1. True or False (14 points)

Mark each statement as either true or false.

a. **T**  F  The typical compiler consists of several phases, including: lexing, parsing, transformation to an IR, optimization, and finally, code generation (in that order).

b. **T**  F  It is possible for a compiler optimization to improve the asymptotically improve the running time of a program (e.g. from $O(n^2)$ to $O(n)$.)

c. **T**  F  The regular expression $(a^*|b^*)^*$ recognizes the language of strings consisting of some number of $a$’s followed by the same number of $b$’s.

d. **T**  F  The LLVM is a “Static Single Assignment” IR, which means that all local identifiers (e.g. %1, %x, etc.) are allocated on the stack.

e. **T**  F  Other than the entry block, the order in which basic blocks appear within an LLVM function declaration does not affect the meaning of the program.

f. **T**  F  There are some X86lite programs that cannot be represented by well-formed LLVMlite control-flow graphs.

g. **T**  F  The linker and loader (as we saw in HW2) together determine the memory addresses represented by each label of the X86 assembly code.
2. Compilation and Intermediate Representations (24 points)

In this problem, we consider different ways to compile boolean expressions to a very simplified LLVM IR target. An OCaml representation of the LLVM subset we use is given in Appendix B.

The appendix also gives a datatype of boolean-valued expressions (repeated below), which will constitute the source language for the purposes of this problem:

```ocaml
type bexp =
  | Var of string
  | True
  | False
  | Not of bexp
  | And of bexp * bexp
  | Or of bexp * bexp
```

The usual way to compile such a boolean expression to an LLVM-like IR is to generate code that computes an answer, yielding the result in an operand. The function `compile_bexp_block`, given in the appendix does exactly that; it relies on the helper `compile_bexp` to do most of the hard work of “flattening” nested expressions into LL code. (Note that a source variable `Var x` is compiled to a LL uid `Id x`, which would be pretty-printed as `%x`.)

(a) (Multiple Choice, 3pts.) Which of the following is the (pretty-printed) LL code that is obtained by compiling the following example via `compile_bexp_block`?

```ocaml
let example : bexp = Not (Or (Var "a", And (Var "b", True)))
```

(i)  
%tmp2 = or i1 %a, %tmp1  
%tmp1 = and i1 %b, %tmp2  
%tmp0 = xor i1 false, %tmp1  
ret i1 %tmp0

(ii)  
%tmp0 = xor i1 false, %a  
%tmp1 = or i1 %b, %tmp0  
%tmp2 = and i1 %tmp1, true  
ret i1 %tmp2

(iii)  
%tmp2 = and i1 %b, true  
%tmp1 = or i1 %a, %tmp2  
%tmp0 = xor i1 false, %tmp1  
ret i1 %tmp0

(iv)  
%tmp0 = and i1 %a, true  
%tmp1 = or i1 %b, %tmp0  
%tmp2 = xor i1 false, %tmp1  
ret i1 %tmp2

(iii) is correct
**Conditional Statements** Suppose that we want to use `compile_bexp` as a subroutine for compiling conditional statements:

```
if (b) { stmt1 } else { stmt2 }
```

represented via the abstract syntax: `If(b, stmt1, stmt2)`.

Suppose `b` is `And(Var "x", huge)`, where huge is a long, complicated boolean expression. A compiler that uses the `compile_bexp` from the appendix would generate code for the `if` statement that looks like:

```plaintext
compile Stmt (If(b, stmt1, stmt2)) =

[...huge_code... %tmp0 = ...] ; could be very long (!)
tmp1 = and i1 %x, %tmp0 ; materialize b into tmp1 (!)
br i1 %tmp1, label %then, label %else ; branch on b's value (!)

%then:
[... stmt1 ...] ; code for stmt1

%else:
[... stmt2 ...] ; code for stmt2
```

Note that LL code above “materializes” the value of `b` into the operand `%tmp1` and then does a conditional branch to either the block labeled `%then` or the block labeled `%else`, as appropriate.

**Short Circuiting** We will now explore an alternate compilation strategy for boolean expressions that allows for “short-circuit” evaluation and is tailored for when the `bexp` is the guard of an `if-then-else` statement. In the example above, it is a waste of time to compute the whole boolean answer if `x` happens to be false—in that case, we know just by looking at `x` that we should jump immediately to the `%else` branch; there’s no need to compute `huge`.

This observation suggests that we can profit by creating a variant of `compile_bexp` called `compile_bexp_br` that, rather than computing a boolean value into an operand, instead takes in two labels (one for the “true” branch and one for the “false” branch) and emits code that jumps directly to the correct one, short circuiting the computation as soon as it’s clear which branch to take.

For example, consider the result of compiling the “huge” example above, where we supply the `then` and `else` labels:

```plaintext
let s : stream = compile_bexp_br (And(Var "x", huge)) "then" "else"
```

When we pretty-print `s` as a sequence of LL blocks, we get the following code, which can replace the lines marked (!) in the code at the top of this page.

```plaintext
br i1 %x, label %lbl1, label %else ; if %x is false, jump to %else
%lbl1:  
[...stream for huge...]
```

Note that the compiler generated the intermediate label `%lbl1`, which marks the start of the huge code block. The stream for huge will contain terminators that branch to `%then` or `%else` as appropriate. Remarkably, this compilation strategy will never need to emit instructions! A boolean expression can be completely compiled into a series of labels and terminators (branches or conditional branches).

(There are no questions on this page.)
(Multiple Choice, 3pts. each) It is not too hard to work out what `compile_bexp_br` should do by translating some small examples by hand. Mark the code that is a correct (pretty-printed) output for each call to `compile_bexp_br`. There is only one correct answer for each case.

(c) `compile_bexp_br (Not(Var "a"))"then""else" = ?

(i)  
```plaintext
br i1 %a, label %then, label %else
```

(ii)  
```plaintext
br i1 %a, label %else, label %then
```

(iii)  
```plaintext
br i1 %a, label %else, label %lbl0
```

(iv)  
```plaintext
br i1 %a, label %then, label %lbl0
```

lbs0:
```plaintext
br i1 %b, label %else
```

(ii) is correct

(d) `compile_bexp_br (Or(Var "a", Var "b"))"then""else" = ?

(i)  
```plaintext
br i1 %a, label %lbl0, label %else
```

(ii)  
```plaintext
br i1 %a, label %then, label %lbl0
```

lbs0:
```plaintext
br i1 %b, label %then, label %else
```

(iii)  
```plaintext
br i1 %a, label %else, label %lbl0
```

(iv)  
```plaintext
br i1 %a, label %then, label %lbl0
```

lbs0:
```plaintext
br i1 %b, label %then, label %else
```

(ii) and (iv) are correct [they were accidentally made the same]

(e) `compile_bexp_br (And(Not(Var "a"), Var "b"))"then""else" = ?

(i)  
```plaintext
br i1 %a, label %lbl0, label %else
```

(ii)  
```plaintext
br i1 %a, label %then, label %lbl0
```

lbs0:
```plaintext
br i1 %b, label %then, label %else
```

(iii)  
```plaintext
br i1 %a, label %else, label %lbl0
```

(iv)  
```plaintext
br i1 %a, label %then, label %lbl0
```

lbs0:
```plaintext
br i1 %b, label %then, label %else
```

(iii) is correct
(c) (12 points) Complete the implementation of `compile_bexp_br` below by filling in each blank with the correct `terminator` (for the first two blanks) or the correct `label` (for the remaining blanks) to implement the short-circuiting code generator. Note that the `And` and `Or` cases introduce a new `lmid` label, which labels the start of the second subexpression. We have done the `True` case for you.

```ocaml
type elt =
  | I of LL.uid * LLinsn
  | T of LL.terminator
  | L of LL.lbl

type stream = elt list

let rec compile_bexp_br (b : bexp ) ( ltrue : LL.lbl) ( lfalse : LL.lbl) : stream =
begin match b with
  | True -> LL.[T (Br ltrue)]
  | False -> LL.[T (Br lfalse)]
  | Var s -> LL.[T (Cbr ((Id s), ltrue, lfalse))]
  | Not c -> compile_bexp_br c lfalse ltrue
  | And (b1, b2) ->
    let lmid = mk_tmp "lbl" in
    let p1 = compile_bexp_br b1 lmid lfalse in
    let p2 = compile_bexp_br b2 ltrue lfalse in
    p1 @ LL.[L lmid] @ p2
  | Or (b1, b2) ->
    let lmid = mk_tmp "lbl" in
    let p1 = compile_bexp_br b1 ltrue lmid in
    let p2 = compile_bexp_br b2 ltrue lfalse in
    p1 @ LL.[L lmid] @ p2
end
```
3. LLVM IR: Structured Data and Getelementptr (21 points)

Consider the following C structured datatypes and global variables array and node. RGB is a record with three fields and Node is a linked-list node that contains an in-lined RGB value.

```c
struct RGB { int64_t r; int64_t g; int64_t b; }
struct Node { struct RGB rgb; struct Node* next; }
```

```c
struct RGB array[] = {{255, 0, 0}, {0, 255, 0}};
struct Node node;
```

These program can be represented in LLVM as the following definitions:

```llvm
% RGB = type { i64, i64, i64 }
%Node = type { %RGB, %Node* }
```

```llvm
@array = global [2 x %RGB] [%RGB {i64 255, i64 0, i64 0}, %RGB {i64 0, i64 255, i64 0}]
@node = global %Node ...
```

(Multiple Choice, 2 pts. each) For each LLVM instruction below, mark the corresponding C expression (i.e. such that a subsequent load from %ptr would get the value of the expression).

a. %ptr = getelementptr %Node, %Node* @node, i32 0, i32 1

- [ ] node
- [ ] node.rgb
- [x] node.next
- [ ] node.next.rgb

b. %ptr = getelementptr [2 x %RGB], [2 x %RGB]* @array, i64 1, i64 0, i32 1

- [ ] array[1][0][1]
- [ ] array[1].r
- [x] array[1].g
- [ ] array[1].b

c. %ptr = getelementptr %Node, %Node* @node, i32 0, i32 0, i32 2

- [ ] node.rgb[2]
- [x] node.rgb.b
- [ ] node[2].rgb
- [ ] node.next.rgb
Suppose that you wanted to compile an OCaml-like language into the LLVM IR. One issue is how to represent OCaml-style “algebraic datatypes”. Complete the following questions which prompt you to think about a strategy for representing the following OCaml type at the LLVM IR-level. (For the purposes of this question, ignore the fact that OCaml supports generic datatypes.)

\[
\text{type } d = \\
\quad | \text{B} \\
\quad | \text{C of int64} \\
\quad | \text{D of } d \times d
\]

d. (5 points) An OCaml value of type \(d\) consists of a “tag” (e.g. B, C, or D) and some associated data values (either an int64 or a pair of references to \(d\) values). Write down a (small) number of LLVM datatypes (including at least one for \(d\)), that can together be used to represent values of type \(d\). Briefly justify your representation strategy.

**Answer:** One possibility is to represent a value of type \(d\) as (a pointer to) a structure containing an integer *tag* plus space for two 64-bit values. The value of the tag determines the contents of the rest of the structure: e.g. if the tag is 0 then the value is B and the payload values are undefined. If the tag is 1 then the value is C and the payload the first 64-bits of the payload are treated as an \(i64\) value. If the tag is 2 then the value is D and the payload is two pointers to \(d\) values.

A minimal possibility is: \%d = \text{type } \{i64, \{i64, i64\}\}

Another possibility is something like the following:

\%d = \text{type } \{ i64, \text{payloadD}\* \}
\%payloadD = \text{type } \{ \%d*, \%d* \}

Where the i64* second field is either a pointer to the D payload or cast to an i64 value for the C payload.

Answers like \{i64, i64, \{i64*, i64*\}\} that “inlined” all the possible data in all constructors received 1 point off because they don’t scale well to datatypes that have many constructors, each carrying different data (e.g. an abstract syntax tree datatype).

e. (5 points) An LLVM program that constructs the representation of the OCaml value \(D(B, C(341))\) as a stack-allocated object would need to use *alloca* (to allocate storage space), *getelementptr* (to compute struct offsets), and *store* (to write values into memory). It would also have to use the *bitcast* instruction (which, if you recall, converts one pointer type to any other pointer type). Briefly explain why.

**Answer:** The value we want to construct is a pointer to the record that looks like:

\{i64 2, \{\%d* \%bptr, \%d* \%cptr\}\}

Here, \%bptr is a pointer to a stack-allocated struct \{i64 0, \{\%d* undef, \%d* undef\}\} and \%cptr is a pointer to a stack-allocated struct \{i64 1, \{i64 341, \%d* undef\}\}. Note that the types of the data stored in the records disagree. This means that to construct and manipulate such values, the pointers will have to be bitcast. For instance, to write the value i64 341 into the first element of inner struct, we use getelementptr with the %d* value, to obtain a %d** pointer, and then bitcast that pointer to have type i64* so that we can perform the store.

Other representation choices might require different casts to reconcile the types. Fully “inlined” representations don’t require casts, so no points were taken off here if the answer to part (d) was fully inlined.
f. (5 points) In English and pseudocode, briefly explain what code you would expect to generate when compiling the following code, assuming that the variable \( x \) of type \( d \) is compiled according to the representation type you explained above.

```ml
let rec sum (x:d) =
    match x with
    | B -> 0
    | C y -> y
    | D (d1, d2) -> (sum d1) + (sum d2)
```

Answer: The invariant is to represent values of type \( d \) as pointers to values of LLVM type \( %d \). Therefore, to compile this pattern match, we need to:

- use `getelementptr` to get the address of the tag component of the \( %d \) structure
- load the tag
- if the tag is 0 branch to the “B” case
- if the tag is 1 load the \( i64 \) value into the operand corresponding to \( y \) and branch to the “C” case
- if the tag is 2 load the two \( %d* \) values into the operands corresponding to \( cdd1 \) and \( d2 \) and branch to the “D” case.

Note that we will have to extend the local environment in the “C” and “D” branches to keep track of the fact that the variables have new bindings.
4. **X86 Assembly and C calling conventions** (17 points)

Recall that according to the x86-64 calling conventions that we have been using, the first argument to a function is passed in register %rdi and %rbp is a callee-save register and %rsp is caller-save. In X86lite syntax, the source operand comes before the destination, as in movq src, dest.

For this problem, consider the small C program and the accompanying X86 assembly code shown in Appendix B. The C code provides a print_i64 function that prints its 64-bit value to the terminal. The main calls the function foo, which is implemented purely in assembly code as shown in foo.s When these two files are compiled together, the resulting executable will print six numbers to the terminal.

(Multiple Choice, 3pts. each). There is only one correct answer for each case. Note that we have written small numbers in decimal and large numbers in hexidecimal.

Suppose that the first number printed to the terminal is 0x7fff5dd00990 (written in hexidecimal), which can be interpreted as a machine address. What will be printed by each of the five subsequent calls to print_i64?

**a.**
- 17 0x7fff5dd00990
- 42 0x7fff5dd00988 (i.e. 0x7fff5dd00990 - 8)
- 341 0x7fff5dd00980 (i.e. 0x7fff5dd00990 - 16)

**b.**
- 17 0x7fff5dd00990
- 42 0x7fff5dd00988 (i.e. 0x7fff5dd00990 - 8)
- 341 0x7fff5dd00980 (i.e. 0x7fff5dd00990 - 16)

**c.**
- 17 0x7fff5dd00990
- 42 0x7fff5dd00988 (i.e. 0x7fff5dd00990 - 8)
- 341 0x7fff5dd00980 (i.e. 0x7fff5dd00990 - 16)

**d.**
- 17 0x7fff5dd00990
- 42 0x7fff5dd00988 (i.e. 0x7fff5dd00990 - 8)
- 341 0x7fff5dd00980 (i.e. 0x7fff5dd00990 - 16)

**e.**
- 17 0x7fff5dd00990
- 42 0x7fff5dd00988 (i.e. 0x7fff5dd00990 - 8)
- 341 0x7fff5dd00980 (i.e. 0x7fff5dd00990 - 16)

**f.** (2 pts.) Briefly explain what will happen if you delete lines 27 and 28 of foo.s, recompile, and then run the resulting executable.

The program will still print the same values but it will crash when it tries to do the retq, since the top of the stack is not a good return address.
5. Lexing, Parsing, and Grammars (14 points)

a. Consider the following unambiguous context-free grammar over the symbols a and b that accepts palindromes—strings that read the same forward and backward. For example, a, bab, and aabaa are all accepted by this grammar, whereas ab, aab, and baaaba are not.

\[
P ::= \epsilon \mid a \mid b \mid aPa \mid bPb
\]

i. (Yes or No) Is this grammar deterministically parsable by an LL(k) parser (for some k)? Briefly explain.
No, there is no way for a left-to-right scanning parser to decide where the “middle” of the palindrome is. That is, a and aa and aaa could always be followed by an equal number of b’s, but determining which case applies cannot be done with any finite amount of lookahead.

ii. (Yes or No) Is this grammar deterministically parsable by an LR(k) parser (for some k)? Briefly explain.
No, there is no way for a left-to-right scanning parser to decide where the “middle” of the palindrome is. That is, a and aa and aaa could always be followed by an equal number of b’s, but determining which case applies cannot be done with any finite amount of lookahead.
b. Consider the following unambiguous context-free grammar over the symbols a and b that accepts balanced strings in which every a is followed by a matching b. For example, ab, aabb, and aababb are all accepted, but ba, a, and aab are not.

\[ Q ::= \]
\[ \epsilon \]
\[ QaQb \]

i. (Yes or No) Is this grammar deterministically parsable by an LL(k) parser (for some k)? Briefly explain.

No, this grammar is left-recursive which can never be parsed by a LL parser.

ii. (Yes or No) Is this grammar deterministically parsable by an LR(k) parser (for some k)? Briefly explain.

Yes.

c. (6 points) The following ambiguous grammar of mathematical expressions includes infix binary multiplication * and exponentiation operators ^ as well as tokens representing variables (ranged over by x).

\[ E ::= \]
\[ x \]
\[ E \ast E \]
\[ E \hat{\ast} E \]

Write down a disambiguated grammar that accepts the same set of strings, but makes multiplication left associative, exponentiation right associative, and gives exponentiation higher precedence than multiplication. For example, the token sequence x * y ^ z ^ w * v * u would be parsed as though it had parentheses inserted like: (x * (y ^ (z ^ w)) * v) * u.

\[ E_0 ::= \]
\[ E_0 \ast E_1 \]
\[ E_1 \]
\[ E_1 ::= \]
\[ E_2 \hat{\ast} E_1 \]
\[ E_2 \]
\[ E_2 ::= \]
\[ x \]