

**Final Exam**  
**December 16, 2010**

**This exam is a closed book exam. Students are allowed to use a calculator (not a smart Phone or PDA with Internet Access) and a single page reference sheet (two sided). Please show all work, justify all approximations and give the units for all calculated parameters.**

1. Consider the four-stage amplifier circuit in Fig. P1. Stage 1 involves of transistors Q1, Q2; stage 2 involves Q3, Q4; stage 3 involves Q5 and stage 4 involves Q6. Assume all six transistors are forward-active with  $|V_{BE}| = 0.7$  V,  $V_A = \text{large}$  and  $\beta = \text{large}$ . Furthermore let transistors Q1 - Q4 be matched and all current sources are ideal.

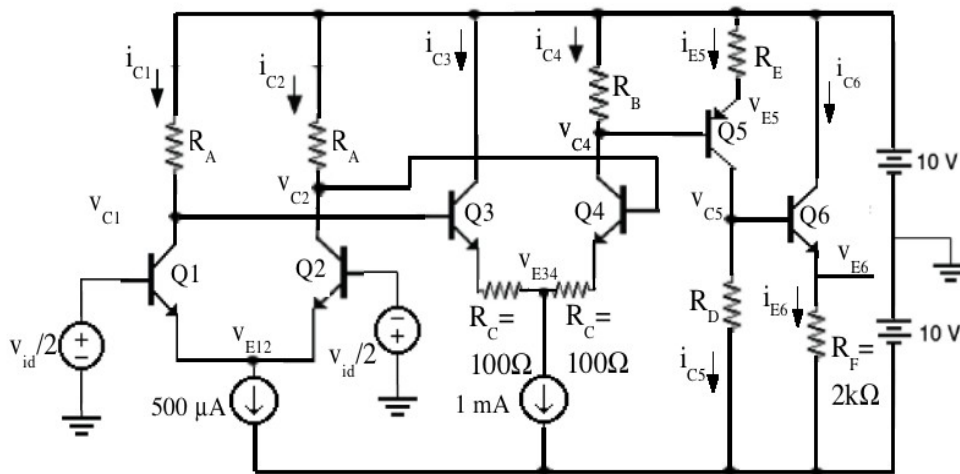


Fig. P1 Four-Stage Amplifier for Problem 1

- (a). Determine values for dc currents  $I_{C1}$ ,  $I_{C2}$ ,  $I_{C3}$  and  $I_{C4}$  and dc voltages  $V_{E12}$ . (5 pts)
- (b). Let the dc voltages be specified:  $V_{C1} = V_{C2} = 7$  V and  $V_{C4} = 8$  V. Determine the values for resistors  $R_A$  and  $R_B$ . Further determine the value for voltage  $V_{E5}$  and  $V_{E34}$ . (10 pts)
- (c). Let  $V_{C5} = 1$  V and  $I_{C5} = 2$  mA. Determine values for resistors  $R_D$  and  $R_E$ . Further determine the value for voltage  $V_{E6}$ . (10 pts)
- (d). Determine the values for currents  $I_{E6}$  and  $I_{C6}$ . (5 pts)
- (e). Let the amplifier be driven by an ac differential input  $\pm v_{id}/2$  and the dc currents be those in parts a through d above. Determine the values for the small-signal transconductance parameters for all six transistors, i.e.  $g_{m1}$ ,  $g_{m2}$ ,  $g_{m3}$ ,  $g_{m4}$ ,  $g_{m5}$  and  $g_{m6}$ . (10 pts)
- (f) Determine the mid-band gains for each of the four stages, i.e.  $A_1 = \frac{v_{old}}{v_{id}}$  ;  $A_2 = \frac{v_{c4}}{v_{old}}$  ;  $A_3 = \frac{v_{c5}}{v_{c4}}$   
and  $A_4 = \frac{v_{e6}}{v_{c5}}$  , where  $v_{old} = v_{c2} - v_{c1}$  . (10 pts)

(g) Let the output be  $v_o = v_{e6}$ , determine the overall voltage gain  $A = \frac{v_o}{v_{id}}$ . (10 pts)

(h) It is required to increase the overall gain  $A$  by 6 dB (actually 6.02 dB), while keeping the dc voltages  $V_{C1}$ ,  $V_{C2}$ ,  $V_{C4}$ ,  $V_{C5}$  and  $V_{E6}$  the same as given in parts b and c, modify the value(s) of the appropriate resistor(s) to implement this requirement. (10 pts)

2. Consider the feedback amplifier where the gain and phase of the open-loop

$$A(s) = \frac{A_0 p_1 p_2 p_3}{(s + p_1)(s + p_2)(s + p_3)} = \frac{2 \times 10^{24}}{(s + 10^5)(s + 3 \times 10^6)(s + 10^8)}$$
 are plotted in Fig. P2.

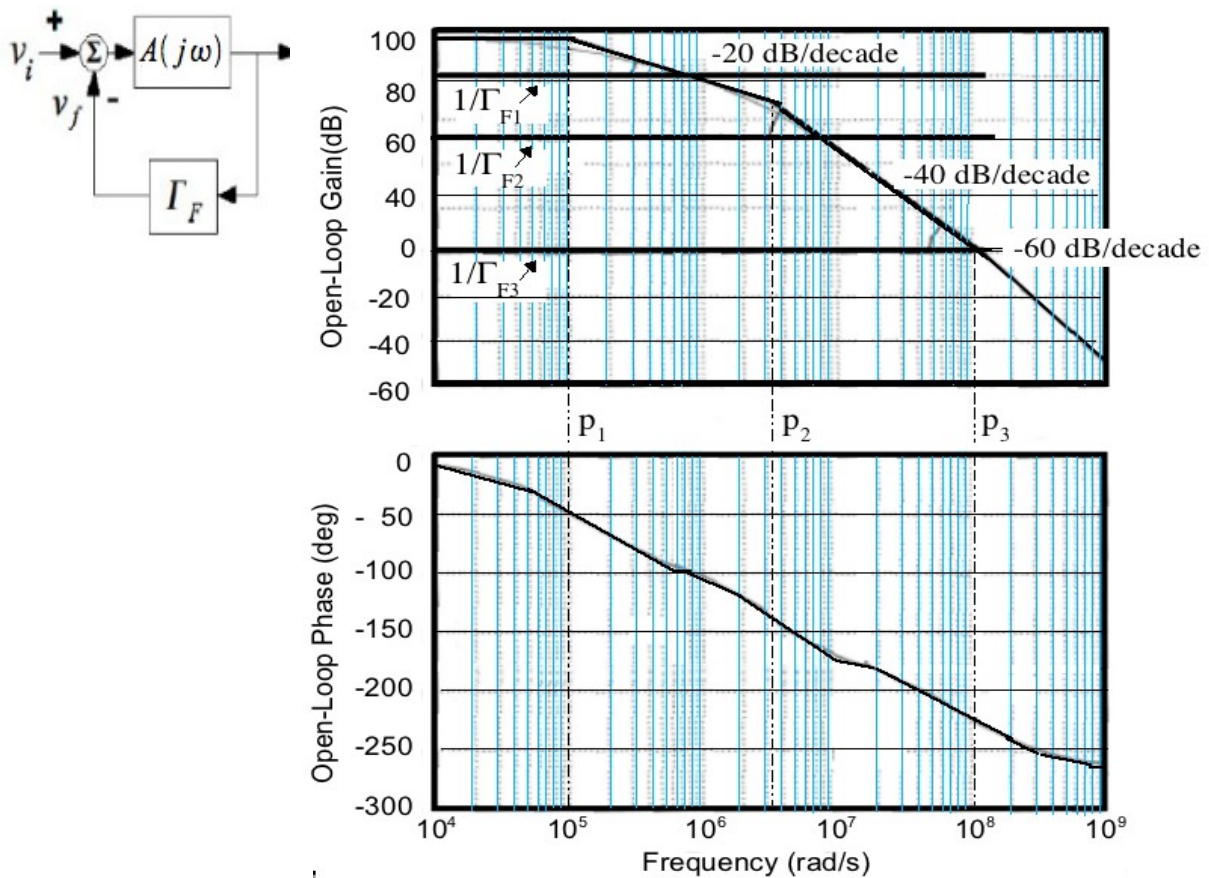


Fig. P2 Bode Plots for Problem 2

- For feedback  $\Gamma_{F1}$  estimate the unity-gain crossover frequency  $\omega_1$ , the  $180^\circ$  phase crossover frequency  $\omega_{180}$  and the phase-margin  $PM_1$ . Is the closed-loop amplifier with  $\Gamma_F = \Gamma_{F1}$  stable? (10 pts)
- For feedback  $\Gamma_{F2}$  estimate the unity-gain crossover frequency  $\omega_1$ , the  $180^\circ$  phase crossover frequency  $\omega_{180}$  and the phase-margin  $PM_2$ . Is the closed-loop amplifier with  $\Gamma_F = \Gamma_{F2}$  stable? (10 pts)
- For feedback  $\Gamma_{F3}$  estimate the unity-gain crossover frequency  $\omega_1$ , the  $180^\circ$  phase crossover frequency  $\omega_{180}$  and the phase-margin  $PM_3$ . Is the closed-loop amplifier with  $\Gamma_F = \Gamma_{F3}$  stable? (10 pts)