 18.1: An example of a paint program built using the GUI developed in this Chapter.

all familiar with such simple paint programs, which let the user draw pictures with the mouse by clicking the button create lines, ovals, rectangles, and other basic shapes. As the picture shows, this GUI application has "buttons" (like Undo and Quit), "checkboxes" (like Thick Lines), "radio buttons" (like those used for Point, Line, Ellipse, and Text), a "text entry field", custom buttons for color selection, and a "canvas" area on which the user draws his or her picture. These and many other kinds of *widgets* are ubiquitous in applications developed for user interaction.

18.3 OCaml's Graphics Library

What do we need to do to build a library that lets us create buttons, text boxes, *etc.* for use in the paint application? First, let's take a look at the OCaml graphics library, to see what we have to work with.²

Note: To compile a program that uses the graphics library, be sure to include graphics.cma (for bytecode compilation) or graphics.cma (for native compilation) as a flag to the ocamic compiler.

Among other things, OCaml's graphics library provides basic functions for creating a new window, open_graph, erasing the picture displayed in the window, clear_graph, setting the window's size resize_window, and getting the current window's width, size_x, and height, size_y.

The graphics library provides the type color, and a variety of predefined color values like black, white, red, blue, etc.. Importantly, the library manages the graphics window in a stateful way—there are notions of the current "pen color", which can be set using set_color, and a the current "pen location", which can be changed by using move_to. You can draw a single pixel with the current color at coordinates (x,y) by using plot \times y. Similarly, you can draw in the current color starting at the current pen location and ending at the coordinates (x,y) by using line_to \times y. In a similar vein, there are functions for drawing rectangles, ellipses, arcs, and filled versions of these shapes. There are also functions for adjusting the line width used to draw the shapes, ways to put text at a certain location in the window, and work with bitmap images.

So much for drawing things on the screen. Examining the graphics library further, we see that it also provides a type called event, whose values describe the the mouse and keyboard. An event is just a record that indicates the current coordinates of the mouse, whether its button is up or down, whether a key is pressed, and which key. There is also a function that causes the program to wait for a new event to be generated by the user—moving the mouse, pressing the mouse button, or pressing a key.

The graphics library also supports a technique called "double buffering", which is used to prevent flicker when changing or animating parts

²See the graphics library documentation at http://caml.inria.fr/pub/docs/manual-ocaml/libref/Graphics.html.

of the window's displayed graphics. The idea is that, when double buffering is enabled, the graphics drawing commands affect a second copy of the window, which is not displayed on the screen. After the entire window is updated, the synchronize function causes the hidden buffer to be displayed (and re-uses the displayed memory space for subsequent drawing). This prevents flicker that would be caused by changing the graphics displayed in the window as they are drawn piece-meal using the primitive graphics operations.

What the graphics library does not provide is any kind of higher-level abstraction like "button" or "text box"—our GUI library will have to implement these features by using the graphics primitives.

18.4 Design of the GUI Library

How do we go from simple drawing operations and rudimentary information about the mouse and keyboard to a full-blown GUI application like the paint program? There are several issues to consider. It's clear that one of the jobs of a GUI library is to provide easy ways to construct buttons and other widgets that a program like paint can use. Since the typical GUI application involves lots of different kinds of buttons, we must consider how to share the code that is common to all (or at least many) buttons—for example, we might want a button to have an associated string (like "Undo" or "Quit") that is displayed as its label. Traditionally, GUI widgets like buttons include a rectangular border (or other visual cue) that separates the button from other regions of the window. One design challenge is thus how to conveniently package the visual attributes of widgets so that they can be reused.

A related issue is how those buttons and other widgets are positioned on the the screen relative to one another. Given the drawing primitives in the graphics library, we could imagine painstakingly drawing each line of every button using the "global" coordinate system of the window, but this would be extremely tedious and very brittle—one small change to how we want to layout the buttons of the application might prompt large, intertwined changes to the program responsible for drawing the entire window. Moreover, it's not clear how we would write that program so that, for example, just one part of the window could easily be changed (for example to put an X in a checkbox widget).

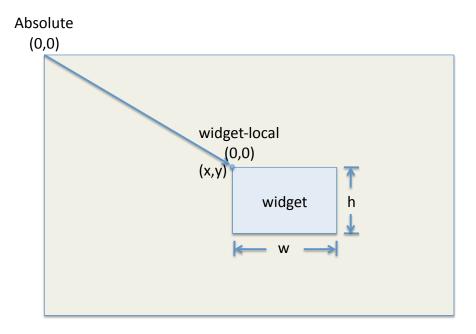


Figure 18.2: A widget draws itself in terms of widget-local coordinates, which are made relative to the global coordinate system by using a Gctxt.t value, which, among other things, contains the (x,y) "offset" from the origin of the graphics window. Here the grey region represents the entire graphics window . Each widget also keeps track of its width and height, which are needed for computing layour information.

Finally, there is the issue of how to process the user-generated mouse and keyboard inputs. This also turns out to be related to how the widgets are arranged in the window, since the GUI library will need to determine, based on the coordinates of the mouse click, which widget the user intended to interact with. For example, when a user clicks on a part of the window occupied by a button widget, our GUI library will have to somehow determine that the button was clicked. Moreover, since each button will typically trigger a different behavior, each button should somehow be associated with a piece of code that gets run when the mouse click occurs.

The next several sections tackle each of these problems in turn.

18.5 Localizing Coordinates

The first challenge we'll tackle is how to structure the code for drawing widget components so that it can be reused. The key idea is to make each widget in charge of drawing itself, but arrange it so that any positional information used to draw the widget can be specified using a *widget-local* coordinate system. The code for drawing a widget can therefore be written as though the widget is always located with its upper-left corner located at (0,0); in reality, the commands used to draw the widget will transparently be translated by some offset (x,y) from the actual origin of the window. Figure 18.2 shows this situation pictorially.

To implement this idea, we create a module called <code>Gctx</code> (for "graphics context") whose main type <code>gctx</code> represents the "contextual information" needed to draw a widget. For now, that context is just the (x,y) offset from the upper-left corner of the window. The main functionality provided by the <code>Gctx</code> module is to translate between the widget-local coordinates used by the widget drawing function and the coordinate system used by the OCaml graphics module.

There's one other discrepancy between the global coordinate system provided by the OCaml graphics library and the one we'd prefer for GUI applications: the graphics library uses Cartesian coordinates where the origin (0,0) is located at the lower-left corner of the graphics window, and the y axis increases upwards in the vertical direction. This set up is handy for plotting mathematical functions—it agrees with the usual way we think of the coordinate system when we graph a function in algebra or calculus. Unfortunately, locating (0,0) in the lower-left is not very good for GUI applications. The issue is that when a user resizes the window, the typical GUI behavior is to make more space available to the application. Importantly, the menu bars, etc. that appear at the top of the screen should remain fixed—the extra space obtained by resizing the window should appear at the bottom of the window, not the top. This means that for GUI applications, the global origin should be located in the top-left corner of the window.

These considerations lead us to a design in which the GCTX module provides a type GCTX that stores the position relative to which a widget should be drawn. Its X and Y coordinates are with respect to the GUI-global origin (0,0), located at the top-left corner of the graphics window, and for which Y values increase downwards in the vertical direction. The

GCTX module also provides functions that translate from widget-local to OCaml graphics coordinates, relative to the GCTX.GCTX offset. The GCTX module also "wraps" each of the primitive OCaml graphics routines to do the translation from widget-local to OCaml coordinates—this means that all of the widget drawing code can be written in a position-independent way.

Since the OCaml graphics library also maintains a current pen color, it is useful to add a color component to the <code>Gctx.gctx</code>, which will allow our GUI library to (potentially) define a widget's visual appearance relative to the color in addition to making them relative to their position in the window. The <code>Gctx</code> drawing operations therefore also set the OCaml graphics pen color accordingly.

Here is a sample of the resulting code for the GCTX module (the full implementation wraps more drawing routines than just the ones shown below):

```
(* Gctx.ml *)
type gctx = {
                 (* offset from (0,0) in GUI coords *)
 x:int; y:int;
  color:Graphics.color; (* the current pen color *)
(* This function takes widget-local coordinates (x, y) to OCaml
   graphics coordinates, relative to the graphics context. *)
let ocaml_coords (g:gctx) ((x,y):int*int) : (int*int) =
  (g.x + x, Graphics.size_y()-(g.y + y))
(* This function takes OCaml Graphics coordinates (x,y)
   to widget-local graphics coordinates, relative to the
   graphics context *)
let local_coords (g:gctx) ((x,y):int*int) : (int*int) =
  (x - g.x, (Graphics.size_y() - y) - g.y)
type color = Graphics.color
(* Produce a new Gctx.gctx with a different pen color *)
let set_color (g:gctx) (c:color) : t =
  {g with color=c}
(* Set the OCaml graphics library's internal state so that it
  agrees with the Gctx settings. *)
let set_graphics_state (g:gctx) : unit =
 Graphics.set_color g.color
(* Each of these functions takes inputs in widget-local
   coordinates, converts them to OCaml coordinates, and then
   draws the appropriate shape. *)
let draw_line (g:gctx) (p1:int*int) (p2:int*int) : unit =
  set_graphics_state g;
  let (x1,y1) = ocaml_coords g p1 in
  let (x2,y2) = ocaml_coords g p2 in
    Graphics.moveto x1 y1;
    Graphics.lineto x2 y2
let draw_string (g:gctx) (p:int*int) (s:string) : unit =
  set_graphics_state g;
  let (_, height) = Graphics.text_size s in
  let (x,y) = ocaml_coords g p in
    Graphics.moveto x (y - height); (* Ocaml coords *)
    Graphics.draw_string s
```

18.6 Simple Widgets & Layout

The Gotx module lets us relativize drawing to a widget-local coordinate system. Now, let us see how we can use the Gotx.gotx structure to address the challenge of laying out widgets on the window. At a minimum, a widget will need to be able to draw itself relative to a graphics context. Since each widget will occupy some region of the window, a widget should also be able to report its size, so that we can position one widget relative to another.

This leads us to the following type for (simple) widget objects³:

```
(* The widget module *)

type widget = {
  repaint : Gctx.gctx -> unit;
  size : Gctx.gctx -> (int * int);
}
```

The repaint function asks the widget to draw itself using the GCTX drawing primitives—we call it "repaint" because, eventually, we repeatedly draw widgets to the screen, which allows for animation or changes to the visual state of the GUI application. For example, a checkbox widget's repaint function might draw an X depending on whether the checkbox is selected (as shown in the "Thick Lines" checkbox of Figure 18.1).

Given just the widget type above, we can already create some simple widgets. The simplest widget does nothing but occupy space in the window—it's repaint function does nothing, and its size is determined by parameters passed in when constructing the widget object.

```
(* The simplest widget just occupies space. *)
let space ((w,h):int * int) : widget =
    {
      repaint = (fun _ -> ())
      size = (fun _ -> (w,h));
    }
```

Another simple widget just draws a string:

³In §18.10 we will extend this type to deal with user events

```
(* Display a string on the screen. *)
let label (s:string) : widget =
    {
      repaint = (fun (g:Gctx.gctx) -> Gctx.draw_string g s);
      size = (fun (g:Gctx.gctx) -> Gctx.text_size g s)
    }
```

The label widget's repaint function just uses the draw_string operation provided by Gctx, its size is just the size of the string when drawn on the window.

Another useful widget simply exposes a fixed-sized region of the screen as a "canvas" that can be painted on by using the Gotx drawing routines. The canvas widget is just a widget parameterized by the repaint function:

The three widgets above don't yet do anything very interesting to the window display. Since we will eventually want to draw buttons and other complex widgets with lines indicating their boundaries, it is useful to create a widget border wrapper. Given a widget w, the widget border w simply draws a rectangular border around the outside of w. The border widget therefore calls the wrapped widget's repaint method and also adds its own code to draw the rectangle around the inner widget. The only wrinkle is that we have to be a bit careful with the graphics context. Figure 18.3 illustrates the situation—the border widget's repaint function should call w's repaint function, but, since w's upper-left corner is not located at the origin, we have to *translate* the graphics context slightly before passing it on to w's repaint. This functionality is easy to add to the Gctx module:

```
(* Gctx.ml *)
(* Shifts the gctx by (dx,dy) *)
let translate (g:t) ((dx,dy):int*int) : gctx =
    {g with x=g.x+dx; y=g.y+dy}
```

Given this translate function, it is then easy to implement the functionality of the border widget: the size function simply pads the size of

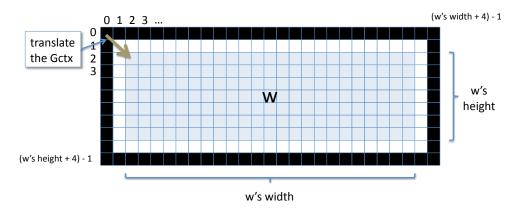


Figure 18.3: The border widget wraps another widget w with a one-pixel thick line set one pixel away from the inner widget. The border widget's repaint funtion calls w's repaint, but must use GCtx.translate to "shift" the inner widget's local coordinate system to (2,2), relative to the border widget's local origin.

the inner widget by four pixels in each direction; the repaint function draws four lines for the border, translates the Gctx.gctx and then calls w's repaint.

```
(* Adds a one-pixel border to an existing widget. *)
let border (w:widget) : widget =
  repaint = (fun (g: Gctx.gctx) ->
        let (width, height) = w.size g in
                  (* not +4 because we count from 0 *)
        let x = width + 3 in
        let y = height + 3 in
          Gctx.draw_line g (0,0) (x,0);
          Gctx.draw_line g (0,0) (0,y);
          Gctx.draw_line g (x, 0) (x, y);
          Gctx.draw_line g (0,y) (x,y);
          let g = Gctx.translate g (2,2) in
            w.repaint g)
  size = (fun (g: Gctx.gctx) ->
        let (width, height) = w.size g in
          width + 4, height + 4);
  }
```

The translate function also suggests how we can create a "wrapper" widget that will lay out two widgets side-by-side in the window. The idea

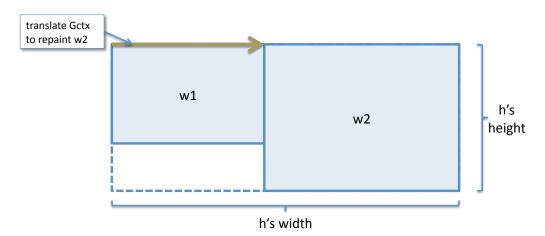


Figure 18.4: The call hpair w1 w2 yields a widget h comprised of w1 and w2 layed out horizontally adjacent to one another. The right widget's Gctxt.t must be translated by the width of the left widget.

is to simply translate the right widget horizontally by the width of the left widget, as shown in Figure 18.4. The <code>size</code> is simply the sum of the two widgets' heights and maximum of their heights. The resulting "horizontal pair" widget code looks like this:

```
(* The hpair widget lays out two widgets horizontally. They
    are aligned at their top edge. *)
let hpair (w1:widget) (w2:widget) : widget =
    {
    repaint =
        (fun (g:Gctx.gctx) ->
        w1.repaint g;
    let g = Gctx.translate g (fst (w1.size g),0) in
            w2.repaint g);
    size =
        (fun (g:Gctx.gctx) ->
        let (x1,y1) = w1.size g in
        let (x2,y2) = w2.size g in
        (x1 + x2, max y1 y2))
}
```

18.7 The widget hierarchy and the run function

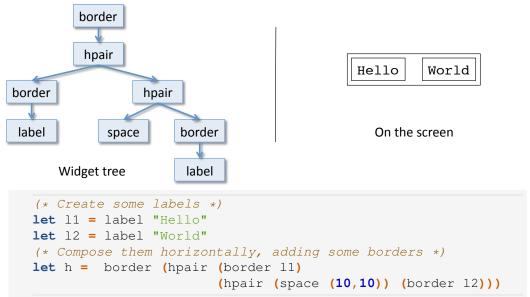


Figure 18.5: Widgets form a tree: each "wrapper" widget like a border or hpair contains one or more children. The tree on the left above corresponds to the widget h created by the program above. When painted to the graphics window, h would be displayed as shown on the right.

So far, we have tackled the problem of layout and modular reuse of widget code. The Gctx and Widget modules together give us a way of constructing more complex widgets out of smaller ones by arranging them spatially in the graphics window.

When we build an application (such as the paint program) that uses the Widget.widget types to construct a user interface, we can think of the widget instances as building a *tree*—the leaves of the tree are the "primitive" widgets like layout, space, and canvas (which don't have any sub-widgets inside them), and the nodes of the tree are those widgets, like border and hpair, that "wrap" one or more children. Figure 18.5 shows pictorially what such a widget tree looks like for a concrete widget program.

To paint a widget hierarchy to a graphics window, all we have to do is invoke the repaint function of the root widget, giving it an initial graphics context. For example, calling h.repaint for the program of Figure 18.5 will cause the image shown on the right-hand side of the Figure to be displayed.

As a first cut for the top-level program, we can thus create a run func-

tion that takes in the root widget, creates a new OCaml graphics window, asks the widget to repaint itself, and then goes into an infinite loop. (We have to use some kind of loop, otherwise the program would draw the widget and then exit too quickly for us to see the resulting graphics!)

As we shall see next, we will modify this top-level loop so that it can process user-generated GUI events, such as mouse motions.

18.8 The Event Loop

We have successfully addressed one of the design challenges for building a GUI library: the combination of GCTX and Widget modules provide a clean way of creating re-usable graphical components that can be positioned relative to one another in the window. The remaining challenge is how to process user-generated *events*, such as mouse clicks, mouse motion, or key presses.

The first step toward solving this problem is to replace the run function we just saw with something more useful. Consider the paint application, for example. Unless the user provides some input, by using the mouse to click a button or draw in the paint canvas, the paint program itself does nothing—it passively waits for a event that it knows how to process, processes the event, which might cause the visual display of the paint program to be altered, and then goes back to waiting for another event. Clearly, the infinite loop of the run function should be replaced by some code that waits for a user event to process and then somehow updates the internal state of the application. At the start of each loop iteration, we can clear the entire graphics window and then ask the root widget to repaint itself. This leads to a run function with the following

structure:

```
open Widget;;
This function takes a widget, which is the "root" of the GUI
interface. It starts with "top-level" \cd{qctx}, and then it
goes into an infinite loop. The loop simply repeats these
steps forever:
    - clear the graphics window
    - ask the widget to repaint itself
    - wait for a user input event
    - forward the event to the widget's event handler
let run (w:widget) : unit =
 Graphics.auto_synchronize false; (* draw to hidden buffer *)
 let rec loop () =
   Graphics.clear_graph ();
   w.repaint g;
   (* show freshly painted window *)
   Graphics.synchronize ();
   (* wait for user input event *)
   let e = Gctx.wait_for_event q in
     (* widget handles the event *)
     w.handle g e; loop ()
   loop ()
```

Here, the OCaml graphics library is set to use double buffering by turning off auto synchronization. Double buffering is a technique used to eliminate flicker caused when graphics are written incrementally to the display device; rather than do that, all of the graphics are written to a "backing buffer", which is then displayed all at once when the Graphics.synchronize function is invoked.

The new part of this run function is what allows the GUI program to be interactive— it consists of two lines of code, which make use of some new functionality that we will add to the GCTX and Widget modules, as explained in more detail below:

```
(* wait for user input event *)
let e = Gctx.wait_for_event g in
    (* widget handles the event *)
    w.Widget.handle g e;
    loop ()
```

First, the new function wait_for_event tells the program to wait for a new user-generated mouse or keyboard event. Second, once an event is received, we call the root widget's handle function to ask it to process the event.

18.9 GUI Events

An event is just a value that represents a signal from the underlying operating system to the OCaml graphics library. As shown by the definition of the type status, found the OCaml graphics module, events carry information about the mouse coordinates, button status, and keyboard information:

Since such events carry coordinate information about where in the window the event occurred (i.e. where the mouse is), we need to extend the GCTX module to provide a way of mapping OCaml event coordinates to widget-local events. We can also create some helper functions for accessing the information about a given event, relative to a graphics context. It is straightforward to add these features to the GCTX module, like so:

```
type event = Graphics.status
(* Waits for a mouse or key event *)
let wait_for_event (g:gctx) : event =
  Graphics.wait next event
    [Graphics.Mouse_motion;
     Graphics.Button_down;
     Graphics.Button_up;
     Graphics.Key_pressed]
(* Determine whether the event has the button pressed *)
let button_pressed (g:gctx) (e:event) : bool =
  e.Graphics.button
(* Get the widget-local coordinates of an event *)
let event_pos (q:qctx) (e:event) : int * int =
 local_coords g (e.Graphics.mouse_x, e.Graphics.mouse_y)
(* Determine whether the event has a key pressed *)
let is_keypressed (g:gctx) (e:event) : bool =
  e.Graphics.keypressed
(* Get the keyboard character associated with an event *)
let get_key (g:gctx) (e:event) : char =
  e.Graphics.key
```

18.10 Event Handlers

Once an event has been received by the top-level event loop (the run function), it asks the root widget w to handle the event. To allow widgets to react to events, we need to extend their type with a new function, called handle. This function takes in a Gctx.gctx and a Gctx.event, and processes the event in a widget-specific fashion.

The type of widgets is thus modified from what we had earlier to be:

```
(* The interface type common to all widgets *)
type widget = {
  repaint: Gctx.gctx -> unit;
  handle: Gctx.gctx -> Gctx.event -> unit;
  size: Gctx.gctx -> int * int
}
```

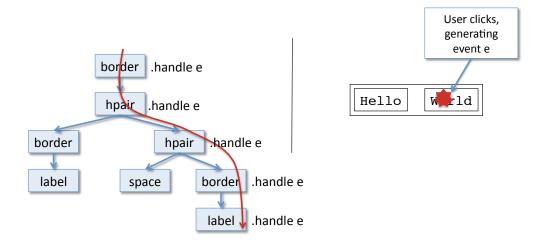


Figure 18.6: When a user clicks some place in the GUI window, the resulting event is routed through the widget heirarchy starting at the root. Each node forwards the event by calling a child widget's handle function after suitably translating the <code>Gctx.t</code> value. Which child gets the event is determined by their size, layout, and the coordinates of the event.

How does our program know what to do when the user clicks on a region of the window that displays a particular button, like "Undo" in the paint program? Clearly each button will (in general) need to be associated with some bit of code that gets executed when it is clicked, but there must also be some way to "route" the event to the appropriate widget of the widget hierarchy.

We have actually already encountered a similar problem twice before, albeit in very different contexts. First, recall that when inserting a new value into a binary search tree we exploited the ordering structure of the values in the nodes of the tree to "route" the new value to its proper location. Second, recall that, for Homework 4 we used quad trees to partition a 2D region of the plane and that inserting a point into the quad tree essentially amounted to "routing" the point to its proper location in the tree based on its coordinates.

For routing events to widgets, we use a similar idea: the "container" widgets like border and hpair use the spatial information about the layout of their subwidgets to decide which of the children's handle functions should be called. This situation is depicted in Figure 18.6.

For example, the border widget simply passes any events received

by its handler to its only child, but only after suitably translating the Gctx.gctx so that the child can interpret the event relative to its own local coordinate system.

Similarly, the hpair widget checks which of its two children should receive the event and forwards it to the appropriate one. Note that, since there is some "dead space" created if one of the two children is shorter than the other, it is possible that neither child will receive the event. Events that occur in the "dead space" are simply dropped by the hpair widget. Thus we have:

```
(* Determines whether a given event is within a
   region of a widget whose upper-left hand corner is (0,0)
   with width w and height h. *)
let event_within (g:Gctx.gctx)
                (e:Gctx.event)
                 ((w,h):int*int) : bool =
  let (mouse_x, mouse_y) = Gctx.event_pos g e in
   mouse_x >= 0 && mouse_x < w &&
   mouse_y >= 0 && mouse_y < h
let hpair (w1:widget) (w2:widget) : widget =
   repaint = ...; (* same as before *)
   size = ...; (* same as before *)
   (fun (g:Gctx.gctx) (e:Gctx.event) ->
     if event within q e (w1.size q)
     then w1.handle g e
      else
        let x = fst (w1.size g) in
        let g = Gctx.translate g (x, 0) in
          if event_within g e (w2.size g)
         then w2.handle q e
         else ());
  }
```

Modifying the space, label, and canvas widgets is straightforward—each of their handle functions simple does nothing. Of course, we might like to add the ability for a widget of one of these types to handle events as well, but we will do so using the notifier widget described below. First, though, we need to consider how widgets with local state can be constructed.

18.11 Stateful Widgets

Consider the simple label widget that we saw earlier.

```
(* Display a string on the screen. *)
let label (s:string) : widget =
    {
      repaint = (fun (g:Gctx.gctx) -> Gctx.draw_string g s);
      size = (fun (g:Gctx.gctx) -> Gctx.text_size g s);
      handle = (fun (g:Gctx.gctx) (e:Gctxt.event) -> ())
}
```

This widget is *stateless* in the sense that, once the string has been associated with the label, the string never changes.

If we wanted to be able to modify the string displayed by a label, we could use the techniques of §17 to give the label widget some *local state*, like this:

However, although the code above creates a mutable string ref in which to store the label's string, code external to the label widget cannot modify the contents of lbl. To do that, we need to also expose a function that lets other parts of the program update lbl. We call such a function a label controller since it controls the string displayed by a label. Given the

type of label_controller records, it is easy to modify the label function to create a widget (of type widget) and a label_controller:

Now when we call the label function, it returns a pair consisting of a widget and a label controller that can be used to change the string displayed by the label.

More generally, any stateful widget will have its own kind of controller that can be used to modify the widgets state.

18.12 Listeners and Notifiers

Different widgets may need to react to different kinds of events. For example, a button needs to "listen" for mouseclick events and then run some appropriate code; a scrollbar might have to "listen" for mouse drag events (mouse motion with the button down); a textbox widget might have to "listen" for key press events. Moreover, the way that a button (or other widget) responds to a certain event might change depending on application context. In general, whether or not a widget should "listen" for a particular event might also depend on application-specific state.

How can we easily capture the wide variety of possible ways that a widget might want to interact with user-generated events? How can we modularly add or remove code for processing events? Our solution (which is based on Java's Swing library) is to introduce a new kind of widget called a *notifier*. The idea is that a notifier widget "eavesdrops on" or "listens to" the events flowing through a part of the widget hierarchy. It manages a list of *event listeners*, which are a bit like handle functions except that they don't really participate in routing events through the widget

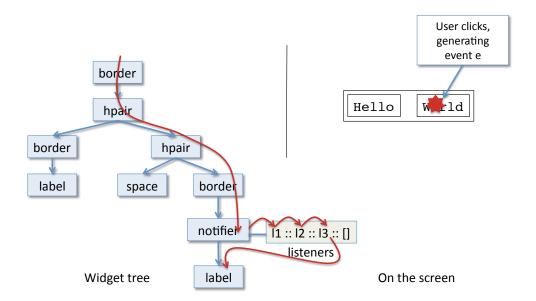


Figure 18.7: A notifier widget maintains in its local state a list of "listeners" that get a chance to process events that flow through the widget tree. Which listeners are associated with the notifier can be changed using a notifier controller.

hierarchy—they simply listen for a particular kind of event, react to it, and then either propagate the event or stop it from being further processed. Figure 18.7 shows pictorially, how we might add a notifier widget to the "Hello World" example.

Notifiers, like the stateful version of label widgets discussed above, maintain some local state—in this case a list of event_listener objects. Thus, each notifier widget comes equipped with a notifier_controller that can be used to modify the list of listeners. For simplicity in the code below, the notifier_controller only allows new event_listener objects to be *added* to the notifier; it is easy to extend this idea to allow event_listeners to be removed as well.

These design criteria lead us to create a type for event_listener functions that looks like this:

```
type event_listener_result =
    | EventFinished
    | EventNotDone

type event_listener =
    Gctx.gctx -> Gctx.event -> event_listener_result
```

An event_listener is just a function that, like a handle method of a widget, takes a Gctx.gctx and Gctx.event and processes the event. Unlike a handler, which always returns unit, an event_listener can return either EventFinished, which signals to the notifier that the event should not be further processed by listeners that are "down stream" in the widget tree, or EventNotDone, which signals that the event should be propagated.

Once we have defined the type of event_listeners, it is straightforward to define the behavior of the notifier widget and its notifier_controller:

```
(*
 A notifier_controller is associated with a notifier widget.
  It allows the program to add event listeners to the
 notifier.
type notifier_controller = {
  add_event_listener: event_listener -> unit
(*
 A notifier widget is a widget "wrapper" that doesn't take up
  any extra screen space -- it extends an existing widget with
  the ability to react to events. It maintains a list of
  "listeners" that eavesdrop on the events propagated through
  the notifier widget.
   When an event comes in to the notifier, it is passed
   to each listener in turn until one of them declares
   the event to be "finished".
*)
let notifier (w: t) : widget * notifier_controller =
  let listeners = { contents = [] } in
    repaint = w.repaint;
   handle =
   (fun (g:Gctx.gctx) (e: Gctx.event) ->
      let rec loop (l: event_listener list) : unit =
        begin match 1 with
          [] -> w.handle g e
          | h::t -> begin match h g e with
                   | EventFinished -> ()
                   | EventNotDone -> loop t
                 end
        end in
        loop listeners.contents);
   size = w.size
    },
    add event listener =
      fun (newl: event_listener) ->
        listeners.contents <- newl::listeners.contents</pre>
```

With this infrastructure in place, it is easy to define specialized event listeners that react to particular kinds of events. For example, it is useful to define a mouseclick_listener, parameterized by an action to perform when the mouse is clicked:

A mouse_listener, in contrast, exposes another convenient way of reacting to mouse events—it unpacks the mouse button and position information from an event e and passes that data to an action function. A client application like the Paint program might add a mouse_listener to a canvas widget to allow the canvas to react to user-generated mouse events on the canvas.

18.13 Buttons (at last!)

Our GUI library finally has enough functionality to implement a traditional button widget: A button is just a label widget wrapped in a notifier. The resulting widget has both a label_controller and a notifier_controller, which can be used to change the state of the button.

To add the ability to react to a mouse click event to the button, which is typically the desired behavior, we can simply use the notifier_controller's add_event_listener function to add a mouseclick_listener. For example, to create a button that prints "Hello, world!" to the console each time it is clicked, we could write the following code:

```
let (hw_button, _, hw_nc) = button "Print It!"

let print_hw () : unit =
    print_endline "Hello, world!"

;; hw_nc.add_event_listener (mouseclick_listener print_hw)
```

The hw_button widget could then be added to a larger widget tree using layout widgets, or, simply run as the entire "application". The latter would be accomplished by doing:

```
;; Eventloop.run hw_button
```

18.14 Building a GUI App: Lightswitch

We're finally in position to build an application on top of the GUI library. Figure 18.8 shows the basic structure of an application built using the GUI library—the application never has to interact directly with the underlying OCaml primitives; instead it works with the operations provided by the Gctx, Widget, and Eventloop modules. Together those three components provide an appropriate collection of abstractions for building GUI programs. Of course, the feature set we have seen in this Chapter is far from

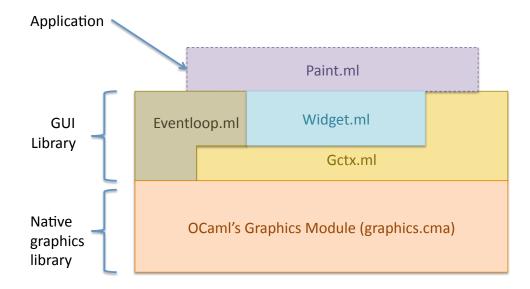
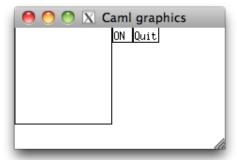


Figure 18.8: The resulting software "architecture" for an application built on top of the GUI library. An application like the Paint program should never interact with the OCaml graphics library directly; it should instead call functions in the <code>Gctx</code>, <code>Widget</code>, and <code>Eventloop</code> modules.

complete—a fully fledged GUI library would provide much more functionality, including, other graphics drawing primitives, layout options, and widgets. Adding such features is simply a matter of extending the GCTX and Widget modules, following more or less the same pattern as we have seen above. The Paint program GUI project associated with this part of the course explores how to make such changes, to the extent that we can implement the paint program pictured in Figure 18.1.

Even though the GUI library is rather primitive, we can still use it to demonstrate how all of the pieces fit together. The program below builds a "lightswitch" application, shown in Figure 18.9.



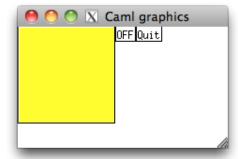


Figure 18.9: The "lightswitch" application both before (left) and after (right) the On/Off button has been pressed.

```
(* This program demonstrates how to build an application
   on top of the CIS 120 GUI library. It assumes that
   the eventloop.ml*, gctx.ml*, and widget.ml* files
   are all present. *)
open Widget
(* Create the state affected by the light switch *)
let switched_on : bool ref = { contents = false}
(* Create a lightswitch button, initially labeled "ON " *)
let (b, l, n) =
   Widget.button "ON "
(* The action associated with clicking the switch. *)
let flip () : unit =
  switched_on.contents <- not (switched_on.contents);</pre>
  if switched on contents then
    l.set_label "OFF"
  else
    l.set_label "ON "
(* Add the flip action as a mouseclick_listener *)
;; n.add_event_listener (Widget.mouseclick_listener flip)
```

```
(* Create the "QUIT" button *)
let (b2, _{-}, n2) =
   Widget.button "QUIT"
(* The action associated with the QUIT button *)
let quit () : unit =
  exit 0
(* Add the quit action as a mouseclick_listener *)
;; n2.add_event_listener (Widget.mouseclick_listener quit)
(* Create the "lightbulb" canvas *)
let repaint_light (g:Gctx.gctx) : unit =
  if !switched_on then
   let g = Gctx.with_color g Gctx.yellow in
   Gctx.fill_rect g (0,0) (100,100)
  else
     ()
let (light,_) = Widget.canvas (100,100) repaint_light
(* Package all the pieces together into a root widget *)
let w : Widget.widget =
 Widget.border (Widget.border (hpair
    (Widget.border light)
    (hpair (Widget.border b) (Widget.border b2))))
(* Start waiting for events *)
;; Eventloop.run w
```

Chapter 19

Transition to Java

19.1 Farewell to OCaml

In this chapter we begin our transition to Java programming. As we shall see, many of the concepts and ideas that we have explored in the context of OCaml arise again for Java—the two languages, despite being very different superficially and having different "feels" are actually more similar than you might expect. Understanding OCaml programming well walues like we do in OCaml, so I kept

By now we have actually seen most of OCaml's important features—the language itself is not very big. But we have left out a few things:

- One of OCaml's strengths is its module system, which provides support for large-scale programming. We saw just the tip of the iceberg here in §9 when we studied *structures* and *signatures*. The key feature we haven't seen is called *functor*, which is a function from one structure to another.

 Student
- The "O" in OCaml stands for "object". OCaml does include a powerful system of classes and objects, similar to those found in other *object-oriented* OO languages. We have left them out so that we can study OO programming in Java, without the potential for confusion.
- OCaml's type system also provides very strong support for *type in-ference*. Almost all of the type annotations that we've been writing as

"Transitioning from one mindset to another was challenging; I forgot syntax and kept thinking about everything in Java as values like we do in OCaml, so I kept leaving "return" off of everything. I also forgot about how instance variables in a class are used. But after I realized those key things, I felt great in Java again." — Anonymous CIS 120 Student

part of our OCaml code can be completely omitted; the compiler's type checker is able to figure out the types of every expression by looking at how the program is structured.

The functional programming style that OCaml promotes emphasizes several key concepts: the idea that program computations should be thought of as computing with values, which, for the most part are immutable tree-structured data. The main ways of working with such data are pattern matching, which lets the program examine the structure of the data, and recursion, which is the natural way to process inductively defined trees.

In this context, we have seen the importance of using abstract types to preserve invariants while manipulating mutable data structures (as in the queue operations of $\S16$.)

The functional style is good for expressing simple, elegant descriptions of complex algorithms and/or data structures. The limited use of mutability, and persistence-by-default, makes functional programming well-suited for parallelism, concurrency, and distributed applications (though we haven't touched on these aspects in this course). OCaml's tree-structured datatypes are also well-suited for a variety of "symbolic processing" tasks, including building compilers, theorem provers, etc..

Dialects of ML, and other functional programming languages like Scheme and Haskell, have had a big impact on the design of "modern" programming languages like C#, Java, and, to a lesser extent, C++. The use of generic programming and type inference, for example, was pioneered in ML. Object-oriented languages like Java and C# are beginning to incorporate features that support functional-programming idioms—for example, future versions of Java will include closures (*i.e.* anonymous functions) that are so pervasive in OCaml. Moreover, while C#, C++, and Java encourage the use of mutable state with their defaults, many "best practice" approaches to software development in these language actively discourage using imperative state.

Finally, some languages strive to merge the functional and the objectoriented styles of programming. These "hybrid" languages including Scala and Python, for example, offer functional programming as one possibility among many styles of writing code.

For all of these reasons, learning OCaml will give you a new perspective on how to go about solving problems in *any* programming language

that you encounter. Understanding when functional programming is an appropriate solution to a problem can let you write better code no matter what language you use to express that solution.

The succinctness and clarity of OCaml for these kinds of tasks, can be about null was probably shown by comparing this (hopefully by now!) straightforward OCaml program that defines the tree type and an is_empty function along with a use of it, to its equivalent in Java.

```
"Having to worry
the hardest [part of the
transition]. Also I really
missed being able to
match things." —
Anonymous CIS 120
Student
```

```
type 'a tree =
  Empty
  | Node of ('a tree) * 'a * ('a tree)
let is_empty (t:'a tree) =
 begin match t with
    | Empty -> true
    | Node (_,_,_) -> false
let t : int tree = Node (Empty, 3, Empty)
let ans : bool = is_empty t
```

The corresponding Java program is much more verbose (and isn't even fully operational, since I have omitted the methods needed to access the tree's values). (Don't worry about understanding the code yet, the next several chapters will explain all of the necessary pieces.)

```
interface Tree<A> {
 public boolean isEmpty();
class Empty<A> implements Tree<A> {
  public boolean isEmpty() {
     return true;
class Node<A> implements Tree<A> {
 private final A v;
 private final Tree<A> lt;
 private final Tree<A> rt;
 Node (Tree<A> lt, A v, Tree<A> rt) {
   this.lt = lt; this.rt = rt; this.v = v;
 public boolean isEmpty() {
    return false;
class Program {
  public static void main(String[] args) {
    Tree<Integer> t =
    new Node<Integer>(new Empty<Integer>(),
    3, new Empty<Integer>());
    boolean ans = t.isEmpty();
}
```

Though working with OCaml and the functional style are a good way to broaden your mental toolbox, it is also essential to be able to work fluently in other programming paradigms. Just as the program above can be written very cleanly in the functional style, there are Java programs that would be difficult to express cleanly in OCaml. For this reason, we will study object-oriented programming using Java.

Java, of course, offers the benefits of being a widely-used, "industrial strength" programming language with a large ecosystem of libraries, tools, and other resources designed for professional software developers. Java as a programming language is itself a rather large and complicated entity (with good reason!), which has evolved over the years and is continuing to change.

The goal of studying object-oriented programming in Java is not, therefore, so that you become an expert Java developer. Instead, the goal is to give you an understanding of the essence of object-oriented languages, and how their features can be used to address programming design problems.

19.2 Objects and Classes

The fundamental difference between OCaml and Java is Java's pervasive use of *objects* as the means of structuring data and code. Java syntax provides a convenient way to *encapsulate* some state along with operations on that state. To see what this means, consider this variant of the counter program that we saw earlier when discussing local state (see §17):

```
(* The type of a counter's local state. *)
type counter_state = {mutable cnt : int}

(* Methods for interacting with a counter object. *)
type counter = {
   inc: unit -> int;
   dec: unit -> int;
}

(* Constructs a fresh counter object with its own local state. *)
let new_counter () : counter =
   let s : counter_state = {cnt = 0} in
   {
      inc = (fun () -> s.cnt <- s.cnt+1; s.cnt);
      dec = (fun () -> s.cnt <- s.cnt-1; s.cnt);
}

(* Create a new counter and then use it. *)
let c : counter = new_counter () in
;; print_int (c.inc ())
;; print_int (c.dec ())</pre>
```

This OCaml program illustrates the three key features of an object:

- An object encapsulates some local, often mutable state. That local state
 is visible only to the methods of the object.
- An object is defined by the set of *methods* it provides—the only way

to interact with an object is by invoking (*i.e.* calling) these methods. Moreover, the type of the encapsulated state does not appear in the object's type.

• There is a way to construct multiple *instances—new* object values—that behave similarly (and therefore share implementation details).

In the OCaml example above, the first feature is embodied by the use of the type <code>counter_state</code>, which describes that local state associated with each counter object. The second feature is realized by the type <code>counter</code>, which exposes only the two methods available for working with counter objects. Finally, the function <code>new_counter</code> provides a way to create new <code>counter</code> instances (i.e. values of type <code>counter</code>). The use of local scoping ensures that the state <code>s</code> is only available to the code of the <code>inc</code> and <code>dec</code> methods, and therefore cannot be touched elsewhere in the program—the state <code>s</code> is encapsulated properly.

Java's notation and programming model make it easier to work with data and functions in this style. A Java class combines all three features—local state, method definitions, and instantiation—into one construct. Think of a class as a template for constructing instances of objects—classes are not values, they describe how to create object values. The Java code below shows how to define the class of counter objects that is analogous to the OCaml definitions above:

Here the notation **public class** Counter { ... } defines a new type, *i.e.* class, of counter objects called Counter. Here, and elsewhere, the keyword **public** means that the definition is globally visible and available for other parts of the program to use. A class consists of three types of declarations: fields, constructors, and methods.

A *field* (also sometimes called an *instance variable*) is one component of the object's local state. In the <code>counter</code> class, there is only one field, called <code>cnt</code>. The keyword <code>private</code> means that this field can only be accessed by code defined inside the enclosing class—it is used to ensure that the state is encapsulated by the object.

A *constructor* always has the same name as its enclosing class—it describes how to build an object instance by initializing the local state. Here, the constructor <code>counter</code> simply sets <code>cnt</code> to <code>0</code>.

A *method* like inc or dec defines an operation that is available on objects that are instances of this class. In Java, a method is declared like this:

```
public T method(T1 arg1, T2 arg2, ..., TN argN) {
    return e;
}
```

Here, T is the method's return type—it says what type of data the method produces. T1 arg1 through TN argN are the method's parameters, where T1 is the type of arg1, etc. The return e statement can be used within the body of a method to yield the value computed by e to the caller. Here again, the keyword public indicates that this method is globally visible. Note that the field cnt is available for manipulation within the body of these methods. As we will see, methods can also define local variables to name the intermediate results needed when performing some computation.

Unlike in OCaml, in which code can appear "at the top level", in Java all code lives inside of some class. A Java program starts executing at a specially designated main method. For example, a program that creates some counter objects and uses their functionality might be created in a class called Main like this:

```
public class Main {
    public static void main(String[] args) {
        Counter c = new Counter();
        System.out.println(c.inc());
        system.out.println(c.dec());
    }
}
```

The type of main must always be declared as shown above—we'll see the meaning of the static keyword in §21. The keyword void indicates that the main method does not return a useful value—it is analogous to OCaml's unit type. To create an instance of the Counter class, the code in the main invokes the Counter constructor using the new keyword. The expressions c.inc() and c.dec() then invoke the inc and dec methods of the resulting object, which is stored in the local variable c.

19.3 Mutability and null

By default, every field or local variable defined in Java is mutable—its value can be modified in place. Java's notation for in-place update is the = operator, and we already saw a use of it in the inc and dec methods of the counter class. The statement:

```
cnt = cnt + 1;
```

is equivalent to the OCaml expression:

```
s.cnt <- s.cnt + 1
```

Another significant distinction between OCaml and Java is that in Java variables and fields that are references to objects are initialized to a special null value. The null value indicates the *lack* or *absence* of a reference. However, since Java's type system considers null to be an appropriate value of any reference type, any variable declared to contain an object might contain null instead. Trying to use a field or value via a null reference will cause your program to raise a NullPointerException when you run it. Here is an example using the Counter objects defined above:

To avoid NullPointerException errors, you should either check to make sure that the reference is not null before trying to use one of its fields or methods, or structure your program so that you maintain an invariant that guarantees that the reference is not null.

Any use of a reference can potentially result in a NullPointerException, and, moreover, Java cannot detect such potential errors statically. For example, consider this well-typed client program that provides a method f that accepts a Counter object as its argument:

```
class Foo {
  public int f (Counter c) {
    return c.inc();
  }
}
```

If \circ is an object of class Foo, the call \circ .f(null) will cause the program to raise a NullPointerException.

OCaml's use of the option types eliminates this problem. Although the option value None plays the same role as null, its type, 'a option is distinct from 'a, and it is therefore not possible to use a 'a option as though it is of type 'a. Java's type system does not make such a distinction, thereby

creating the possibility that null is erroneously treated as an object.

19.4 Core Java

We conclude this transitional Chapter by examining some of the core pieces of Java syntax. The goal is not to be comprehensive, but rather to cover the basic features of the language, emphasizing the similarities and differences with OCaml.

Statements vs. Expressions

Java is a *statement* language—we think of the program as consisting of a series of *commands* that execute one after another. Java's statements themselves are built from *expressions*, which, as in OCaml, evaluate to values. Statements in Java are *terminated* by semi-colons';'. (Recall that in OCaml, ';' *separates* a command on the left from an expression on the right.)

Local variable declarations and imperative assignment to a local variable are statements, as illustrated by these examples, which might appear in the body of some method:

Conditional tests are statements in Java—they are not expressions and don't evaluate to values. As a consequence, the else block can be omitted, as shown by the two examples below:

```
if (cond) {
    stmt1;
    stmt2;
    stmt3;
}

if (cond) {
    stmt1;
    stmt2;
} else {
    stmt3;
    stmt4;
}
```

Within the body of a method, the **return** e; statement indicates that the value of expression e should be the result yielded to the caller of the method. If a method's return type is **void**, then the return statement can be omitted entirely.

Expressions in Java are built using the usual arithmetic and logical operations like x + y, x & y, and literals like 1.0, **true**, and "Hello". A method invocation whose return type is non-**void** can be used as an expression of the corresponding type. For example, since inc returns an int, c.m() + 3 is a legal Java expression. Constructor invocations, using the **new** keyword, are also expressions, as in: (**new** Counter()).inc() + 5.

Primitive Types

Java supports a large variety of *primitive* types:

Java supports essentially the same set of arithmetic and logical operators that OCaml does, as summarized in table of Figure 19.1

Unlike in OCaml, some of Java's operations are *overloaded*—the same syntactic operation might cause different code to be executed. This means that the arithmetic operators +, *, etc., can be applied to all of the numeric types. Java will also introduce automatic conversions to change one numeric type to another:

OCaml	Java	description
= ==	==	equality test
<> !=	!=	inequality
< <= > >=	< <= > >=	comparisons
+	+	addition
_	_	substration
/	/	division
*	*	multiplication
mod	96	remainder (modulus)
not	!	logical "not"
& &	& &	logical "and"
		logical "or"

Figure 19.1: Java's primitive operations compared to OCaml's.

Moreover, + is also overloaded to mean String concatenation, so we also have:

```
"Hello," + "World!" \Longrightarrow "Hello, World!".
```

Overloading is a much more general concept than indicated by just these examples—we will study it it more detail later.

Equality

Just as OCaml includes two notions of equality—structural (or deep) equality, written v1 = v2, and reference (or pointer) equality, written v1 = v2—Java also has two notations of equality. Java uses the same notation, v1 = v2, to check for reference equality of objects or equality of primitive datatypes. Java supports structural equality only for objects. Every object in Java has a equals method that should be used for structural comparisons: o1.equals(o2)

In particular, String values in Java, although they are written using quote notation, should be compared using the equals method:

```
"Hello".equals("Hello") ⇒ true.
"Hello".equals("Goodbye") ⇒ false.
```

Identifier Abuse

Java uses different namespaces for class names, fields, methods, and local variables. This means that it is possible to use the *same* identifier in more than one way, where the meaning of each occurrence is determined by context. This gives programmers greater freedom in picking identifiers, but poor choice of names can lead to confusion. Consider this well-formed, but hard to understand, example:

```
public class Turtle {
    private Turtle Turtle;
    public Turtle() { }

    public Turtle Turtle (Turtle Turtle) {
        return Turtle;
    }
}
```

Books about Java

There are literally hundreds of Java books available. For a good, succinct introduction to the language, we recommend the first section of Flanagan's *Java in a Nutshell*, published by O'Reilly Media [4] (the second section is mostly description of the Java libraries). It is available electronically free of charge from the University of Pennsylvania library web site. For guidelines on using Java in good style and "best practices" approaches to Java development, we recommend Bloch's *Effective Java* [2].

Chapter 20

Interfaces and Subtypes

Programming languages use *types* to constrain how different parts of the code interact with one another. Primitive types, like integers and booleans, can only be manipulated using the appropriate arithmetic and logical operations. OCaml provides a rich vocabulary of structured types—tuples, records, lists, options, functions, and user-defined types like trees—each of which comes equipped with a particular set of operations (field projection, pattern matching, application) that define how values of those types can be manipulated. When the OCaml compiler typechecks the program, it verifies that each datatype is being used in a consistent way throughout the program, thereby ruling out many errors that would otherwise manifest as failures with the program is run.

Java too is a strongly typed language—every expression can be given a type, and the compiler will verify that those types are used consistently throughout the program, again preventing many common programming errors. We saw in §19 that the primary means of structuring data and code in Java is by use of *objects*, which collect together data *fields* along with *methods* for working with those fields. A Java *class* provides a template for creating new objects.

Importantly, a class is also a *type*—the class describes the ways in which its instances can be manipulated. A class thus acts as a kind of contract, promising that its instance objects provide implementations of the class's public methods. Any instance of class c can be stored in a variable of type c.

20.1 Interfaces

Java provides a second way of giving objects types: *interfaces*. An interface gives a type to an object based on what the object *does*, not how the object is implemented. Unlike a class, an interface provides only signatures for the set of methods that must be supported by an object. As such, an interface represents a "point of view" about an object, not a prescription about how that object is implemented.

As an example, consider the following interface, which might be used to describe objects that have 2D Cartesian coordinates and can be moved:

```
public interface Displaceable {
    public int getX ();
    public int getY ();
    public void move(int dx, int dy);
}
```

Note that the interface, like a class, has a name—in this case Displaceable—but, unlike a class, the interface provides no implementation details. There are no fields, no constructors, and no method bodies.

Since the Displaceable interface is a type of any "moveable" object, we can write code that works over displaceable objects, regardless of how they are implemented. For example, we might have a method like the one below:

```
public void moveItALot(Displaceable s) {
    s.move(3,3);
    s.move(100, 1000);
    s.move(s.getX(), s.getY());
}
```

This method will work on an object created from any class, so long as the class implements the Displaceable interface.

To tell the Java compiler that a class meets the requirements imposed by an interface, we use the <u>implements</u> keyword. For example, the follow Point class implements the Displaceable interface:

```
public class Point implements Displaceable {
    private int x, y;
    public Point(int x0, int y0) {
        x = x0;
        y = y0;
    }
    public int getX() { return x; }
    public int getY() { return y; }
    public void move(int dx, int dy) {
        x = x + dx;
        y = y + dy;
    }
}
```

In addition to the private fields x and y and the constructor Point (which takes in the initial position for the point and sets x and y accordingly), this class provides implementations for the three methods required by the Displaceable interface—if one of them was omitted, or included but with a different signature, the Java compile would issue an type checking error.

In the case of Point, the class provides only the methods of the Displaceable interface. A class that implements an interface may supply *more* methods than the interface requires. For example, the ColorPoint class also includes a color field and a way to access it:

```
class ColorPoint implements Displaceable {
  private Point p;
  private Color c;
  ColorPoint (int x0, int y0, Color c0) {
    p = new Point(x0,y0);
    c = c0;
    }
  public void move(int dx, int dy) {
      p.move(dx, dy);
  }
  public int getX() { return p.getX(); }
  public int getY() { return p.getY(); }
  public Color getColor() { return c; }
}
```

Note that this implementation provides a different implementation of the Displaceable methods—it *delegates* their implementation to the Point object p. It is easy to see how we might create other classes of objects like Circle or Rectangle that have similar implementations and all implement the Displaceable interface.

20.2 Subtyping

Because interfaces, like classes, are types, Java programs can declare variables, method arguments, and return values whose types are given by interfaces. For example, we might declare a variable and use it like this:

```
Displaceable d;
d = new Point(1,2);
d.move(-1,1);
```

Note that, since every Point object satisfies the Displaceable contract, this assignment makes sense—d holds Displaceable objects and all Point objects are Displaceable, so d can store a Point. Similarly, since ColorPoints are also Displaceable, we could continue the program fragment above with:

```
d = new ColorPoint(1,2, new Color("red"));
d.move(-1,1);
```

However, because d's type is Displaceable—which only offers the getX, getY, and move methods—it would be a type error to try to use the ColorPoint method getColor on it:

```
Color c = d.getColor(); // Error! d may not be a ColorPoint
```

This situation illustrates the phenomenon of *subtyping*: A type A is a *subtype* of B if an object of type A can meet all of the obligations that might be required by the interface or class B. Intuitively, an A object can do anything that a B object can, or more succinctly still: an A is a B.

Since Point implements the Displaceable interface, every Point is Displaceable, *i.e.* Point is a subtype of Displaceable. We also say that Displaceable is a *supertype* of Point.

Subtyping, as we have already seen, justifies updating a variable of type Displaceable to contain a Point object. Similarly, for a method such as moveItALot, it is permissible to pass an object of any subtype as the arguments of a method invocation. Thus, both of the following would be allowed:

```
o.moveItALot(new Point(0,0));
o.moveItALot(new ColorPoint(10,10, new Color("red")));
```

20.3 Multiple Interfaces

A class may implement more than one interface. This makes sense because an interface offers a "point of view" about the objects it describes, and there may be more than one point of view about the objects in a class.

For example, we might have another interface for working with shapes that have a well-defined area:

```
public interface Area {
    public double getArea();
}
```

A Circle class might implement both the Displaceable and Area interfaces. To do so, it simply has to satisfy the method requirements of *both*. Note that multiple interfaces are given in a comma-separated list after the **implements** keyword:

```
public class Circle implements Displaceable, Area {
    private Point center;
    private int radius;

public Circle (int x0, int y0, int r0) {
        r = r0; p = new Point(x0,y0);
    }

public double getArea () {
        return 3.14159 * r * r;
    }

public int getRadius () { return r; }

public getX() { return center.getX(); }

public move(int dx, int dy) {
        center.move(dx,dy);
    }
}
```

Rectangle would be implemented similarly:

```
public class Rectangle implements Displaceable, Area {
   private Point lowerLeft;
   private int width, height;

public Rectangle(int x0, int y0, int w0, int h0) {
     lowerLeft = new Point(x0,y0);
     width = w0;
     height = h0;
}

public double getArea () {
   return width * height;
}

public getX() { return lowerLeft.getX(); }

public getY() { return lowerLeft.getY(); }

public move(int dx, int dy) {
   lowerLeft.move(dx,dy);
}
```

Classes like Rectangle and Circle that implement multiple interfaces have multiple supertypes. The following examples are all permitted:

```
Circle c = new Circle(10,10,5);
Displaceable d = c;
Area a = c;

Rectangle r = new Rectangle(10,10,5,20);
d = r;
a = r;
```

Of course, since Rectangle and Circle are not in any subtype relation (neither is a supertype of the other) it doesn't make sense to store a Rectangle in a variable declared to hold Circle objects. Similarly, even though it is possible that a Displaceable variable contains a Circle, it is not possible to store a Displaceable in a Circle variable:

```
Circle c = new Circle(10,10,5);
Rectangle r = c;  // not OK

Displaceable d = c; // OK
Circle c2 = d;  // not OK, even though d contains a Circle
```

Chapter 21

Static vs. Dynamic

In Java, the term *static* refers to any property that is determined purely by examining the text (syntax) of the program at compile time, *i.e.* when the compiler type checks the program and generates executable bytecode. In contrast, the term *dynamic* refers to a property that is determined only when the program is actually running.

Understanding the difference between static and dynamic properties is essential to understanding the behavior of Java programs. We have already seen two instance where a distinction between the static and dynamic features is important:

- static methods versus "ordinary" dynamically dispatched methods, and
- the static type of an expression versus the dynamic class of the object the expression denotes

This Chapter explores each of these in turn.

21.1 Static vs. Dynamic Methods

Most of the time in Java, executable code is packaged together with an object that provides some encapsulated local state (its member fields) that is modified or otherwise used by the methods. A typical example is the move method of the Point class—it updates a Point object's local coordinates by displacing them by some amount. Crucially, the code of a method like

move makes sense only in the context of a Point or other Displaceable object. Therefore the move method must always be invoked relative to some receiving object o as in the expression o.move(10,10).

This "ordinary" method invocation is a *dynamic* property of the program—its behavior can't be determined until the program is actually running. To see why, recall that a variable of type <code>Displaceable</code> might store an object of *any* class that meets the required interface obligations. This means that, in general, many different possible implementations of the <code>move</code> method might be called when the expression <code>o.move(10,10)</code> is evaluated. Here is a simple example:

```
Displaceable o;
if (...) {
    o = new Point(10,10);
} else {
    o = new Rectangle(10,10,5,20);
}
o.move(2,2); // method called depends on the conditional
```

Suppose the the omitted conditional test depended on user input. Then whether a Point or Rectangle is assigned to o can't be known until the program is actually run and the input is resolved. Therefore the method invocation o.move(2,2)) after the conditional might require executing either the Point version of move or the Rectangle version. This is called dynamic dispatch—the method invocation "dispatches" to some version of move depending on the *dynamic class* of the object stored in o.

Java also supports a notion of **static** methods (and fields), which are associated with a class and *not* object instances of the class. The standard example is the main method, which must be declared with the following signature (in some class):

```
public static void main(String[] args) {
    ...
}
```

As the use of the keyword **static** implies, which code is called when a **static** method is invoked can be determined at compile time (without running the program). The way this works is that, rather than invoking a static method from an object, **static** methods are called relative to the class in which they are defined. For example, suppose that a class c defines a static method m, like this:

```
public class C {
    public static int m(int x) {
       return 17 + x;
    }
}
```

c's m method can be invoked from anywhere by using an expression of the form C.m(3). Here, the class name c says which method named m will be called (in general, there can be many methods named m, perhaps defined in different classes).

Thus, **static** methods act like globally-defined functions. Similarly, **static** fields behave like global variables that can be referenced by "projecting" from the name of the defining class. Such **static** fields cannot be initialized in a constructor for the class (since they aren't associated with objects) and so must be initialized in the class scope itself. For example, we might modify the class c above to use a static field like this:

```
public class C {
    private static int big = 23;

    public static int m(int x) {
        return big + x;
    }
}
```

A **static** method cannot access non-static fields or call non-static methods associated with the class because, as there is not object to provide the state for the non-static fields of the class, those methods might not be well defined. For example, the following example will cause the Java compiler to issue an error:

When should static methods be used? Generally they should be used for implementing functions that don't depend on any objects' states. One good source of examples is the Java Math library, which defines many standard mathematical functions like Math.sin, or the various "type conversion" operations, like Integer.toString and Boolean.valueOf.

21.2 Static Types vs. Dynamic Classes

The discussion above implicitly relies on another key idea: the difference between the *static type* of an expression, and the *dynamic class* of the value that the expression denotes. Again, the difference is whether the information is determined at compile time, or whether it isn't available until the program is run.

Consider the following example code, which uses the Displaceable and Area interfaces along with the shape classes Point and Circle that were introduced earlier.

```
Point p = new Point(10,10);
Circle c = new Circle(10, 10, 10);
Displaceable d1 = p;
Displaceable d2 = c;
Displaceable d3;
if (...) {
   d3 = p;
} else
   d3 = c;
}
Area a1 = c;
Area a2 = d2;  // This assignment will cause a type error
```

Here, the type annotations on the variable declarations indicate the static type information about the variable that the compiler checks while type checking the program. For example, p has the static type Point, while d1, d2, and d3 all have static type Displaceable.

At run time, the variable d1 will always store a value whose class is Point, but the variable d3 might end up with a value whose dynamic class is Point or Circle.

Note that it is the static type of a variable that restricts how the value can be used by the program. For example, even though d2 always stores a Circle at run time, because d2's static type is Displaceable, it isn't possible to assign the value in d2 to a2, which expects to be given an object of type Area.

Also note that the static type is associated with a program *expression*, which can be a complex construction involving multiple method calls or other operations. For example and expression like:

```
(new Circle(10, 10, 10)).getCenter()
```

has static type Point. Note that, due to *subtyping*, such an expression might have more than one valid static type—for example this particular expression also has type Displaceable, because Point is a subytpe of Displaceable.

At run time, such expressions evaluate to values, which, if they are objects (and not a primitive value like an integer), are always associated with a single *dynamic class*, namely the class whose constructor was invoked to create the object. For this reason, the dynamic class of the variable all above will be Circle. As we saw in the discussion above about the difference between dynamic and static method invocation, it is the dynamic class of the object that determines which method will be invoked at run

time. After running the code fragment above, d3.move() will either call the Point or the Circle implementation of move, depending on which way the conditional branch evaluates at runtime.

Chapter 22

Java Design Exercise: Resizable Arrays

Before moving on to Java's more advanced object-oriented features, like inheritance and overriding, let us first work through a design exercise that emphasizes the use of *encapsulation* as a means to enforce program invariants. Along the way, we'll introduce Java's array types, which provide a convenient way to collect together a sequence of similar data values.

22.1 Arrays

Java, like most programming languages (including OCaml), provides built-in support for *arrays*. An array is a sequentially ordered collection of element values that are arranged in the computer's memory in such a way that the elements can be accessed in constant time. The array elements are *indexed* with integer positions as shown in Figure 22.1. Arrays thus provide a very efficient way to structure large amounts of similar data.

In Java, array types are written using square brackets after the type of the array's elements. So int[] is the type of arrays containing int values, and Counter[] is the type of arrays containing Counter values.

If a is an array, then a[0] denotes the element at index 0 in the array. Similarly, if e is any expression of type int and $e \Longrightarrow i$, then a[e] denotes the element at index i. Note that Java array indices start at 0, so a 10-element array a has values a[0], a[1], ..., a[9].

If you try to access an array at a negative index or an index that is larger

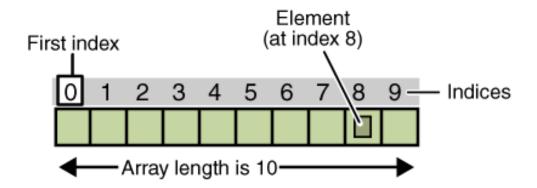


Figure 22.1: Arrays and array indices.

than (or equal to) the array's length, Java signal that no such element exists by raising an ArrayIndexOutOfBoundsException. Every array object has an length field, which can be accessed using the usual "dot" notation: the expression a.length will evaluate to the number of elements in the array a. Note that a[a.length] is always out of bounds—the largest legal array index is always a.length - 1.

Array elements are mutable—you can update the value stored in at array index by using the assignment command: a[i] = v;

The new keyword can be used to create a new array object by specifying the array's length in square brackets after the type of the object. The program snippet below declares an array of ten Counter values:

```
Counter[] arr = new Counter[10];
```

Note that array types, like <code>counter[]</code>, never include any size information, but the length of the array is *fixed* when it is created using the <code>new</code> operation. Once created, an array's length never changes.

When an array is created, the elements of the array are initialized to the default value of the corresponding element type. For numeric values like integers and floating points, the default values is zero, for objects, the default is null. Java also provides syntax for *static initialization* of arrays, for the case where the array values are known when writing the program. In this case, the elements are written as a comma-separated sequence inside of { and } brackets. Here are some examples:

```
int[] a = new int[4];
int[] b = a;
a[2] = 7;
System.out.println(b[2]);
```

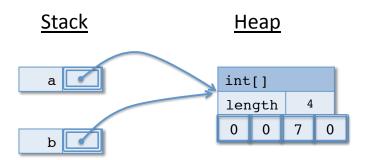


Figure 22.2: This figure shows a portion of the stack and heap configuration that would be reached by running the program above. Observe that, like other kinds of mutable reference values, array references can alias.

```
int[] myArray = {10, 20, 30, 40, 50, 60, 70, 80, 90, 100};

String[] yourArray = { "foo", "bar", "baz" };

Point[] herArray = { new Point(1,3), new Point(5,4) };
```

As you would expect, creating a new array object allocates space in the program's heap in which to store the array values—the amount of space required is proportional to the length of the array. The array object also includes an immutable field, length, which contains the size of the array when it was created. When you declare a variable of array type (or of any other object type, for that matter), Java creates a *reference* to the array on the stack. Because array elements are mutable, all of the issues with aliasing (recall §14) arise here as well. Figure 22.2 shows the program stack and heap configuration that arises in a typical array program. We will study the Java version of the abstract stack machine in more detail later (see §23).

Array iteration

Arrays provide efficient and convenient "random access" to their elements, since you can simply look up a value by calculating its index. Often, however, it is useful to process *all* (or many) of the elements of an array by *iterating* through them. Like most imperative languages, Java provides **for** loops for just that purpose. Java's **for** loop syntax is inherited from the C and C++ family of languages. Here is an example:

```
public static double sum(double[] arr) {
    double total = 0;
    for (int i = 0; i < arr.length; i++) {
        total = total + arr[i];
    }
}</pre>
```

This method takes an array of double width floating-point values. The for loop shows the canonical way of iterating over every element of the array. The int i = 0; part initializes a loop index variable i to 0, the starting index of the array. The loop guard or termination condition, i < arr.length; indicates that this loop should execute while the value of i is less than array length. The loop variable update i++ is short-hand for i = i + 1; it says that index i should be incremented by one after each loop iteration. The body of this for loop simply accumulates the total value of all the elements in the array.

The general form of a **for** loop is:

```
for (init; cond; update) {
   body
}
```

Here, init is the initializer, which may declare new variables (as in the sum example above). The cond expression is a boolean valued test that governs how many times the loop executes—when the cond expression becomes false, the loop terminates. The update statement is executed after each loop iteration; it typically modifies the loop variables to move closer to the termination condition.

Java also provides a while loop construct. The example above could be written using while loops like this:

Using for loops to iterate over arrays is often quite natural, since the number of times the loop body executes is usually determined by the length of the array. As we shall see (§27.4), Java also provides support for iterating over other kinds of datatypes, particularly collections and streams of data.

Whether you use **for** or **while** loops, pay particular attention to the loop guards and indexing—a common source of errors is starting or stopping iteration at the wrong indices, which can lead to either missing an array element or an ArrayOutOfBoundsException.

Multidimensional Arrays

Since an array type like <code>C[]</code> is itself a type, one can also declare an array of arrays—each element of the "outer" array is itself an array. Such arrays have more than one dimension, so Java allows multiple levels of indexing to access the elements of the "inner" array:

This example shows that array initializers can be nested to construct multi-dimentional arrays. An expression like names[0][2] should be read as (names[0])[2], that is, first find the array at index 0 from names and then find the element at index 2 from that array. For the example above, $names[0][2] \Longrightarrow "Ms."$.

This example also demonstrates that the inner arrays need not be all

of the same length—Java arrays can be "ragged". This is a simple consequence of Java's array representation: An object of type <code>c[][]</code> is an array, each of whose elements is itself a reference to an array of <code>c</code> objects. There isn't necessarily any correlation among the lengths or locations of the inner arrays. Note that this is in stark contrast to languages like <code>C</code> or <code>C++</code> in which multidimensional arrays are represented as "rectangular" regions of memory that are laid out contiguously.

The static array initialization syntax suggests that we should read the indices of a two-dimensional array as "row" followed by "column". That is, in the expression <code>names[row][col]</code>, the first index selects an inner array corresponding to a row of values, and the second index then picks the element at the corresponding column.

This view of 2D arrays is very convenient when working with many kinds of data, but for some applications, it is useful to think of the first index as the "x" coordinate and the second index as the "y" coordinate of elements in a plane. For example, for image-processing applications, we might represent an image as a 2D array of Pixel objects. That would allow us to write img[x][y] when thinking in cartesian coordinates, which looks more natural than the "row"-major img[y][x] indexing suggested by the row/column analysis above.

Both of these ways of thinking about 2D arrays are simply useful conventions. So long as you write your program to consistently use either the <code>arr[row][column]</code> view or the <code>arr[x][y]</code> view, it will be correct. Problems arise when these two different points of view are confused in the same program.

Note that since the inner arrays might not be all of the same length, you must use some care when writing nested loops to process all of the array elements. For example, the following program might be incorrect if the array is not rectangular:

```
int rows = arr.length;
int cols = arr[0].length;  // will fail if arr.length == 0
for (int r=0; r < rows; r++) {
    // may fail if array is not rectangular
    for (int c=0; c < cols; c++) {
        arr[r][c] = ...
    }
}</pre>
```

A simpler and more robust way of iterating over all of the elements of

an array is to always use the length field, like this:

```
for (int r=0; r < arr.length; r++) {
    // use the length of the inner array
    for (int c=0; c < arr[r].length; c++) {
        arr[r][c] = ...
    }
}</pre>
```

To create multidimensional arrays without using a static initializer, it is necessary to create an array of arrays and then initialize each of the inner arrays separately, like this:

```
int[][] products = new int[5][];
for(int row = 0; row < 5; row++) {
    products[row] = new int[row+1];
    for(int col = 0; col <= col; col++) {
        products[row][col] = row * col;
    }
}</pre>
```

This program is equivalent to the following one that uses a static initializer:

```
int[][] products =
  { { 0 },
      { 0, 1 },
      { 0, 2, 4 },
      { 0, 3, 6, 9 },
      { 0, 4, 8, 12, 16 }
}
```

A common pitfall that you should avoid is accidentally sharing a single inner array among all of the elements of the outer array, like this:

```
int[][] arr = new int[5][];
int[] shared = new int[10];
for(int i = 0; i<5; i ++) {
   arr[i] = shared;
}</pre>
```

22.2 Resizable Arrays

The built-in arrays provided by Java are very convenient, except for one thing: their size is fixed at creation time. Sometimes, however, the number of elements that will need to be stored in the array is not known early enough. For example, suppose you wanted to keep track of an inventory of comic books, which are given issue numbers starting at 0 and increasing as each new issue is produced. Since the number of issues isn't determined in advance, it is not easy to allocate an array ahead of time. One could imagine allocating a very large array in anticipation of many issues, but that will consume a lot of wasted memory in the case that there only a few issues of the comic book produced.

A different alternative is to implement a kind of "adaptive" or "resizable" array datatype that strikes a balance between over provisioning and array-like performance. We'll call this datatype a Resarray for "resizable array". For the purposes of this design exercise, we will simplify things a bit and assume that the array stores only int values (which would be sufficient to keep track of the number of comics of a particular issue number in the inventory, but would not be as general as you might want).

The basic idea of the Resarray structure is to use a "backing" array to store the data and provide access to the elements via set and get operations. Unlike regular arrays, however, a Resarray acts as though its capacity is unbounded—a client of the Resarray can set and get any non-zero index. Of course, since the Resarray will use a real array internally, the Resarray structure will have to adjust the size of the backing array to ensure that it has enough space. This might occasionally cause the Resarray to have to copy the contents of the backing array to a new backing array with more room.

The Resarray interface

The next step of designing the Resarray data structure is, as usual, to specify the types of its methods. In this case, the job is made simpler because a Resarray acts almost as if it is a regular array—it therefore needs set and get methods that take int indices. We might also want to ask about the location of the largest non-zero element of the Resarray. Also, for ease

¹Resizable arrays are loosely similar to the Java library's ArrayList structures.

of inter-operation with regular Java libraries, we might want to provide a way to extract an ordinary Java array from a Resarray. This leads us to the following skeleton for the Resarray class:

```
* An "infinitely large array" of integers; the backing buffer
 * automatically resizes itself as new values are added.
 */
public class ResArray {
        public ResArray()
        /** access the array at position i. If position i has
         * not yet been initialized, return 0.
         * @param i - index into the array
         * @return value of the array at that index
        public int get(int i) {
            return 0; // TODO: this is a stub
        /** Modify the array at position i to contain value v.
         * @param i - index
         * @param v - new value
        public void set(int i, int v) {
            return; // TODO: this is a stub
        /** the "extent" is the size of an array that would be
         * necessary to store the smallest prefix
         * that contains all of the nonzero data.
         * @return extent
        public int getExtent() {
                return 0; // TODO: this is a stub
        }
}
```

ResArray Test Cases

Programming against this stubbed-out specification, we can easily create a collection of test cases that help explain the expected behavior. We record these cases as Java JUnit tests—the import clauses at the top of the program bring the needed classes and operations into scope. Programming environments such as Eclipse know how to run such JUnit tests automatically, providing visual feedback about which tests pass and which tests fail. Running the tests against the stub implementation will reveal that almost all of the tests fail, as expected.

The important thing about the process of generating such tests is that it forces us to consider how the operations of a ResArray should interact. For example, the getExtent method must return 0 if we set and then zero-out an element of the ResArray, as shown in TestExtent3. Similarly, if we set two elements and then zero-out the second one, the extent should "shrink" back to the one past the index of the first element, as shown in TestExtent4.

The ability to design a set of good tests cases takes practice. It's often not clear how many tests to generate or when to stop making them up. A good rule of thumb is to start with tests for all of the "obvious" behaviors that match your intuitions (such as testGet0 and testGet1), and then add more as you develop and debug your program. It is good practice to record each bug you find as a test case so that future changes to the program don't re-introduce old bugs.

Following these guidelines, we generate the following test program for the ResArray structure.

ResArray Implementation

Developing the test cases has revealed some of the issues we must address with the Resarray implementation. First, the size of the underlying array—the *backing buffer*—might be larger than the index returned by getExtent. The reason is shown by testExtent3, which first sets the value at index 47 to 2 and then resets it to 0. Presumably, we must grow the backing buffer to hold at least 48 elements in order to write at index 47, but it would be unecessary to re-size the backing buffer after resetting the value to 0.

This analysis suggests that the ResArray class contains two pieces of

local state: the backing buffer itself, which is an array of integers, and an integer value that we'll call extent, which keeps track of (one past) the index of the last non-zero element of the ResArray.

How are the extent and the buffer related? The buffer must always be at least big enough to hold elements indexed up to (but not including) the extent. If the extent is smaller than the length of the buffer, then all of the elements whose indices are greater than (or equal to) the extent must be 0. If extent - 1 is positive, then buffer[extent - 1] must be non-zero.

Putting all of these considerations together, we arrive at the following ResArray invariant, which are defined in terms of two private fields extent and buffer:

- 0 <= extent <= buffer.length
- if extent = 0 then all of the elements of the ResArray are 0.
- if extent > 0 then buffer[extent 1] is the last non-zero value in the ResArray.

Guided by these invariants, we can easily implement the first few parts of the ResArray class. There are two private fields, and the constructor simply creates an "empty" ResArray.

```
public class ResArray {
    private int[] buffer;
    private int extent;

public ResArray() {
        extent = 0;
        buffer = new int[0];
}
```

The get operation is slightly more interesting—it uses the fact that if i < extent then buffer[i] is well defined (unless i is negative, in which case it is appropriate to throw an array bounds exception). If the index is greater than or equal to extent, then the invariants tell us that we should always return 0.

```
/** Access the array at position i. If position i has
  * not yet been initialized, return 0.

*
  * @param i - index into the array
  * @return value of the array at that index
  */
public int get(int i) {
        if (i < extent) {
            return buffer[i];
        } else {
            return 0;
        }
}</pre>
```

The set operation is more interesting still. Here there are several cases to consider. First, if the value being set is 0 and the index \pm is above the extent, then nothing needs to be done—all of the array invariants are preserved and there is no reason to change the backing buffer.

Second, if i is too big to fit into the existing buffer space, we must grow the buffer—for now, we defer defining this operation, but observe that it should modify the buffer field so that it's size is at least equal to i+1.

After possibly growing the array, it is safe to update the i^{th} index to contain the value v. Doing so might break the Resarray invariants, though, so we must add code to re-establish them. In particular, if v is non-zero then we have to adjust extent in the case that i is larger than the old extent. On the other hand, if v is 0 and the index we're updating happens to be the *last* non-zero element of the array, then we have to search backwards through the array to find the remaining largest non-zero element. This is done in the method shrinkExtent.

Both grow and shrinkExtent should be **private** methods—they are used only internally to the ResArray class and so should not be exposed to outside code.

Putting all of this together, we arrive at:

Writing shrinkExtent is fairly straightforward. Its job is to search backwards through buffer starting from index i to find the last non-zero element. Once it is found (if any) then extent is set to one more than its index, which re-establishes the invariants:

```
/* Adjust the extent when assigning a 0 to the buffer */
private void shrinkExtent(int i) {
    int j = i;
    while (j >= 0 && buffer[j] == 0) {
        j--;
    }
    extent = j+1;
}
```

The grow method must, at a minimum, create a new backing array large enough to store i+1 elements, and then copy the old contents into the new array. A straightforward implementation would be the following:

```
/* Grow the backing buffer to accommodate up to i */
private void grow(int i) {
    int newlen = i+1;
    int [] newbuffer = new int[newlen];
    for (int j=0; j<extent; j++) {
        newbuffer[j] = buffer[j];
    }
    buffer = newbuffer;
}</pre>
```

The above implementation is perfectly functional and will meet the requirements of the Resarray invariant, but if you use it in practice, it might give poor performance in the case that you set a sequence of consecutive indices: a.set(0,v0); a.set(1,v1); a.set(2,v2); The problem is that each subsequent call will make a copy of *all* the preceding elements. This means that the total amount of work done to set an n element sequence is proportional to n^2 .

A better strategy (which, incidentally, is used in many other contexts, including networking protocols like TCP) is to *double* the previous size of the array. Doing so means that, when setting a consecutive sequence as in the case above, the grow method will not make so many copies of the preceding elements. Intuitively, doubling the array over provisions the space needed to store the elements, but, is at most twice as much space as would otherwise be needed. Note that to maintain the ResArray invariants, we must still ensure that at least index i is included in the new buffer. We are thus led to the following implementation of grow:

```
/* Grow the backing buffer to accommodate up to i */
private void grow(int i) {
    int newlen = Math.max(i+1, 2 * buffer.length);
    int [] newbuffer = new int[newlen];
    for (int j=0; j<extent; j++) {
        newbuffer[j] = buffer[j];
    }
    buffer = newbuffer;
}</pre>
```

The getExtent method is trivial to implement:

```
/** the "extent" is the size of an array that would be
  * necessary to store the smallest prefix
  * that contains all of the nonzero data.
  *
  * @return extent
  */

public int getExtent() {
    return extent;
}
```

Chapter 23

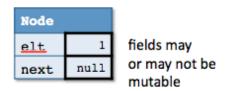
The Java ASM and encapsulation

The Abstract Stack Machine model that we used in chapter 15, provided a model of computation for OCaml programs that use mutable state. This stack machine lets us trace through execution in an abstract manner so that we can understand what our program does.

It turns out that we can use the *same* model for Java programs, with a few minor alterations. Like the OCaml abstract machine, the Java machine includes the same components: the *workspace*, the *stack*, and the *heap*.

23.1 Differences between OCaml and Java Abstract Stack Machines

- Almost everything, including variables stored on the stack is mutable.
- Heap values include (only) arrays and objects. Java does not include lists, options, tuples, other datatypes, records or first-class functions.
- Java includes a special reference called *null*.
- Method bodies are stored in an auxiliary component called a *class ta-ble*. For our initial discussion, we will omit some of the details about how the class table works. We will come back to it in a later chapter.





length never mutable elements always mutable

Figure 23.1: A picture of the heap of the Java Abstract Stack Machine containing two reference values: an object value (on the left) and an array value (on the right).

Reference values in the Java ASM

Java primitive types are much like the primitive types of OCaml.

There are two sorts of Java values that are stored on the heap: objects and arrays.

Objects are stored on the heap similarly to OCaml record values. The object value contains a value for each of its fields (instance variables). Fields may or may not be mutable, if they are mutable (the default in Java) we mark them with a heavy black box.

For example the Java class:

```
class Node {
   private int elt;
   private Node next;
}
```

creates object values that are represented in the heap as in the left side of Figure 23.1. Note that the only members of the class that are part of the heap value are the name of the class and the field members. The constructors and methods in the class are stored in the class table.

Likewise, Java arrays are represented in the abstract stack machine as in the right half of Figure 23.1. $int[] a = \{0, 0, 7, 0\};$

Array values contain the length of the array as well as one location for each array value. The array locations are always mutable, but the length of the array never can be changed. Arrays also record the type of the array, this restricts the array to storing only certain types of values.



Figure 23.2: The initial state of the Java ASM example

Object Aliasing example

As in OCaml, Java object references can alias eachother. In otherwords, two reference values can point to the same location in the heap.

In what follows, we will walk through an example of object aliasing.

```
class Node {
   private int elt;
   private Node next;
   public Node (int e0, Node n0) {
     elt = e0;
     next = n0;
   public static int m () {
     Node n1 = new Node (1, null);
     Node n2 = new Node (2, n1);
     Node n3 = n2;
     n3.next.next = n2;
     Node n4 = new Node (4, n1.next);
     n2.next.elt = 17;
     return n1.elt;
   }
}
```

Consider the code above. What will be the result of a call to the static method Node.m()? The Abstract Stack Machine can help us figure out the answer.

We start the ASM by putting the code on the workspace. The Java ASM simplifies a static method call in much the same way as it simplifies an OCaml function call.

1. The first step is to save the current workspace on the stack, marking the spot where the ANSWER should go with a "hole". In our example,

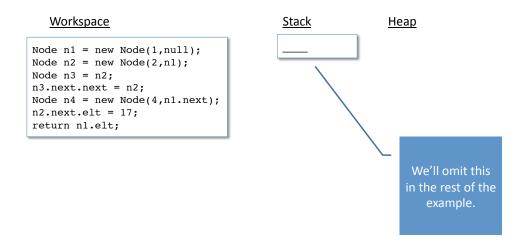


Figure 23.3: After the static method call—saving the workspace on the stack and putting the method body in the workspace.

since the original workspace was Node.m(), the saved workspace is merely _____.

- 2. The next step is to find the method definition. The Java uses the class table for this purpose, looking up the Node class and its method named m.
- 3. Next, the ASM adds new stack bindings for each of the called method's parameters. These stack bindings are *always* mutable in Java. In our running example, the method m takes no parameters, so there will be nothing pushed on the stack.
- 4. Next, the workspace is replaced by the body of the method.

Once the method body is in the workspace, simplification continues as usual. This process may involve adding more bindings to the stack, doing yet more method calls, or allocating new data structures in the heap. When the code of the function body reaches a return v statement, and the returned value has been computed, then the value is returned as the ANSWER to the saved workspace on the stack, plugging the hole, and popping all bindings off the stack.

Each local variable initialization in the method body adds a new (mutable) binding to the stack, which continues as long as the variable is in

scope. If a variable is declared without being initialized, Java uses the default values for the type to initialize the variable. The default value for reference types is always <code>null</code>.

The constructor invocation **new** Node(1, null) allocates and initializes an object value on the heap. We won't go into the details about how this process works at this point (we will return to these details later). For now, we can just assume that this invocation creates the object with the appropriate values for the fields.

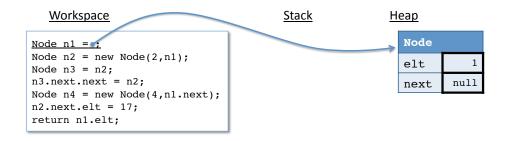


Figure 23.4: After the creation of an object. In the next step, the ASM will add the (mutable) variable n1 to the stack, with a reference to this object.

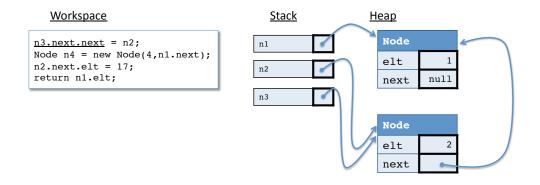


Figure 23.5: After a few more steps. The variable n3 contains an *alias* to a previously allocated object.

After Figure 23.7, we can see what the final result of the method will be. The value of nl.elt is 17 when the method returns.

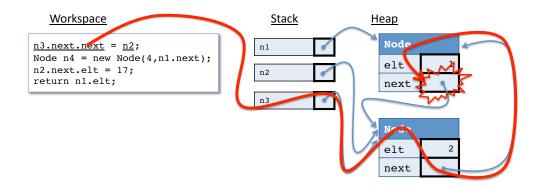


Figure 23.6: An update to a field of an object, tracing the references.

Encapsulation

Encapsulation is the process of controlling access to the state of an object. In particular, in an encapsulated object, all changes to an objects state should be done directly by the methods of the object.

The purpose of encapsulation is to preserve the *invariants* of an object. Recall that an invariant of a data structure is a property that should always hold, for any instance of that data structure, throughout its lifespan.

For example, in Chapter 22, resizable arrays have the following invariant, which states a relationship between the two private fields extent and buffer:

- 0 <= extent <= buffer.length
- if extent = 0 then all of the elements of the ResArray are 0.
- if extent > 0 then buffer[extent 1] is the last non-zero value in the ResArray.

The establishment of the invariant guided the implementation of the ResArray class, including the code that updates the extent field as the buffer is modified.

If the class ResArray is encapsulated, then to assure ourselves that this invariant holds for all instances of this class, we only need to consider the methods of the object. If external methods cannot modify the state of

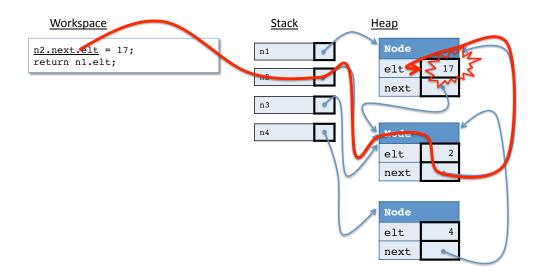


Figure 23.7: After a few more steps, the final update.

extent or buffer, then we need not look for invariant violations outside of the object's code.

However, making sure that an objects state is encapsulated can be tricky. Because of aliasing, to preserve encapsulation, we must be sure that no aliases to any of the objects internal state escape.

For example, consider extending the ResArray class with a values method, which returns a regular Java array, containing the nonzero values of the dynamic array. The size of this array is the extent.

To implement this method, it is simple enough to create a copy, like so:

There is one slight subtlety: it would be erroneous to return the backing buffer itself. First, the extent might not agree with the size of the backing buffer. Even if the backing buffer is the same size as the extent, returning an alias to the encapsulated buffer would allow client programs to break the invariants by manipulating the backing buffer directly. That is, the following appealing "optimization" is wrong:

Chapter 24

Extension and Inheritance

We saw in Chapter 20 that Java's use of interfaces to separate the *specification* of an object from its *implementation* induces a notion of *subtyping*—each class is a subtype of the interfaces it implements. In this Chapter, we will see that Java's subtyping relation is actually richer still. First, it is possible for one interface to *extend* another, by adding extra methods that must be supported. Second, one class can also *extend* or *inherit from* another, allowing the two to share common implementation code. Both of these mechanisms create new subtyping relationships.

We explore each of these possibilities in turn below.

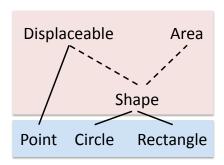
24.1 Interface Extension

Suppose, as in §20, that we were developing a paint program for working with various kinds of shapes. Previously, we had defined two interfaces, Displaceable and Area as follows:

```
public interface Displaceable {
    public int getX ();
    public int getY ();
    public void move(int dx, int dy);
}

public interface Area {
    double getArea();
}
```

If we wanted to define an interface of shapes that had both the methods



```
class Point implements Displaceable {
    ... // omitted
}
class Circle implements Shape {
    ... // omitted
}
class Rectangle implements Shape {
    ... // omitted
}
```

Figure 24.1: An example subtyping hierarchy for the three classes shown on the right. Subtyping induced by the <u>implements</u> keyword is shown as a solid line; that induced by the <u>extends</u> keyword is shown as dotted. Interface Shape extends both Displaceable and Area. Classes Circle and Rectangle are both subtypes of Shape, and, by transitivity, both are also subtypes of Displaceable and Area. Point is not a subtype of Shape or Area.

of the Displaceable and Area interfaces, along with a new method for obtaining the shape's boundingBox, we could define it directly like this:

```
public interface Shape {
    public int getX ();
    public int getY ();
    public void move(int dx, int dy);
    public double getArea();
    public Rectangle getBoundingBox();
}
```

However, this approach is not very good. Even though this <code>Shape</code> interface has all of the methods of both the <code>Displaceable</code> and <code>Area</code> interfaces, if we wanted to implement a class that could be used either as a <code>Shape</code> or as <code>Area</code> or as a <code>Displaceable</code> object, we would have to explicitly declare that it is a subtype of all three interfaces in the class's <code>implements</code> clause, like this:

```
public class SomeShape implements Shape, Area, Displaceable {
    ...
}
```

This is neither elegant, nor is it very scalable—in a large development, we might have to write down many interfaces, even though many of them

share method specifications. Moreover, this approach forces us to duplicate those shared methods signatures in multiple interfaces (*i.e.* getX() appears once in Displaceable and once in Shape).

Interface extension solves this problem by allowing one interface to extend others, possibly also adding additional required methods. For example, we could define a better version of the <code>Shape</code> interface like this:

```
public interface Shape extends Displaceable, Area {
    public Rectangle getBoundingBox();
}
```

This declaration says that the Shape interface is a subtype of *both* the Displaceable and Area interfaces, and thus any class that implements Shape must supply all of their methods, as well as the getBoundingBox method required by Shape.

The use of interface extension means that the subtyping hierarchy can be quite rich. One interface may extend several others, and interfaces can be layered on top of one another, forming an (acyclic) graph of types related by **extends** edges. The resulting subtyping relationship follows these chains transitively: if A is a subtype of B and B is a subtype of C, then A is a subtype of C. Figure 24.1 shows an example hierarchy.

24.2 Inheritance

Classes, like interfaces, can also extend one another. Unlike in the case of interfaces, however, a class may only extend *one* class. Here is an example:

```
class D {
  private int x;
  private int y;
  public int addBoth() { return x + y; }
}

class C extends D { // every C is a D
  private int z;
  public int addThree() {return (addBoth() + z); }
}
```

The way to think about class inheritance is that the *subclass*, in this case c, gets its own copy of all the fields and methods of the *superclass* that it extends. Given the definitions above, when we create an instance of c, the

resulting object will have three private fields (x, y, and z) and two public methods (addBoth) and addThree.

Just as with interface extension, a class is a subtype of the class it extends, so, in this case, c is a subtype of d. For this reason, inheritance should be used to model the "is a" relation between two classes: every c is a d, and wherever the program requires a d it should be possible to supply a c instead. When considering how to represent a program concepts using classes, carefully examine whether there is an "is a" relationship to be found. For example, every truck is a vehicle, so one might consider making a classes <code>Vehicle</code> and <code>Truck</code> such that <code>Truck</code> extends <code>Vehicle</code>.

Note that the keyword private means that the field or method is visible only within the enclosing class. Therefore, even though C extends D, the fields x and y cannot be mentioned directly within C's methods. Java provides a different keyword, protected, which designates a field or method as visible within the class and all subclasses, no matter where they are defined. The protected keyword should be used with care, however, since it is not in general possible to know how a class will be extended—if the object's local state requires the fields to satisfy an invariant, making them protected means that all subclasses will have to preserve the invariants. This may not be feasible when the person who's writing the subclass does not even necessarily have access to the source code of the superclass.

Constructors and super

One issue with class inheritance is that it is not possible to inherit a constructor from the superclass—a constructor must have the same name as the class, and the superclass must have a different name than a class that extends it. However, constructors often establish invariants on an object's local state, so when one class inherits from another, it is usually necessary to let the the superclass initialize the private fields provided by the superclass.

Java therefore provides a keyword **super**, which can be invoked as a method. The effect is to call the superclass constructor. Here is an example of how it could be used:

```
class D {
    private int x;
    private int y;

    public D (int initX, int initY) {
        x = initX;
        y = initY;
    }

    public int addBoth() { return x + y; }
}

class C extends D {
    private int z;

    public C (int initX, int initY, int initZ) {
        super(initX, initY); // call D's constructor
        z = initZ;
    }

    public int addThree() { return (addBoth() + z); }
}
```

Note that c's constructor uses the **super** keyword to invoke D's constructor, and thereby initialize the private x and y fields. Such a call to **super** must be the first thing done in the constructor body.

An example of inheritance

Returning to the shapes example, we might consider how to share some of the implementation details among several classes. For instance, the Point, Circle, and Rectangle classes all implement the same functionality to meet the Displaceable interface. We could *share* those implementation details by creating a common superclass, like this:

```
class DisplaceableImpl implements Displaceable {
  private double x;
  private double y;
  public DisplaceableImpl(double initX, double initY) {
      x = initX;
     y = initY;
  public double getX () {
      return x;
  public double getY () {
      return y;
  public void move (double dx, double dy) {
     x = x + dx;
     y = y + dy;
}
class Point extends DisplaceableImpl {
  public Point (double initX, double initY) {
      super(initX, initY);
class Circle extends DisplaceableImpl implements Shape {
    private double r;
    public Circle (double initX, double initY,
                 double initR) {
      super(initX, initY);
      r = initR;
    public double getArea () {
     return 3.14159 * r * r;
    public double getRadius () {
     return r;
    public Rectangle getBoundingBox () {
     return new Rectangle (getX()-r, getY()-r, getX()+r, getY()+r);
    }
```

```
class Rectangle extends DisplaceableImpl implements Shape {
    private double w, h; // width and height
    public Rectangle (double initX, double initY,
                    double initW, double initH) {
      super(initX, initY);
      w = initW;
      h = initH;
    public double getArea () {
      return w * h;
    public double getWidth () {
      return w;
    public double getHeight () {
      return h;
    public Rectangle getBoundingBox () {
      return new Rectangle(getX(), getY(), w, h);
}
```

24.3 Object

The root of the class hierarchy is a class called <code>Object</code>. All types in Java are a subtype of <code>Object</code>—even interfaces and those classes that aren't declared to <code>extend</code> any other class. Note that since Java supports only "single inheritance" for classes, *i.e.* each class may inherit from at most one superclass or, implicitly from <code>Object</code>, the classes of the subtype hierarchy for a tree. <code>Object</code> is the root of the tree.

The Object class provides a few methods that are supported by *all* objects: toString, which converts the object to a String representation, and equals, which can be used to test for structural equality.

End:

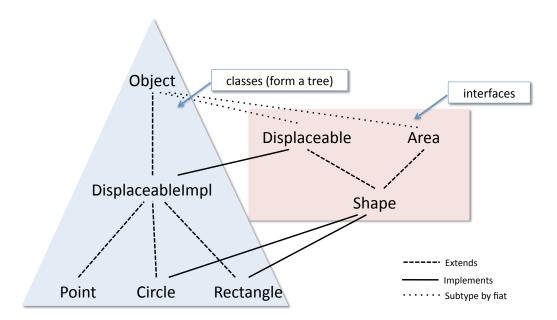


Figure 24.2: A picture of (part of) the Java subtype hierarchy. Interfaces *extend* (possibly many) interfaces. Classes *implement* (possibly many) interfaces and (except for <code>Object</code>) extend exactly one class (<code>Object</code> implicitly). Interfaces are "subtypes by fiat" of the <code>Object</code> class. Classes form a tree, rooted at <code>Object</code> (shown in blue). Interfaces (shown in pink) do not form a tree.

Chapter 25

The Java ASM and dynamic methods

In Chapter 23, we looked at simple form of the Java Abstract Stack Machine. That form included the representation of objects and arrays in the heap and explained the operation of static methods. However, in those examples, we were deliberately vague about how constructors and nonstatic method worked. We understood them at an intuitive level, but could not model them precisely in the ASM.

In this chapter we fill in the details about an essential aspect of the operation of Java, called *dynamic dispatch*. Dynamic dispatch describes the evaluation of normal method calls. It is dynamic because it is controlled by the *dynamic class* of an object—the actual class that created the object determines what code actually gets run in a method call. In a method call \circ .m(), there may be several methods in the Java Class Table called m. Dynamic dispatch resolves this ambiguity.

Another difficulty with modeling method calls are references in the method to the fields of the object that invoked the method. In particular, if

the method m includes the line:

x = x + 1;

where x is intended to be a field, how does the ASM find that field and update it?

Understanding dynamic methods also helps us to model the execution of *Constructors* in the Java ASM, especially those from classes that extend other classes. The last refinement we make to the Java ASM in this chapter is an explanation of how constructors initialize objects when they are

created.

Our goal in this chapter is to extend the ASM enough so that we can precisely model the following example:

```
public class Counter {
 private int x;
 public Counter () {
   x = 0;
  public void incBy(int d) {
    x = x + d;
  public int get() {
   return x;
public class Decr extends Counter {
 private int y;
  public Decr (int initY) {
    y = initY;
 public void dec() {
    incBy(-y);
}
// somewhere in main:
Decr d = new Decr(2);
d.dec();
int x = d.get();
```

Figure 25.1: Running example of dynamic dispatch

This example includes two classes <code>Counter</code> and <code>Decr</code>, which extends <code>Counter</code>. The execution that we would like to model is at the bottom of the listing—how is it that we can create an instance of the <code>Decr</code> class? What does the constructor invocation look like? What happens when we invoke its <code>dec</code> method? What about its inherited <code>get</code> method?

Class Table Object String toString(){... boolean equals... ... Counter extends Counter() { x = 0; } void incBy(int d){...} int get() {return x;} Decr extends Decr(int initY) { ... } void dec(){incBy(-y);}

Figure 25.2: The class table for the example above

25.1 Refinements to the Abstract Stack Machine

In this chapter we explicitly add the *Class Table* as an explicit part of the Java ASM, together with the workspace, stack and heap. The class table is a special part of the heap that is initialized when the Java ASM starts. The purpose of the class table is to model the extension hierarchy (i.e. tree) among classes. Each class in the class table includes a reference to its parent or super class. It also includes code for the constructors and methods defined in that class, as well as any static class members.

The next refinement concerns the code that we run in the workspace itself. Every dynamic method allows a references to the object that invoked through a special variable called this. In fact, every field access x, is short for this.x. We will only execute code in the workspace where these references have been made explicit. In other words, even though we may write the code in Figure 25.1, the code that we will actually use is the one in Figure 25.3.

The code in the figure also makes one more feature of Java explicit. The first line of every constructor should start with an invocation of the constructor of the superclass of the class, using the keyword super. (Recall that if a class does not have an explicit superclass, its superclass is <code>Object</code>). Often we will write this invocation explicitly, especially if the superclass requires arguments. However, even if we leave it out, Java will implicitly add it. For the ASM, we will assume that all code for constructors starts with a call to super.

25.2 The revised ASM in action

To demonstrate how the ASM models constructors and method invocation, we next step through the operation of the ASM for the example program. The starting configuration has the given class table and puts the given code in the workspace.

Constructor invocation

The next step is to invoke the constructor for the Decr class, giving it the argument 2. Figure 25.5 shows the result of this action. A constructor invocation is a lot like a function call in OCaml, or a static method call in Java. It saves the current workspace, puts bindings for the parameters on the stack, and puts the body of the constructor in the workspace. In this case the Decr constructor takes one argument, so the binding inity is added to the stack.

The difference is that constructors also *allocate*, i.e. create the new object in the heap. The object values store the values of the fields (or instance variables) of the object. For a class like <code>Decr</code>, which extends another class, the fields include the fields declared in the <code>Decr</code> class plus all fields declared in the super classes (i.e. <code>Counter</code>). Furthermore, the variable <code>this</code>, a reference to the newly created object is also pushed onto the stack. Finally, the object value

Next, the code in the constructor begins to execute. The first line of the Decr constructor is to invoke the constructor of its super class, i.e. the Counter constructor. The result of this step is in Figure 25.6. As before, the current workspace is saved to the stack, and the code for the Counter constructor is copied from the class table to the workspace. However, this

time, because the object is already allocated, the constructor merely pushes a this pointer to the same heap object onto the stack. Furthermore, the Counter object takes no parameters, so no additional variables are added to the stack.

The first step of the Counter constructor is to call the constructor for *its* superclass, Object. Here we will skip this step—the object constructor has no effect in the ASM model. The next step is to update the x field of the newly created object, as shown in Figure 25.7. As the default value of the field was 0, this action does not actually change the object.

After the Counter constructor completes its execution, the ASM pops the stack and restores the saved workspace. The next step is to continue the execution of the Decr constructor, as shown in Figure 25.8.

The this reference directs the initialization of the y field of the object. This time, the field is updated to the value that was originally provided as the argument to the constructor, as shown in Figure 25.9.

After the Decr constructor finishes its execution, the ASM again restores the saved workspace. The reference to the new object is pushed onto the stack as the value of the local variable d.

The important things to remember about how the ASM treats a constructor call are:

- The newly allocated object value is tagged with the class that created it.
- The newly allocated object value includes fields that are declared in the class that constructs the object as well as *all superclasses of that class*.
- The first step of a constructor invocation is to call its superclass constructor. Even if the source code does not do this explicitly, Java will implicitly add this call.
- Each constructor pushes its own this pointer onto the stack so that it can modify the newly allocated object. However, all of these pointers refer to the same object value.

Dynamic method call

The next line of code is a dynamic method call to the dec method. Dynamic method calls again work like static method calls—they save the

current workspace and push their parameters onto the stack. There are two important differences between dynamic and static method calls.

- 1. The method body that is placed on the workspace is retrieved from the class table. The class tag in the object value (Decr in this case) tells the ASM where to look for this method. Because the Decr class contains a dec method, the code from that method declaration is the one that is run. This process of finding the correct method is called *dynamic dispatch* because it depends on the dynamic class of the object that calls the method. It is illustrated in Figure 25.11.
- 2. As well as pushing the parameters on the stack, the method also pushes a reference to the object which called the method. This reference is called this, and the method code can refer to the this variable whenever it needs a reference to the current object.

The execution of the dec method continues as before. However, when the code gets to the invocation of the incBy method, the ASM must do another dynamic dispatch to determine what code to run. This time, the method is not defined in the Decr class, so the ASM searches for the method in the superclasses of Decr. The method is found in the Counter class, so that is the code that is placed on the workspace for this call.

The incBy method modifies the value of the x field of the object. Note that this field is private to the Counter class. That means that methods in the Decr class cannot modify the field directly. However, even though the Decr class *inherits* the incBy method, it may modify the x field because it was *declared* as a part of the Counter class.

After the completion of the incBy (and dec) method calls, the next step in the computation is a call to the get method of the object. Again, the ASM uses dynamic dispatch to find the code to run (this time from the counter class).

The get method returns the value -2, which is the value of the local variable x placed on the stack.

The important points to remember from this example are:

- When objects method is invoked, as in o.m(), the code that runs is determined by o's dynamic class.
- The dynamic class, which is just a pointer to a class, is included in the object structure in the heap.

- If the method is inherited from a super class, determining the code for m might require searching up the class hierarchy via pointers in the class table.
- This process is called dynamic dispatch.

Once the code for m has been determined, a binding for this is pushed onto the stack. The this pointer is used to resolve field accesses and method invocations inside the code.

Static fields

Some fields in Java can be declared as **static**. This means that the values of those fields are stored with the *Class Table* instead of with individual objects.

```
public class C {
  public static int x = 23;
  public static int someMethod(int y) {
    return C.x + y;
  }
  public static void main(String args[]) {
    ...
  }
}

C.x = C.x + 1;
C.someMethod(17);
```

Like static methods, static fields can be accessed without having an object around. Essentially, the class table itself serves as a container for the data. Because all objects refer to the same class table, all objects have *aliases* to the static fields. Changes to the value of a static field in a method called by one object will be visible to all other objects. As a result, static fields are like *global variables*, and generally not a good idea.

The best use of static fields is for constants, such as Math.PI.

What about static methods?

We have already seen how static methods execute in the ASM, and the refinements of this chapter do not change that execution. But, we can now

look more closely at the difference between static and dynamic methods in Java.

In particular, the biggest difference is that static methods do not have access to a **this** pointer while they are executing. This is because they are invoked directly via the class name (e.g. C.m()) instead of through an object. There is no object around for the **this** pointer to refer to.

As a result, static methods cannot refer to the fields in the class that they are defined in (because there is no way for the method to access those fields) nor can they call nonstatic methods directly. (Of course, they could create a new object and call the nonstatic methods using that object.)

```
public class Counter extends Object {
 private int x;
 public Counter () {
    super();
   this.x = 0;
 public void incBy(int d) {
    this.x = this.x + d;
 public int get() {
    return this.x;
}
public class Decr extends Counter {
 private int y;
 public Decr (int initY) {
    super();
   this.y = initY;
 public void dec() {
   this.incBy(-this.y);
}
// somewhere in main:
Decr d = new Decr(2);
d.dec();
int x = d.get();
```

Figure 25.3: Example with explicit uses of this and super.



Figure 25.4: The initial state of the Java ASM example

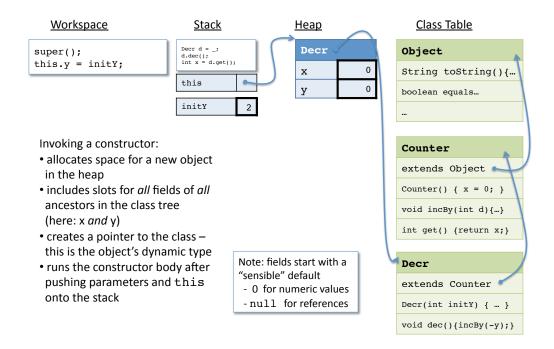


Figure 25.5: Invoking the constructor for the Decr class

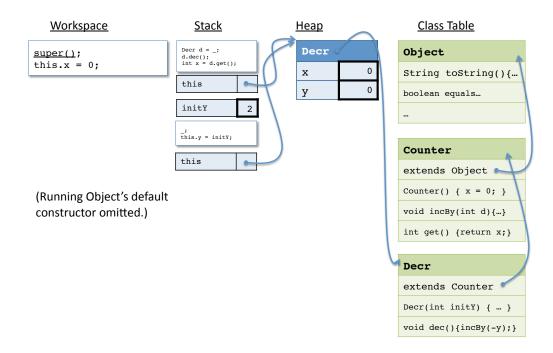


Figure 25.6: Invoking the constructor for the ${\tt counter}$ class

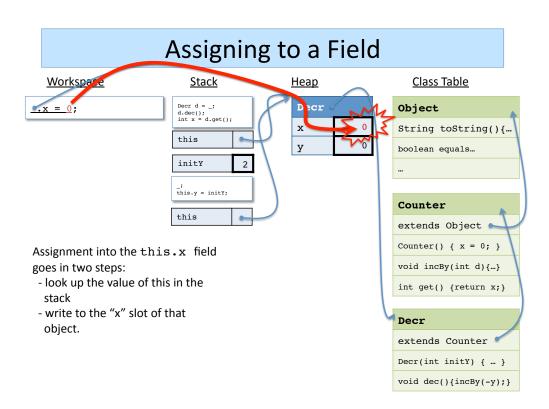


Figure 25.7: Executing the code from the Counter constructor

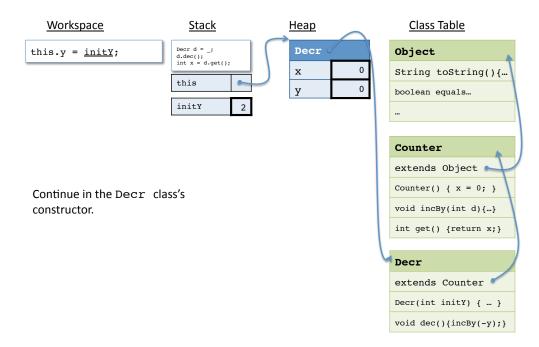


Figure 25.8: Executing the code from the Decr constructor



Figure 25.9: Initializing the y field.

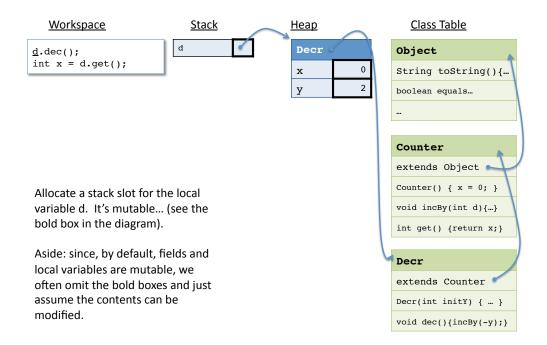


Figure 25.10: Ready to call method dec

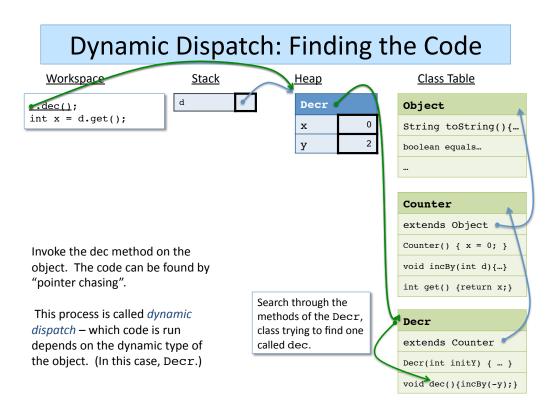


Figure 25.11: Dynamic Dispatch

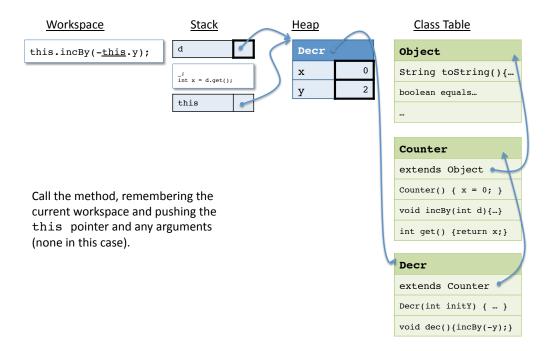


Figure 25.12: During the execution of the dec method

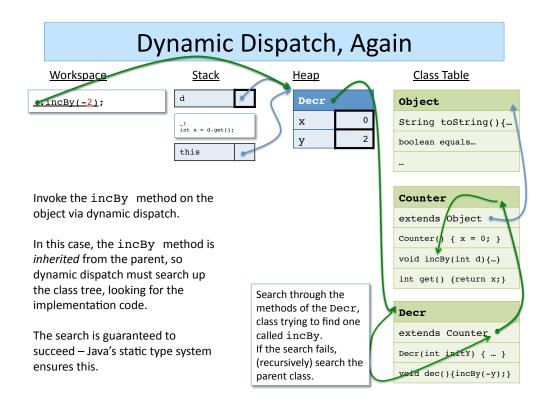


Figure 25.13: Invoking the incBy method

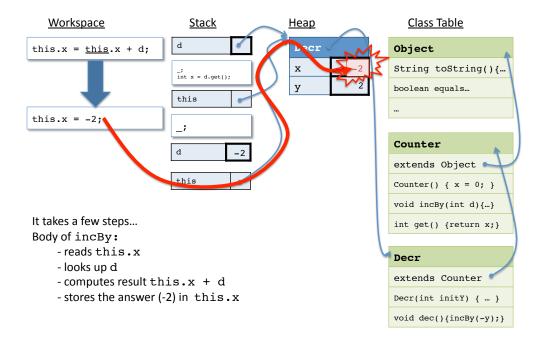


Figure 25.14: Executing the incBy method

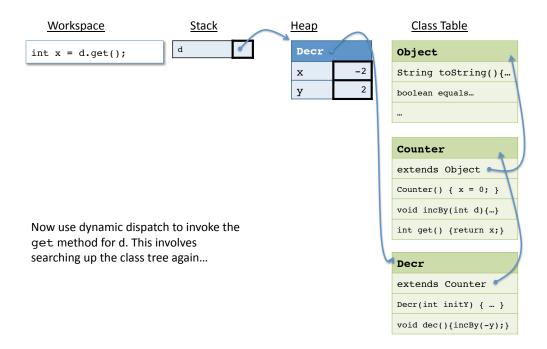


Figure 25.15: Last step: the get method

Chapter 26

Encapsulation and Queues

In Chapter 9, we discussed the power of type abstraction. By hiding the implementation of a data structure we can better preserve the invariants about its implementatin. For example, there are many ways to represent the mathematical idea of a set of elements—different implementations leads to different properties that must be preserved by the set operations. For example, if we represent sets by lists, we may have to maintain the invariant that there are no duplicate elements. Alternatively, if we represent sets by binary-search trees, then we must maintain the binary search tree invariants to know that our set implementation is correct.

Type abstraction allows us to reason about invariants compositionally. Because the actual representation type is abstract, no client of the set module can modify its representation. Therefore, set operations, such as member and equal can assume that their arguments satisfy the appropriate invariants, without worrying that the clients are supplying bad sets.

Java too supports this idea of hiding the implementation of a data structure so that its invariants may be maintained. In Java, this representation hiding is done via the access modifiers on the class members. Typically, the fields are declared **private** and access to them is provided through the **public** methods of the class.

If there is no way to violate the invariants of an object, then we say that the methods *encapsulate* the object state.

26.1 Queues in ML

One example of a data structure that benefitted from type abstraction in OCaml was the queue data structure. Externally, we defined queues to be an abstract type, satisfying the following OCaml interface.

```
module type QUEUE = sig
  (* type of the data structure *)
  type 'a queue

  (* Make a new, empty queue *)
  val create : unit -> 'a queue

  (* Determine if the queue is empty *)
  val is_empty : 'a queue -> bool

  (* Add a value to the tail of the queue *)
  val enq : 'a -> 'a queue -> unit

  (* Remove the head value and return it (if any) *)
  val deq : 'a queue -> 'a
end
```

Internally, queues were implemented using two related data structures the top level queue structure itself, represented as as mutable record:

```
type 'a queue = {
    mutable head : 'a qnode option;
    mutable tail : 'a qnode option;
}
```

and the linked list of qnodes:

```
type 'a qnode = {
   v : 'a;
   mutable next : 'a qnode option;
}
```

Because the users of queues had no idea about the linked list of qnodes, there was no way for them to violate the invariants of the queue data structure. Recall:

Definition 26.1 (Queue Invariant). A data structure of type 'a queue satisfies the queue invariants if (and only if), either

1. both head and tail are None, or,

- 2. head is Some n1 and tail is Some n2, and
 - n2 is reachable by following next pointers from n1
 - n2.next *is* None

26.2 Queues in Java

We can also implement queues in Java, and use the Java mechanisms for encapsulation to maintain the queue invariants. In this section we will walk through a Java implementation of queues and discuss how it compares to the OCaml version.

The Java queue implementation will implement the following interface.

```
public interface Queue<E> {
    /** Determine if the queue is empty*/
    public boolean is_empty ();

    /** Add a value to the end of the queue */
    public void enq (E elt);

    /** Remove the front value and return it (if any) */
    public E deq ();
}
```

We start with the interface, because this definition specifies only what a queue should do, not how to implement it. Java interfaces provide the flexibility that OCaml interfaces do. There can be several different class that satisfy this interface, and they may not necessarily implement queues with linked lists of queue nodes. However, unlike in OCaml, we cannot use the interface for encapsulation. Instead, in our implementation, we must carefully use our access modifiers so that we can restrict access to the internal state of this implementation.

Let us compare the Java interface a bit more to the OCaml interface before we continue to the implementation. The analogue to the OCaml abstract type 'a queue is the interface name itself <code>Queue<E></code>. Like OCaml, this type is parameterized by the elements of the queue. The Java type parameter <code><E></code> is the analogue of the OCaml 'a.

In the Java interface definition, the type parameter E can appear throughout the interface. When this interface type is instantiated, such as Queue < String>, then the methods use String instead of E in their types. For example, if the variable o had type Queue < String>, then the method invocation o.enq(x) would only type check if x had type String.

Java Generics (i.e. the type parameters) work similarly to OCaml generics in this example. However, there is one big difference between the OCaml interface and the Java interface. The OCaml interface includes a way to construct queues, the create function. There is no analogue to this declaration in the Java interface. The reason is that the only type of value that could satisfy this interface in Java is an object. And objects are always created by the constructors of their classes. Interfaces do not include the constructors, and there is no easy way to abstractly construct objects.¹.

26.3 Implementing Java Queues

Now let's consider how the implementation of this interface uses encapsulation to preserve its invariants. As in the OCaml version, the Java implementation has two parts: the top-level queue data structure called <code>QueueImpl</code> (containing references to the head and the tail of the queue), and a linked list of queue nodes, each of which is an instance of the <code>QNode</code> class.

It is the responsibility of the <code>QueueImpl</code> class to encapsulate the queue nodes. Therefore, the queuenodes themselves are rather lightweight. For simplicity, we make the fields of this class public. The <code>QueueImpl</code> class will ensure that no outside code can modify the <code>next</code> reference. (For similarity with the OCaml implementation, we declare that the value stored in the node is immutable with the <code>final</code> keyword.)

¹Advanced Java programmers use *factory methods* to control object creation. For more information see the classic book on Java Design Patterns [5]

```
public class QNode<E> {
   public final E v;  // the value in the qnode is immutable
   public QNode<E> next; // next can be arbitrarily changed

   public QNode (E v0, QNode<E> next0) {
      this.v = v0;
      this.next = next0;
   }
}
```

Note that the type of the <code>next</code> field is a <code>QNode<E></code>, whereas in OCaml it was a 'a <code>qnode option</code>. The <code>QNode<E></code> type includes a null reference, so we do not need to make the field an explicit option. That is more convenient because we can directly access the next queue node without pattern matching. However, it is more error prone because we have to remember to make sure to check that the next queue node is not null.

The constructor for this class merely initializes the two fields.

The top-level class is responsible for encapsulating the state of the queue. Like the OCaml version, its state includes two mutable references to the head an the tail of the queue. This class is also the one that implements the queue interface—the methods of this class implement the queue operations.

```
public class QueueImpl<E> implements Queue<E> {
 private QNode<E> head;
 private QNode<E> tail;
  /** Constructor */
 public QueueImpl () {
   head = null;
   tail = null;
  /** Determine if the queue is empty. */
 public boolean is_empty() {
   return (head == null);
  /** Add a new value to the end of the queue */
 public void enq(E x) {
  /** Remove the front value and return it (if any).
  * Othrows a NullPointerException if the queue is empty. */
 public E deq() {
  }
```

To encapsulate the queue state note that the head and tail fields of this class are declared private. No classes outside of this one are allowed to access these components. Furthermore, none of the methods of this class mention the QNode class. Other parts of the program that use this class may as well not know about the existence of the QNode class.

The methods of the <code>QueueImpl</code> class follow the OCaml implementation. An empty queue is one where the head and tail references do not point to queue nodes. We can determine whether a queue is empty by determining if the head is null.

Adding a new value to the queue means making a new queue node. Then, if the queue is empty, then we make the head and tail references point to the new node. Otherwise, we modify the node at the tail of the queue to point to the new node, and also update the tail reference.

```
/** Add a new value to the end of the queue */
public void eng(E x) {
    QNode<E> newnode = new QNode<E>(x, null);
    if (tail == null) {
        head = newnode;
        tail = newnode;
    } else {
        tail.next = newnode;
        tail = newnode;
    }
}
```

Likewise, dequeueing from the queue modifies the linked list of queue nodes.

```
/** Remove the front value and return it (if any).

*
     * @throws a NullPointerException if the queue is empty. */
public E deq() {
     E x = head.v;
     QNode<E> next = head.next;
     head = next;
     if (next == null) {
        tail = null;
     }
     return x;
}
```

Note that if the queue is empty, this method will throw a NullPointerException with the access head.next. There are better ways to deal with this situation in Java, but we have not covered them yet.

How could this class violate encapsulation? What could it do that would be wrong? One bad idea would be to make the head and tail public members of the <code>QueueImpl</code> class. Then, any method, not just <code>enq</code> and <code>deq</code> could modify the links in the list. It would be equally bad to for the <code>QueueImpl</code> class to return a reference to any queue node from any public method.

```
public QNode<E> getNode(int i) {
    ... find and return the ith node in the list...
}
```

Chapter 27

Generics, Collections, and Iteration

In the next few lectures, we will be covering parts of the Java standard library. In particular, we will focus on three main parts of the library:

- 1. The Java Collections Framework, which include a number of data structures for aggregating data values together.
- 2. The IO libraries, which allow Java programs to process input and output from various sources.
- 3. Swing, a Java GUI library.

We cover these libraries in CIS 120 for a number of reason. The formost is that they are *useful*. Part of being a good programmer is knowing how to use library code so that you don't have to write everything from scratch. Not only is the code faster to write, but it has already been debugged. It is also good style: using the abstractions of standard libraries means that others will be able to more quickly understand your code.

However, knowing *how* to use libraries is a skill in itself. The libraries are documented, and you will need to know how to read that documentation. The libraries also include features of Java that we haven't yet covered—some of those features, such as packages, generics, exceptions and inner classes, we will cover in lecture, and these libraries provide examples of those features. However, some language features you will have to learn on your own if you would like to use that part of the library.

Finally, the library designs themselves are worthy of study. This code is designed for reusability. What about the interface makes it reusable? Where does it succeed? What design patterns can you learn from it?

27.1 Polymorphism and Generics

Polymorphism is a feature of typed programming language that allows functions to take different types of arguments. The name, polymorphism, comes from the Greek word for "many shapes" because polymorphic functions work for many different shapes of data.

The Java language includes two different forms of polymorphism, *subtype polymorphism* and generics (also called *parametric polymorphism*). Although both sorts are available, it turns out that generics are more appropriate for container data types, such as found in the collections framework. To see why, consider the following comparison between the two different sorts of polymorphism in the queue interface.

Subtype polymorphism is enabled by using the type <code>Object</code> in the interface of a data structure, such as in the type of the <code>enq</code> and <code>deq</code> methods. Because every (reference) type is a subtype of <code>Object</code>, then this queue can store any type of value.

```
public interface ObjQueue {
  public void enq(Object o);
  public Object deq();
  public boolean isEmpty();
  public boolean contains(Object o);
}
```

Alternatively, we can also make the queue data structure polymorphic by using Generics, as we did in Chapter 26. In this case, we parameterize the interface by the type E. This type appears as the argument of the enq method and the result of the deq method.

```
public interface Queue<E> {
   public void enq(E o);
   public E deq();
   public boolean isEmpty();
   public boolean contains(E o);
}
```

To see the difference between these two interfaces, compare how queues with these interfaces may be used.

In the first example, suppose we have a queue q of type <code>ObjQueue</code>. Then we can add a string to this queue with the <code>enq</code> method because the type <code>String</code> is a subtype of the type <code>Object</code>. However, when we remove the first element of the queue, with the <code>deq</code> method, its static type is <code>Object</code>, as declared by the interface. Therefore, the next line in the example, <code>x.toLowerCase()</code>, contains a type error. The <code>toLowerCase</code> method is part of the <code>String</code> class, not and not supported by <code>Object</code>.

Alternatively, if we use generics as in the second example, then we must instantiate the queue with a specific type, such as String. This means that when we deq from the queue, then the Java type checker knows that the resulting value must be a String. So in this case, the method call x.tolowerCase() type checks.

However, the cost of permitting this method call is that all elements of the elements in the queue must be a subtype of the <code>string</code> type. Going back to the first example, it is allowed to <code>enq</code> a point into a queue that contains strings. The reason is because they are both considered <code>Objects</code> when they are in the queue. In the second example, the line <code>q.enq(new Point(0.0,0.0))</code> contains a type error. The type <code>Queue<String></code> prevents the queue from storing anything except for (subtypes of) strings.

We could recover the heterogeneity of the first queue by instantiat-

ing the second interface with the <code>Object</code>. A queue of type <code>Queue<Object></code> would behave exactly the same as one of type <code>ObjQueue</code>. Therefore, to give programmers the choice of behaviors, the Java Collections Framework uses Generics to give the data structures defined in the library flexible interfaces.

27.2 Subtyping and Generics

When considering the subtyping relationship between Generic types in Java, the rule to remember is that the type parameter must be *invariant*. In other words, even though type B may be a subtype of type A, it is not the case that the type Queue is a subtype of Queue<A>.

Although this restriction seems counter-intuitive, without it the type checker could miss serious bugs in your code. For example, consider this program:

```
Queue<String> qs = ...
Queue<Object> qo = qs;

qo.enq(new Integer(4));
String s = qs.deq(0);
s.toLowerCase();

// oops!
```

In the first line, we create an object qs that stores strings. We then rename it (alias it) so that its type claims that the queue stores objects. This line is only allowed if <code>Queue<String></code> is a subtype of <code>Queue<Object></code>. That relationship is not true in Java, but suppose for a moment that it is allowed. Then, in the next line, we can use the alias to add a new object to the queue, because <code>Integer</code> is a subtype of <code>Object</code> (as usual). However, when we remove that integer from the queue using qs, and name that value s, we can fool Java. The static type of s is <code>String</code>, because that is what the result of <code>deq</code> is for in the interface <code>Queue<String></code>. However, the dynamic class is actually <code>Integer</code>, because that is actually the value that we put in and removed from the queue. That is a problem because the dynamic class is always supposed to be a subtype of the static type. If Java thinks that an integer has type <code>String</code>, then it won't stop us from trying to call string methods on the integer.

The basic problem with covariant generics [i.e. making

Queue a subtype of Queue<A>] is that it lets you take a bowl of apples and call it a bowl of fruit. Thats fine if youre just going to eat from the bowl and you like all fruits, but what if you decide to contribute a banana to the fruit bowl? Someone taking from the bowl expecting an apple might choke. And someone else could call the same bowl a bowl of things then put a pencil in it, just to spite you. ¹

The Java Tutorial² includes additional information about the behavior and meaning of Generics in Java. It goes much beyond what is covered in CIS 120.

27.3 The Java Collections Framework

The Java Collections Framework includes implementations of several of the data structures that we have already seen in CIS 120. In particular, it includes binary search trees (from Chapter 6), linked lists (from Chapter 16) and resizable arrays (from Chapter 22). It uses these data structures to implement deques, sets and finite maps (from Chapter 9).

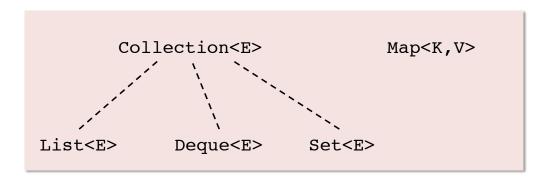


Figure 27.1: A few of the interfaces in the Java collections library.

The most important interfaces in this library appear in Figure 27.1. In particular, the collections framework unifies the interfaces for (muta-

¹Chung-chieh Shan, "Why not covariant generics?" at http://conway.rutgers.edu/~ccshan/wiki/blog/posts/Unsoundness/

²http://docs.oracle.com/javase/tutorial/java/generics/index. html

ble) lists, deques, and sets under a common interface called a <code>collection</code>. The library also includes a separate interface for finite maps, <code>Map</code>. The <code>collection</code> interface is parameterized by <code>E</code>, the type of elements stored in the collection. While the finite map interface is parameterized by two different types <code>K</code> for the type of keys, and <code>V</code> for the type of values.

A portion of the collections interface itself is shown below.

```
public interface Collection<E> ... {
    // basic operations
    int size();
    boolean isEmpty();
    boolean add(E o);
    boolean contains(Object o); // why not E?*
    boolean remove(Object o);
}
```

This interface includes operations for returning the number of elements in the collection (its size), determining whether the collection is empty or not, adding a new element to the collection, determining whether the collection contains a specified element, and removing a specified element. This interface is very similar to the ones that we used in the OCaml part of the course for Queues and Deques.

Note that contains and remove both take arguments of type <code>Object</code> instead of type <code>E</code>. This is because these methods use the <code>.equals</code> method from the object class to determine whether the supplied object matches the element in the collection. It could be that the provided element is not a subtype of <code>E</code>, but is still equivalent to it. (The equality method does not have to return false for objects of different types, it may only look at the common parts of the object values to determine if they are "equal". Most applications only store and remove one type of element in a collection, in which case this subtlety never becomes an issue.)

Lists and Deques are both ordered collections of elements, which we will informally call *Sequences*. Figure 27.2 shows several implementations of these interfaces in the Java Collections Framework. In particular, the ArrayList and ArrayDeque implementations are similar to the resizable array class which we developed in Chapter 22. The LinkedList class is similar to the deque implementation from Chapter 26. When you are reasoning about how long operations take for these implementations, you should

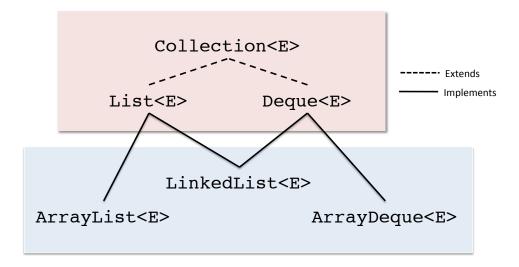


Figure 27.2: Sequence implementations.

use the related implementations as a model. For example, both <code>ArrayList</code> and <code>LinkedList</code> allow you to access elements by their position in the sequence. However, since the <code>ArrayList</code> stores the elements in an array, it is just as fast to access the last element in the list as the first one. On the other hand, accessing the last element in an <code>LinkedList</code> can take a long time if the implementation has to trace through the entire list of linked nodes to find the element. Conversely, both implementations also allow you to add elements to the middle of the sequence. In this case, it is much faster to add an element in the middle of a linked list (where it needs to only create a new node), then to add one to the middle of an array (which needs to allocate a new array and copy the elements over).

Figure 27.3 shows some implementations of the set interface (also a collection) and the map interface. The most important implementations of these interfaces are based on *hashing* (in HashSet and HashMap) and *binary search trees* (in TreeSet and TreeMap). The BST based implementation of sets actually implements a subinterface of set called SortedSet. This is the interface of sets that requires an ordering on elements in the set. In OCaml, all data values were ordered by the pre-defined < operator. However, in this library design, each can use a specific comparison method for the elements in the set. That makes these BSTs (and BST-based maps) more

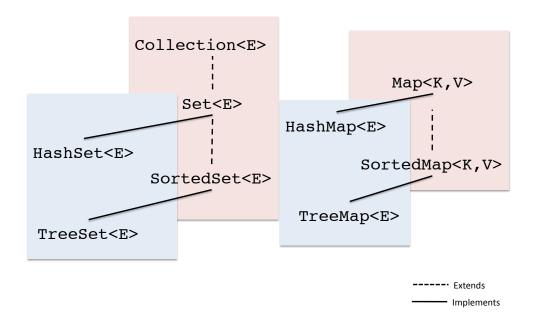


Figure 27.3: Set and Map implementations.

flexible.

Hashing is an implementation technique that is beyond the scope of this course—you'll learn more about it in CIS 120. We include those implementations here to point out the difference between sets and sorted sets.

27.4 Iterating over Collections

Java provides a powerful tool for working with all of the elements of a collection in a generic way.

As shown in Figure 27.4, the Collections interface in Java itself extends another interface, called Iterable.

This interface specifies that all collections must provide an iterator. I.e. the definition of an iterable object is one that provides at least the method iterator, which itself provides access to an *iterator* for the object.

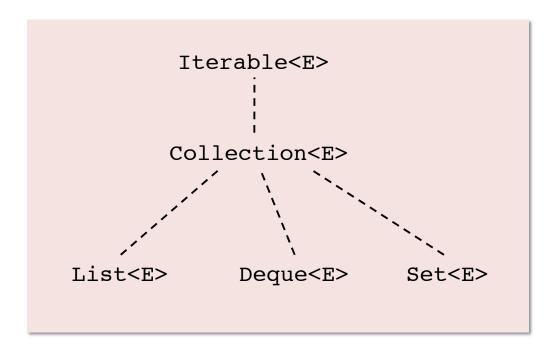


Figure 27.4: The iterable interface.

```
interface Iterable<E> {
     public Iterator<E> iterator();
}
```

An iterator object is an object whose sole purpose is to provide access to a sequence of elements. It must satisfy the Iterator interface, shown below.

```
interface Iterator<E> {
        public boolean hasNext();
        public E next();
        public void delete(); // optional
}
```

An iterator provides access to elements through repeated calls to the hasNext and next methods. The first method determines if there is a next element for the iterator to produce, the second method actually produces it.

For example, consider this code that catalogs the books contained in a list (called shelf).

Because List is a subinterface of Collection, and Collection is a subinterface of Iterable, we know that the shelf has an iterator method. This method returns an Iterator for the elements in the list (which are books). The while loop executes as long as not all of the books have been accessed (or iterated). For each book supplied by the iterator (using iter.next()), the example adds the book information to the catalog and increments the number of books.

The iterator means that we can access the elements of the list in sequence, regardless of the actual implementation of the list. What matters is that we are doing something for each element of the list—not how we are accessing each of those elements. The iterator hides the complexity of array indexing (if we are working with an ArrayList for example) or of walking down a list of nodes (if we are working with a LinkedList). If we were to change our implementation from one implementation to another, we would not need to update this code. At the same time, it provides efficient access to the elements in either version.

Java also provides special "syntactic sugar" for working with objects that are Iterable. The code below uses a "for-each" loop to catalogue all of the books on the shelf. This code is equivalent to the previous two versions. The loop successively binds the variable book of type Book to each element in the collection shelf. For each of these elements, it executes the body of the loop.

```
// iterate through the elements on a shelf
for (Book book : shelf) {
     catalogue.addInfo(book);
     numBooks = numbooks+1;
}
```

The general for a for-each loop is shown below. The for loop declares the variable var of type type with a scope that includes the body of the

for-each loop. The loop iterates once for each element in the collection coll.

```
// repeat body for each element in collection
for (type var : coll) {
   body
}
```

A nice feature of Java is that arrays are also Iterable. For example, we could use a for-each loop to count the non-zero elements of an array with the following code:

```
int[] arr = | // create an array of ints

for (int elt : arr) {
      if (elt != 0) { cnt = cnt+1; }
}
```

In fact, *any* object that satisfies the Iterable interface can be used with a for-each loop.

Chapter 28

Exceptions

Programs often have to deal with unexpected inputs.

• Some methods require that their arguments satisfy certain preconditions. For example, a function that calculates the maximum value of an array requires that its input not be null or the empty array.

```
public static int max(int[] arr) {
  int v = arr[0];
  for (int x : arr) {
    if (x > v) {
        x = v;
    }
  }
  return v;
}
```

The Java type checker cannot prevent this method from being called with null or a zero-length array. How can this method deal with that situation?

• Some interfaces have optional methods. This means that a class can implement this interface with a "stub" method. For example, the iterator interface includes a delete operation (which modifies the underlying sequence, removing the element most recently returned by next from the collection).

```
interface Iterator<E> {
   public boolean hasNext();
   public E next();
   public void delete(); // optional
}
```

However, not every iterator can support that operation. Those classes *must* define a delete method to implement the interface, but the only thing that method should do is report an error that it shouldn't be called with that particular iterator.

- Some parts of the program deal with external resources. Those resources may or may not be present. For example, a Java method in the IO library may try to open and read from a file on the computer's hard drive. But what if that file doesn't exist?
- Sometimes during the execution of a Java program, a resource may be exhausted. What if the program tries to write to a file on the disk, but the disk is full? What if the program makes too many nested method calls and runs out of stack space?
- Some parts of the program just may not be finished. How can a programmer indicate that some methods are not ready to be used and only present in an object to satisfy interfaces?

All of the above are *exceptional* circumstances.

28.1 Ways to handle failure

There are several ways to design methods to deal with failure and exceptional circumstances.

The simplest way is for the method to return an *error* value in the case of failure. For example, the Math.sqrt method returns NaN ("not a number") if its given input is less than zero. Likewise, it is common for methods to return the null reference, if the appropriate value cannot be computed.

However, there is a drawback to this practice. It puts the burden on the caller of the method to check the result to make sure that it is not the *error*

value. However, it is very easy for the caller to forget to do such checks, leading to subtle bugs in the program.

In Chapter 11 we introduced an alternative method. The option type in OCaml allows partial functions to indicate that they are partial in their type. Callers cannot forget to check the return value because the type forces them to pattern match the option. It is possible to replicate this solution in Java, using a special class to indicate possible failure.

However, although this strategy is much more likely to produce correct code, it can be tedious. The caller of every method *must* check the return value, even if there is nothing that caller can do to mitigate the failure. Furthermore, the logic of the program that deals with failure is scattered throughout the normal execution of the method, making the method difficult to read.

This chapter presents a new alternative to dealing with exceptional circumstances—the use of a language feature called *exceptions*. Most modern languages, including OCaml and Java, support this feature. Exceptions allow functions and methods to signal errors in a way that any indirect caller can handle the error, not just the most immediate one. Furthermore, if the error is not handled, the program immediately terminates, meaning that bugs are easier to detect and therefore *not* as subtle.

28.2 Exceptions in Java

An Exception in Java is an object (Surprise!) that represents an abnormal circumstance. The dynamic class and fields of the object indicate information about what went wrong. For example, the Java language and libraries include a number of pre-defined Exception classes to indicate run time errors. Calling a method or accessing a field with a null reference triggers a NullPointerException. Many IO functions return IOExceptions. Exceptions can be created, just like other objects with the new keyword.

For example, you could create your own instance of the null pointer exception class (i.e. an object with dynamic class NullPointerException) by invoking its constructor.

```
NullPointerException ex = new NullPointerException();
```

Creating an exception like this does not do anything special. The unique aspect of exceptions is that they can be thrown.

Throwing an exception is like an emergency exit from the current method. The exception propagates up the invocation stack until it either reaches the top and the stack, in which case the program aborts with the error, or the exception is caught. We've already seen exception throwing before, we just didn't call it that. In OCaml, the failwith expression throws an exception (called Failure) in that language. To throw an exception in Java, use the throw keyword. For example, to exit a method when its argument is three, we could throw an illegal argument exception.

```
static void m (int x) {
  if (x == 3) {
    throw new IllegalArgumentException();
  }
  // here we know that x cannot be 3.
}
```

Catching an exception lets callers take appropriate actions to handle the abnormal circumstances. This lets programs have a chance to recover from the abnormal situation and try something else. Exceptions thrown within the block of a try statement are caught using a catch block.

For example, if a file for reading is not found, then the program can give an alert to the user and ask for a different filename. For example, consider this method from a GUI for displaying images (such as in HW07). The constructor of the Picture class takes a string that is the filename of a new picture to show in the window. If the file is successfully read, then the new picture is displayed by this method (we've ommitted that code). However, because this process could fail, it is put inside of a try block.

If the Picture constructor cannot read from the specified file, then it throws an IOException, indicating that trouble. The catch expression after the try block includes code to execute in the case that an IOException is thrown. The actual exception that was thrown is bound to the variable ex, and information that it carries, such as an error message, can be accessed in the catch. For example, the code above uses ex.getMessage() to get further details about why the file cannot be read.

Note that constructors must return a reference to a newly constructed objects. They do not have the choice to return null instead, indicating an error. Exceptions are the only way that constructors can indicate difficulties in object construction.

28.3 Exceptions and the abstract stack machine

The Java ASM gives us a model of how exceptions work by demonstrating both how exception objects are represented in the heap, and what happens when exceptions are thrown and caught. Each exception handler (i.e. catch clause) is saved on the stack whenever execution reaches the accompanying try block in the workspace. When exceptions are thrown, the stack is popped until a saved exception handler is found. If there are no exception handlers, then program execution terminates. The program stops with an error.

The lecture slides from Lecture 29 demonstrate the ASM in action.

28.4 Catching multiple exceptions

The code in a try block may encounter many different sorts of exceptional circumstances. For example, when trying to load a file, several errors could occur. Perhaps the file might not exist, or perhaps the file does exist but is locked by the operating system and unable to be read. In these situations, the method for loading the file would throw different exceptions, indicating the different sources of trouble.

For this reason, Java allows try blocks to have *multiple* catch clauses. Each clause can catch a different class of exception. For example, suppose we wished to separate the handling of file not found exceptions from other sorts of IO exceptions. Then we could use the following code:

In this example the first clause catches any FileNotFoundException and the second clause catches all other IOExceptions that could be thrown by the body of the try block. Other exceptions, such as NullPointerExceptions, are not caught and propagate outward.

This example demonstrate that it is the *dynamic class* of the thrown exception object that determines what handling code is run. The exception handlers are examined in order and any one that binds an exception variable with some type that is a superclass of the dynamic class of the thrown exception is the one that is triggered.

Note that, in the Java IO libraries, the class FileNotFoundException extends the IOException class. This means that FileNotFoundException is a subtype of IOException. As a result, if we had exchanged the order of the exeception handlers above:

then the handler for FileNotFoundExceptions would never be triggered. If such an exception were thrown, it would be handled by the first compatible exception hander, in this case IOException.

All exceptions in Java are subclasses of a special class called Exception. This means that it is possible to create an exception handler that can handle any sort of exception whatsoever:

However, such exception handlers are usually *not a good idea*. If you use one in your code, you are claiming that you know how to handle any sort of exceptional circumstance whatsoever, and that is not usually the case. It is much more likely that your code will handle some sorts of exceptions, but completely ignore other sorts, such as <code>NullPointerExceptions</code>. This is particularly bad because those exceptions will not propagate to the top level, hiding bugs that exist in your code. And, if you cannot detect bugs early, they are much more difficult to eliminate.

28.5 Finally

Exception handlers can also include finally clauses.

A finally clause of a try/catch/finally statement always gets run, regardless of whether there is no exception, a propagated exception, a caught exception, or even if the method returns from inside the try.

These sorts of clauses are most often used for releasing resources that might have been held/created by the "try" block. For example, whenever files are opened for reading in Java, they must also be closed afterwards. The operating system can only allow so many files to be open at once,

closing the file when reading is complete means that other file operations are more likely to succeed. The code below uses the FileReader class to open and read from a file.

While reading from the file, an IOException may occur. If that is the case, then the method should still close the file afterwards.

```
public void doSomeIO (String file) {
  FileReader r = null;
  try {
    r = new FileReader(file);
    // do some IO
  } catch (FileNotFoundException e) {
    // handle the absent file
  } catch (IOException e) {
    // handle other IO problems
  } finally {
    if (r != null) {
         // don't forget null check! If the file
         // doesn't exist, then r will be null.
      try { r.close(); } catch (IOException e) {
         // handle an IOException if caused by closing the file
    }
  }
```

28.6 The Exception Class Hierarchy

Figure 28.1 shows the relationship between several classes in Java.

All exceptions in java are instances of some class that is a subtype of the Exception class.

Not just exceptions can be thrown. Any object that is a subtype of the Throwable class is throwable. This includes exceptions and Errors. Errors are intended to stop the execution of a Java program. They indicate a serious runtime violation or abnormal condition. They should never be caught by the program.

Exceptions are all subtypes of the Exception class. Java uses the class hierarchy to make a further distinction—exception classes that extend RuntimeExceptions are treated differently than other exceptions.

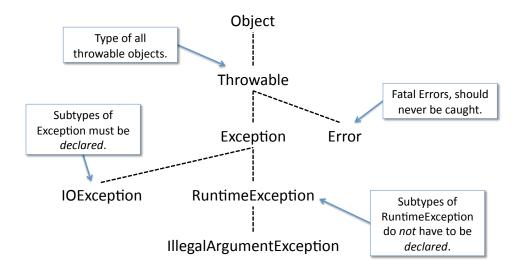


Figure 28.1: The Java Exception class hierarchy

28.7 Checked exceptions

Most methods that possibly throw exceptions (and do not handle them) must include this information in their interface, or method *declaration*. They do so by adding a throws clause, after the parameters of the method.

For example, this method below could throw an instance of the AnException class.

```
public void maybeDoIt() throws AnException {
   if (this.moonIsFull()) {
      throw new AnException();
   } else {
      // do something else
   }
}
```

Therefore, it must *declare* that this is a possiblity. If the programmer forgets to add the throws Anexception to the method header, then the compile will not compile. The Java type checker will check that this exception must be declared whereever it may be thrown.

This throws clause is part of the method type. In an interface that includes the maybeDoIt method, the throws clause must be present as well.

```
public interface Doable {
   public void maybeDoIt() throws AnException;
}
```

That is so that every caller of the method knows that the exception could be triggered by this method call.

Methods that call other methods that could throw exceptions must also include throws annotations. For example, the method below might call the method above, and because maybeDoIt might throw AnException, this method might throw AnException.

```
public void maybeNot() throws AnException {
  if (this.starsAligned()) {
    this.maybeDoIt();
  } else {
    // do something else
  }
}
```

Note that if a method successfully handles a potentially thrown exception, it does not need to declare it. For example, even though the method call below, could throw Anexception, that code is in a try block that will catch the exception and prevent its propagation to the users of the definitelyNot method.

```
public void definitelyNot() {
   try {
     this.maybeDoIt();
   } catch (AnException ex) {
     // ... handle the exception ...
   }
}
```

28.8 Undeclared exceptions

However, some exceptions do not need to be declared. (There is an exception to the rule about exceptions.) Methods that could throw RuntimeExceptions do not need to indicate this possibility.

Many of the exceptions that you have already seen are runtime exceptions. They do not need to be declared by the objects that throw them. These include NullPointerException, IndexOutOfBoundsException and

IllegalArgumentException. Requiring methods to declare that they could throw these exceptions would be excessive. Almost every method that uses an array or object could potentially throw a NullPointerException.

Why are only some exceptions declared? The original intent was that runtime exceptions represent disastrous conditions from which it was impossible to sensibly recover. Furthermore, the prevalence of potential null pointer exceptions means that every method would have to declare them, making the declaration itself tedious but meaningless.

As you define your own exception classes, you have the choice of whether they should be declared or not, by choosing whether to extend RuntimeException or Exception. Declared exceptions provide better documentation for users—the interface for the method is more explicit when it includes the potential exceptions that the caller should be aware of. With undeclared exceptions, it is easier for the callers to not even know that they should set up exception handlers for exceptional circumstances.

However, the cost of declared exceptions is that it is more difficult to maintain code as this interface must be adapted each time the code is modified. In practice, developers have not seen much benefit to declared exceptions. Test-driven development encourages a "fail early/fail often" model of code design and lots of code refactoring, so undeclared exceptions are prevalent.

As a compromise, only general purpose libraries tend to use declared exceptions, as the explicit interfaces are much more important in that situation.

28.9 Good style for exceptions

We end this chapter with some style suggestions for using exceptions sucessfully in your code.

- In Java, exceptions should be used to capture exceptional circumstances. Exception throwing and handling (i.e. Try/catch/throw) incurs performance costs and, more importantly complicates reasoning about the program. Dont use them when better solutions exist.
- Just as it is good style to re-use data structures from the standard library, it is also good style to re-use existing exception types when

they are meaningful to the situation. For example, if you are implementing your own sort of container class, it makes sense to use the NoSuchElementException from the Java collections framework.

- However, for exceptional circumstances that are specific to your application, it makes sense to define your own subclasses of Exception. By doing so, you can convey useful information to possible callers that can handle the exception. At the very least, you will give a new name to the exception class, so that it can be caught independently of other exceptions. Furthermore, because exceptions are objects, the fields of the object are a great place to store additional information about the exceptional circumstance, such as the values of variables that were in scope when the exception was thrown. Such values can help exception handlers recover from the situation more gracefully, and if necessary, provide more insightful error messages to users.
- It is often sensible to catch one exception and re-throw a different (more meaningful) kind of exception. For example, suppose you were implementing a class that provides an Iterator interface to a file. This class would read from the file one word at a time, and would provide the next work with each call of the next method. However, file reading could trigger an IOException if there are no more characters to be read. It is much better style if this iterator catches that exception and replaces it with a NoSuchElementException.
- Catch exceptions as near to the source of failure as makes sense. You could put all of your exception handling code in the main method of your application, which would prevent your program from being terminated by a thrown exception. However, the main method probably does not have enough information to recover from the situation. It is better to handle the exception as soon as possible.
- As mentioned above, it is best to catch exceptions with as much precision as possible. In other words, don't do: try catch (Exception e) . Instead use an exception handler tailored to the specific class of exception that you would like to handle. For example, try catch (IOException e)

See the Java Tutorial 1 for further information about exceptions in Java.

¹http://docs.oracle.com/javase/tutorial/essential/exceptions/

Chapter 29

IO

Like Chapter 27, this chapter concerns a very useful part of the Java Standard library, the *IO* library. The abbreviation *IO* is short for Input-Output. This library contains classes so that Java programs can interact with its environment.

The fundamental abstraction in the IO library is a *stream*, a communication channel to the outside world. A stream is a sequence of values that the program processes in order, and may not have a fixed end (unlike a list or array). For example, an *input* stream may consist of the sequence of characters being read from the keyboard or a file, a sequence of bytes read from a network connection. *Output* streams allow the program to send information, either to the console, a text window, a file, or the network. Values are read or written to the stream in order, one-by-one.

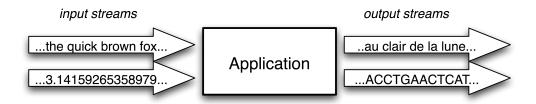


Figure 29.1: Input and Output streams

Java unifies all of these sources and sinks of data using a common type. The two abstract classes InputStream and OutputStream describe the inter-

face for basic operations in the stream hierarchy¹

The basic operation from the InputStream class is a method to read data from the stream.

Likewise, the OutputStream class is based on writing writing data.

```
abstract void write(int b)
throws IOException; // writes the byte b to the output
```

In both cases, these methods are abstract—they just declare the methods that subclasses must implement. Subclasses that extend these classes will implement read and write to actually pull data from and push data to the appropriate devices (files, keyboards, network, etc.) Furthermore, although the types of these methods look like they read and write integer values, in actuality, input and output is based on *bytes*. Bytes are 8-bit integers—i.e. numbers in the range 0-255. The read method will never return the integer 256 or higher. Likewise, the write method will produce strange results when given numbers that are not within 0-255.

The read method returns -1 when the end of the stream is detected and there are no more bytes to be read.

Both of these methods could throw an IOException if the stream cannot be read or written to.

29.1 Working with (Binary) Files

The classes FileInputStream and FileOutputStream extend the InputStream and OutputStream classes respectively. These two classes allow you to read and write data to files. Note however, that these classes are for working with *binary* data, such as the bytes in an image file.

For example, here is a constructor for class that represents black-andwhite images. The constructor for this class creates an image by reading

¹Abstract classes are a cross between interfaces and classes. Like interfaces, they include method declarations and cannot be instantiated. However, they may also include method definitions, constructors and fields, like regular classes. They are useful for describing an interface and providing basic functionality to all subclasses based on that interface. Abstract classes are most useful in building big libraries, which is why we arent focusing on them in this course.

in a file in binary format. This simple format contains first the width, then the height of the image. After that, each byte represents a pixel in the image. Because this is a black-and-white image each pixel only contains one component, a value between 0 (pure black) and 255 (pure white).

```
class Image {
   private int width;
  private int height;
   private int[][] data; // each value is in the range 0-255
   // create a new input stream from the specified file
   public Image (String fileName) throws IOException {
      InputStream fin = new FileInputStream(fileName);
      width = fin.read(); // read the width
      height = fin.read();
                             // read the height
      if (width == -1 || height == -1) {
         throw new IOException ("Height/Width not available.");
      data = new int[width][height];
      for (int i=0; i < width; i++) {</pre>
         for (int j=0; j < height; j++) {</pre>
            int ch = fin.read();
            if (ch == -1) {
               throw new IOException ("File ended too early.");
            data[i][j] = ch;
      fin.close();
```

Note that after the constructor is finished with the file, it *closes* the input stream. File streams are managed by the operating system. Only *open* files may be read from or written to. Furthermore, the operating system should be notified when the file access is complete by *closing* the file. This lets the operating system know that it no longer needs to manage the file.

Furthermore, this constructor explicitly throws *exceptions* indicating that the file is not in the correct format. Furthermore, some of the operations that the constructor uses to read the file could also throw exceptions. For example, if the file could not be opened by the FileInputStream constructor, then that constructor may throw an FileNotFoundException. Likewise, the read methods could throw IOExceptions for other sorts of errors.

Input streams provide the most basic support for working with input and output, but some times you would like more help. For example, we could make the code above more efficient by using a <code>BufferedInputStream</code>. This class groups together multiple reads into one file access, while still providing the data byte by byte. Because setting up the file access is the slow part, its much faster to read multiple bytes at once.

Using a BufferedInputStream is simple. This class just "wraps" another InputStream to add buffering. For example, we could add buffering to the example above by changing the beginning of the constructor, thus:

```
public Image(String fileName) throws IOException {
    FileInputStream fin1 = new FileInputStream(fileName);
    InputStream fin = new BufferedInputStream(fin1);
```

A BufferedInputStream is also an input stream, so anywhere an input stream could be used, a buffered input stream is permissible.

Buffering is not the only functionality that the Java libraries builds on top of IO streams. For example, many Java applications need to process character-based input, instead of raw binary data. Therefore, the Java library includes many more classes and higher-level abstractions to assist with this sort of stream processing.

29.2 PrintStream

For example, one class that you have already used (without even knowing about it) is the PrintStream class.² This class extends OutputStream with methods for printing various different types of values to the console, including Strings. Unlike the OutputStream above, which only writes bytes, this stream can write any Java value.

The System class (part of Java) contains a static field called out that is an instance of this class.³ So every use of System.out.println is calling a method of the PrintStream class.

The println method is an example of an overloaded method. This means

²See http://docs.oracle.com/javase/6/docs/api/java/io/PrintStream.html for the documentation of the PrintStream class.

³Note that System.out is a static member of the class System—this means that the field out is associated with the class, not an instance of the class. Recall that static members in Java act like global variables, as described in §21.

that there are actually several different variants of the println method in the PrintStream class. For example, the javadocs for this class include the following methods, useful for printing both primitive values and objects.

```
void println()
       Terminates the current line by writing the
       line separator string.
void println(boolean x)
// Prints a boolean and then terminate the line.
void println(char x)
// Prints a character and then terminate the line.
void println(double x)
// Prints a double and then terminate the line.
void println(float x)
       Prints a float and then terminate the line.
void println(int x)
     Prints an integer and then terminate the line.
void println(Object x)
// Prints an Object and then terminate the line.
void println(String x)
        Prints a String and then terminate the line.
```

With overloading, the number and *static types* of the arguments determine which version of the method executes. The java IO library uses overloading of constructors pervasively to make it easy to glue together the right stream processing routines.

Other useful methods in the PrintStream class include a method to print values without terminating the line (overloaded like println above)

and a method to flush the output.

```
void print(String x)
// write x without terminating the line
          (output may not appear until the stream is
void flush()
// actually output any characters waiting to be see
```

What does the flush method do? The PrintStream class actually buffers output to the console. What this means is that it gathers together the output of several calls to print in a special data structure called a buffer. It does not display them immediately. Only when the buffer is flushed does the output appear in the console. Flushing happens when the buffer is full, with every newline, and when it is flushed explicitly with the flush method.

29.3 Reading text

For reading streams text, Java provides another abstract class called a Reader. Just like subclasses of the InputStream class provide streams of bytes, the subclasses of the Reader class provide streams of characters. While bytes can be stored with 8 bits, characters are 16 bit values. Like InputStreams, Readers have a read method. However, this time, the read method returns an integer in the range 0 to 65535. Also like InputStreams, the read method returns -1 when there are no more characters to be read from the input stream.

The FileReader class creates a reader that reads characters from an input text file. For example, given a string fileName, we can construct a reader as follows:

Reader reader = new FileReader (fileName);

If we would like to add buffering to the file access (as we did for input streams above) the BufferedReader class serves the same role as the BufferedInputStream class. For example, creating a file reader with buffering can be done just by wrapping the file reader with a buffered reader:

```
Reader reader = new BufferedReader(new FileReader(fileName));
```

We will walk through an example using the Reader class in \histogram.

29.4 Writing text

The output analogue to the Reader class is the abstract Writer class. This class is similar to the OuputStream class. Instead of writing data byte-by-byte, this class writes data character-by-character. For example, if you would like to write text to an output file, it would be a good idea to create an instance of the FileWriter class, a subclass of the Writer class that sends its output to a specified file.

The Java library provides a very useful form of writer called a StringWriter. Recall in Java that strings are immutable. Suppose you were creating a string of characters, one by one, but you didn't know in advance what the

⁴In some languages characters and bytes are the same thing. However, Java distinguishes these two sorts of values.

string would be (perhaps you are reading in the characters from an input file).

For example, you could use the following code to read all of the text of a file into a new string value.

```
Reader in = new FileReader("one.txt");
int ch = in.read();
String str = "";
while (ch != -1) {
    str = str + ((char)ch); // cast to primitive char type
    ch = in.read();
}
```

This code opens a new file reader for a specified input file. It then reads the file character-by-character until there are no characters remaining in the file. As each character is read, it updates the string value to include that new character at the end by concatenating the current string and the new character. (Note that before the int character can be added to the string it must be casted to the primitive Java type char. This makes sure that the value is interpreted as a character as it is appended to the string instead of a number.)

All of these appends make this routine very slow. As each character is read, a new string must be allocated in the heap and all of the previous values of the old string, plus the new string must be copied into it.

Instead, the <code>StringWriter</code> class uses a resizable array to read into a string of unknown size more efficiently. This class doubles the array each time that it needs to grow, so it does not need to do as many copies as the code above. The <code>StringWriter</code> is a <code>Writer</code>, so its <code>write</code> method appends its input to the end of the output. The <code>toString</code> method of the <code>StringWriter</code> class returns the current output as a <code>String</code> value.

```
Reader in = new FileReader("one.txt");
int ch = in.read();
StringWriter outputWriter = new StringWriter();
while (ch != -1) {
   outputWriter.write(ch);
   ch = in.read();
}
String output = outputWriter.toString();
```

29.5 Histogram demo

In the last part of this chapter, we use a design exercise to put these ideas together. This exercise also demonstrate the use of the Java Collections framework at the same time, and is good preparation for homework HW09.

Consider the following problem:

Write a command-line program that, given a filename for a text file as input, calculates the frequencies (i.e. number of occurrences) of each distinct word of the file. The program should then print the frequency distribution to the console as a sequence of word: freq pairs (one per line).

For example, if the above text were stored in an input file, then the console should print

```
Histogram result:
The : 1
Write: 1
a : 4
as : 2
calculates : 1
command : 1
console : 1
distinct: 1
distribution: 1
e : 1
each: 1
file : 2
filename: 1
for : 1
freq: 1
frequencies: 1
frequency: 1
given: 1
i : 1
input: 1
line : 2
```

```
number: 1
occurrences : 1
of : 4
one : 1
pairs: 1
per: 1
print: 1
program: 2
sequence: 1
should: 1
text: 1
that: 1
the : 4
then: 1
to : 1
word: 2
```

Note that in this example, punctuation is ignored. The program merely breaks up the input into words and then counts the number of occurrences of each word in the program.

When thinking about this exercise, we must ask a number of questions.

- how do we input data?
- what do we need to do to process it?
- what is a word?
- how do we iterate over the input?
- how do we keep track of the frequencies?
- how do we extract the output data?

The answers to these questions help us break up the whole problem into subproblems and define the interface between those components. Furthermore, in answering these questions, we may need to look at the Java libraries to see if there is some pre-defined functionality that can help us.

One observation that we can make is that since we need to work through the file word-by-word, we need some way to return each of

the words in the file until there aren't any more. The Iterator interface describes a class that returns a sequence of values, because we will represent words by strings, we will create a class that implements the Iterator<String> interface.

WordScanner

We will call this class a WordScanner. We have already defined some of the interface for this class—it should be an iterator.

The other part of the interface to define is the constructor for the class. How will we create a WordScanner?

The constructor for this class needs a place to read the words from. Since we are working with words, we will want an input stream that works with text. Therefore, we will make the constructor take a Reader as an argument. The class itself will read characters from the reader and assemble them into words.

Before we write the code, we should create a few test cases. These test cases will need to supply a Reader to the word scanner:

For example, given a blank input, we should not be able to read any words from it. Because the word scanner will use a reader, we can test it with any subclass of reader. Even though in the full program we will read from files, for the test cases, we can use a StringReader to test the WordScanner.

```
@Test public void testEmpty() {
    WordScanner ws = new WordScanner(new StringReader(""));
    assertFalse(ws.hasNext());
}
@Test public void testOne() {
    WordScanner ws = new WordScanner(new StringReader("one"));
    assertTrue(ws.hasNext());
    String word = ws.next();
    assertTrue(word.equals("one"));
    assertFalse(ws.hasNext());
}
```

After designing a few test cases, including those with multiple words, and with punctuation or other non-letter characters, we can then move onto the implementation of the word scanner. The implementation of this class is in Figure 29.2 and Figure 29.3.

The WordScanner class needs two pieces of private state. It needs to remember the Reader that it gets the input from (we'll call this r) and the last character read (we'll call this c) from this Reader.

The invariant is that if the character is -1 then there are no more characters in the input, and therefore no more words to return. Therefore, the hasNext method can just return whether this character is -1.

Furthermore, the reader will be in a state such that the last character read is always a letter. If any of the methods reads a nonletter character, the method will keep reading until it either reaches -1 or a letter. In fact, the private method <code>skipNonLetters</code> does just this. Note that the static method <code>Character.isLetter</code> can determine whether a specific character is a letter or not.

Every time the next method is invoked, the wordscanner needs to read all of the letter characters in the input and return that as a word. Also, to maintain the invariant about c, it needs to skip all of the nonletter characters following the word. This method uses a StringWriter to gather the read characters as above.

Histogram

Figure 29.4 uses the Wordscanner class to solve the design problem in its main method. The first step is to make sure that the method was called correctly. The arguments to the main method are the *commandline arguments* to the program. In this case, we want to make sure that the program is called with a single argument, the name of the file to process. This file name should be stored in the first position of the args array, i.e. args[0]. If this argument is not present, or if there are additional arguments, the program terminates with a message describing how to run the program from the command line.

Next, the method uses a word scanner to read in the words from the file one by one. As each word is read, the method stores the word in a *finite map*. The Collections framework includes TreeMap an implementation of the Map interface. In this case we would like to map words to their number of occurrences. So the Map that want to create maps String keys to Integer values.

The Reader for the WordScanner is created inside of a try block. This is because this process could fail. If the given filename (args[0]) then

```
public class WordScanner implements Iterator<String> {
  private Reader r;
  private int c;
   // Invariant:
   ^{\prime\prime} c is -1 for EOF, otherwise the int representation
           for a *letter* starting the next word.
   public WordScanner (Reader initR) {
     r = initR;
     c = 0;
     skipNonLetters();
   // scans the file to make c equal to the next letter
   // character in the file. If there are none left, c is -1.
  private void skipNonLetters() {
     try {
         c = r.read(); // returns -1 at the end of the file
         while (c != -1 && !Character.isLetter(c)) {
            c = r.read();
         }
      } catch (IOException e) {
        c = -1; // use -1 for other IOExceptions
   }
   * Returns true if there is a word available.
   public boolean hasNext() {
     return (c != -1);
```

Figure 29.2: Implementation of the WordScanner(Part I)

```
* Returns the next word available from the Reader and
 * then skips all non-letter characters.
 * Throws "NoSuchElementException" if there is not
 * another character
 * @see java.util.Iterator#next()
public String next() {
   if (c == -1) throw new NoSuchElementException();
   // a "buffer" to read the word into
   StringWriter buf = new StringWriter();
   try {
      while (Character.isLetter(c)) {
         buf.write(c);
         c = r.read();
   } catch (IOException e) {
      throw new NoSuchElementException();
   skipNonLetters();
   return buf.toString();
}
 * Unsupported by this iterator.
 */
public void remove() {
  throw new UnsupportedOperationException ();
}
```

Figure 29.3: Implementation of the WordScanner (Part II)

the constructor for the FileReader class will throw an exception. For efficiency, we wrap the file reader inside a BufferedReader before passing it to the constructor of the WordScanner class.

The main loop of the program iterates through all of the words in the file. If the word is already found in the TreeMap, the program increments its value. Otherwise, the program inserts the word into the TreeMap with the value 1, indicating that the word has been seen once.

After the entire file has been processed, the program closes the input file, using the close method of the FileReader class. The program then uses the iterator of the TreeMap class to print out the frequencies of all of the words. The for-each expression gives access to all the entries in the finite map, represented using the class Map.Entry. The getKey() method of this class gives the key (i.e. the word) and likewise getValue() returns the number of occurrences that were calculated. Because we used a binary search tree to implement the map, the entries are returned in alphabetical order.

```
public class Histogram {
   public static void main(String[] args) {
      if (args.length != 1) {
         System.out.println("Usage: java Histogram <file>");
         return;
      }
      // Basic idea:
      // Use a WordScanner to read in the words from the file.
      // Then use a TreeMap to calculate the word frequencies
      // Then use a PrintWriter to display the key value data
      Map<String, Integer> freq = new TreeMap<String, Integer>();
      try {
         FileReader freader = new FileReader(args[0]);
         Reader reader = new BufferedReader(freader);
         WordScanner s = new WordScanner (reader);
         while (s.hasNext()) {
            String word = s.next();
            if (freq.containsKey(word)) {
               Integer i = freq.get (word);
               freq.put (word, i+1);
            } else {
               freq.put (word, 1);
            }
         // release the resources used by the input streams
         reader.close();
         // Print the result
          System.out.println("Histogram result:");
          for (Map.Entry<String, Integer> kv : freq.entrySet()) {
            System.out.println(
               kv.getKey() + " : " + kv.getValue().toString());
          }
      } catch (FileNotFoundException e) {
         System.out.println("File not found.");
      } catch (IOException e) {
         System.out.println("IO error from closing reader.");
   }
```

Chapter 30

Swing: GUI programming in Java

The third major library that we cover in CIS 120 is *Swing*, the Java library for developing GUI applications.

We study this library in CIS 120 for a number of reasons:

• It is an example of the event-based (or reactive-) programming model.

One goal of CIS 120 is to expose students to many different forms of programming, from functional (computation produces values), to iterative (where computation does something, such as modify data structures and print output), to object-oriented (where computation is the interaction between state-hiding components) to reactive (where computation means installing actions that happen in response to events).

- It is also an example of Object-Oriented programming.
 - The Swing library makes extensive use of subtyping, inheritance and overriding to define its abstractions and produce reusable code. In §18 we designed a GUI library in OCaml without any of these features. So we will be able to make a good comparison so that we understand and justify these constructs.
- As with the other libraries that we have covered, we can look at how this one is organized to learn a bit about library design.
- It enables fun applications! The Swing library gives us a rich set of classes to work with.

In this chapter we introduce the basic framework of the Swing library and discuss how it compares to the OCaml GUI library that we developed earlier in the course. For more information about Swing and developing GUI applications in Java, we recommend the Java Swing Tutorial¹.

	OCaml	Java
Graphics Context	Gctx.t	Graphics
Widget type	Widget.t	JComponent
Basic Widgets	button label checkbox	JButton JLabel JCheckBox
Container Widgets	hpair, vpair	JPanel, Layouts
Events	event	ActionEvent MouseEvent KeyEvent
Event Listener	mouse_listener mouseclick_listener (any function of type event -> unit)	ActionListener MouseListener KeyListener

Figure 30.1: Concepts from OCaml GUI library have analogues in Swing

The OCaml GUI library that we developed in §ch:gui was intended to serve as a model of Swing. There were three important parts of that model.

The fundamental building block of the OCaml GUI library was the widget, defined in Widget.ml. This module provided an abstract type of "things" displayed on the screen, giving a uniform interfaces to the building blocks of GUIs (buttons, canvas, labels, checkboxes, etc.). Other widgets provide layout of these basic elements, by placing them beside or above each other. In this way, the widgets divide up the window of the

http://docs.oracle.com/javase/tutorial/ui/index.html.

application in a hierarchical fashion. The widget interface included three components: a function from drawing the widget on the screen (called repaint), a function for calculating the size of the drawn widget (called size), and a function for handling events that occur in the widget's area of the window.

For drawing, GUI library included the idea of a *graphics context*, implemented in <code>Gctx.ml</code>. This module provided the drawing operations that we used to build the rest of the library. It also relativized the coordinates for drawing, so that each widget could draw itself using the same code, no matter where the widget was located in the final application. Finally the graphics context tracked the state necessary for drawing, such as the current pen color or line thickness.

To handle events, the GUI library stored certain higher-order functions as *event listeners*. When an event is triggered, the event listeners would update the state of the application. The program would then communicate the changed state by redrawing all of the widgets.

The concepts that you saw in the OCaml GUI library have analogues in the Java Swing library, as listed in Figure ??. In OCaml, the concepts were usually represented by a module, type definition or functions. In Java, they are always classes.

30.1 Drawing with Swing

We will first just discuss how to draw pictures using the Swing libraries. Using the OCaml GUI library, we could draw a picture by creating a widget where the repaint method uses the graphics context to draw pictures every time the widget is displayed.

For example, the following OCaml code creates a window with a line

In our Java example, we will draw in roughly the same way. The Swing analog to widget is the class <code>JComponent</code>. All Swing GUI components are subclasses of this class. To create a component that draws a picture in the window, like the one above, we need to create a subclass of this class that <code>overrides</code> the methods that correspond to <code>repaint</code> and <code>size</code> above.

The two analogous methods in the JComponent class are:

(A Dimension is an object that contains an height and width fields.)

For example, to produce a component that displays as in Figure 30.2 we would first create the class shown in Figure 30.3. During the execution of the paintComponent method, this class uses the graphics context Graphics to set the pen color to green and draw lines in the window. The coordinate system for drawing is relative to the upper-left corner of the Component. The tree starts drawing at pixel position (75,100) and each recursive call to the fractal method adds to the image.

Note that the first line of the paintComponent method is an invocation of super.paintComponent. This method definition overrides the definition of paintComponent in the superclass. However, that method definition already does things like paint the background of the component. Therefore, the first line of the new method is a call to the old method. After the background is painted, then the tree is painted on top.

²Recall that method overriding is when a subclass replaces a method definition with a definition of its own.

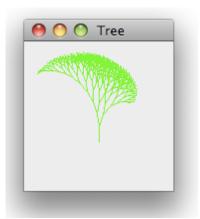


Figure 30.2: A fractal tree

In OCaml, to display a widget, we just needed to start the eventloop with the widget at the toplevel. In Java, to get things started we need to create a <code>JFrame</code>, a container that stores the toplevel <code>JComponent</code>. This frame corresponds to the window that your operating system uses to display GUI applications. The same Java code will produce different windows on different platforms because it uses the window drawing routines supported by that platform.

The run method below demonstrates this process. This method creates and displays the window containing the drawing defined above.

```
class DrawingApplication implements Runnable {
   public void run() {
      // a frame is a top-level window
      JFrame frame = new JFrame("Tree");
      // set the content of the window to be the drawing
      frame.add(new Drawing());
      // make sure the application exits when the frame closes
      frame.setDefaultCloseOperation(JFrame.EXIT_ON_CLOSE);
      // resize the frame based on the size of the canvas
      frame.pack();
      // show the frame
      frame.setVisible(true);
   }
}
```

The argument to the JFrame constructor is the name on the "title" of the window (usually shown at the top of the window by most operating

```
public class Drawing extends JComponent {
    /* This paint function draws a fractal tree
     * Google "L-systems" for more explanation / inspiration.
    private static void fractal (Graphics gc, int x, int y,
                                 double angle, double len) {
        if (len > 1) {
            double af = (angle * Math.PI) / 180.0;
            int nx = x + (int) (len * Math.cos(af));
            int ny = y + (int)(len * Math.sin(af));
            gc.drawLine(x, y, nx, ny);
            fractal (gc, nx, ny, angle + 20, len - 2);
            fractal(gc, nx, ny, angle - 10, len - 1);
        }
    }
    public void paintComponent (Graphics gc) {
        super.paintComponent(gc);
        // set the pen color to green
        gc.setColor(Color.GREEN);
        // draw a fractal tree
        fractal (gc, 75, 100, 270, 15);
    }
    // get the size of the drawing panel
    public Dimension getPreferredSize() {
        return new Dimension (150, 150);
    1
}
```

Figure 30.3: Source code for Figure 30.2.

systems.) The window shown in Figure 30.2 has the word "Tree" at the top. This line is where that is specified. The next line of the program instructs the frame that it should display a new instance of the Drawing class. Frames are containers, in that they hold a single JComponent, and this line determines the component that will be displayed in the frame. The next line instructs the frame what to do when the user clicks the close button on the window (on Mac OS, the red circle in the titlebar). The program doesn't end automatically when this happens unless we include this line in the code. After that, the frame must calculate how big it should be. The pack method performs this calculation automatically, using the getPreferredSize method of the component, and making sure that the frame is exactly big enough to contain the drawing panel.

Finally, although we have created the frame, it doesn't display until we tell it to show itself. This <code>setVisible</code> actually makes the frame appear on the screen. This frame can be interacted with using the standard windowing commands (move, resize, minimize, maximize, close) provided by the operating system. But it doesn't really do anything else.

We start a Swing application using the following main method. The static method <code>SwingUtilities.invokeLater</code> makes sure that the GUI starts correctly. Its argument must be something that implements the <code>Runnable</code> interface (which only requires the class to have a <code>run</code> method).

```
public class Main {
    public static void main(String[] args) {
        SwingUtilities.invokeLater(new DrawingApplication());
    }
}
```

30.2 User Interaction

Next, we show how to use reactive programming to develop applications that react to standard user input, such as mouse events and key presses. Our eventual goal will be to re-create something like the Paint program using Swing instead of our hand-rolled OCaml GUI.

However, before we do that, we will start with something much more modest. We will go back to the lightswitch demo that we used for OCaml (back in Figure 18.9) and rewrite it using the Swing libraries. Our first goal is the simple design problem:

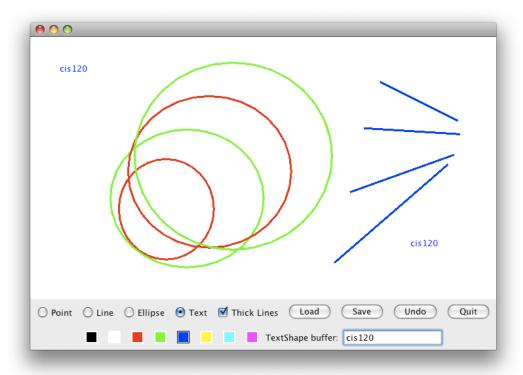


Figure 30.4: Java Paint

Program an application that displays a button. When the button is pressed, it toggles a lightbulb on and off.

To implement the lightswitch, we will first assemble the components and then add the interactivity. In this case, our application is composed of two different components, a button (labeled On/Off) and a section of the window that changes color from yellow to black. For the latter, we will create a component similar to the <code>Drawing</code> above. The difference is that this time the object will include a boolean field, called <code>ison</code>, that will determine whether to repaint itself yellow or black. If the value of <code>ison</code> is true, then the object will repaint itself with a yellow rectangle. Otherwise, it will use black. (Note that this time we omit the call to <code>super.paintComponent</code> because our painting completely fills the component. We don't need the background.)

The method flip changes the state of the lightbulb. If it is on, then it turns off and vice versa. However, there is one more important part

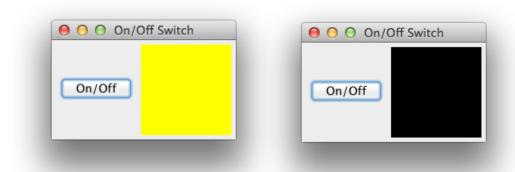


Figure 30.5: Java Lightbulb, both on and off states

to flip. The last line of the method, the call repaint, tells the swing event loop that this component should be redisplayed. Unlike the OCaml GUI library, which repaints every widget at every time step, the Swing library only repaints the components that indicated that they need to be repainted.

We can get this started as we did for the fractal tree drawing above. Again we create a frame and specify its title. However, this time we would like to add *two* components to the frame, a button and an instance of the Lightbulb class above. A frame can only contain one component, if we tried to add two of them, then only the most recently added component would be displayed.

Therefore, we need a *Container* component that can hold multiple components. The class <code>JPanel</code> is such a component. We create after creating an instance of this class, we can add both a button (created from the class <code>JButton</code>) and a lightbulb to the panel. (By default, these two components will appear side-by-side, as in a hpair.)

```
public class Lightbulb extends JComponent {
    private boolean isOn;
    public void paintComponent (Graphics gc) {
        if (isOn) {
            gc.setColor(Color.YELLOW);
            gc.fillRect(0, 0, 100, 100);
        } else {
            gc.setColor(Color.BLACK);
            gc.fillRect(0, 0, 100, 100);
    }
    public Dimension getPreferredSize() {
        return new Dimension(100, 100);
    public void flip() {
        isOn = !isOn;
        // In Swing you have to explicitly ask to repaint
        // a component. You should call repaint whenever
        // the display of the component changes.
        this.repaint();
```

Figure 30.6: The Lightbulb class

```
public class OnOff implements Runnable {
   public void run() {
      JFrame frame = new JFrame("On/Off Switch");

      JPanel panel = new JPanel();
      frame.add(panel);

      JButton button = new JButton("On/Off");
      panel.add(button);

      Lightbulb bulb = new Lightbulb();
      panel.add(bulb);

      frame.setDefaultCloseOperation(JFrame.EXIT_ON_CLOSE);
      frame.pack();
      frame.setVisible(true);
    }
}
```

However, although the code above will display the button and the lightbulb, it doesn't *do* anything. Pushing the button has no effect. That is because we haven't added an event handler to the button to *react* to button presses.

30.3 Action Listeners

In the OCaml GUI library, we used *notifiers* to handle events. These widgets maintained a list of higher-order functions that would execute in the case of an event.

The Swing library works in a similar manner. However, because Java lacks higher-order functions, the library uses objects instead. Any class that implements the ActionListener interface (see below) can be used to handle events that are triggered as the result of user actions. This interface is defined in the package <code>java.awt.event</code>.

In our lightswitch example, we would like to implement an ActionListener that changes the state of the lightbulb by calling its flip method. To do

this, we create a class that stores a reference to the lightbulb (using the private field bulb) and then, in the actionPerformed method, calls the flip method of the bulb object. The only other part of this class is a constructor that initializes the field.

```
class BulbSwitch implements ActionListener {
   private Lightbulb bulb;

public BulbSwitch(Lightbulb b0) {
     this.bulb = b0;
}

public void actionPerformed(ActionEvent e) {
     bulb.flip();
}
```

The final step is to "wire up" the button. In other words, we need to create an instance of the <code>BulbSwitch</code> class and tell the button to store this object as an action listener. We do this by adding the following line to the <code>main</code> method, after the <code>button</code> and <code>bulb</code> components have been created. The <code>addActionlListener</code> method of the <code>JButton</code> class adds its argument to the list of action listeners to the button. Whenever the button is pressed, the <code>actionPerformed</code> methods of all of the action listeners will be called.

```
// "wire up" the bulb to the button
button.addActionListener(new BulbSwitch(bulb));
```

30.4 Timer

Suppose we would like to implement a blinking light bulb, one that turns itself on and off without waiting for user input. To control this light bulb, we use a Timer object, as in the code below.

```
// Add a blinking light too
Lightbulb blinker = new Lightbulb();
panel.add(blinker);
// Create a timer that will call actionPerformed() on the
// given TimerAction object every second (1000ms)
    Timer timer = new Timer(1000, new BulbSwitch(blinker));
    timer.start();
```

The Timer constructor takes two arguments, an time interval (in milliseconds), and an ActionListener to run whenever the timer "goes off". The method start gets the timer started.

Note that both the Timer and the JButton can use the same ActionListener. We didn't have to change anything in the BulbSwitch class. This is a nice property of the Swing library design, it separates the description of what should happen (toggling a lightbulb) from the description of why it should happen (because the user pressed a button, or because a timer went off.)

In fact, even though in the example above, the button and timer control different bulbs, there is no reason that they can't control the same bulb—which bulb changes is specified by the argument of the BulbSwitch constructor. Likewise, a button or timer could control multiple bulbs, merely by adding additional action listeners.

Chapter 31

Swing: Layout and Drawing

31.1 Layout

A GUI application typically is composed of several components: buttons, canvases, checkboxes, textboxes etc. One challenge for the programmer is specifying how these components should be arranged on the screen in relation to each other.

In the OCaml GUI library, we used <code>vpair</code> and <code>hpair</code> to simply put widgets side-by-side, or on top of each other. By nesting these operations, we can lay out widgets in many different configurations. However, this work is tedious.

In Swing, we can use layout managers to more succinctly develop standard component arrangements. In this chapter, we demonstrate how to use a few of the layout managers. However, we don't intend to be comprehensive. For more information about various forms of layout see the Java Swing Tutorial "Lesson: Laying Out Components Within a Container" available at: http://docs.oracle.com/javase/tutorial/uiswing/layout/index.html.

In this section, we will demonstrate the effect of three different layout managers, used to assemble a graphical application. Our application in these examples just consists of five different buttons. These buttons won't do anything, we will just arrange them in different configurations.

The listing below includes the entire code of the application. The run method below creates a frame and five buttons. It also creates a container component, a <code>JPanel</code> to store the five buttons. The frame contains the

panel, and the panel contains the buttons.

```
public class LayoutExample implements Runnable {
    public void run() {
        JFrame frame = new JFrame ("LayoutExample");
        JButton b1 = new JButton("one");
        JButton b2 = new JButton("two");
        JButton b3 = new JButton("three");
        JButton b4 = new JButton("four");
        JButton b5 = new JButton("five");
        JPanel panel = new JPanel();
        frame.add(panel);
        panel.add(b1);
        panel.add(b2);
        panel.add(b3);
        panel.add(b4);
        panel.add(b5);
        frame.pack();
        frame.setDefaultCloseOperation(JFrame.EXIT_ON_CLOSE);
        frame.setVisible(true);
    public static void main(String[] args) {
        SwingUtilities.invokeLater(new LayoutExample());
```

The default layout for a JPanel is called FlowLayout. This layout means that all components added to the panel will be positioned in order left-to-right. If there is not enough width to fit all of the components, then the layout starts a new line of components. Within each line, all of the included components are centered on the line.

Because FlowLayout is the default layout, we do not have to do anything special to use this configuration. Furthermore, the JPanel does not fix its width, so the layout puts all of the buttons on a single line, and resizes the panel to fit around all of the buttons. The effect of this layout is shown on the left side of Figure 31.1. However, as the window (and panel) changes width, the buttons rearrange themselves. The "flow" so that they



Figure 31.1: FlowLayout before and after window resize

still fit into the narrower window, as in the right side of the figure.

The next layout we will demonstrate is the <code>GridLayout</code>. This layout puts the buttons into a grid configuration. Changing the application to use this layout merely requires adding the line

```
panel.setLayout (new GridLayout (3,2));
```

to run method right before all of the buttons are added to the panel. This command instructs the panel to divide itself into a grid containing three rows and two columns. The resulting window of buttons is shown in Figure 31.2.



Figure 31.2: GridLayout

No matter how this window is resized, it maintains this grid configuration. Furthermore, as the window is enlarged or shrunk, the buttons

resize themselves to always take one sixth of the size of the window.

The last layout that we will demonstrate is the border layout. This layout has exactly five positions, as demonstrated in Figure 31.3. The application can use this layout by first instructing the panel to use a BorderLayout, and then changing how the buttons are added to the panel. Each button must specify which position it should occupy. (Not all positions must be occupied in the border layout.)

```
panel.setLayout (new BorderLayout());
panel.add(b1,BorderLayout.LINE_START);
panel.add(b2,BorderLayout.CENTER);
panel.add(b3,BorderLayout.LINE_END);
panel.add(b4,BorderLayout.PAGE_START);
panel.add(b5,BorderLayout.PAGE_END);
```

As the window is resized, the button in the center position is resized to accommodate the new space. The components on the top and bottom retain their heights, but adjust their widths. The components on the left and right retain their widths, but adjust their heights.

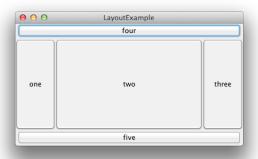


Figure 31.3: BorderLayout

31.2 An extended example

In the next section, we will go through a few variations of a simple graphical application. These variations will provide a bigger example of GUI layout, but also discuss design patterns for object-oriented programming.

To begin, let's consider the following application. The window looks like this:

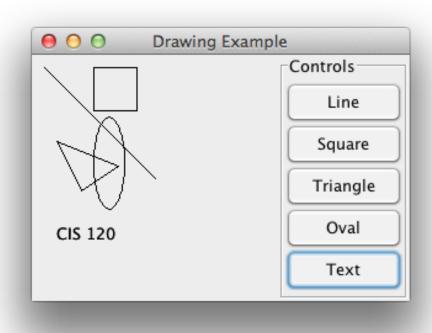


Figure 31.4: A Simple GUI Application

The idea behind this application is that it a *very* simplified paint program. The part of the window on the left is a canvas, and the right are the controls. Each button adds a new drawing at a fixed location to the canvas. Figure 31.4 shows the result after all of the buttons have been pressed.

Initial design

The first question is, what components should we use to build the interface? The drawing area to the left should be a component where we override the paintComponent method so that it displays the shapes. We'll design the class DrawingExampleCanvas to do that. For the buttons on the right, we can use the standard JButton class. As above, we will store references to these components in the fields of a class that uses a run method

to set up the interface.

Next we should think about how we layout such an application. As we change the size of the window, we would like the canvas to grow in size. This implies that we should use a BorderLayout for the top-level frame and insert the canvas in the center position. The buttons, on the right of the window, will need to be stored in their own *container* component, a JPanel, so that they can be inserted into the frame at the position JFrame.LINE_END. We would like to lay out the buttons vertically within the panel. Therefore we will use a GridLayout with 5 rows and a single column.

```
public void run() {
    JFrame frame = new JFrame("Drawing Example");
    // Create the buttons
    b1 = new JButton ("Line");
    b2 = new JButton ("Square");
    b3 = new JButton("Triangle");
    b4 = new JButton("Oval");
    b5 = new JButton ("Text");
    // canvas for displaying the shapes
    drawingCanvas = new DrawingExampleCanvas(this);
    // panel to contain the buttons
    JPanel eastPanel = new JPanel();
    eastPanel.setBorder(
       BorderFactory.createTitledBorder("Controls")
    );
    // layout the panel with a grid of 5 rows and 1 column
    // each grid cell will be the same size and the buttons
    // will expand to fill each cell
    eastPanel.setLayout (new GridLayout (5, 1));
    eastPanel.add(b1);
    eastPanel.add(b2);
    eastPanel.add(b3);
    eastPanel.add(b4);
    eastPanel.add(b5);
    frame.setLayout (new BorderLayout ());
    frame.add (drawingPanel, BorderLayout.CENTER);
    frame.add(eastPanel, BorderLayout.LINE_END);
    // Put it on the screen
    frame.pack();
    frame.setDefaultCloseOperation(JFrame.EXIT_ON_CLOSE);
    frame.setVisible(true);
```

Next, we should consider the interactions between the components. What sort of state should be shared between them? How will the DrawingExampleCanvas know what shapes to display? How will the buttons toggle that state?

For our first cut, we will add some boolean fields to the DrawingExample class to remember which buttons have been pushed. The idea is that can-

vas will look at these fields to determine which shapes to draw, and the buttons will set the appropriate one to true when pressed.

Note that we make these boolean fields public because they must be read and modified by other classes. The class for the <code>DrawingExampleCanvas</code> must read them to find out which shapes to display. To do this, it must also keep a reference (called <code>owner</code>) to the object that contains these boolean fields. (See the line above which creates the canvas—the constructor is invoked with the <code>this</code> reference.)

```
class DrawingExampleCanvas extends JComponent {
    // must include a reference to the "top-level"
    // application to be able to access its state.
    private DrawingExample owner;
    public DrawingExampleCanvas (DrawingExample p) {
        owner = p;
    // We override this method to perform our own custom drawing.
    public void paintComponent (Graphics gc) {
        super.paintComponent(gc);
        if (owner.drawLine) {
            // code for drawing lines
        if (owner.drawSquare) {
            // code for drawing squares
        if (owner.drawTriangle) {
            // code for drawing triangles
        if (owner.drawOval) {
            // code for drawing ovals
        if (owner.drawText) {
           // code for drawing text
    public Dimension getPreferredSize() {
        return new Dimension(200,200);
}
```

Finally, we need to add the action listeners to the buttons so that they modify the correct boolean value. We use the same listener for each button, and pass a reference to the button that the listener is associated with. When the button is pressed, we compare this reference to each of the buttons in the application to determine which shape to draw.

```
class DrawingExampleListener implements ActionListener {
   private DrawingExample owner;
   private JButton button;
    // Store a reference to our "owner object"
   public DrawingExampleListener (DrawingExample p,
                                  JButton b) {
        owner = p; button = b;
   public void actionPerformed(ActionEvent e) {
        // Find out which button generated the event, and
        // use this information to set the appropriate
        // flag in the owner object
        if (button.equals(owner.bl)) {
            owner.drawLine = true;
        } else if (button.equals(owner.b2)) {
            owner.drawSquare = true;
        } else if (button.equals(owner.b3)) {
            owner.drawTriangle = true;
        } else if (button.equals(owner.b4)) {
            owner.drawOval = true;
        } else if (button.equals(owner.b5)) {
            owner.drawText = true;
        // Notify Swing that the drawing panel needs
        // to be repainted
        owner.drawingCanvas.repaint();
    }
```

Again, because the execution of the actionPerformed method accesses the fields of the top-level object, the constructors for the DrawingExampleListener class must take in a reference to it.

In the run method, after the buttons are created, we add their action listeners with the following code.

```
// Attach actions to the buttons.
b1.addActionListener(new DrawingExampleOListener(this, b1));
b2.addActionListener(new DrawingExampleOListener(this, b2));
b3.addActionListener(new DrawingExampleOListener(this, b3));
b4.addActionListener(new DrawingExampleOListener(this, b4));
b5.addActionListener(new DrawingExampleOListener(this, b5));
```

Variant A: Using Dynamic Dispatch

The code above gets the job done and works correctly, but it is clumsy. In the next few subsections, we discuss how to refactor the code to improve the object-oriented style of its implementation. One problem with this implementation is the lack of encapsulation: we made the fields public in the top-level class so that they could be accessed by the helper class. (We could improve things with "package" scope, but as we will see, there are still better strategies.) Another problem concerns extensibility: if we wanted to add a new shape-drawing button, then what must we modify? We must not only add a new button, a new boolean field for that shape, but we must also modify the if statements in the methods paintComponent and actionPerformed to test this new boolean value.

In general, sequences of boolean tests, of the form

```
if (test1) {
   // do something
}
if (test2) {
   // do something
}
```

are not extensible. Instead, it is much better to refactor the application to avoid these if statements. In this section, we will demonstrate how to use *dynamic dispatch* to eliminate this sequence in paintComponent. In the next section, we will refactor the code again to remove the if statements in actionPerformed.

The code in the paintComponent class must display all of the shapes that have been selected by the buttons. This code dispatches on the boolean values to do the shape drawing, instead we would like to refactor the code so that instead of using a fixed set of boolean fields to remember which shapes to draw, we will use a mutable collection of shapes. In other words, we will replace the boolean fields with the single field:

```
public List<Shape> shapes = new LinkedList<Shape>();
```

That way we can refactor the paintComponent method to look like this:

```
public void paintComponent (Graphics gc) {
    super.paintComponent (gc);
    for (Shape shape : owner.shapes) {
        shape.draw(gc);
    }
}
```

Here, the toplevel applications uses the field shapes to store a collection of object that all implement the Shape interface. Because owner.shapes is a collection, we can use the "for-each" notation to iterate through each shape in the collection. Each shape knows how to draw itself, so that is what the paintComponent method does for each shape in the collection.

What is a shape? It is an object that knows how to draw itself. Therefore, we can create an interface that declares exactly this:

```
interface Shape {
  public void draw(Graphics gc);
}
```

and define various classes that implement that interface:

```
class Line implements Shape {
    public void draw(Graphics gc ) {
        gc.drawLine(10, 10, 100, 100);
    }
}
class Oval implements Shape {
    public void draw(Graphics gc ) {
        gc.drawOval(50, 50, 25, 75);
    }
}
```

Variant B: Refactoring references

Now there is one more change to finish out the first variation—we need to modify the actionPerformed method of the event listener to add shapes to the collection instead of modifying boolean values.

```
class DrawingExampleListener implements ActionListener {
    private DrawingExample owner;
    private JButton button;
    // Store a reference to our "owner object" and the button
    public DrawingExampleListener(DrawingExample p, JButton b) {
        owner = p; button = b;
    public void actionPerformed(ActionEvent e) {
        // Find out which button generated the event, and
        // use this information to set the appropriate flag in
        // the owner object
        if (button.equals(owner.b1)) {
            owner.shapes.add (new Line());
        } else if (button.equals(owner.b2)) {
            owner.shapes.add(new Square());
        } else if (button.equals(owner.b3)) {
            owner.shapes.add(new Triangle());
        } else if (button.equals(owner.b4)) {
            owner.shapes.add(new Oval());
        } else if (button.equals(owner.b5)) {
            owner.shapes.add(new Text());
        }
        // Notify Swing that the drawing panel needs
        // to be repainted
        owner.drawingCanvas.repaint();
    }
}
```

However, this code is still a series of if expressions! Like the original version of the paintComponent it is not automatically extensible. If we want to add more shapes, we have to modify this code.

However, our previous modification suggests a simple fix. Instead of remembering the button that was pressed to figure out which shape to add, ActionListener should just skip a step and remember the actual shape to add. In other words, we'll change the class definition to include a shape reference, which should be initialized by the constructor.

As an added bonus, we can avoid adding the same shape twice. We can test whether the collection already contains the shape before adding it.

```
class DrawingExampleListener implements ActionListener {
    private DrawingExample owner;
    private Shape shape;

    // Store a reference to our "owner object"
    public DrawingExampleListener(DrawingExample p, Shape s) {
        owner = p; shape = s;
    }

    public void actionPerformed(ActionEvent e) {
        if (!owner.shapes.contains(shape)) {
            owner.shapes.add(shape);
        }

        // Notify Swing that the drawing panel needs
        // to be repainted
        owner.drawingCanvas.repaint();
    }
}
```

Now, when we add the action listeners to the buttons, we need to merely create the appropriate shape for each button. Whenever the button is pressed, that shape will be added to the collection.

```
// Attach actions to the buttons.
b1.addActionListener(
   new DrawingExampleListener(this, new Line()));
b2.addActionListener(
   new DrawingExampleListener(this, new Square()));
b3.addActionListener(
   new DrawingExampleListener(this, new Triangle()));
b4.addActionListener(
   new DrawingExampleListener(this, new Oval()));
b5.addActionListener(
   new DrawingExampleListener(this, new Text()));
```

Variant C: Using a helper method

Now we can see that there is some redundancy in button creation. First the method calls the JButton constructor five times to create the buttons.

Then it calls the addActionListener five times to attach the action listeners to the buttons. The next refactoring we will do will be do create a helper method to factor out this repeated code.

The helper method should create a button and add its action listener. To do this, the method needs to know two things: the name of the button, and the shape that should be drawn when the button is pressed. Therefore we add the following method to the DrawingExample class.

```
// Create a new button, given the name of the shape and
// a shape object for drawing
private JButton makeButton(String name, Shape shape) {
    JButton b = new JButton(name);
    b.addActionListener(new DrawingExampleListener(this, shape));
    return b;
}
```

Now we can go back to the run method and replace the repeated code with calls to this method. Now the button creation code read succinctly:

```
// Create the buttons
JButton b1, b2, b3, b4, b5;
b1 = makeButton("Line", new Line());
b2 = makeButton("Square", new Square());
b3 = makeButton("Triangle", new Triangle());
b4 = makeButton("Oval", new Oval());
b5 = makeButton("Text", new Text());
```

This code is better because it is easier to read. Each button declares exactly what is important about it, compared to the other buttons. We know that all the buttons roughly do the same thing, because they are all created by the makeButton method. But we know that they differ in their name, and in the shape that they create.

Variant D: Inner Classes

These previous refactorings solved the problem of extensibility and code redundancy, but the encapsulation problem still remains. The canvas and the action listeners still need to access the fields of the <code>DrawingExample</code> object. Therefore, these fields are public.

Furthermore, these two classes are very related to the DrawingExample class. They don't include a lot of code (especially after the refactoring) and only make sense in conjunction. In this section, we will see how the Swing

feature of Inner classes can tie these classes together.

Basically, *Inner classes*¹ allow classes to contain each other. They are useful in situations where two objects require "deep access" to each other's internals. The basic idea is that we can define one class inside of another. The inner class can then refer to the fields of the outer class. As a result, instances of the inner class must be created using instances of the outer class.

For example, a cut down version of the drawing example stores the list of shapes in instances of the class <code>DrawingExample</code>, and displays them in instances of the class <code>DrawingCanvas</code>.

```
public class DrawingExample implements Runnable {
    public List<Shape> shapes = new LinkedList<Shape>();
    private DrawingPanel drawingPanel;
    public void run() {
        JFrame frame = new JFrame("Drawing Example");
        drawingPanel = new DrawingPanel(this);
    }
class DrawingCanvas extends JComponent {
    private DrawingExample owner;
    public DrawingCanvas (DrawingExample p) { owner = p; }
    public void paintComponent (Graphics gc) {
        super.paintComponent(gc);
        for (Shape s: owner.shapes) {
            s.draw(gc);
    }
}
```

Alternatively, we can make DrawingCanvas an *Inner class* of DrawingExample. Note below that the canvas class is defined inside the DrawingExample class.

¹Also called "dynamic nested classes."

Likewise, we can move the DrawingExampleListener class to be inside the DrawingExample class and eliminate its owner field.

Inner classes are a replacement for tangled workarounds like "owner" references (as in the drawing example). They help clarify the code: the solution with inner classes is easier to read. Furthermore, they better support encapsulation as there is no need to allow public access to instance variables of outer class.

For example, consider this definition, with outer class <code>Outer</code> and inner class <code>Inner</code>. The inner class constructor can refer to the field <code>outerVar</code>, even though it is a private field. That is because <code>Inner</code> itself is a part of <code>outer</code>. The full name of the inner class is actually <code>Outer.Inner</code>, which is the type of objects that this class creates.

```
public class Outer {
   private int outerVar;
   public Outer () {
      outerVar = 6;
   }
   public class Inner {
      private int innerVar;
      public Inner(int z) {
        innerVar = outerVar + z;
    }
}
```

Inner classes must be creating using instances of the outer classes. Even though the class name is Outer. Inner, we cannot create an instance of this class with

```
Outer.Inner inner = new Outer.Inner(3);
```

Usually, instances of the inner class will be created in the nonstatic methods of the outer class. This situation looks like normal object creation:

```
public Outer () {
        Inner b = new Inner ();
}
```

but it is not quite the same. Just like a field access x is different than a local variable and really short for this.x, the above code is short for using the current outer object to create a new inner one.

```
public Outer () {
        Inner b = this.new Inner ();
}
```

Outside the outer class, we need to specify what object to use to create instances of the inner class. For example, in some other file, we could first create an object a, and then use it to create an inner object b.

```
Outer a = new Outer();
Outer.Inner b = a.new Inner();
```

Variant E: Anonymous Inner Classes

For the last refactoring of the <code>DrawingExample</code> class, we will observe a few things about the inner classes that we defined above (<code>DrawingExampleListener</code> and <code>DrawingExampleCanvas</code>). Both of these classes are fairly short (now that we've made them inner classes), and both of them are used *only once* to create new objects. Given these two properties, it is annoying that we have to name these classes and define them far away from their single use. In deed, in OCaml we might just use an anonymous function as an event listener, and forgo a separate definition.

Anonymous Inner Classes are the closest Java feature to OCaml's anonymous higher-order functions. This feature will let us refactor the DrawingExample so that the code that gets run by the button can be defined at the same place where the button's action listener is installed.

We'll do this by revising the button creation helper method (which is the code that installs the action listeners for the button). Instead of new DrawingExampleListener(shape), we will inline the actual code for the DrawingExampleListener class right there. This code only defines the actionPerformed method, so we will defined that method in place.

```
// Create a new button, given the name of the shape and
// a shape object for drawing
private JButton createButton(String name, final Shape shape) {
   JButton b = new JButton(name);
   b.addActionListener(new ActionListener() {
        public void actionPerformed(ActionEvent e) {
        if (!shapes.contains(shape)) {
            shapes.add(shape);
        }
        drawingCanvas.repaint();
   }
   });
   return b;
}
```

Note that the class <code>DrawingExampleListener</code> goes away. With the definition above we can remove this class definition. Instead, we have an anonymous class—all we know about it is that it is an instance of the interface <code>ActionListener</code>. This is the one place in Java where we can put an interface name after the <code>new</code> keyword. The reason that we can do this is that we immediately satisfy that interface with the definition of the

actionPerformed method.

Note that this method definition is allowed to refer to the variable shape, which is a parameter to the createButton method. Java allows this reference only for final variables, those with values that cannot be mutated.

Anonymous Inner classes are a new expression form that defines a class and instantiates it (creating an object) all at once. The general format starts with the **new** keyword. However, after that comes either an interface or a class name, followed by the definition of perhaps multiple members for that class (i.e. fields and methods.)

```
new InterfaceOrClassName() {
    public void method1(int x) {
        // code for method1
    }
    public void method2(char y) {
        // code for method2
    }
}
```

Note that there is a limitation here: the anonymous class cannot define a constructor. Such classes rarely need them however, the scoping rules mean that the objects fields can be initialized using values in the current context. The static type of this expression is the interface or class that was used to create the object. This static type is a supertype of the object's dynamic class, however the object's dynamic class is *anonymous*, we didn't give it a name. Therefore, Java will not allow us to refer to it.

Why do we say that anonymous Java's inner classes are similar to OCaml's higher-order functions? Both of these features create anonymous structures. In Java we don't define the actual name of the class that constructs the object above, and in OCaml, we don't define a name for the function when we say fun (x:int) -> x + 1.

Furthermore, both of these language features create "delayed computation" that can be stored in a data structure and run later. For example, in Java these are commonly used in GUI programming for event listeners, while in OCaml, we used first-class functions for the same purpose. The computation is delayed because it only runs when the button is pressed, and could run once, many times, or not at all.

Finally, the scoping of these constructs is similar. Both sorts of computation can refer to variables in the current scope. In OCaml, all variables

are immutable, so OCaml first class functions could refer to any available variable. In Java, these methods can refer to only instance variables (fields, which are referenced through the immutable variable this) and variables marked final (which are also immutable).

Chapter 32

Swing: Interaction and Paint Demo

In this chapter we will use a larger example to demonstrate user interaction with Swing. In particular, we will go back to the paint program that we developed with the OCaml GUI library and reimplement it with Java's swing library. This application requires installing mouse listeners to interact with the drawing on the screen. It will also give us a chance to make some comparisons between the OCaml and Java languages, with respect to Object-Oriented programming.

32.1 Version A: Basic structure

The basic structure of the application is similar to the drawing example of the previous chapter. The top-level application contains the 'state' of the application, in this case the color for drawing (will only be black in this chapter) and the list of shapes that should be drawn. Shapes are drawn on the canvas, an area of the screen. Below the canvas is the *modeToolbar*, the section of the screen used to select the shape to be drawn. The run method of this application creates the GUI elements and lays them out in the window.

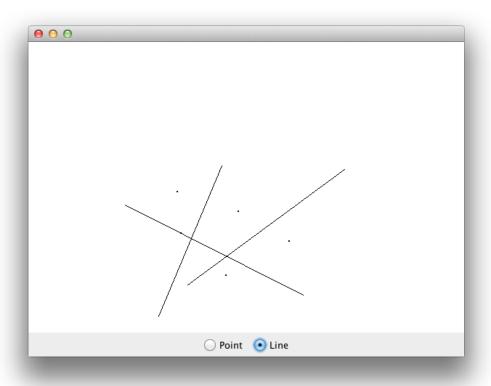


Figure 32.1: A Simple Paint Application

```
public class Paint implements Runnable {
    /** Area of the screen used for drawing */
    private Canvas canvas;

    /** Current drawing color */
    private Color color = Color.BLACK;

    /** The list of shapes that will be drawn on the canvas. */
    private List<Shape> shapes = new LinkedList<Shape>();
```

```
public void run () {

    JFrame frame = new JFrame();
    canvas = this.new Canvas();

    frame.setLayout(new BorderLayout());
    frame.add(canvas, BorderLayout.CENTER);
    frame.add(createModeToolbar(), BorderLayout.PAGE_END);

    frame.pack();
    frame.setDefaultCloseOperation(JFrame.EXIT_ON_CLOSE);
    frame.setVisible(true);
}

public static void main(String[] args){
    SwingUtilities.invokeLater(new Paint());
}
```

The code for the canvas, is almost identical to that of the previous chapter. As before, it is an inner class so that it can access the private fields of the top-level application. It also inherits from the <code>JPanel</code> class so that it can set the background color to be white in the constructor.

```
private class Canvas extends JComponent {

   public void paintComponent (Graphics gc) {
        super.paintComponent (gc);
        for (Shape s : shapes) {
            s.draw(gc);
        }

   public Dimension getPreferredSize() {
        return new Dimension(600,400);
   }

   public Canvas() {
        super();
        setBackground(Color.WHITE);
   }
}
```

The mode toolbar is created by an auxiliary method in the Paint class.

This method constructs a panel to store the controls. So far, the controls include two radio buttons (one for drawing shapes, one for drawing lines). Radio buttons are UI elements, where only one can be selected at a time. We could extend the application to include more shapes by adding more radio buttons to this toolbar.

```
private JPanel createModeToolbar() {

    JPanel modeToolbar = new JPanel();

    // Create the group of buttons that select the mode
    ButtonGroup group = new ButtonGroup();

    // create buttons for points and lines, and add them to the list
    JRadioButton point =
        makeShapeButton(group, modeToolbar, "Point");
    JRadioButton line =
        makeShapeButton(group, modeToolbar, "Line");
    // add more shapes here

    // start by selecting the buttons for points
    point.doClick();
    return modeToolbar;
}
```

The makeShapeButton method actually creates the radio buttons. The radio buttons must be added to both the toolbar panel and the ButtonGroup group. This button group controls which radio buttons are associated with one another. As one button is selected within the group, the others are deselected.

This method also adds an action listener to each button. This code runs whenever the button is selected. We use an anonymous inner class to define the action listener class inline. Currently the action listener does nothing.

32.2 Version B: Drawing Modes

Our first goal is to add some interaction to this application. In the example from the previous chapter, shapes were drawn at fixed positions by pressing buttons. Here we'd like to use the mouse to select the spots on the canvas to draw a number of points and lines.

In our first cut, we'll copy the implementation of the OCaml Paint program that we built in HW 6. In OCaml, we used a datatype to keep track of the current *mode* of the application. In Java, we can implement similar behavior with an <code>enum</code>. Below, we add the following two members to the <code>Paint</code> class—note that the enum is a nested class, and <code>mode</code> is a new field. We'll initialize this field with <code>Mode.PointMode</code> to record that we start drawing points.

```
public enum Mode {
    PointMode,
        LineStartMode,
        LineEndMode
    }

private Mode mode = Mode.PointMode;
```

Furthermore, we'll modify the action listener for the radio buttons so that when they are selected, they will change the mode. We can do this by adding an additional parameter to the makeShapeButton method. This parameter must be marked as final so that it may be referred to in the

actionPerformed method of the anonymous inner class.

```
private JRadioButton makeShapeButton (ButtonGroup group,
    JPanel modeToolbar, String name, final Mode buttonMode) {
    JRadioButton b = new JRadioButton (name);
    // ... add to button group and toolbar
    b.addActionListener(new ActionListener() {
        public void actionPerformed(ActionEvent e) {
            mode = buttonMode;
        }
    });
    return b;
}
```

When the radio buttons are created, we also need to specify their initial mode.

32.3 Version C: Basic Mouse Interaction

Now that the application can keep track of the drawing *mode*, we can set up the canvas so that it will respond to mouse clicks and movements. The behavior that we want is this: when we are in point mode, and the user clicks the mouse, we want to add a point at that particular location. When we are in LineStartMode and the user clicks the mouse, we want to remember where the user clicked and change the mode to LineEndMode. When we are in LineEndMode, we want to draw a line from the saved point to the point where the user clicked and revert back to LineStartMode.

We can implement this behavior with a mouse listener object that has methods for reacting to mouse behavior. The MouseListener interface describes the methods that such an event listener must include.

This interface includes several methods that run in response to mouse events such as mouse clicks, mouse button presses and mouse button releases. Because we only want to add a listener for mouse clicks, we can implement this interface by extending the MouseAdapter class. This class has "stub" methods for the required methods in the MouseListener interface. In our implementation, we will *override* only the mouseClicked method.

```
private class Mouse extends MouseAdapter
  implements MouseListener {
    /** Location of the mouse when it was last pressed. */
    private Point modePoint;
    @Override
            public void mouseClicked(MouseEvent arg0) {
        Point p = arg0.getPoint();
        switch (mode) {
        case PointMode:
            shapes.add (new PointShape (color, p));
            break:
        case LineStartMode:
            mode = Mode.LineEndMode;
            modePoint = p;
            break;
        case LineEndMode:
            shapes.add(new LineShape(color,p,modePoint));
            mode = Mode.LineStartMode;
            break;
        canvas.repaint();
}
```

After the canvas is created (in the run method) we can add the mouse listener so that it can react to mouse events.

```
canvas.addMouseListener(new Mouse()); // mouse clicked events
```

32.4 Version D: Drag and Drop

The interaction in the previous version was very primitive. What if we'd like to emulate the drag-and-drop behavior of the OCaml Paint program? We can do so by copying that implementation.

For drag-and-drop, we need to add a new field, called preview, that stores a preview shape, to the Paint class.

```
/** an optional shape for preview mode */
private Shape preview;
```

During the paintComponent method of the Canvas class, we also need to draw this shape, if it is non-null.

```
public void paintComponent(Graphics gc) {
    super.paintComponent(gc);
    if (shapes != null) {
        for (Shape s : shapes) {
            s.draw(gc);
        }
    }
    if (preview != null) {
        preview.draw(gc);
    }
}
```

Furthermore, we need to change how the canvas listens to mouse events, using the mouse class. Before, all the action was in the mouseClicked method. This time, we need to spread the action between several methods. We don't need to change the behavior for points too much, but for lines, we need to refine the behavior by overriding the mousePressed, mouseReleased and mouseDragged methods.

If the mode is LineStartMode, then when the mouse is pressed we need to save the location of the current click (in the field modePoint). We then switch modes to await dragging and the eventual end of the line (signaled by releasing the mouse button). Finally, we store the current location of the line

```
public void mousePressed(MouseEvent arg0) {
    Point p = arg0.getPoint();
    switch (mode) {
    case LineStartMode:
        mode = Mode.LineEndMode;
        modePoint = p;
        break;
    }
    canvas.repaint();
}
```

When the mouse is dragged, and we are in LineEndMode, we need to update the preview shape to reflect the current mouse position. As the mouse moves across the screen, the preview line will be continuously re-

drawn.

```
public void mouseDragged(MouseEvent arg0) {
   Point p = arg0.getPoint();
   switch (mode) {
    case LineEndMode:
        preview = new LineShape(color, modePoint, p);
        break;
   }
   canvas.repaint();
}
```

Only when the mouse is finally released do we add a new shape to the canvas. In this case we set the preview shape to null and switch back to LineStartMode to await a new shape.

```
public void mouseReleased(MouseEvent arg0) {
    Point p = arg0.getPoint();
    switch (mode) {
    case PointMode:
        shapes.add(new PointShape(color,p));
        break;
    case LineEndMode:
        mode = Mode.LineStartMode;
        shapes.add( new LineShape(color,modePoint, p));
        preview = null;
        break;
    }
    canvas.repaint();
}
```

32.5 Version E: Keyboard Interaction

In this next version of the paint program, we'd like to add the ability to control the program using the keyboard. In particular, we'd like to be able to switch between modes by pressing buttons. If the user presses the 'l' or 'L' button, the application should immediately switch to line mode (if it isn't there already). Likewise, if the user presses the 'p' or 'P' button, the application should switch to point drawing.

Giving a GUI component access to keyboard events requires that component to have the keyboard *focus*. There could be several different parts of the application that would like to react to key presses, but usually only

one should be reacting at a time. For example, if there are several text input areas in a window, only the selected one should display the typed text.

The component that we would like to add keyboard control to is the modeToolbar, the panel that contains the two radio buttons. We can add this functionality in the method that creates the component:

```
private JPanel createModeToolbar() {
    JPanel modeToolbar = new JPanel();
    // Create the group of buttons that select the mode
    ButtonGroup group = new ButtonGroup();
    // create buttons for points and lines,
    // and add them to the list
    final JRadioButton point =
        makeShapeButton(group, modeToolbar, "Point",
                        Mode.PointMode);
    final JRadioButton line =
        makeShapeButton(group, modeToolbar, "Line",
                        Mode.LineStartMode);
    // Add Keyboard control to application
   modeToolbar.setFocusable(true);
   modeToolbar.addKeyListener(new KeyAdapter() {
            public void keyTyped(KeyEvent arg0) {
                char c = arg0.getKeyChar();
                if (c == 'l' || c == 'L') {
                    line.doClick();
                } else if ( c == 'p' || c == 'P' ) {
                    point.doClick();
            }
        });
   modeToolbar.requestFocusInWindow();
    // start by selecting the buttons for points
   point.doClick();
    return modeToolbar;
}
```

Note that after the radio buttons are created, we have inserted new code to add keyboard control. This code code first sets the panel to be "focusable", i.e. able to receive the keyboard focus. It then adds a key

listener to the panel using an anonymous inner class. This anonymous class extends the KeyAdapter class and overrides the keyPressed method. When the panel has the focus and when a key is pressed on the keyboard, this method will be called.

The action of this method is to change the mode. We do that by forcing a click on the point and line radio buttons. We are faking button presses with these calls. Note that for the radio buttons to be accessible in the inner class, they must be declared to be **final** when they are initialized.

The last step is to actually request the keyboard focus, using the line <code>modeToolbar.requestFocusInWindow()</code>. No other component in the application will request the focus, so it will stay with the <code>modeToolbar</code>.

For more information about how to use key board control, see the Java tutorial: http://docs.oracle.com/javase/tutorial/uiswing/events/keylistener.html.

32.6 Interlude: Datatypes and enums vs. objects

How does our treatment of shape drawing in our current Java Paint example compare with the treatment in the OCaml GUI project?

In Java, we have

• An interface called Shape for drawable objects:

```
public interface Shape {
    public void draw(Graphics gc);
}
```

• Classes implement that interface (and describe how to draw themselves).

```
public class PointShape implements Shape { | }
public class LineShape implements Shape { | }
```

• A canvas that uses dynamic dispatch to draw the shapes

Alternatively, in the OCaml implementation, we had

A datatype that specifies variants of drawable objects

A Canvas that uses pattern matching to draw the shapes

The difference between these two versions is extensibility. The Java code can easily add more shapes by adding more classes. In the OCaml code, we add more shapes by adding more variants, and by modifying the repaint code in the canvas for drawing.

This example demonstrates the differences between using datatypes and objects. With datatypes, the focus is how the data is stored. It is easy to add more operations that work with the data, but harder to add more variants, or different types of data. Conversely, with objects, the focus is on how the data is used. It is east to add more variants (i.e. another class), but harder to add more operations to the interface, because all existing classes need to be modified.

Datatypes are better for situations where the structure of the data is fixed, such as in binary search trees. However, objects are better when the interface to the data is fixed, such as drawing shapes.

Returning to our paint example, we've used objects for storing the shapes, but we are still using variants for the drawing modes. That's not very extensible, as we add new shapes we'll have to add new drawing modes, and modify the mouse listener to react to those new modes. Can we do better?

32.7 Version F: OO-based Refactoring

In this section we will replace the enum for the drawing mode with a new definition that will be more extensible. It will require refactoring the code in several places, as well as a bit of indirection (or delegation) in the mouse listener.

Currently, the mouse listener uses a switch statement (on the current mode) to decide what code to execute. We would like to change that to use dynamic dispatch with the mode itself. In otherwords, we would like to modify the mouse listener so that the current mode determines the action in each situation.

```
private class Mouse extends MouseAdapter {
   public void mousePressed(MouseEvent arg0) {
        mode.mousePressed(arg0);
        canvas.repaint();
   }
   public void mouseDragged(MouseEvent arg0) {
        mode.mouseDragged(arg0);
        canvas.repaint();
   }
   public void mouseReleased(MouseEvent arg0) {
        mode.mouseReleased(arg0);
        canvas.repaint();
   }
}
```

What this implies is that *the mode is itself a mouse listener*. Therefore, we will change the definition of the mode type to reflect that:

```
interface Mode extends MouseListener, MouseMotionListener {
}
```

The various modes themselves (such as PointMode, LineStartMode, etc.) will be classes that implement the Mode interface. Because this interface requires that the class implement the mousePressed, mouseDragged and mouseReleased methods, the code above makes sense.

The advantage of this design means that we can think about the mouse reactions in each mode independently. For example, the PointMode class needs to only react to mouseReleased events. All other events are ignored in this mode.

```
class PointMode extends MouseAdapter implements Mode {
   public void mouseReleased(MouseEvent e) {
        Point p = e.getPoint();
        shapes.add(new PointShape(color,p));
    }
}
```

The line drawing modes work together, defined by the following pair of classes. The starting mode just switches the current mode to the ending mode, saving the current point by passing it as a constructor to the newly created mode.

The ending mode updates the preview field as the mouse is dragged (creating the line using the saved point in the mode as well as the current location of the mouse.) When the mouse is released, it switches the mode back to the starting mode, adds the new shape to the list of shapes to draw, and resets the preview field.

```
class LineStartMode extends MouseAdapter implements Mode {
   public void mousePressed(MouseEvent e) {
       mode = new LineEndMode(e.getPoint());
    }
}
class LineEndMode extends MouseAdapter implements Mode {
    Point modePoint;
    LineEndMode (Point p) { modePoint = p; }
    public void mouseDragged (MouseEvent arg0) {
        Point p = arg0.getPoint();
        preview = new LineShape(color, modePoint, p);
    public void mouseReleased(MouseEvent arg0) {
        mode = new LineStartMode ();
        Point p = arg0.getPoint();
        shapes.add( new LineShape(color, modePoint, p));
        preview = null;
    }
}
```

Compared to the previous version, the switching based on the mode is implicit. The mouse listener uses dynamic dispatch to figure out the correct reaction to mouse events.

As we add new shapes to this application, we can add new modes just by adding new classes. We don't need to modify any existing classes. Indeed, these classes are defined as inner classes of the Paint application for convenient access to the mode, shapes and preview fields. However, we could move these class definitions outside of the class as long as each mode had a way of accessing these components.

Chapter 33

Overriding and Equality

In this chapter we talk more about *method overriding*, the idea that a subclass can redefine a method that is already present in one of its ancestor classes. In the previous chapters, we have already seen an example where method overriding is important: subclasses of <code>JComponent</code> typically override the the <code>paintComponent</code> method to control how they are displayed on the screen. Here we both make the semantics of overriding precise by showing what it looks like in the abstract stack machine, and also discuss when and where method overriding is appropriate in Object-Oriented programming.

The former turns out to be trivial. Our ASM model for dynamic dispatch already explains what happens when methods are overridden—we don't need to add any new functionality to our model. However, the latter is a much deeper issue. Method overriding can make code confusing and difficult to reason about if not used carefully.

33.1 Method Overriding and the Java ASM

Consider the following Java class definitions.

```
public class C {
   public void printName() { System.out.println("I'm a C"); }
}

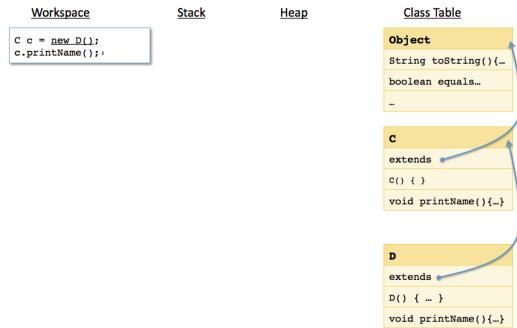
public class D extends C {
   public void printName() { System.out.println("I'm a D"); }
}
```

Now, when the following code is run, what is printed to the console? And why?

```
C c = new D();
c.printName();  // what gets printed?
```

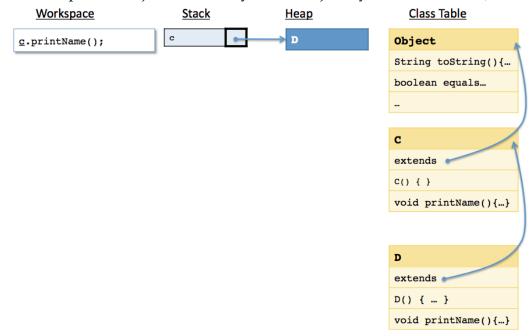
The result is that, even though the static class of c is C, dynamic dispatch means that the method definition in class D is the one that is selected. Therefore $I'm \ a \ D$ is the result printed in this example.

We can see how this works precisely by stepping through the execution of the ASM for this example. The ASM is initialized by putting the code snippet on the workspace, and the class definitions above in the Class Table.

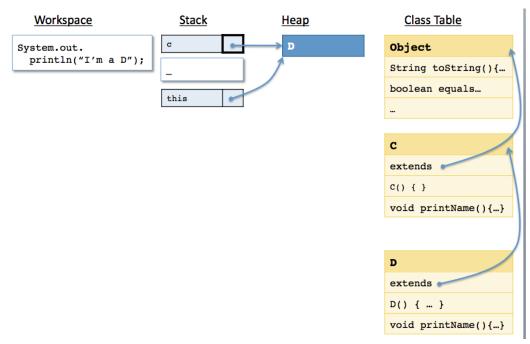


After executing the first line on the workspace, the stack contains the variable c which is the reference to some object, with dynamic class D,

stored on the heap. (Because the class D does not declare any instance variables, we represent objects created by this class just by their classname.)



Next, for the method call to the printName method, we look up the dynamic class of the object to find where to look in the class table for this method definition. After this method call, the body of this method is placed on the workspace and the saved workspace and this reference are pushed onto the stack.



Finally, after this code executes, the message I'm a D appears in the console. Because we started looking for the definition of the printName method in the class D, we found that version of the method to execute. Even though the C class also contains a definition of that method, we did not use it.

This behavior is true for all method invocations, even those for code defined in superclasses.

For example, consider these two classes:

```
class C {
  public void printName() {
    System.out.println("I'm a " + getName());
  }
  public String getName() {
    return "C";
  }
}

class E extends C {
  public String getName() {
    return "E";
  }
}

// in main
C c = new E();
c.printName();
// The string "I'm a E" is printed to the console
```

Above, the definition of the class E overrides the getName method. As a result, even though the printName method is defined in the class C, it calls the getName method defined in class E. This is because the dynamic class of the method determines every method invocation.

This behavior of dynamic dispatch can make reasoning about programs difficult. The class c may be written in a different library than the class E, and by different authors. The author of the c class must think about not just their own method implementations, but the implementations of any other subclass. There is no way for c to predict the result of getName. Instead, the author must define the expected properties (i.e. behavioral contract) of any overriding method, document it in the code, and hope that all subclasses respect that contract.

Sometimes overriding is the right thing to do, especially when the parent class is designed specifically to support such modifications, and the expected properties of the overridden methods is clearly defined by the super class. For example, the paintComponent method in the class JComponent is designed to be overridden, and the Swing documentation discusses what overriding methods should and should not do. In this case

the library designer will specifically provide a behavior contract that the parent methods assume about overridden methods.

As we will see, there are a few other methods in the Java libraries where overriding makes sense (and in fact, is necessary).

Another opportunity for overriding is if both parent and child class are controlled by the same author. As long as this author will maintain control of both parts as the software evolves, overriding *may* be ok.

However, there are usually better ways of structuring software that avoid overriding. For example, *composition* and *delegation* often achieve similar benefits with minor overheads and much less confusion about behavior. For further discussion about this topic, see Joshua Bloch's Item 16 in *Effective Java* [2]. In particular, this reference discusses how inheritance can break encapsulation.

Class authors can prevent subclasses from overridding their methods by using the final modifier. When applied to methods, the final modifier prevents subclasses from overriding that particular method. That way the class author can always reason about what happens during a method call—the final modifier means that a dynamic method invocation must be to an existing method.

33.2 Overriding and Equality

The equals method of the object class is an example of a method often should be overridden. To see why, consider this definition of a class that *does not* override the equals method:

```
public class Point {
    private final int x;
    private final int y;
    public Point(int x, int y) { this.x = x; this.y = y; }
    public int getX() { return x; }
    public int getY() { return y; }
}
```

Now, suppose we use this class with the linked lists defined in Java Collections framework.

```
// somewhere in main
List<Point> l = new LinkedList<Point>();
l.add(new Point(1,2));
System.out.println(l.contains(new Point(1,2)));
```

Unfortunately, even though we have added the point at position (1,2) to the list, the contains method returns *false*.

The reason is that in the linked list class, the contains method works in a way something like this:

```
public boolean contains(Object o) {
   if (o == null) {
      for (E e : this) {
        if (e==null) { return true; }
      }
   } else {
      for (E e : this) {
        if (o.equals(e)) { return true; }
      }
   }
   return false;
}
```

This code iterates over all of the elements in the linked list (using the for-each notation). If the argument is null, then the method returns true if any of the elements are null. Otherwise, if the argument is non-null, then the method returns true according to the equals method of the argument.

The point class above inherits the equals method of the <code>Object</code> class. This method returns true only for reference equality. In other words, it behaves as if we had said $\circ == e$. However, in the example above, we are comparing against an object with the same structure, but that object is not an alias to any of the other objects stored in the list.

To solve this problem we should override the equals method in the Point class.

33.2.1 When to override equals

In general, classes should override the equals method when they represent immutable values. For example, the point class above represents locations—there is not reason to distinguish locations with the same x and y coordinates, we really do want to identify all points that represent the

same location in the coordinate space.

Another example is the <code>string</code> class. Java's implementation of this class overrides the default equality with one that compares strings character-by-character. This behavior is often what we want anyways when we compare string, and the reason why we often say "use <code>.equals</code> when comparing strings."

Furthermore, the set implementation itself overrides the .equals method because there is a non-trivial definition of equality for sets. In particular, no matter how sets are represented (using arrays, binary trees or hash tables), two sets should be equal if and only if they contain equal elements. This definition even allows two sets with completely different representations to be determined equal (i.e. such as a TreeSet and a HashSet, for example). As long as these sets contain the same elements then .equals will return true.

As the example above demonstrates, it is particularly important to override equals when objects need to serve as elements of a set or keys in a map. In these cases, it is very unlikely that reference equality should be used to determine whether a set contains a particular value or the map contains a particular key. The mathematically inspired abstractions typically use the more mathematically inspired definition of structural equality.

33.2.2 How to override equals

The .equals method is one that is intended to be overridden. That means that the documentation of this method specifies a contract that all subclasses should satisfy. Specifically, the documentation states the following¹

The equals method implements an equivalence relation on non-null object references:

- It is reflexive: for any non-null reference value x, x.equals (x) should return true.
- It is symmetric: for any non-null reference values x and y, x.equals (y) should return true if and only if y.equals (x) returns true.

 $^{^1}$ This text is taken directly from: http://docs.oracle.com/javase/7/docs/api/java/lang/Object.html

- It is transitive: for any non-null reference values x, y, and z, if x.equals(y) returns true and y.equals(z) returns true, then x.equals(z) should return true.
- It is consistent: for any non-null reference values x and y, multiple invocations of x.equals(y) consistently return true or consistently return false, provided no information used in equals comparisons on the objects is modified.
- For any non-null reference value x, x.equals(null) should return false.

This contract is itself adapted from the mathematical concept of an equivalence relation.

So let's try to override equals for the Point class. Here's a first (incorrect) attempt. It seems like it should work, but there is something wrong with this definition. What is it?

There are two problems with this definition. The first is that it doesn't account for that point to be null. If the argument to the equals method is null, then this code throws a NullPointerException.

A more subtle issue with this code is that it actually doesn't *override* the equals method. Recall that the type of equals requires its argument to be an <code>Object</code>. Instead, it uses *overloading* to add an additional method to the <code>Point</code> class. The inherited <code>equals</code> method is still available, and Java uses the static type of an argument to determine which method to call.

For example, in the code below, the first invocation of equals is to the inherited method, so reference equality is used. The second invocation is to the overridden method from the point class above, which implements a structural equality.

```
Point p1 = new Point(1,2);
Point p2 = new Point(1,2);
Object o = p2;
System.out.println(p1.equals(o));
// prints false!
System.out.println(p1.equals(p2));
// prints true!
```

We can avoid unintentional overloading by using the <code>@override</code> annotation when we define the method in the <code>Point</code> class. In this case, if the types of the argument to the method are incorrect (i.e. if the method does not actually override an existing method in the superclass) then the compiler can issue a warning.

Furthermore, we can also prevent NullPointerExceptions. In the case that the argument is null we can immediately return false. We can only call the equals method for a non-null object, and null should never be equal to a non-null object. (This is the last part of the specification of equals.)

```
@Override
    public boolean equals(Object o) {
if (o == null) { return false; }
    // what do we do here???
}
```

However, because the type of the argument must be <code>Object</code>, we are a bit stuck. How do we access the \times and y components of the argument? How do we know whether the argument even has these components (i.e. is a <code>Point</code>)? We need some way to check the *dynamic* type of an object.

The **instanceof** operator tests the dynamic class of an object. If the dynamic class is a subtype of the provided class or interface, the test returns true.

For example, suppose we define the following variables.

```
Point p = new Point(1,2);
Object o1 = p;
Object o2 = "hello";
```

Then the expression

System.out.println(p instanceof Point);

prints true because p is a reference to a Point object stored on the heap. Similarly, the expression

```
System.out.println(o1 instanceof Point);
```

also prints true. Even though the static type of old is Object it is a reference to a Point object (in fact, it is an alias to the same object as above).

On the other hand, the expression

```
System.out.println(o2 instanceof Point);
```

prints false because o2 is a reference to a String object. Again, o1 and o2 have the same static type but give different results from the instanceof test.

Furthermore, the dynamic class could be a subtype of the queried class. This expression also returns true

```
System.out.println(p instanceof Object);
```

because Point is a subtype of Object. In fact, any reference to an object will return true for this test because all classes are subclasses of Object. On the other hand, the null reference

```
System.out.println(null instanceof Object);
```

is not an instance of any class, so this test prints false.

With <code>instanceof</code> we can add another line to our implementation of <code>equals</code>. We can make sure that the argument has a dynamic class that is compatible with this one. However at this point we are still stuck. The next thing that we would like to do in the method is compare the fields of this object with the fields of \circ . However, even though we know that \circ is a <code>Point</code> and so has fields x and y, its static type is <code>Object</code>. Java's type system will prevent us from accessing those fields from \circ .

```
@Override
  public boolean equals(Object o) {
    if (o == null) { return false; }
    if (!(o instanceof Point)) { return false; }
    // o is a Point - how do we treat it as such?
    ...
}
```

To finish out our implementation, we need one more piece: we need a *dynamic cast* to convert the static type of o from <code>Object</code> to <code>Point</code>. The expression (<code>Point</code>) o checks that o has dynamic class <code>Point</code>. If so, it returns the reference to that object (with the new type). Otherwise, it throws a

classCastException. In this case, because of the instanceof test, we know that this dynamic cast cannot throw the exception. But we can use it to create a new variable (called that) with a more precise type. With this new variable, we can make sure that both the x and y components of Point agree. If all of the tests succeed, we know that \circ is equal to the point that invoked the method.

```
@Override
public boolean equals(Object o) {
   if (o == null) { return false; }
   if (!(o instanceof Point)) { return false; }
        Point that = (Point) o;
   if (x != that.x) { return false; }
   if (y != that.y) { return false; }
        return true;
}
```

There is one last optimization that equals methods often use. They check to see if the argument happens to be an alias of this object (the one that invoked the equals method.) If this is true, the method can immediately return true. This initial check can eliminate the need for more expensive testing in certain cases, an especially valuable trade-off for large data structures.

```
@Override
public boolean equals(Object o) {
   if (this == o) { return true; }
   if (o == null) { return false; }
   if (!(o instanceof Point)) { return false; }
        Point that = (Point) o;
   if (x != that.x) { return false; }
   if (y != that.y) { return false; }
        return true;
}
```

The code above is a standard example of an equals method. Other classes that override equals should do so in a similar manner. In fact, Eclipse can and other Java IDEs can generate these methods automatically. (See the Source >> Generate hashCode() and equals() ... menu option.)

We need to use instanceof and the dynamic cast in the case of equals because the method behavior depends on the dynamic types of two objects: ol.equals(o2). However, use instanceof and dynamic casts judiciously in your code—usually dynamic dispatch works better.

For example, if you find yourself writing code that follows this pattern:

```
if (o instanceof Point) {
    Point p = (Point)o;
    // special case for points...
} else if (o instanceof Circle) {
    Circle c = (Circle)o;
    // special case for circles...
} else if (o instanceof Rectangle) {
    Rectangle r = (Rectangle) o;
    // special case for rectangles ...
} ...
```

consider refactoring your development so that dynamic dispatch is used to determine the special cases instead of the nested if-statements. The resulting code will be more extensible.

33.3 Equals and subtyping

The above recipe for equality works for simple class hierarchies, but the combination of subclassing and structural equality is much more subtle.

Suppose that we add a subclass of the Point class that adds a new field. We would also like to override equals in the subclass so that it too implements structural equality. Our first try at overriding equals in the ColoredPoint class might look like this:

```
public class ColoredPoint extends Point {
   private final int color;
   public ColoredPoint(int x, int y, int color) {
        super(x,y);
        this.color = color;
   }
   @Override
      public boolean equals(Object obj) {
        if (this == obj) { return true; }
        if (!super.equals(obj)) { return false; }
        if (!(obj instanceof ColoredPoint)) { return false; }
        ColoredPoint other = (ColoredPoint) obj;
        if (color != other.color) { return false; }
        return true;
    }
}
```

This method adapts the code above to the ColoredPoint class. It also uses the method call super.equals(obj) to compare the x and y components of the object.

Unfortunately, there is a problem with this definition. It doesn't satisfies all of the requirements of an implementation of equals. In particular, this method is not *symmetric* when a Point is compared with a ColoredPoint.

For example, consider the following declarations.

```
Point p = new Point (1,2);
ColoredPoint cp = new Colo
```

According to the implementation, the expression p.equals(cp) returns true, because a ColoredPoint is an instance of a Point. On the other hand, the expression cp.equals(p) returns false, because the reverse doesn't hold.

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