

# VideoPlus: A Method for Capturing the Structure and Appearance of Immersive Environments

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**Abstract.** This paper describes an approach to capturing the appearance and structure of immersive environments based on the video imagery obtained with an omnidirectional camera system. The scheme proceeds by recovering the 3D positions of a set of point and line features in the world from image correspondences in a small set of key frames in the image sequence. Once the locations of these features have been recovered the position of the camera during every frame in the sequence can be determined by using these recovered features as fiducials and estimating camera pose based on the location of corresponding image features in each frame. The end result of the procedure is an omnidirectional video sequence where every frame is augmented with its pose with respect to an absolute reference frame and a 3D model of the environment composed of point and line features in the scene.

By augmenting the video clip with pose information we provide the viewer with the ability to navigate the image sequence in new and interesting ways. More specifically the user can use the pose information to travel through the video sequence with a trajectory different from the one taken by the original camera operator. This freedom presents the end user with an opportunity to immerse themselves within a remote environment.

**Keywords:** Reconstruction, Immersive Environments, Omnidirectional Video, Pose Estimation

## 1 Introduction

This paper describes an approach to capturing the appearance and structure of immersive environments based on the video imagery obtained with an omnidirectional camera system such as the one proposed by Nayar [15]. The scheme proceeds by recovering the 3D positions of a set of point and line features in the world from image correspondences in a small set of key frames in the image sequence. Once the locations of these features have been recovered the position of the camera during every frame in the sequence can be determined by using these recovered features as fiducials and estimating camera pose based on the location of corresponding image features in each frame. The end result of the procedure is an omnidirectional video sequence where every frame is augmented with its pose with respect to an absolute reference frame and a 3D model of the environment composed of point and line features in the scene.

One area of application for the proposed reconstruction techniques is in the field of virtual tourism. By augmenting the video clip with pose information we provide the viewer with the ability to navigate the image sequence in new and interesting ways. More specifically the user can use the pose information to travel through the video sequence with a trajectory different from the one taken by the original camera operator. This freedom presents the end user with an opportunity to immerse themselves within a remote environment and to control what they see.

Another interesting application of the proposed technique is in the field of robotics since it allows us to construct 3D models of remote environments based on the video imagery acquired by a mobile robot. For example, the model of an indoor environment shown in Figure 5 was constructed from the video imagery acquired by the mobile robot shown in Figure 14c as it roamed through the scene.

Such a model would allow the remote operator to visualize the robots operating environment. It could also be used as the basis for an advanced human robot interface where the robot could be tasked by pointing to a location on the map and instructing it to move to that position. The robot would be able to automatically plan and execute a collision free path to the destination based on the information contained in the map.

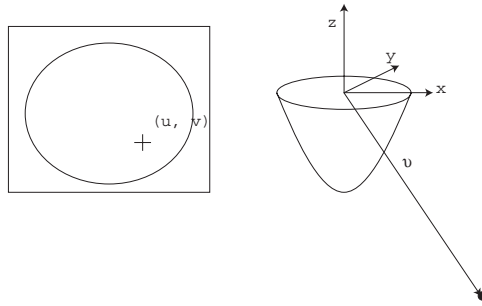
The rest of this paper is arranged as follows Section 2 describes the process whereby the 3D locations of the model features and the locations of the cameras are estimated from image measurements. Results obtained by applying these techniques to actual video sequences are presented in Section 3. Section 4 discusses the relationship between this research and previously published work. Section 5 briefly describes future directions of this research and section 6 presents some of the conclusions that have been drawn so far.

## 2 Reconstruction

This section describes how the 3D structure of the scene and the locations of the camera positions are recovered from image correspondences in the video

sequence. The basic approach is similar in spirit to the reconstruction schemes described in [20] and [4]. The reconstruction problem is posed as an optimization problem where the goal is to minimize an objective function which indicates the discrepancy between the predicted image features and the observed image features as a function of the model parameters and the camera locations.

In order to carry out this procedure it is important to understand the relationship between the locations of features in the world and the coordinates of the corresponding image features in the omnidirectional imagery. The catadioptric camera system proposed by Nayar [15] consists of a parabolic mirror imaged by an orthographic lens. With this imaging model there is an effective single point of projection located at the focus of the parabola as shown in Figure 1.



**Fig. 1.** The relationship between a point feature in the omnidirectional image and the ray between the center of projection and the imaged point.

Given a point with coordinates  $(u, v)$  in the omnidirectional image we can construct a vector,  $v$ , which is aligned with the ray connecting the imaged point and the center of projection of the camera system.

$$v = \begin{pmatrix} s_x(u - c_x) \\ s_y(v - c_y) \\ (s_x(u - c_x))^2 + (s_y(v - c_y))^2 - 1 \end{pmatrix} \quad (1)$$

This vector is expressed in terms of a coordinate frame of reference with its origin at the center of projection and with the  $z$ -axis aligned with the optical axis of the device as shown in Figure 1.

The calibration parameters,  $s_x$ ,  $s_y$ ,  $c_x$  and  $c_y$  associated with the imagery can be obtained in a separate calibration procedure [5]. It is assumed that these calibration parameters remain constant throughout the video sequence.

Note that since the catadioptric camera system has a single point of projection it is possible to resample the resulting imagery to produce “normal” perspective with arbitrary viewing directions [15]. The current system exploits this capability by providing a mechanism which allows the user to create a virtual viewpoint which she can pan and tilt interactively.

The current implementation of the reconstruction system allows the user to model two types of features: point features and straight lines aligned with one of the vertical or horizontal axes of the global frame of reference. These types of features were chosen because they are particularly prevalent and salient in man-made immersive environments but other types of features, such as lines at arbitrary orientations, could easily be included. The locations of point features can be represented in the usual manner by three vectors  $(X_i, Y_i, Z_i)$ <sup>1</sup> while the locations of the straight lines can be denoted with only two parameters. For example, the location of a vertical line can be specified by parameterizing the location of its intercept with the xy-plane  $(X_i, Y_i)$  since the vertical axis corresponds to the z-axis of the global coordinate frame. Note that for the purposes of reconstruction the lines are considered to have infinite length so no attempt is made to represent their endpoints.

The position and orientation of the camera with respect to the world frame of reference during frame  $j$  of the sequence is captured by two parameters, a rotation  $R_j \in SO(3)$  and a translation  $\mathbf{T}_j \in \mathbb{R}^3$ . This means that given the coordinates of a point in the global coordinate frame,  $\mathbf{P}_{iw} \in \mathbb{R}^3$  we can compute its coordinates with respect to camera frame  $j$ ,  $\mathbf{P}_{ij}$  from the following expression.

$$\mathbf{P}_{ij} = R_j(\mathbf{P}_{iw} - \mathbf{T}_j) \quad (2)$$

The reconstruction program takes as input a set of correspondences between features in the omnidirectional imagery and features in the model. For correspondences between point features in the image and point features in the model we can construct an expression which measures the discrepancy between the predicted projection of the point and the vector obtained from the image measurement,  $v_{ij}$ , where  $\mathbf{P}_{ij}$  is computed from equation 2.

$$\|(v_{ij} \times \mathbf{P}_{ij})\|^2 / (\|\mathbf{P}_{ij}\|^2 \|v_{ij}\|^2) \quad (3)$$

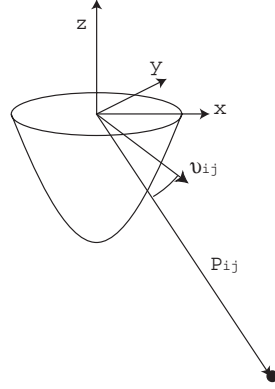
This expression yields a result equivalent to the square of the sine of the angle between the two vectors,  $v_{ij}$  and  $\mathbf{P}_{ij}$  shown in Figure 2.

For correspondences between point features in the image and line features in the model we consider the plane containing the line and the center of projection of the image. The normal to this plane,  $\mathbf{m}_{ij}$  can be computed from the following expression.

$$\mathbf{m}_{ij} = R_j(\mathbf{v}_i \times (\mathbf{d}_i - \mathbf{T}_j)) \quad (4)$$

Where the vector  $\mathbf{v}_i$  denotes the direction of the line in space and the vector  $\mathbf{d}_i$  denotes an arbitrary point on the line. As an example, for vertical lines the vector  $\mathbf{v}_i$  will be aligned with the z axis  $(0, 0, 1)^T$  and the vector  $\mathbf{d}_i$  will have the form  $(X_i, Y_i, 0)^T$ .

<sup>1</sup> the subscript  $i$  serves to remind us that these parameters describe the position of the  $i$ th feature in the model.



**Fig. 2.** Given a correspondence between a point feature in the omnidirectional image and a point feature in the model we can construct an objective function by considering the disparity between the predicted ray between the camera center and the point feature,  $\mathbf{P}_{ij}$ , and the vector  $v_{ij}$  computed from the image measurement.

The following expression measures the extent to which the vector obtained from the point feature in the omnidirectional imagery,  $v_{ij}$ , deviates from the plane defined by the vector  $\mathbf{m}_{ij}$ .

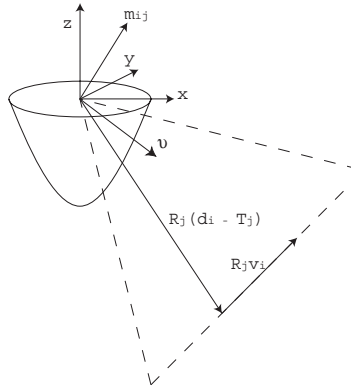
$$(\mathbf{m}^T v_{ij})^2 / (\|\mathbf{m}_{ij}\|^2 \|v_{ij}\|^2) \quad (5)$$

A global objective function is constructed by considering all of the correspondences in the data set and summing the resulting expressions together. Estimates for the structure of the scene and the locations of the cameras are obtained by minimizing this objective function with respect to the unknown parameters,  $R_j$ ,  $\mathbf{T}_j$ ,  $X_i$ ,  $Y_i$  and  $Z_i$ . This minimization is carried out using a variant of the Newton-Raphson method [19, 20, 10].

An initial estimate for the orientation of the camera frames,  $R_j$ , can be obtained by considering the lines in the scene with known orientation such as lines parallel to the x, y, or z axes of the environment. If  $v_1$  and  $v_2$  represent the vectors corresponding to two points along the projection of a line in the image plane then the normal to the plane between them in the camera's frame of reference can be computed as follows  $\mathbf{n} = v_1 \times v_2$ . If  $R_j$  represents the rotation of the camera frame and  $\mathbf{v}$  represents the direction of the line in world coordinates then the following objective function represents the fact that the normal to the plane should be perpendicular to the direction of the line in the coordinates of the camera frame.

$$(\mathbf{n}^T R_j \mathbf{v})^2 \quad (6)$$

An objective function can be created by considering all such lines in an image and summing these penalty terms. The obvious advantage of this expression is that the only unknown parameter is the camera rotation  $R_j$  which means that



**Fig. 3.** Given a correspondence between a point feature in the omnidirectional image and a line feature in the model we can construct an objective function by considering the disparity between the predicted normal vector to the plane containing the center of projection and the model line,  $\mathbf{m}_{ij}$ , and the vector,  $v_{ij}$ , computed from the image measurement.

we can minimize the expression with respect to this parameter in isolation to obtain an initial estimate for the camera orientation.

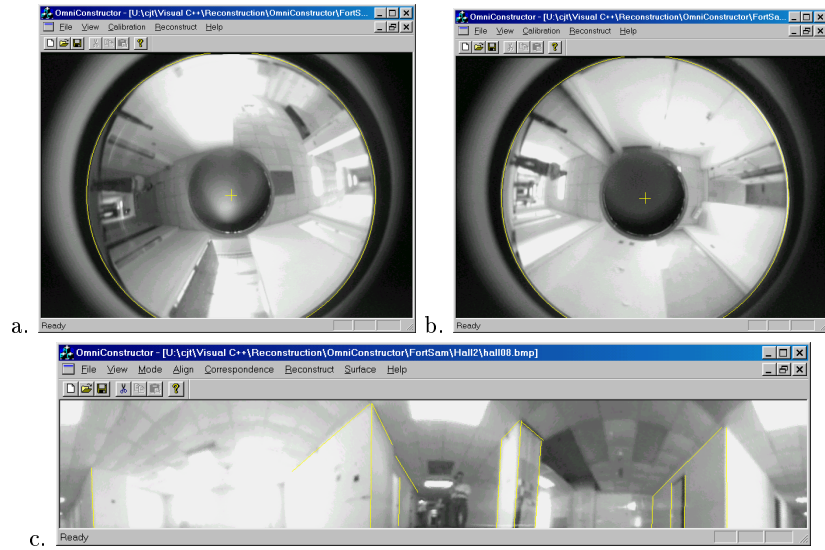
The current implementation of the reconstruction system also allows the user to specify constraints that relate the features in the model. For example the user would be able to specify that two or more features share the same  $z$ -coordinate which would force them to lie on the same horizontal plane. This constraint is maintained by reparameterizing the reconstruction problem such that the  $z$ -coordinates of the points in question all refer to the same variable in the parameter vector.

The ability to specify these relationships is particularly useful in indoor environments since it allows the user to exploit common constraints among features such as two features belonging to the same wall or multiple features lying on a ground plane. These constraints reduce the number of free parameters that the system must recover and improve the coherence of the model when the camera moves large distances in the world.

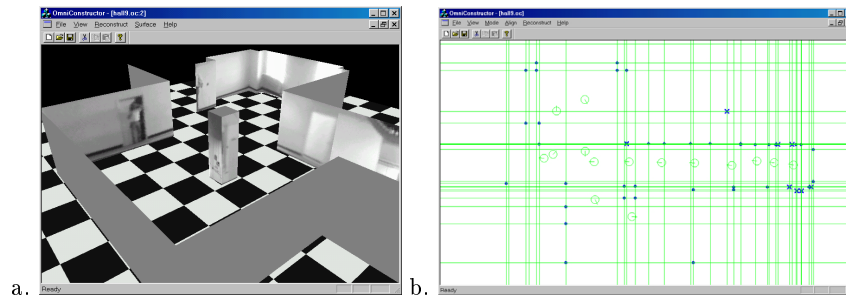
Using the procedure outlined above we were able to reconstruct the model shown in Figure 5 from 14 images taken from a video sequence of an indoor scene.

The polyhedral model is constructed by manually attaching surfaces to the reconstructed features. Texture maps for these surfaces are obtained by sampling the original imagery.

An important practical advantage of using omnidirectional imagery in this application is that the 3D structure can be recovered from a smaller number of images since the features of interest are more likely to remain in view as the camera moves from one location to another.



**Fig. 4.** Two of the omnidirectional images from a set of 14 keyframes are shown in a and b. A panoramic version of another keyframe is shown in c.



**Fig. 5.** a. 3D model of the environment constructed from the data set shown in Figure 4. b. Floor plan view showing the estimated location of all the images and an overhead view of the feature locations. The circles correspond to the recovered camera positions while the dots and crosses correspond to vertical line and point features.

Once the locations of a set of model features have been reconstructed using the image measurements obtained from a set of keyframes in the sequence, these features can then be used as fiducials to recover the pose of the camera at other frames in the sequence.

For example, if frame number 1000 and frame number 1500 were used as keyframes in the reconstruction process then we know where a subset of the model features appears in these frames. Correspondences between features in the intervening images and features in the model can be obtained by applying standard feature tracking algorithms to the data set. The current system employs a variant of the Lucas and Kanade [14] algorithm to localize and track feature points through intervening frames.

Based on these correspondences, the pose of the camera during these intermediate frames can be estimated by simply minimizing the objective function described previously with respect to the pose parameters of the camera. The locations of the feature points are held constant during this pose estimation step. Initial estimates for the camera pose can be obtained from the estimates for the locations of the keyframes that were produced during the reconstruction process.

Another approach to estimating the pose of the camera during the intervening frames is to simply interpolate the pose parameters through the frames of the subsequence. That is, given that the camera pose in frames 1000 and 1500 is known we could simply estimate the roll, pitch and yaw angles of the intervening frames along with the translational position by interpolating these parameter values linearly. This approach is most appropriate in situations where the camera is moving with an approximately constant translational and angular velocity between keyframes.

Once the video sequence has been fully annotated with camera pose information the user is able index the data set *spatially* as well as temporally. In the current implementation the user is able to navigate through an immersive environment such as the office complex shown in Figure 6 in a natural manner by panning and tilting his virtual viewpoint and moving forward and backward. As the user changes the location of her viewpoint the system simply selects the closest view in the omnidirectional video sequence and generates an image in the appropriate viewing direction.

The system also allows the user to generate movies by specifying a sequence of keyframes. The system automatically creates the sequence of images that correspond to a smooth camera trajectory passing through the specified positions. This provides the user with the capability of reshooting the scene with a camera trajectory which differs from the one that was used to capture the video initially.

### 3 Results

In order to illustrate what can be achieved with the proposed techniques we present results obtained from three different immersive environments.

Figure 6 shows three images taken from a video sequence acquired in the Fine Arts Library at the University of Pennsylvania. This building was designed

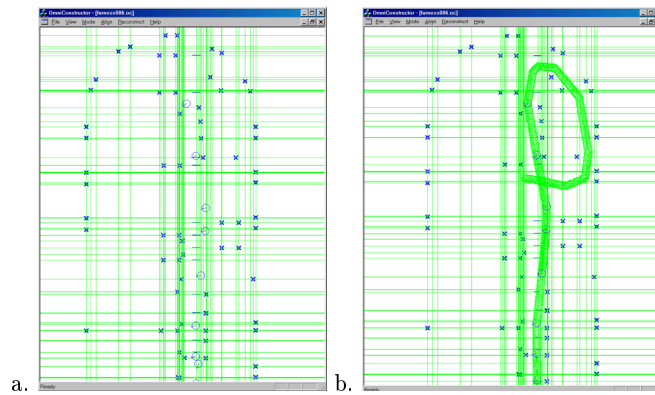




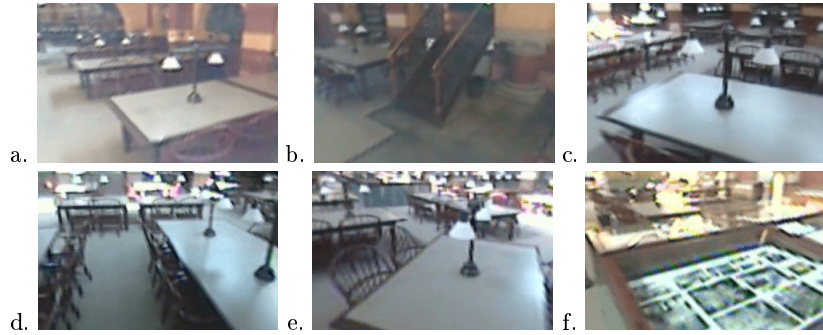
**Fig. 6.** Three images taken from a video sequence obtained as the camera is moved through the library.



**Fig. 7.** Images of the Fine Arts library at the University of Pennsylvania. The building was designed by Frank Furness in 1891 and remains one of the most distinctive and most photographed buildings on campus.



**Fig. 8.** a. A floor plan view of the library showing the locations of the features recovered from 9 keyframes in the video sequence. The circles correspond to the recovered camera positions while the dots and crosses correspond to line and point features. b. Based on these fiducials the system is able to estimate the location of the camera for all the intervening frames.



**Fig. 9.** Views generated by the system as the user conducts a virtual tour of the library.

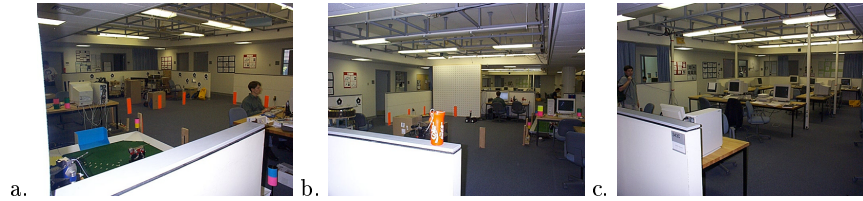
by Frank Furness in 1891 and refurbished on its centenary in 1991, images of the interior and exterior of the building are shown in Figure 7.

The reconstruction of this environment was carried out using approximately 100 model features viewed in 9 frames of the video sequence. Figure 8a shows a floor plan view of the resulting reconstruction. The reconstructed feature locations were then used as fiducials to recover the position of 15 other frames in the sequence. Pose interpolation was employed to estimate the position and orientation of the camera during intervening frames. Figure 8b shows the resulting estimates for the camera position during the entire sequence. The original video sequence was 55 seconds long and consisted of 550 frames. During the sequence the camera traveled a distance of approximately 150 feet. Figure 9 shows viewpoints generated by the system as the user conducts a virtual tour of this environment.

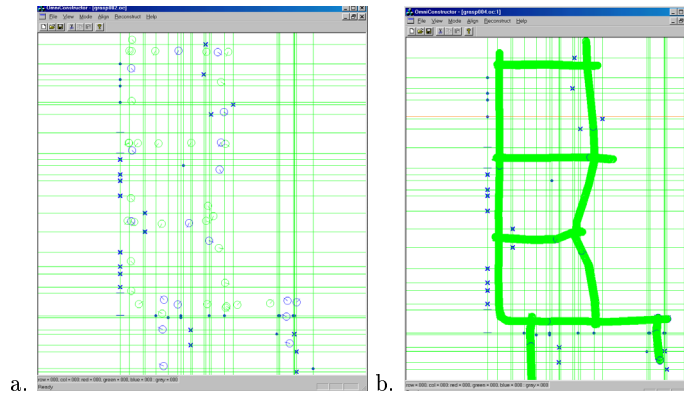


**Fig. 10.** Three images taken from a video sequence obtained as the camera is moved through the GRASP laboratory.

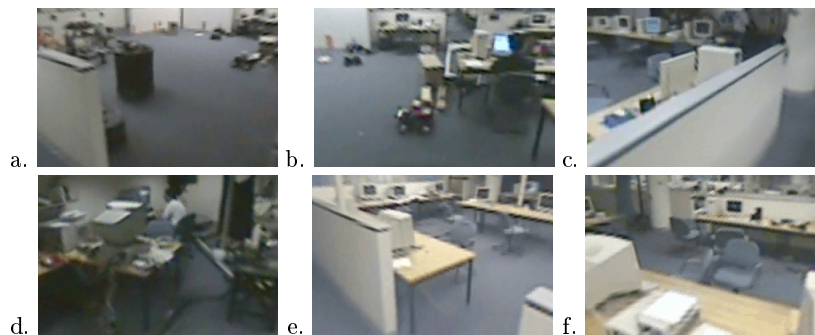
Figure 10 shows three images taken from a video sequence acquired in the GRASP laboratory at the University of Pennsylvania; snapshots of the lab are shown in Figure 11. In this case the video imagery was obtained in a sequence of short segments as the camera was moved through various sections of the laboratory. The entire video sequence was 154 seconds long and consisted of 4646 frames. The approximate dimensions of the region of the laboratory explored are



**Fig. 11.** Images of the GRASP laboratory at the University of Pennsylvania.



**Fig. 12.** a. A floor plan view of the laboratory showing the locations of the features recovered from 17 keyframes in the video sequence. The circles correspond to the recovered camera positions while the dots and crosses correspond to line and point features. b. Based on these fiducials the system is able to estimate the location of the camera for all the intervening frames. Notice that during the exploration the camera is moved into two side rooms that are accessed from the corridor surrounding the laboratory; these are represented by the two excursions at the bottom of this figure.



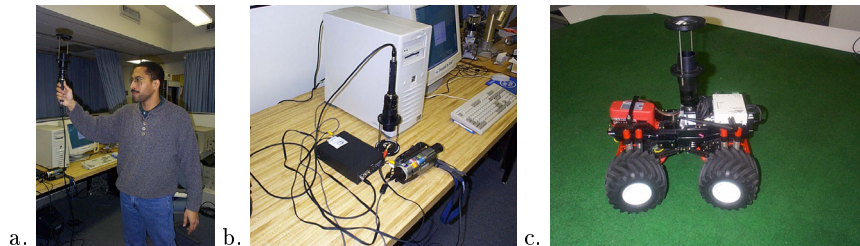
**Fig. 13.** Views generated by the system as the user conducts a virtual tour of the library.

36 feet by 56 feet and the camera moved over 250 feet during the exploration. The reconstruction of this scene was carried out using approximately 50 model features viewed in 16 images of the sequence. The resulting model is shown in Figure 12a, Figure 12b shows the result of applying pose estimation and interpolation to the rest of the video sequence. Figure 13 shows some samples of images created as the user explores this environment interactively. Notice that the user can freely enter and exit various rooms and alcoves in the laboratory.

Figure 5 shows the results of applying the reconstruction procedure to 14 images acquired from a sequence taken inside an abandoned hospital building. This figure demonstrates the capability of constructing polyhedral models from the recovered model features.

The fact that the reconstruction process can be carried out entirely from the video sequence simplifies the process of data collection. Figure 14c shows a mobile platform outfitted with an omnidirectional camera system produced by Remote Reality inc.. This system was used to acquire the imagery that was used to construct the model shown in Figure 5. Note that the only sensor carried by this robot is the omnidirectional camera it does not have any odometry or range sensors. During the data collection process the system was piloted by a remote operator using an RC link.

The video data that was used to construct the models shown in Figures 8 and 12 was collected with a handheld omnidirectional camera system as shown in Figure 14. In both cases the video data was captured on a Sony Digital camcorder and transferred to a PC for processing using an IEEE 1394 Firewire link. The images were digitized at a resolution of 720x480 at 24 bits per pixel.



**Fig. 14.** a. The video imagery used to produce the reconstructions of the library and the laboratory environments was acquired using a handheld omnidirectional camera system b. The equipment used to acquire the data c. Mobile platform equipped with an omnidirectional camera system that was used to acquire video imagery of an indoor environment.

## 4 Related Work

The idea of using omnidirectional camera system for reconstructing environments from video imagery in the context of robotic applications has been ex-

plored by Yagi, Kawato, Tsuji and Ishiguro [21, 8, 7, 9]. These authors presented an omnidirectional camera system based on a conical mirror and described how the measurements obtained from the video imagery acquired with their camera system could be combined with odometry measurements from the robot platform to construct maps of the robots environment. The techniques described in this paper do not require odometry information which means that they can be employed on simpler platforms like the one shown in Figure 14c which are not equipped with odometers. It also simplifies the data acquisition process since we do not have to calibrate the relationship between the camera system the robots odometry system.

Szeliski and Shum [18] describe an interactive approach to reconstructing scenes from panoramic imagery which is constructed by stitching together video frames that are acquired as a camera is spun around its center of projection. Coorg and Teller [3] describe a system which is able to automatically extract building models from a data set of panoramic images augmented with pose information which they refer to as pose imagery

From the point of view of robotic applications, reconstruction techniques based on omnidirectional imagery are more attractive than those that involve constructing panoramas from standard video imagery since they do not involve moving the camera and since the omnidirectional imagery can be acquired as the robot moves through the environment.

The process of acquiring omnidirectional video imagery of an immersive environment is much simpler than the process of acquiring panoramic images. One would not really consider constructing a sequence of tightly spaced panoramic images of an environment because of the time required to acquire the imagery and stitch it together. However, this is precisely the type of data contained in an omnidirectional video sequence. By estimating the pose at every location in the sequence the Video Plus system is able to fully exploit the range of viewpoints represented in the image sequence.

Boult [1] describes an interesting system which allows a user to experience remote environments by viewing video imagery acquired with an omnidirectional camera. During playback the user can control the direction from which she views the scene interactively. The VideoPlus system described in this paper provides the end user with the ability to control her viewing position as well as her viewing direction. This flexibility is made possible by the fact that the video imagery is augmented with pose information which allows the user to navigate the sequence in an order that is completely different from the temporal ordering of the original sequence.

The VideoPlus system is similar in spirit to the Movie Map system described by Lippman [13] and to the QuickTime VR system developed by Chen [2] in that the end result of the analysis is a set of omnidirectional images annotated with position. The user is able to navigate through the scene by jumping from one image to another. The contribution of this work is to propose a simple and effective way of recovering the positions of the omnidirectional views from image

measurements without having to place artificial fiducials in the environment or requiring a separate pose estimation system.

Shum and He [16] describe an innovative approach to generating novel views of an environment based on a set of images acquired while the camera is rotated around a set of concentric circles. This system builds on the plenoptic sampling ideas described by Levoy and Hanrahan [11] and Gortler, Grzeszczuk, Szeliski and Cohen [6]. The presented approach shares the advantage of these image based rendering techniques since the VideoPlus scheme allows you to explore arbitrarily complex environments without having to model the geometric and photometric properties of all of the surfaces in the scene. The rerendered images are essentially resampled versions of the original imagery. However, the scheme presented in this paper dispenses with the need for a specific camera trajectory and it can be used to capture the appearance of extended environments such as office complexes which involve walls and other occluding features which are not accounted for by these plenoptic sampling schemes.

## 5 Future Work

The scheme used to generate views of an environment during a walkthrough is currently quite simple. Given the users desired viewpoint the system selects the omnidirectional image that is closest to that location and generates an image with the appropriate viewing direction. The obvious limitation of this approach is that the viewing position is restricted to locations which were imaged in the original video sequence.

This limitation can be removed by applying image based rendering techniques. One approach to generating novel images is to resample the intensity data from other images depending on the hypothesized structure of the scene. The video plus system has access to the positions of all of the frames in the sequence along with a coarse polyhedral model of the environment which could be used to transfer pixel data from the original views to the virtual view.

Another approach to generating novel views would be to find correspondences between salient image features in nearby omnidirectional images in the sequence and to use these correspondences to construct a warping function which would map pixels from the original images to the virtual viewpoint [12].

The success of any view generation technique will depend upon having a set of images taken from a sufficiently representative set of viewpoints. A better understanding of how to go about capturing such a data set taking into account the structure of the scene and the viewpoints that are likely to be of most interest is needed. The ultimate goal would be to produce a system where the user could arbitrarily select the desired viewpoint and viewing direction so as to explore the environment in an unconstrained manner.

The largest drawbacks to using omnidirectional video imagery is the reduced image resolution. This effect can be mitigated by employing higher resolution video cameras. One of the tradeoffs that is currently being explored is the possibility of acquiring higher resolution imagery at a lower frame rate. This would

allow us to produce sharper images of the scene but would either slow down the data acquisition process or require better interpolation strategies.

## 6 Conclusions

This paper presents a simple approach to capturing the appearance of immersive scenes based on an omnidirectional video sequence. The system proceeds by combining techniques from structure from motion with ideas from image based rendering. An interactive photogrammetric modeling scheme is used to recover the positions of a set of salient features in the scene (points and lines) from a small set of keyframe images. These features are then used as fiducials to estimate the position and orientation of the omnidirectional camera at every frame in the video clip.

By augmenting the video sequence with pose information we provide the end user with the capability of indexing the video sequence spatially as opposed to temporally. This means that the user can explore the image sequence in ways that were not envisioned when the sequence was initially collected.

The cost of augmenting the video sequence with pose information is very slight since it only involves storing six numbers per frame. The hardware requirements of the proposed scheme are also quite modest since the reconstruction is performed entirely from the image data. It does not involve a specific camera trajectory or a separate sensor for measuring the camera position. As such, the method is particularly appropriate for immersive man-made structures where GPS data is often unavailable.

We envision that this system could be used to acquire representations of immersive environments, like museums, that users could then explore interactively. It might also be appropriate for acquiring immersive backgrounds for video games or training simulators.

Future work will address the problem of generating imagery from novel viewpoints and improving the resolution of the imagery generated by the system.

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