

Evaluating ML

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Probability vs loss

Confusion matrix: TP/TN/FP/FN

Precision, Recall, Sensitivity, Specificity

ROC curves

What is Netflix trying to do?



?



Top



Loss functions come from decision making

- ◆ We often optimize a loss function which is a surrogate for our true loss function
- ◆ Don't confuse *probability* or *score* with loss
 - One can optimize a model for probability and then use the probability in a decision rule
 - Or just directly optimize the loss resulting from a decision rule

Regression loss function

- ◆ **For a linear regression predicting dollar amounts (e.g., income, housing prices)**
 - What is the loss function being optimized for?
 - What is the residual plot likely to look like?
- ◆ **Does this meet the assumptions of the linear regression model?**
 - If not, how could you fix it?

Precision, Recall, Sensitivity, Specificity and ROC curves

Have you seen ROC curves?

- A) Yes
- B) No



Ways to be right or wrong

Claim\Is	True Yes	True No
Classify Yes	True Positive	False Positive
Classify No	False Negative	True Negative

$$\text{Accuracy} = (TP + TN) / (TP + FP + FN + TN)$$

Measuring Performance

◆ Accuracy (symmetric)

- % correctly classified

◆ Asymmetric measures

- Precision

- $P(\text{yes} \mid \text{predicted as yes})$

- Recall (or Sensitivity)

- $P(\text{predicted as yes} \mid \text{yes})$

- Specificity

- $P(\text{predicted as no} \mid \text{no})$

Precision/Recall Sensitivity/Specificity

Claim\Is	True Yes	True No	
Classify Yes	True Positive	False Positive	
Classify No	False Negative	True Negative	

- **Precision**
 - $P(\text{yes} \mid \text{predicted as yes}) = \text{TP}/(\text{TP}+\text{FP})$
- **Recall (or Sensitivity)**
 - $P(\text{predicted as yes} \mid \text{yes}) = \text{TP}/(\text{TP}+\text{FN})$
- **Specificity**
 - $P(\text{predicted as no} \mid \text{no}) = \text{TN}/(\text{TN}+\text{FP})$

Precision/Recall Example

Claim\Is	True Good	True Not Good	
Classify "Good"	70	50	
Classify "Not good"	30	350	
			500

- **Precision**
 - $P(\text{good} \mid \text{predicted as good}) = 70/(70+50)$
- **Recall (or Sensitivity) = True Positive Rate (TPR)**
 - $P(\text{predicted as good} \mid \text{good}) = 70/(70+30)$
- **Specificity = 1 – (False Positive Rate)**
 - $P(\text{predicted as bad} \mid \text{bad}) = 350/(350+50)$

F1 combines Precision and Recall

Claim\Is	True Yes	True No	
Classify Yes	True Positive	False Positive	
Classify No	False Negative	True Negative	

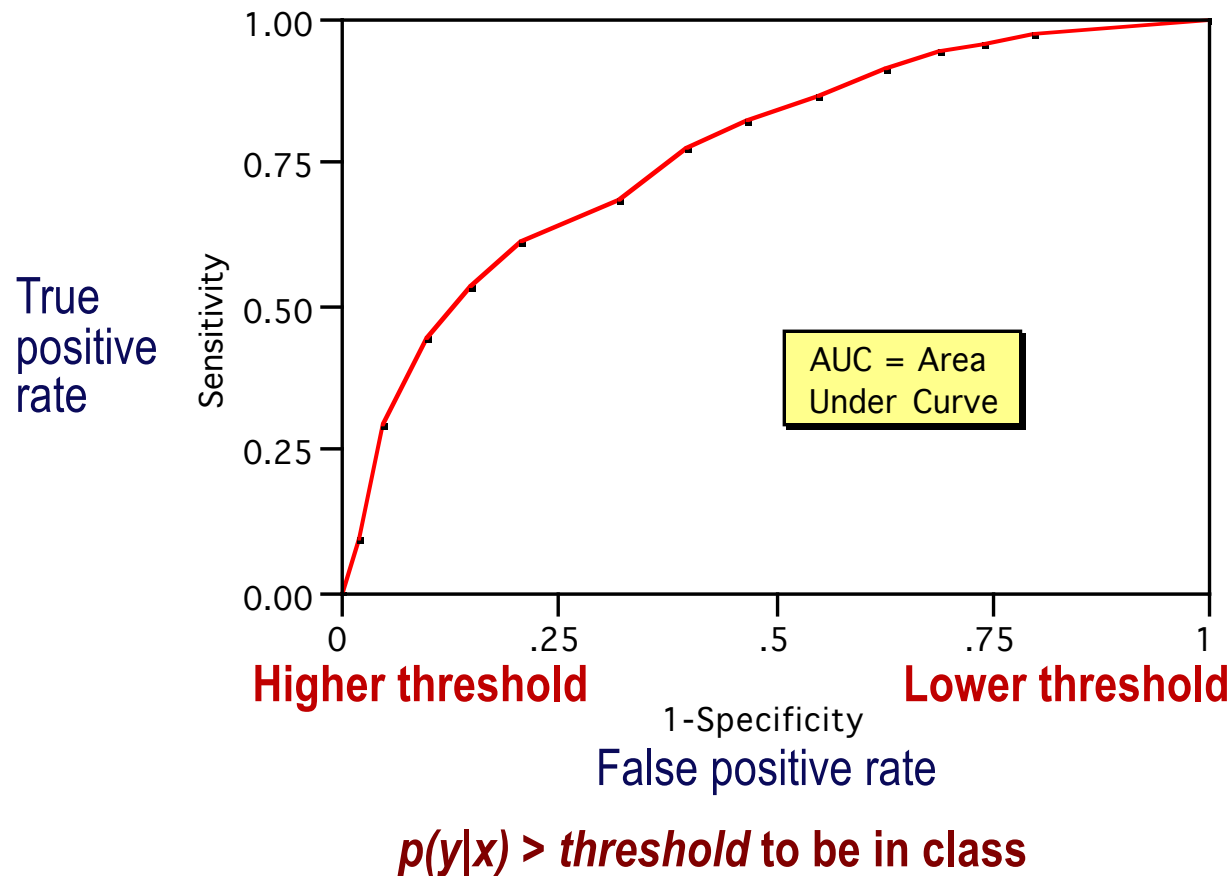
- **Precision**
 - $TP/(TP+FP)$
- **Recall**
 - $TP/(TP+FN)$
- **F1**
 - $2 \text{ precision} * \text{recall} / (\text{precision} + \text{recall})$

ROC (Receiver Operating Characteristic) Curve

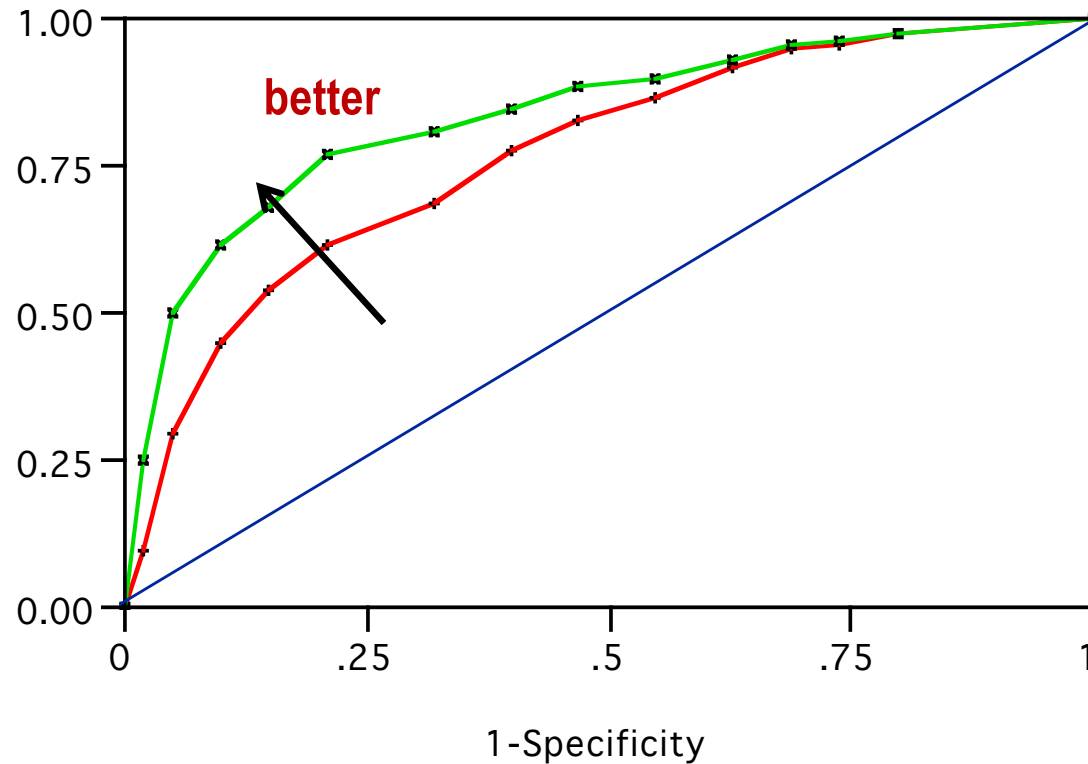
- ◆ Sort all examples from highest probability (or score) of being 'yes', $p(y='yes'|\mathbf{x})$, to lowest
- ◆ Sweep the threshold for predicting an example to be labeled 'yes' from 1 down to 0
 - This varies *specificity* from 1 to 0.
- ◆ At each threshold compute the *sensitivity*
 - i.e., the fraction of the true positives you found
- ◆ Plot the curve

https://en.wikipedia.org/wiki/Receiver_operating_characteristic

ROC Chart Varies Threshold



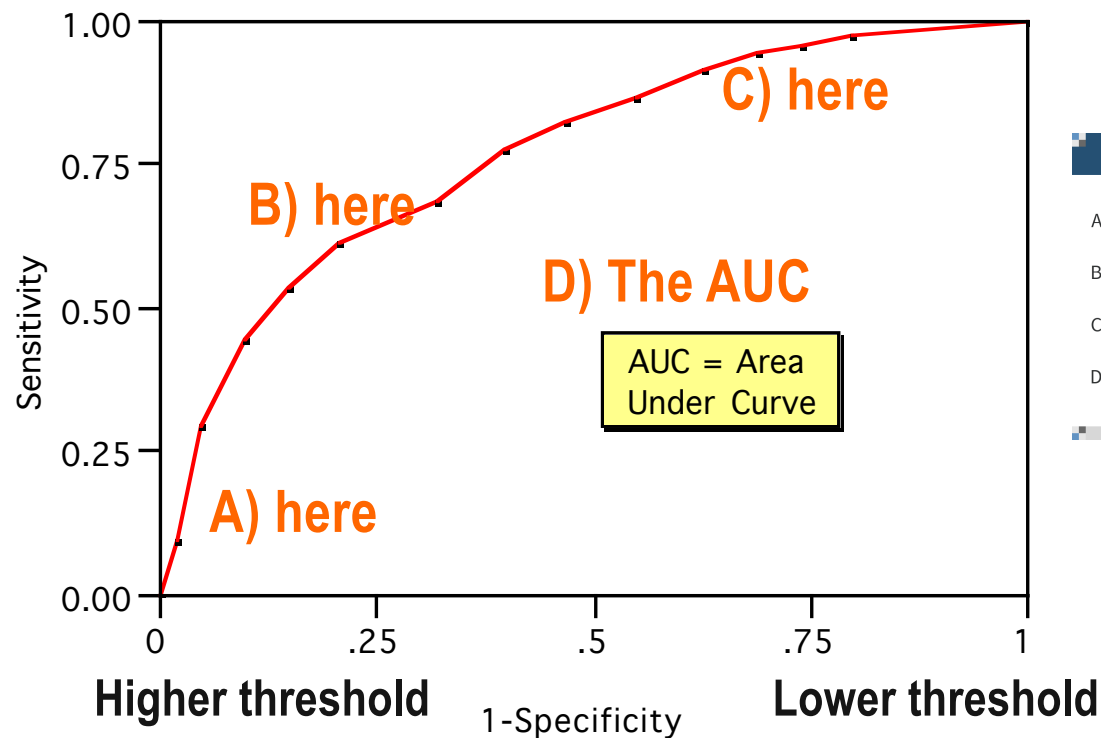
ROC charts support comparison



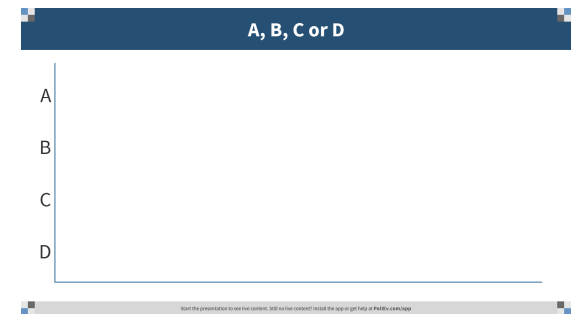
***AUC = 0.5 is random guessing
AUC = 1.0 is perfection***

**AUC = Area Under
the Curve**

Where does google care about?



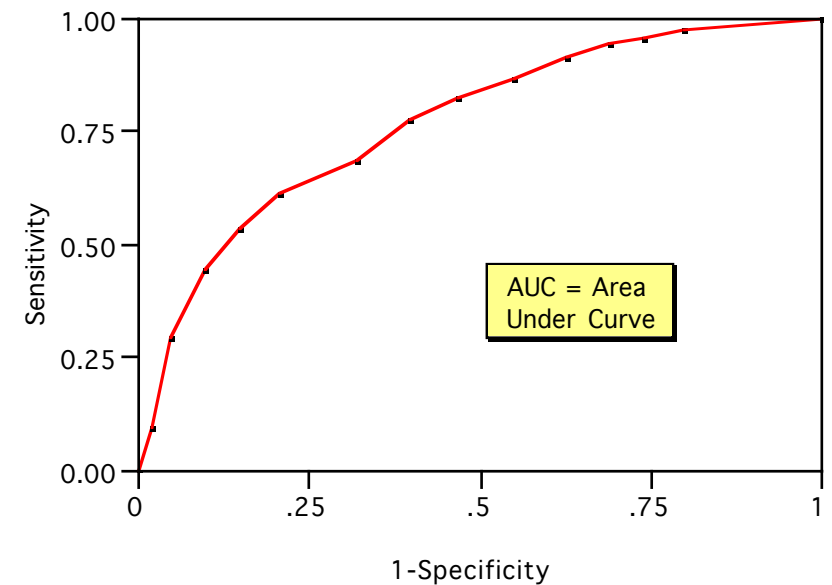
$p(y|x) > \text{threshold}$ to be in class



◆ Which method is most likely to be better for generating an ROC curve?

A) Logistic regression

B) SVM



		The Truth		
		Has the disease	Does not have the disease	
Test Score:	Positive	True Positives (TP) <div>a</div>	False Positives (FP) <div>b</div>	$PPV = \frac{TP}{TP + FP}$
	Negative	False Negatives (FN) <div>c</div>	True Negatives (TN) <div>d</div>	$NPV = \frac{TN}{TN + FN}$

	Sensitivity	Specificity
	$\frac{TP}{TP + FN}$	$\frac{TN}{TN + FP}$
Or,	$\frac{a}{a + c}$	$\frac{d}{d + b}$

Confusion Matrix

- ◆ A confusion matrix shows the counts of the actual versus predicted class values.
- ◆ Example (overall accuracy rate of 73.9%)

		Actual Class		
		Class A	Class B	Class C
Predicted Class	Class A	20	5	2
	Class B	6	20	4
	Class C	4	2	25

For the confusion matrix

Actual
purchase no purchase

Predicted	purchase	no purchase
	purchase	10
no purchase	20	200

- ◆ What is its precision?
- ◆ What is its recall?
- ◆ How do you
 - a) increase precision (but decrease recall)
 - b) increase both precision and recall

- a) $10/20$
- b) $10/(10+20)$
- c) $10/60$
- d) $10/(10+60)$
- e) other

A, B, C, D or E

A

B

C

D

E

Optimizing for true utility

- ◆ **Could one directly learn a model to optimize**
 - An asymmetric loss function?
 - AUC?

You should know

◆ Probability vs. loss

- Often use model to estimate score; then threshold for decision

◆ Loss function vs. utility function

◆ Confusion matrix:

- TP/TN/FP/FN or TPR/TNR/FPR/FNR

◆ Precision, Recall, Sensitivity, Specificity, F1

◆ ROC curves

- AUC