

ESE370: Circuit-Level Modeling, Design, and Optimization for Digital Systems

Lec 13: March 20, 2023
Distributed RC Wire and Elmore Delay



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Today

- Estimate delay in RC Network
 - Elmore delay calculation
- Apply to wire delay
- Apply to pass transistor circuits
- Apply to CMOS gates

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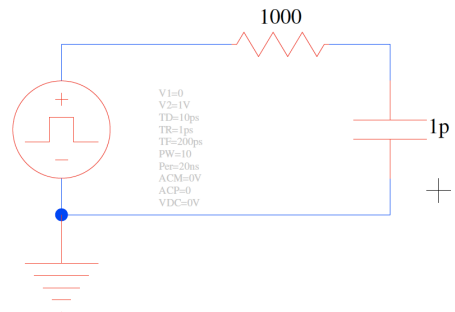
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Distributed RC (setup)



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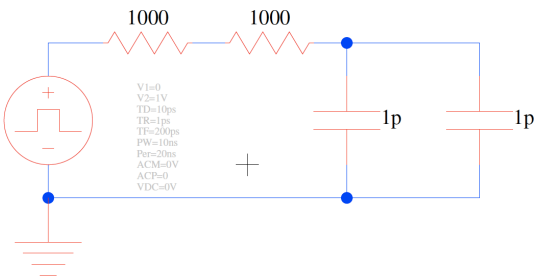
What is response? (Preclass 1)



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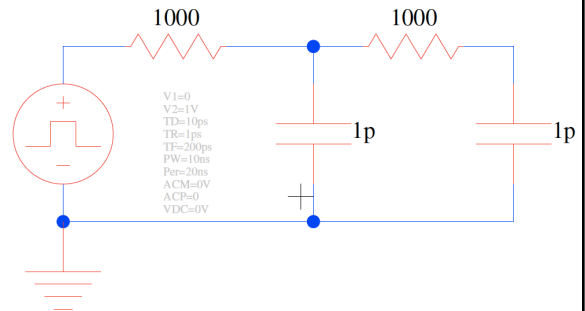
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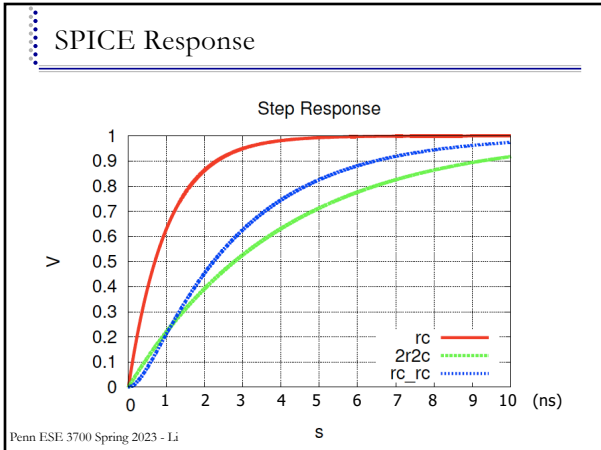
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What is response? (Preclass 1)

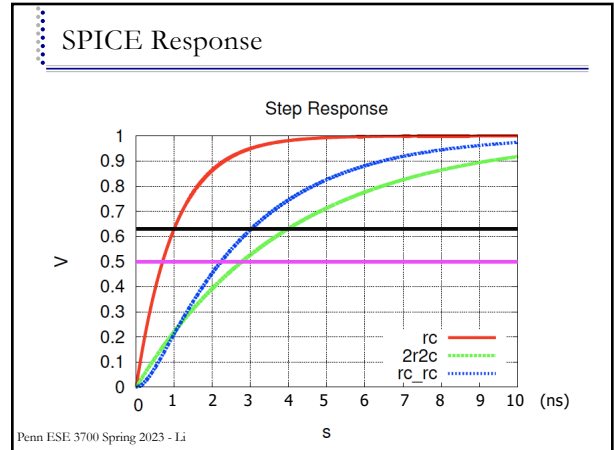


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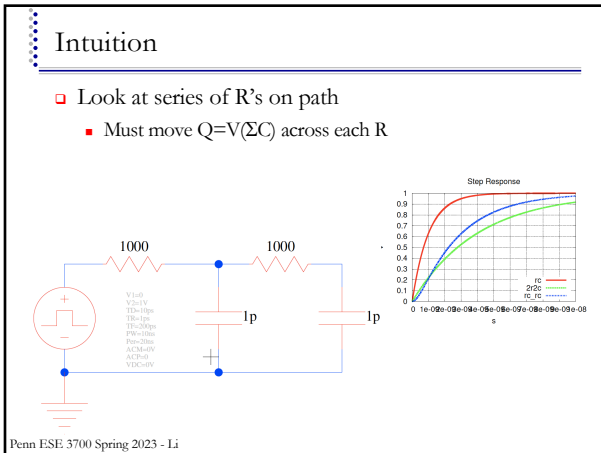
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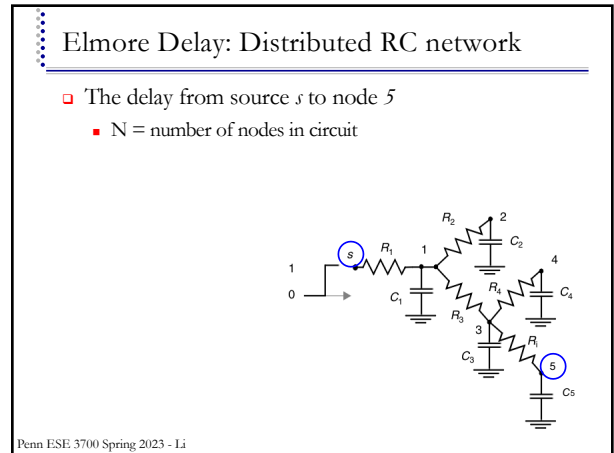
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Elmore Delay: Distributed RC network

- The delay from source s to node 5
 - N = number of nodes in circuit

$$R_{5k} = \sum R_j \Rightarrow (R_j \in [\text{path}(s \rightarrow 5) \cap \text{path}(s \rightarrow k)])$$

$$\tau_{D5} = \sum_{k=1}^N C_k R_{5k}$$

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Elmore Delay: Distributed RC network

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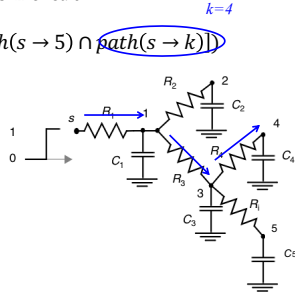
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Elmore Delay: Distributed RC network

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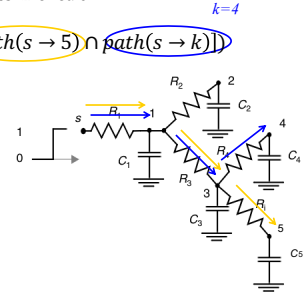
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Elmore Delay: Distributed RC network

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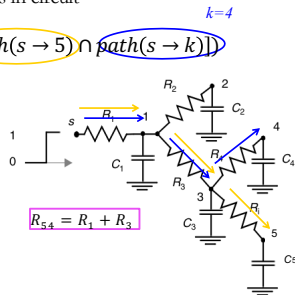
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Elmore Delay: Distributed RC network

- The delay from source s to node 5
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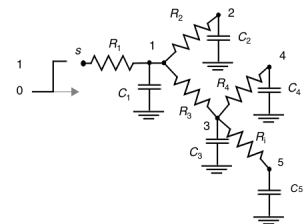
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Elmore Delay: Distributed RC network

- The delay from source s to node 5
 - N = number of nodes in circuit

$$R_{5k} = \sum R_j \Rightarrow (R_j \in [\text{path}(s \rightarrow 5) \cap \text{path}(s \rightarrow k)])$$

$$\tau_{D5} = \sum_{k=1}^N C_k R_{5k} = ?$$



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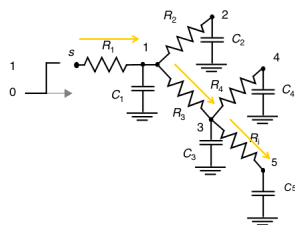
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Elmore Delay: Distributed RC network

- The delay from source s to node 5
 - N = number of nodes in circuit

$$R_{5k} = \sum R_j \Rightarrow (R_j \in [\text{path}(s \rightarrow 5) \cap \text{path}(s \rightarrow k)])$$

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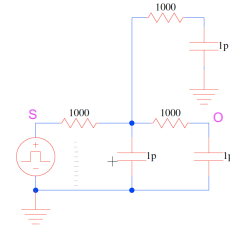
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Elmore Delay: Practice

- The delay from source s to node O
 - N = number of nodes in circuit

$$R_{Ok} = \sum R_j \Rightarrow (R_j \in [\text{path}(s \rightarrow O) \cap \text{path}(s \rightarrow k)])$$

$$\tau_{DO} = \sum_{k=1}^N C_k R_{Ok} = ?$$



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Previously: Equivalent RC

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What is response?

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Elmore Delay: Practice (preclass 1)

- The delay from source s to node i
 - N = number of nodes in circuit

$$R_{ik} = \sum R_j \Rightarrow (R_j \in [path(s \rightarrow i) \cap path(s \rightarrow k)])$$

$$\tau_{Di} = \sum_{k=1}^N C_k R_{ik}$$

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Apply (preclass 1)

- What is Elmore delay?
 - $S \rightarrow Z$

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SPICE Response

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Elmore Delay: Special Ladder Case

- For each resistor C_k in path
 - Compute R_{kk} = sum of all R_s upstream of C_k

$$\tau_{DN} = \sum_{k=1}^N C_k \sum_{j=1}^k R_j = \sum_{k=1}^N C_k R_{kk}$$

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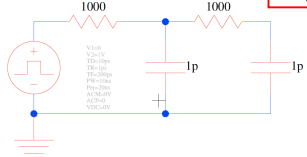
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Elmore Delay: Special Ladder Case

- For each resistor C_k in path
 - Compute $R_{k,k}$ = sum of all Rs upstream of C_k

$$\tau_{DN} = \sum_{k=1}^N C_k \sum_{j=1}^k R_j = \sum_{k=1}^N C_k R_{kk}$$

$$C_1*(R_1)+C_2*(R_1+R_2)$$



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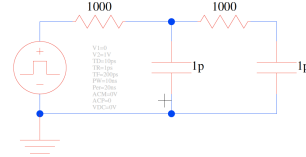
Elmore Delay: Special Ladder Case

- For each resistor C_k in path
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$$\tau_{DN} = \sum_{k=1}^N C_k \sum_{j=1}^k R_j = \sum_{k=1}^N C_k R_{kk}$$

$$C_1*(R_1)+C_2*(R_1+R_2)$$

$$\begin{aligned} &= 3RC \\ &= 3ns \end{aligned}$$



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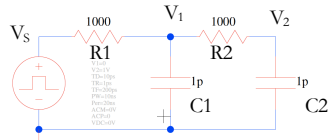
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Compare KCL: Setup

- Equations from KCL?

$$\text{@V}_1: \frac{V_S - V_1}{R_1} = \frac{V_1 - V_2}{R_2} + C_1 \frac{dV_1}{dt}$$

$$\text{@V}_2: \frac{V_1 - V_2}{R_2} = C_2 \frac{dV_2}{dt}$$



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Compare KCL: Math

@V₁:

$$\frac{V_S - V_1}{R_1} = \frac{V_1 - V_2}{R_2} + C_1 \frac{dV_1}{dt}$$

$$\frac{V_S}{R_1} = \frac{V_1}{R_1} + \frac{V_1 - V_2}{R_2} + C_1 \frac{dV_1}{dt}$$

$$V_S = V_1 \left(1 + \frac{R_1}{R_2} \right) - \frac{R_1 V_2}{R_2} + R_1 C_1 \frac{dV_1}{dt}$$

@V₂:

$$\frac{V_1 - V_2}{R_2} = C_2 \frac{dV_2}{dt}$$

$$\frac{V_1}{R_2} = \frac{V_2}{R_2} + C_2 \frac{dV_2}{dt}$$

$$V_1 = V_2 + R_2 C_2 \frac{dV_2}{dt}$$

$$\frac{dV_1}{dt} = \frac{dV_2}{dt} + R_2 C_2 \frac{d^2 V_2}{dt^2}$$

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Compare KCL: Math

$$V_S = V_1 \left(1 + \frac{R_1}{R_2} \right) - \frac{R_1 V_2}{R_2} + R_1 C_1 \frac{dV_1}{dt}$$

$$V_S = \left(V_2 + R_2 C_2 \frac{dV_2}{dt} \right) \left(1 + \frac{R_1}{R_2} \right) - \frac{R_1 V_2}{R_2} + R_1 C_1 \left(\frac{dV_2}{dt} + R_2 C_2 \frac{d^2 V_2}{dt^2} \right)$$

$$V_S = V_2 + \left(R_2 C_2 \left(1 + \frac{R_1}{R_2} \right) + R_1 C_1 \right) \frac{dV_2}{dt} + R_1 C_1 R_2 C_2 \frac{d^2 V_2}{dt^2}$$

$$V_S = V_2 + (R_2 C_2 + R_1 C_2 + R_1 C_1) \frac{dV_2}{dt} + R_1 C_1 R_2 C_2 \frac{d^2 V_2}{dt^2}$$

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Compare KCL: Math

$$R_1 = R_2 = R$$

$$C_1 = C_2 = C$$

$$V_S = V_2 + (R_2 C_2 + R_1 C_2 + R_1 C_1) \frac{dV_2}{dt} + R_1 C_1 R_2 C_2 \frac{d^2 V_2}{dt^2}$$

$$V_S = V_2 + 3RC \frac{dV_2}{dt} + R^2 C^2 \frac{d^2 V_2}{dt^2}$$

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Compare KCL: Math

$$R_1 = R_2 = R$$

$$C_1 = C_2 = C$$

$$V_S = V_2 + (R_2 C_2 + R_1 C_2 + R_1 C_1) \frac{dV_2}{dt} + R_1 C_1 R_2 C_2 \frac{d^2 V_2}{dt^2}$$

$$V_S = V_2 + 3RC \frac{dV_2}{dt} + R^2 C^2 \frac{d^2 V_2}{dt^2}$$

$$V_2 = A(1 + e^{-\alpha t}) \rightarrow$$

$$V_S = A(1 + e^{-\alpha t}) - 3RC \cdot \alpha A e^{-\alpha t} + R^2 C^2 \cdot \alpha^2 A e^{-\alpha t}$$

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Compare KCL: Math

$$V_2 = A(1 + e^{-\alpha t}) \rightarrow$$

$$V_S = A(1 + e^{-\alpha t}) - 3RC \cdot \alpha A e^{-\alpha t} + R^2 C^2 \cdot \alpha^2 A e^{-\alpha t}$$

$$t = \infty \rightarrow V_2 = V_S = A$$

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Compare KCL: Math

$$V_2 = A(1 + e^{-\alpha t}) \rightarrow$$

$$V_S = A(1 + e^{-\alpha t}) - 3RC \cdot \alpha A e^{-\alpha t} + R^2 C^2 \cdot \alpha^2 A e^{-\alpha t}$$

$$t = \infty \rightarrow V_2 = V_S = A$$

$$V_S = V_2(1 + e^{-\alpha t}) - 3RC \cdot \alpha V_2 e^{-\alpha t} + R^2 C^2 \cdot \alpha^2 V_2 e^{-\alpha t}$$

$$0 = e^{-\alpha t} - 3RC \cdot \alpha e^{-\alpha t} + R^2 C^2 \cdot \alpha^2 e^{-\alpha t}$$

$$0 = e^{-\alpha t} (1 - 3RC\alpha + R^2 C^2 \cdot \alpha^2)$$

$$0 = 1 - 3RC\alpha + R^2 C^2 \cdot \alpha^2$$

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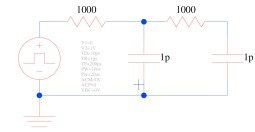
Compare KCL: Math

$$V_2 = V_S(1 + e^{-\alpha t})$$

$$0 = 1 - 3RC\alpha + R^2 C^2 \cdot \alpha^2$$

$$\alpha = \frac{3RC \pm \sqrt{9(RC)^2 - 4(RC)^2}}{2(RC)^2} = \frac{3RC \pm \sqrt{5}RC}{2(RC)^2} = \frac{3 \pm \sqrt{5}}{2RC}$$

$$\rightarrow \tau = \frac{2}{3 \pm \sqrt{5}} RC \approx 2.6RC$$



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Compare KCL: Math

$$V_2 = V_S(1 + e^{-\alpha t})$$

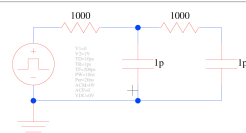
$$0 = 1 - 3RC\alpha + R^2 C^2 \cdot \alpha^2$$

$$\alpha = \frac{3RC \pm \sqrt{9(RC)^2 - 4(RC)^2}}{2(RC)^2} = \frac{3RC \pm \sqrt{5}RC}{2(RC)^2} = \frac{3 \pm \sqrt{5}}{2RC}$$

$$\rightarrow \tau = \frac{2}{3 \pm \sqrt{5}} RC \approx 2.6RC$$

$$= 3RC$$

$$= 3ns$$



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Elmore Delay: Distributed RC network

- The delay from source to node i

- N = number of nodes in circuit

$$R_{ik} = \sum R_j \Rightarrow (R_j \in [path(s \rightarrow i) \cap path(s \rightarrow k)])$$

$$\tau_{Di} = \sum_{k=1}^N C_k R_{ik}$$

- Special ladder case

$$\tau_{DN} = \sum_{k=1}^N C_k \sum_{j=1}^k R_j = \sum_{k=1}^N C_k R_{kk}$$

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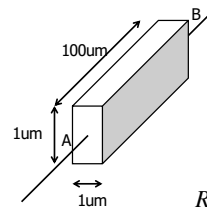
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Wire Delay



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Wire Resistance



$$R = \frac{\rho L}{A}$$

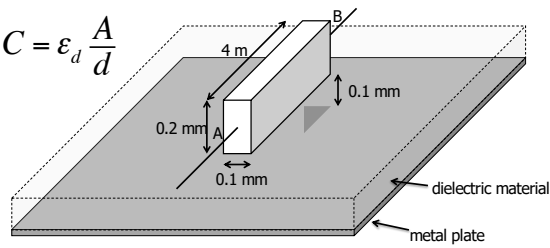
$$R = \frac{10^{-7} \Omega \cdot m \cdot 100 \mu m}{1 \mu m \cdot 1 \mu m} = 10 \Omega$$

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Wire Capacitance

$$C = \epsilon_d \frac{A}{d}$$

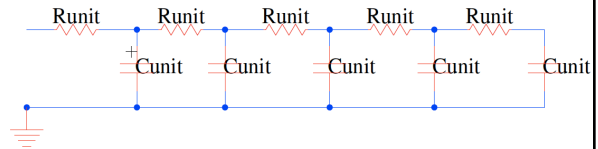


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Wire as Distributed RC Ladder

- Measure wire length in units
 - Say λ
 - Each λ unit has C_{unit} , R_{unit}
 - Unit capacitance and resistance of wire of length λ

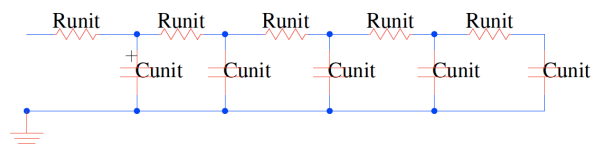


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Wire Delay

- Delay of Wire N units long:



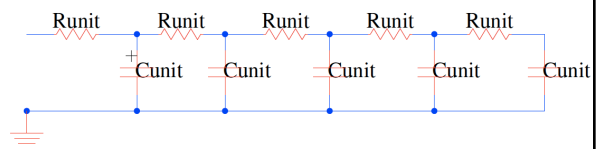
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Wire Delay

- Delay of Wire N units long:

$$R_{\text{unit}} C_{\text{unit}}$$



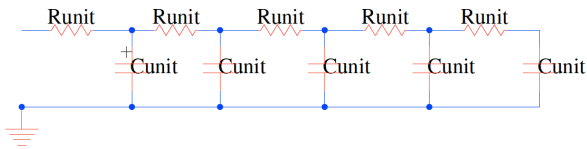
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Wire Delay

- Delay of Wire N units long:

$$R_{\text{unit}}C_{\text{unit}} + 2R_{\text{unit}}C_{\text{unit}}$$



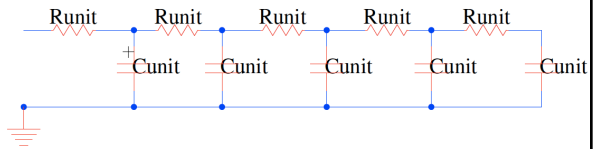
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Wire Delay

- Delay of Wire N units long:

$$R_{\text{unit}}C_{\text{unit}} + 2R_{\text{unit}}C_{\text{unit}} + 3R_{\text{unit}}C_{\text{unit}} + \dots + NR_{\text{unit}}C_{\text{unit}} = (R_{\text{unit}}C_{\text{unit}})(N + (N-1) + (N-2) + \dots + 1)$$



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Sum of integers (preclass 2)

- What's the sum of the integer 1 to N?

$$\sum_{k=0}^N k =$$

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Sum of integers

- What's the sum of the integer 1 to N?

$$\sum_{k=0}^N k = \frac{N(N+1)}{2} \approx \frac{N^2}{2}$$

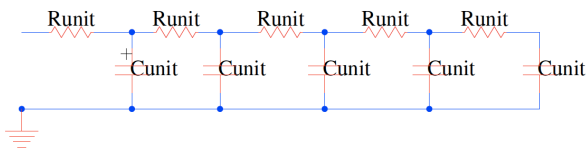
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Wire Delay (preclass 3)

- Delay of Wire N units long:

$$R_{\text{unit}}(N \times C_{\text{unit}}) + R_{\text{unit}}((N-1) \times C_{\text{unit}}) + R_{\text{unit}}(N-2) \times C_{\text{unit}} + \dots + R_{\text{unit}} \times C_{\text{unit}} = (R_{\text{unit}} \times C_{\text{unit}})(N + N-1 + N-2 + \dots + 1) \approx R_{\text{unit}} \times C_{\text{unit}} \times N^2 / 2$$



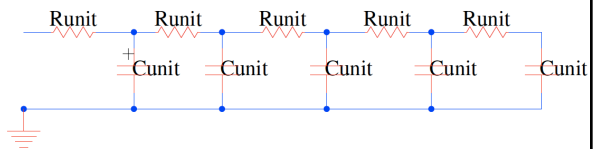
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Lumped RC Wire? (preclass 4)

- What would the delay be if we treated the wire as lumped R and C?

$$R_{\text{wire}} = N \times R_{\text{unit}} \quad C_{\text{wire}} = N \times C_{\text{unit}}$$



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Wire Delay

- $R_{\text{wire}} = N \cdot R_{\text{unit}}$
- $C_{\text{wire}} = N \cdot C_{\text{unit}}$
- Lumped RC wire delay = $R_{\text{unit}} \cdot C_{\text{unit}} \cdot N^2$
- Distributed RC Wire delay = $R_{\text{unit}} \cdot C_{\text{unit}} \cdot N^2 / 2$

- Distributed has half the delay of lumped RC product
- Delay is quadratic in length of wire in both cases

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Apply to Gates

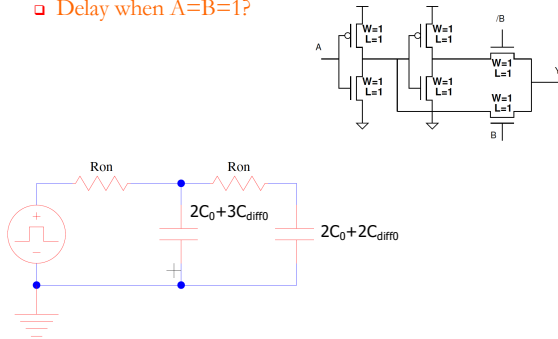
Pass Transistor and CMOS



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Pass Transistor XOR

- Delay when $A=B=1$?



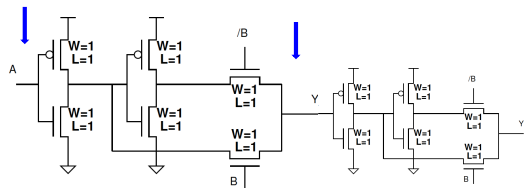
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Pass Transistor XOR (preclass 5)

- Delay when $A=1, B=0$?

- Start with equivalent RC circuit



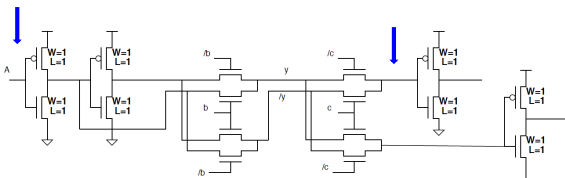
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Unbuffered (preclass 6)

- Circuit → Delay?

- 2 stages



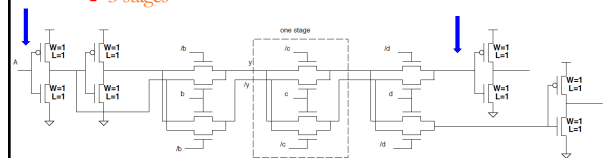
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Unbuffered (preclass 7)

- Circuit → Delay?

- 3 stages

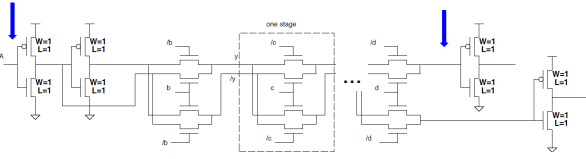


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Unbuffered (preclass 8)

- Delay as a function of number of stages, k ?

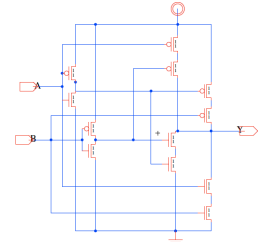


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CMOS XOR (preclass 9)

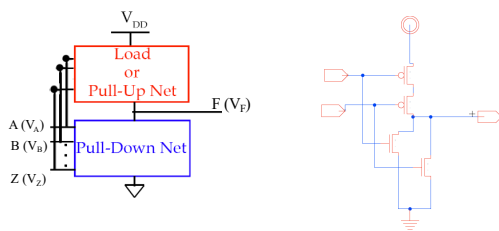
- Delay with $C_{diff} > 0$?



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Review: Two-Input NOR Gate (NOR2)

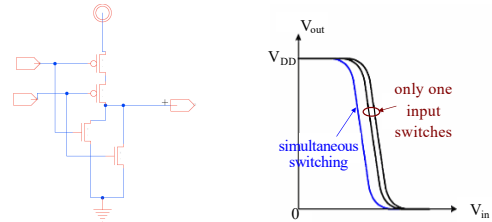


- Worst case delay of NOR2?
 - Minimum size, Loaded with itself

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NOR2 Transfer Curve



- 3 VTC Cases
 - $V_1 = 0 V; V_2 = 0 \rightarrow V_{DD}$
 - $V_1 = 0 \rightarrow V_{DD}; V_2 = 0$
 - $V_1 \text{ and } V_2 = 0 \rightarrow V_{DD} \text{ simultaneously}$

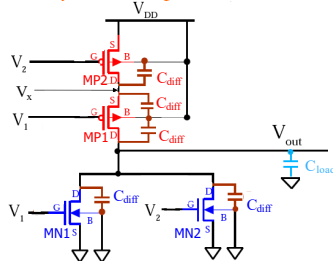
Switching Threshold Voltage:
 $V_1 = V_2 = V_{out} = V_t$

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NOR2 Delay (preclass 10)

- Worst case delay for Pull-up?

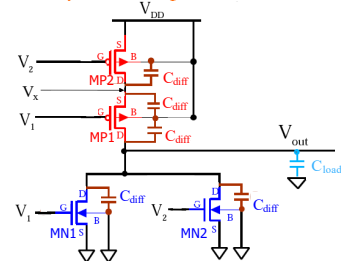


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NOR2 Delay

- Worst case delay for Pull-up?



Worst Case for Pull-up $\rightarrow V_1 = 0, V_2 = V_{DD} > 0 @ t=0 \& V_x \approx V_{out} = 0 \rightarrow V_{DD}$

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NOR2 Delay

Worst case delay for Pull-up?

$$C_{load-NR2} \approx 2C_{diff} + 3C_{diff} + C_{load}$$

$$R_{EQV} = R_{p2} + R_{p1}$$

Lumped Model

Worst Case for Pull-up $\rightarrow V_1 = 0, V_2 = V_{DD} > 0 @ t=0 \& V_x \approx V_{out} = 0 \rightarrow V_{DD}$

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NOR2 Delay

Worst case delay for Pull-up?

$$C_{load-NR2} \approx 2C_{diff} + 3C_{diff} + C_{load}$$

$$= 5\gamma C_0 + 2C_0$$

$$R_{EQV} = R_{p2} + R_{p1} = 2R_0$$

Lumped Model

Worst Case for Pull-up $\rightarrow V_1 = 0, V_2 = V_{DD} > 0 @ t=0 \& V_x \approx V_{out} = 0 \rightarrow V_{DD}$

$$\text{delay} = (5\gamma C_0 + 2C_0)(2R_0) = (10\gamma + 4)\tau$$

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NOR2 Delay

Worst case delay?

$$C_{load-NR2} \approx 2C_{diff} + 3C_{diff} + C_{load}$$

$$= 5\gamma C_0 + 2C_0$$

$$R_{EQV} = R_{p2} + R_{p1} = 2R_0$$

Elmore Model?

Worst Case for Pull-up $\rightarrow V_1 = 0, V_2 = V_{DD} > 0 @ t=0 \& V_x \approx V_{out} = 0 \rightarrow V_{DD}$

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NOR2 Delay

Worst case delay?

$$C_{load-NR2} \approx 2C_{diff} + 3C_{diff} + C_{load}$$

$$= 5\gamma C_0 + 2C_0$$

$$R_{EQV} = R_{p2} + R_{p1} = 2R_0$$

Elmore Model?

Worst Case for Pull-up $\rightarrow V_1 = 0, V_2 = V_{DD} > 0 @ t=0 \& V_x \approx V_{out} = 0 \rightarrow V_{DD}$

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NOR2 Delay

Worst case delay?

$$C_{load-NR2} \approx 2C_{diff} + 3C_{diff} + C_{load}$$

$$= 5\gamma C_0 + 2C_0$$

$$R_{EQV} = R_{p2} + R_{p1} = 2R_0$$

Elmore Model?

Worst Case for Pull-up $\rightarrow V_1 = 0, V_2 = V_{DD} > 0 @ t=0 \& V_x \approx V_{out} = 0 \rightarrow V_{DD}$

$$\text{delay} = (2C_{diff})(R_{p2}) + (3C_{diff} + C_{load})(R_{p1} + R_{p2}) = (8\gamma + 4)\tau$$

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NOR2 Delay

Worst case delay Pull-down?

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NOR2 Delay

□ Worst case delay Pull-down?

Worst case for Pull-down $\rightarrow V_1 = 0, V_2 = 0 \rightarrow V_{DD} @ t=0$ & $V_x \approx V_{out} = V_{DD} > 0$

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NOR2 Delay

□ Worst case delay Pull-down?

Elmore Model?

Worst case for Pull-down $\rightarrow V_1 = 0, V_2 = 0 \rightarrow V_{DD} @ t=0$ & $V_x \approx V_{out} = V_{DD} > 0$

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NOR2 Delay

□ Worst case delay Pull-down?

Elmore Model?

Worst case for Pull-down $\rightarrow V_1 = 0, V_2 = 0 \rightarrow V_{DD} @ t=0$ & $V_x \approx V_{out} = V_{DD} > 0$

$$\text{delay} = (2C_{diff})(R_{p1} + R_{n2}) + (3C_{diff} + C_{load})(R_{n2}) = (7\gamma + 2)\tau$$

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NAND2 Delay (preclass 11)

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Parasitic Caps for NAND2 (worst case)

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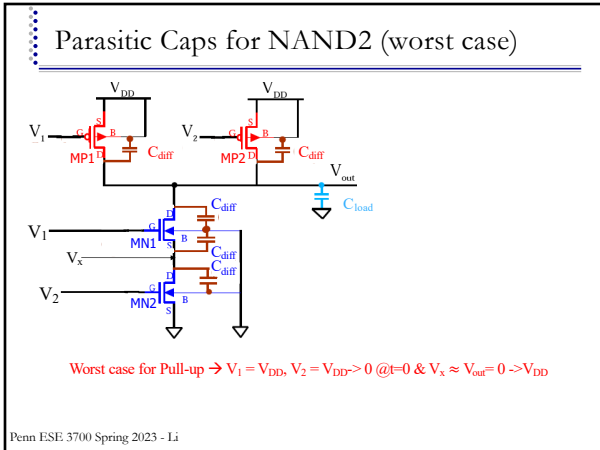
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Parasitic Caps for NAND2 (worst case)

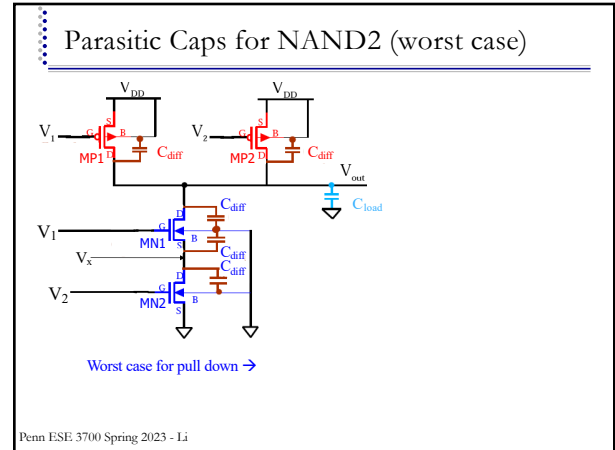
Worst case for Pull-up \rightarrow

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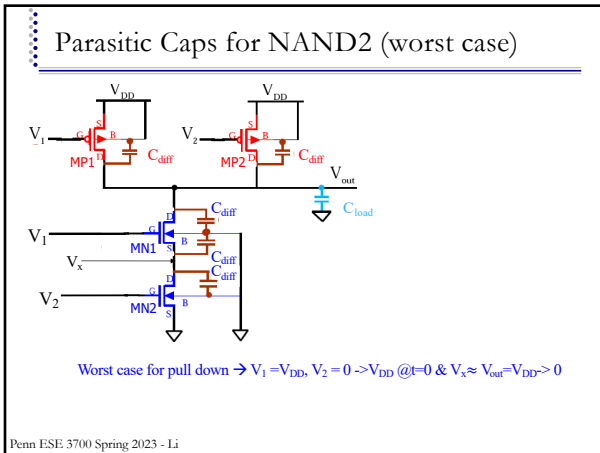
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- ### Logic Types
- CMOS Gates
 - Dual pull-down and pull-up networks, only one enabled at a time
 - Performance of gate is strong function of the fanin of gate
 - Techniques to improve performance include sizing, input reordering, and buffering (staging)
 - Ratioed Gates
 - Have active pull-down (-up) network connected to load device
 - Reduced gate complexity at expense of static power asymmetric transfer function
 - Techniques to improve performance include sizing to improve noise margins and reduce static power
 - Pass Gates
 - Implement logic gate as switch network for area and often delay win
 - Long cascades of switches result in quadratic increase in delay
 - Also suffer from reduced noise margins (V_I drop)
 - Use level-restoring buffers to improve noise margins
 - Dynamic logic ... next time
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- ### Idea
- Elmore delay calculation allows us to estimate delay for distributed RC network
 - Necessary for pass transistors
 - Wires are distributed RC
 - Half delay lumped calculation
 - Still quadratic in length
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- ### Admin
- Project 1
 - Final report due **Friday 3/24** midnight
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