

ESE370: Circuit-Level Modeling, Design, and Optimization for Digital Systems

Lec 6: February 6, 2023

MOS Transistor Operating Regions

Part 2, Parasitics





Today

- Operating Regions
 - Resistive
 - Saturation
 - Subthreshold
 - Velocity Saturation
- Short Channel Effects
 - V_{th}
 - Drain Induced Barrier Lowering
- Capacitance

Velocity Saturation





Carrier Velocity

- Model assumes carrier velocity increases with field
 - Increases with voltage proportionally to mobility

$$v = \mu_n \cdot \frac{V_{DS}}{L_{eff}} = \left(\frac{\mu_n}{L_{eff}} \right) V_{DS}$$

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Preclass 1

- (a) What is the electrical field in the channel?

$$L_{eff} = 25nm, V_{DS} = 1V$$

$$\text{Uniform Field} = \frac{V_{DS}}{L_{eff}}$$

- Velocity:

$$v = F \cdot \mu_n$$

- Electron mobility: $\mu_n = 500cm^2 / (V \cdot s)$

- (b) What is the electron velocity?



Moving Charge

$$I = \left(\frac{1}{R}\right)V$$

- ❑ I increases linearly in V
- ❑ What's I?



Moving Charge

$$I = \left(\frac{1}{R}\right)V$$

- I increases
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- What's I ?
 - $\Delta Q / \Delta t$
 - Speed at which charge moves

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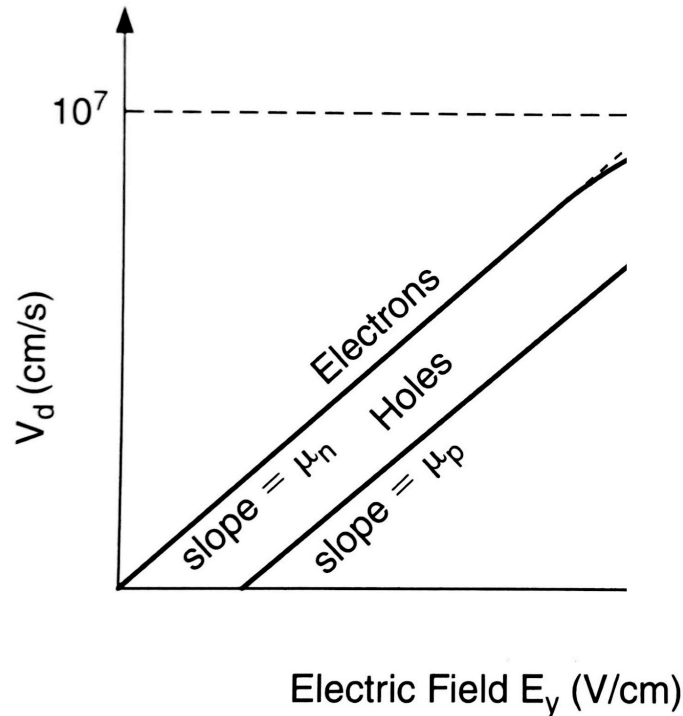
$$\text{Field} = \frac{V_{DS}}{L_{eff}}, v = \mu_n \cdot F$$

$$v = \mu_n \cdot \frac{V_{DS}}{L_{eff}} = \left(\frac{\mu_n}{L_{eff}}\right)V_{DS}$$

- Velocity increases linearly in V

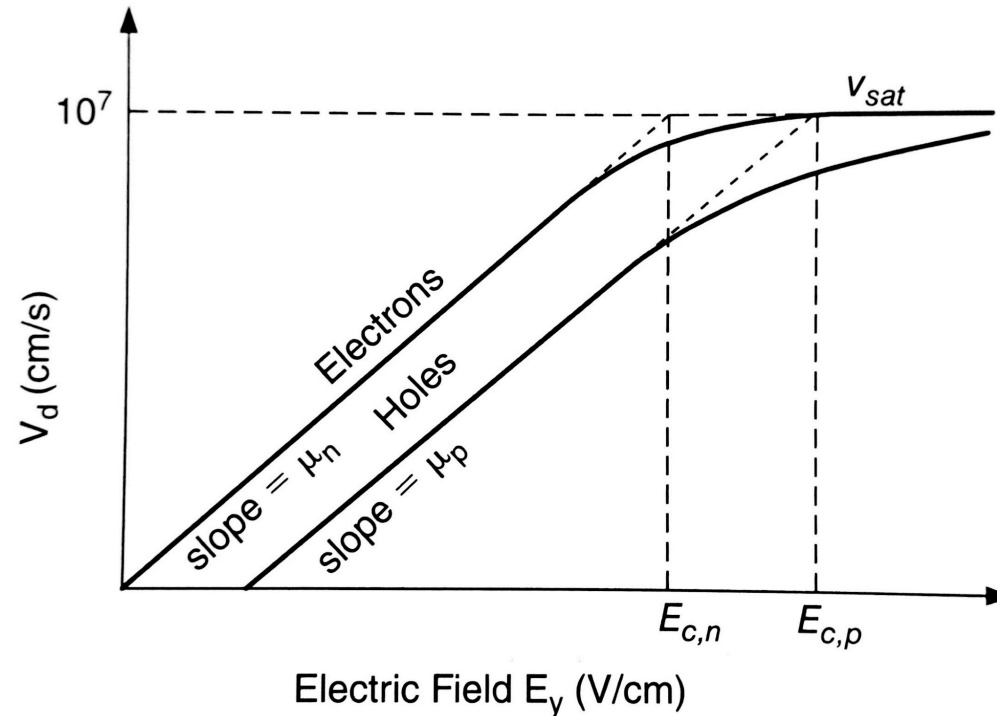
- What's a moving electron?

Carrier Velocity



- Velocity –
 - increases for increasing field with slope of mobility

Carrier Velocity



□ Velocity –

- increases for increasing field with slope of mobility
- saturates for increasing field
 - More likely to hit the critical field in short channel



Short Channel

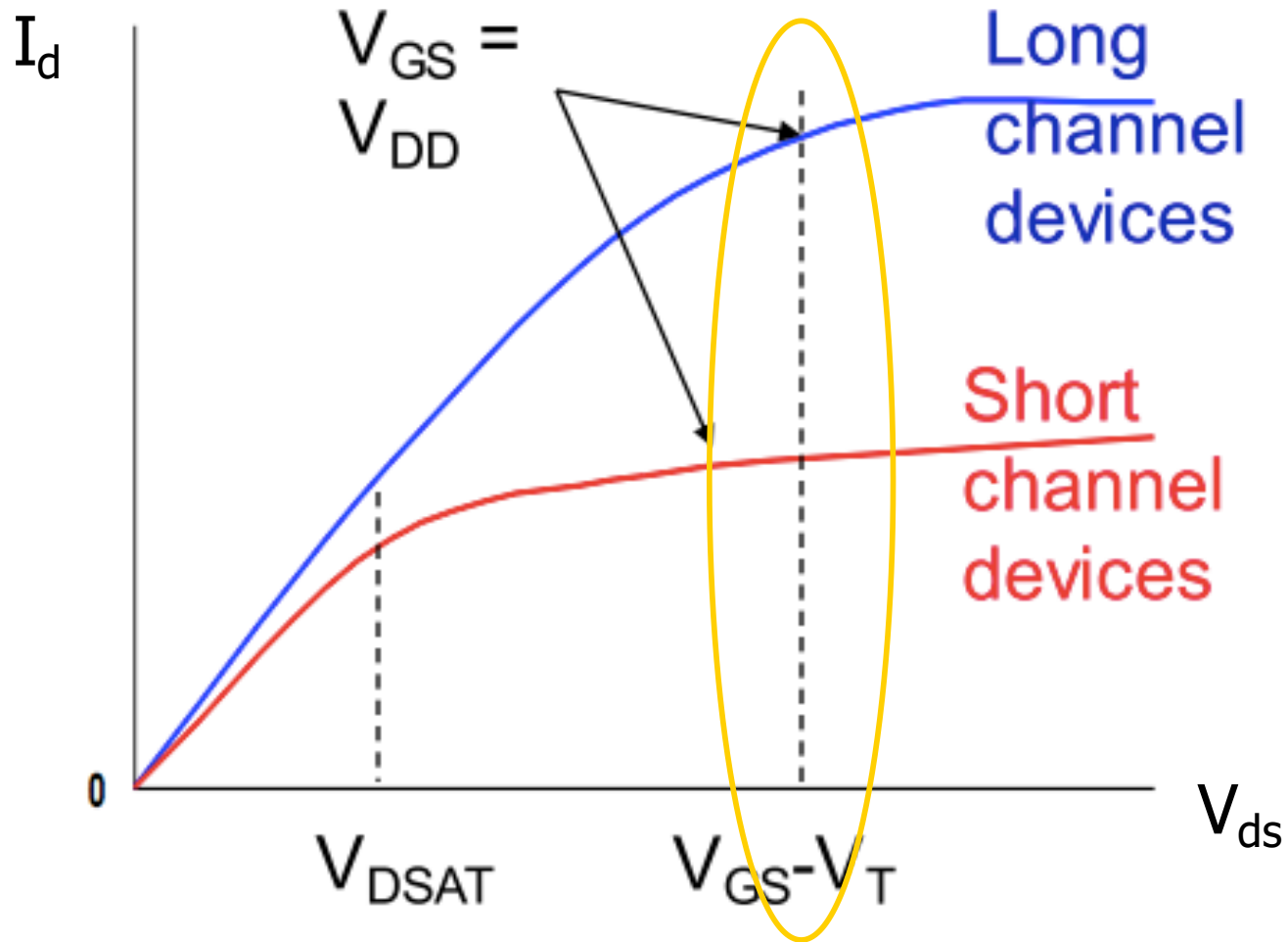
- ❑ Model assumes carrier velocity increases with field
 - Increases with voltage proportionally to mobility
- ❑ There is a limit to how fast carriers can move
 - Limited by scattering effects
 - $\sim 10^5\text{m/s}$
- ❑ Encounter *velocity saturation* when channel short
 - Modern processes, L is short enough to reach this region of operation



Velocity Saturation (Preclass 1)

- (c) At what voltage do we hit the speed limit 10^5m/s
 - $L_{\text{eff}}=25\text{nm}$, $V_{\text{ds}}=1\text{V}$
 - V_{DSAT} = voltage at which velocity (current) saturates

Velocity Saturation





Velocity Saturation

- Our current model equation:

$$I_{DS} = \mu_n C_{OX} \left(\frac{W}{L} \right) \left[(V_{GS} - V_{th}) V_{DS} - \frac{V_{DS}^2}{2} \right]$$

- Once velocity saturates:



Velocity Saturation

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- Once velocity saturates:

$$V_{DS} = V_{DSAT} \Rightarrow I_{DS} = \mu_n C_{OX} \left(\frac{W}{L} \right) \left[(V_{GS} - V_{th}) V_{DSAT} - \frac{V_{DSAT}^2}{2} \right]$$

Velocity Saturation

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$$I_{DS} = \left(\mu_n \frac{V_{DSAT}}{L} \right) C_{OX} W \left[(V_{GS} - V_{th}) - \frac{V_{DSAT}}{2} \right]$$

Velocity Saturation

- Our current model equation:

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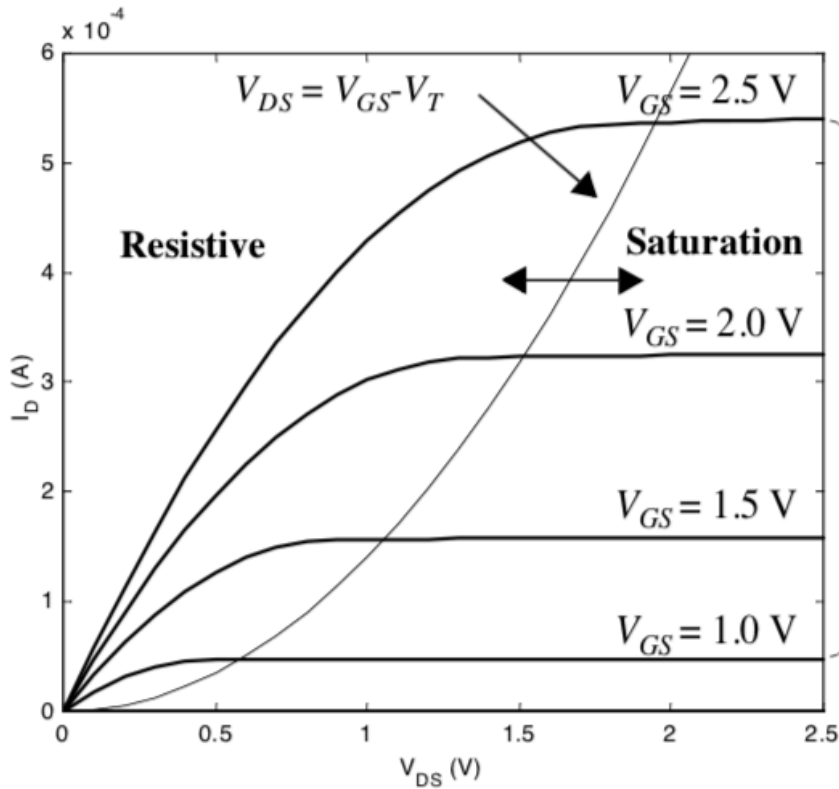
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$$I_{DS} = \left(\mu_n \frac{V_{DSAT}}{L} \right) C_{OX} W \left[(V_{GS} - V_{th}) - \frac{V_{DSAT}}{2} \right]$$

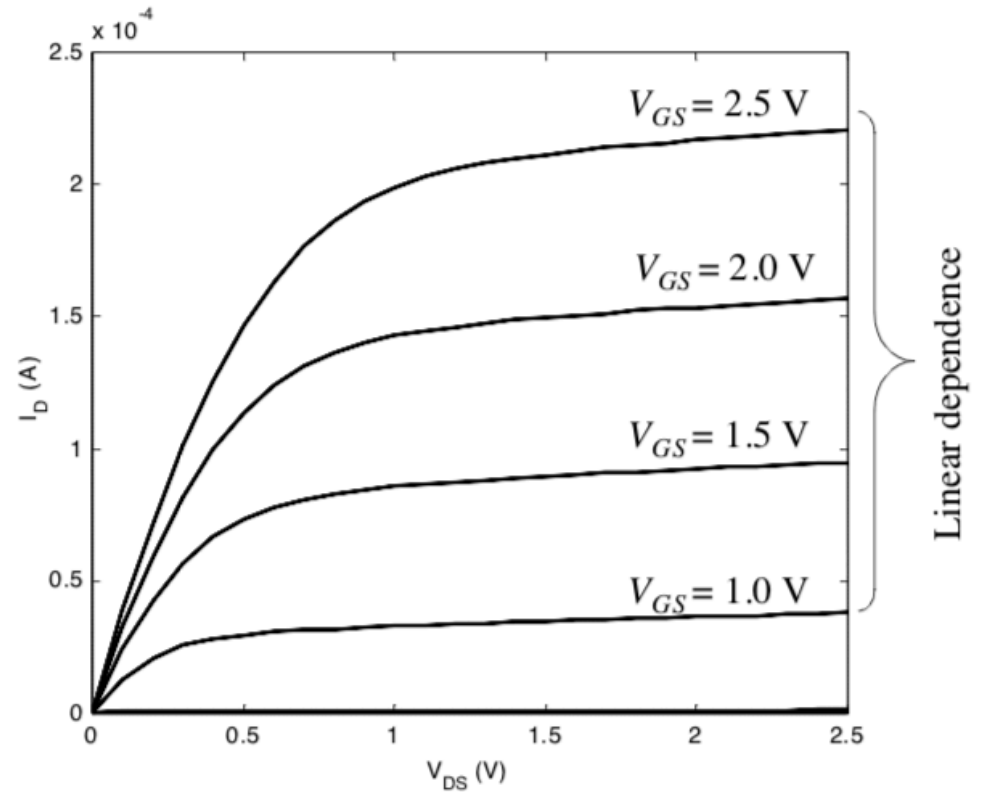
$$I_{DS} \approx v_{sat} C_{OX} W \left[(V_{GS} - V_{th}) - \frac{V_{DSAT}}{2} \right]$$

Velocity Saturation



(a) Long-channel transistor ($L_d = 10 \mu\text{m}$)

□ Long Channel

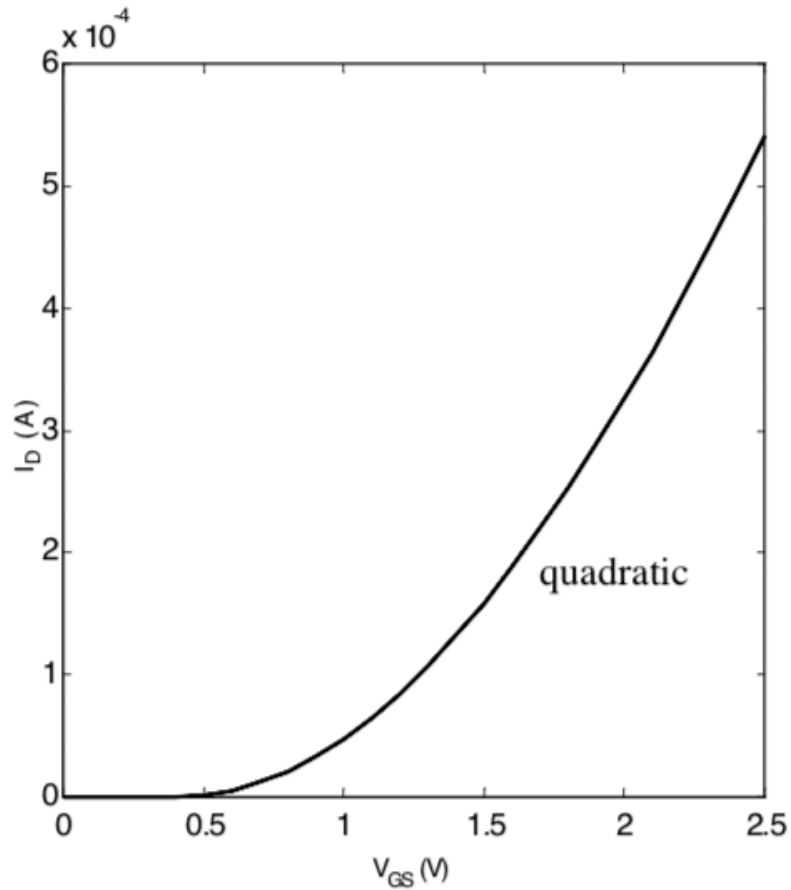


(b) Short-channel transistor ($L_d = 0.25 \mu\text{m}$)

□ Short Channel

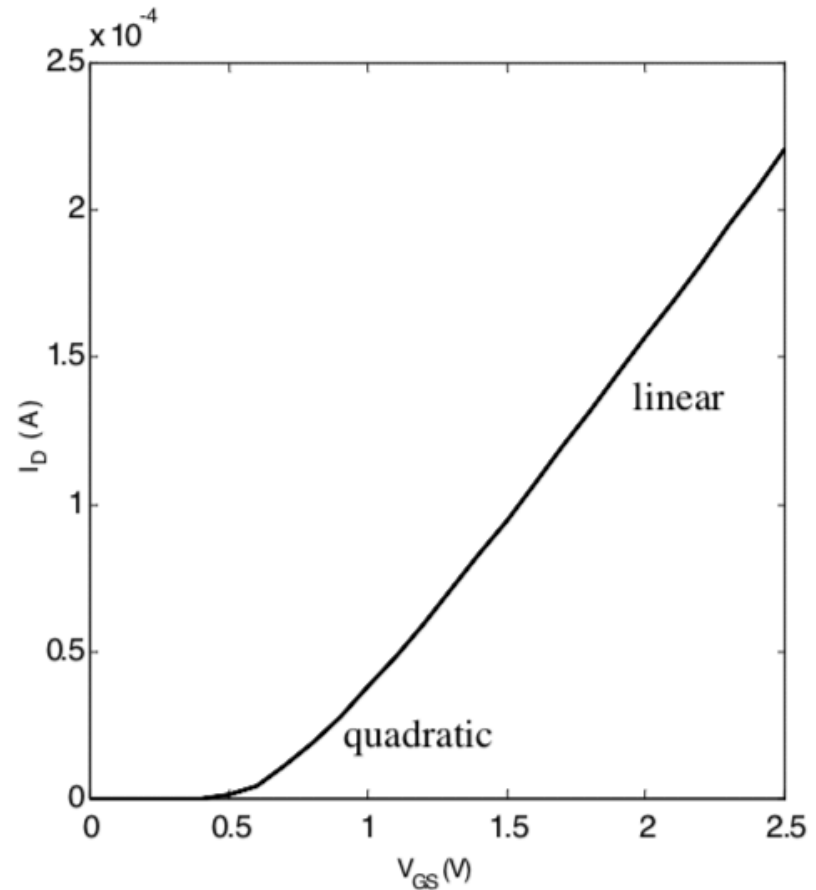


Velocity Saturation



(a) Long-channel device ($L_d = 10 \mu\text{m}$)

□ Long Channel



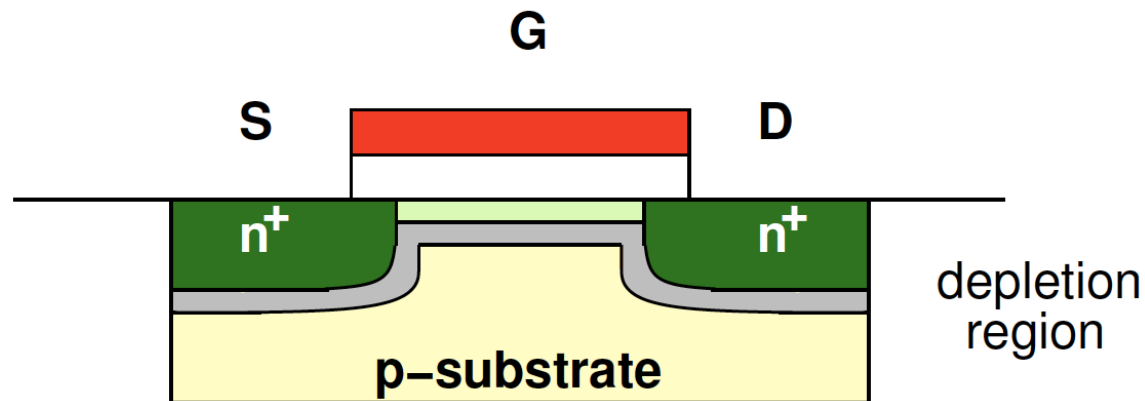
(b) Short-channel device ($L_d = 0.25 \mu\text{m}$)

□ Short Channel

Velocity Saturation

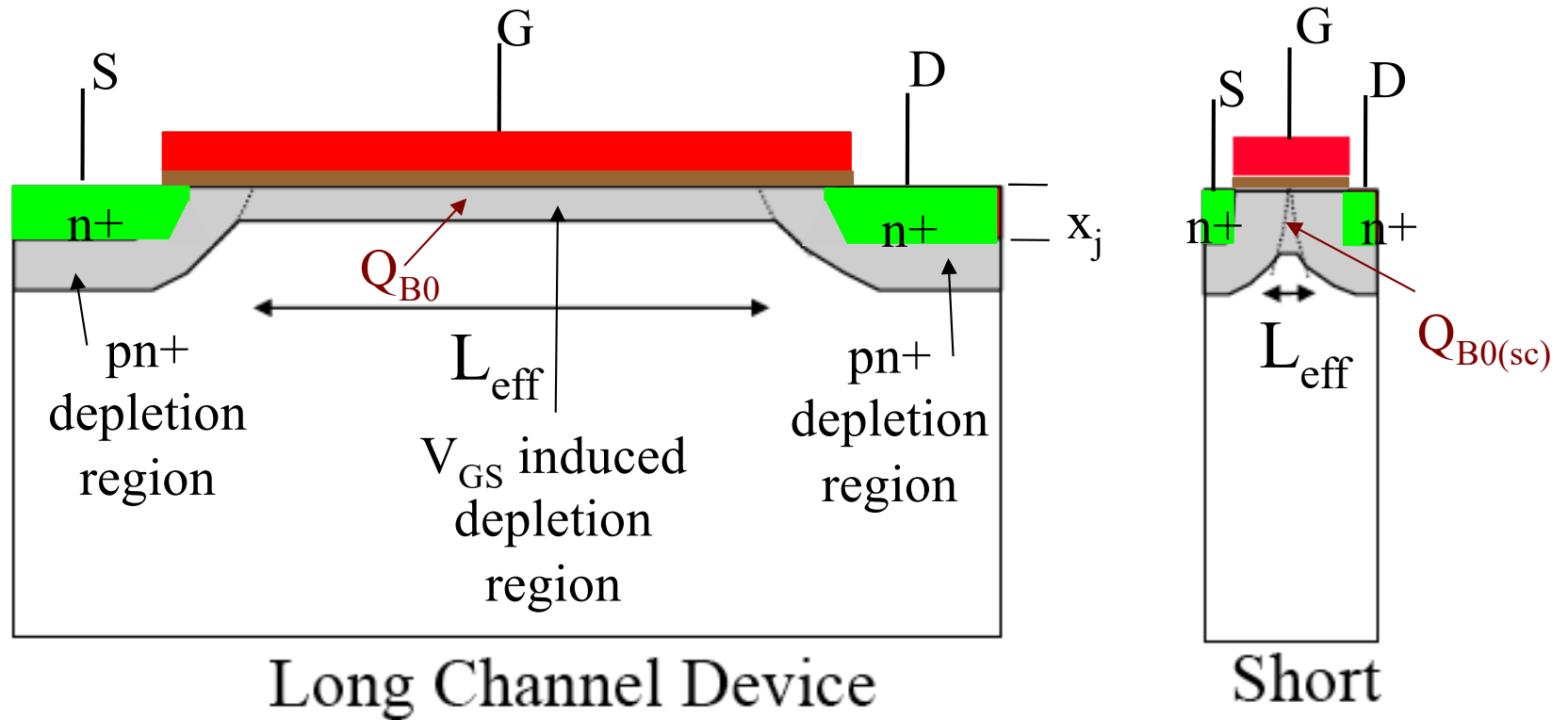
- Once velocity saturates we can still increase current with parallelism
 - Effectively make a wider device

$$I_{DS} \approx v_{sat} C_{OX} W \left[(V_{GS} - V_{th}) - \frac{V_{DSAT}}{2} \right]$$



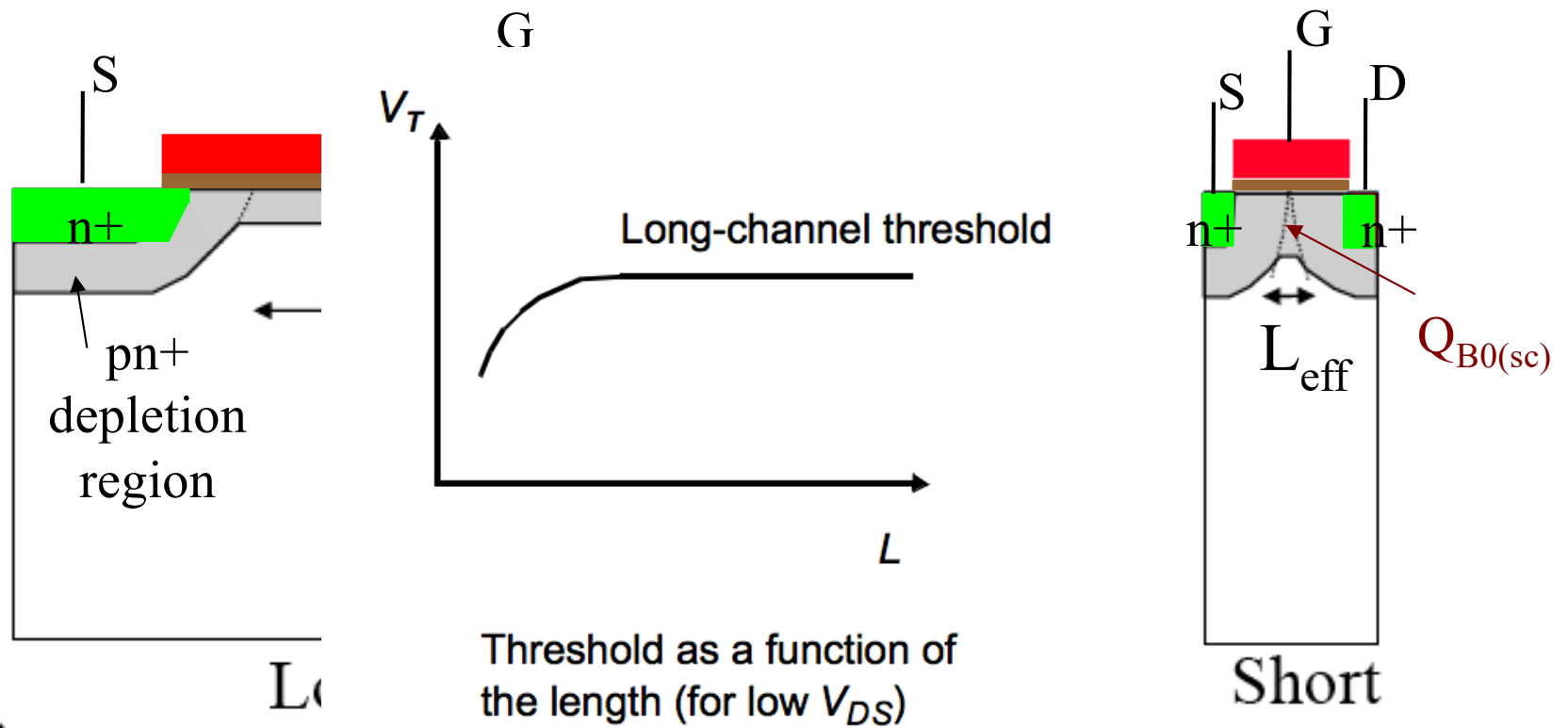
Threshold

Short Channel Effects – V_T Reduction



$$V_{T0} \text{ (short channel)} = V_{T0} - \Delta V_{T0}$$

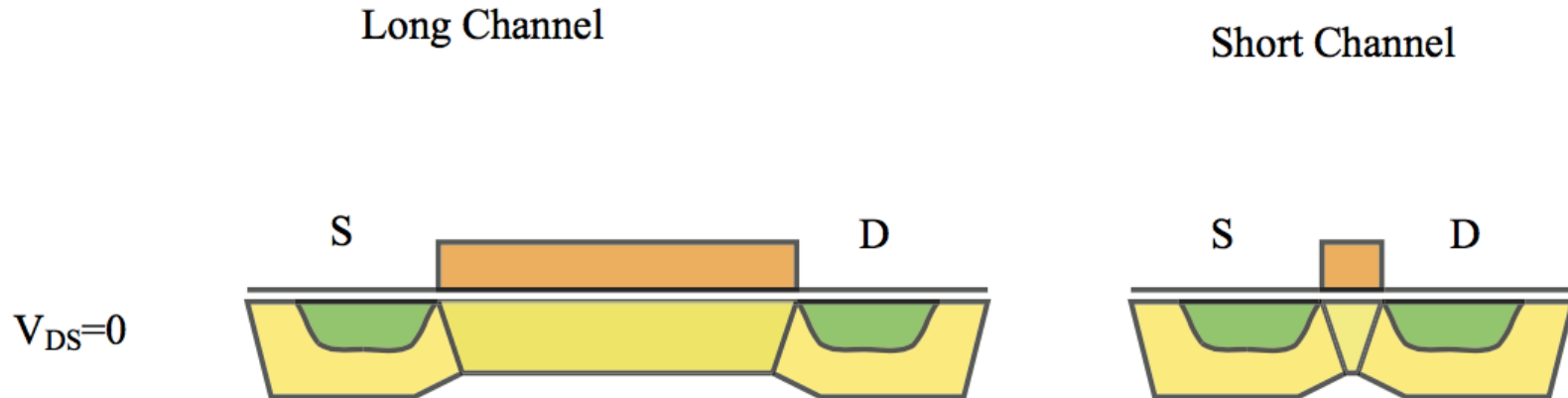
Short Channel Effects – V_T Reduction



$$V_{T0} (\text{short channel}) = V_{T0} - \Delta V_{T0}$$

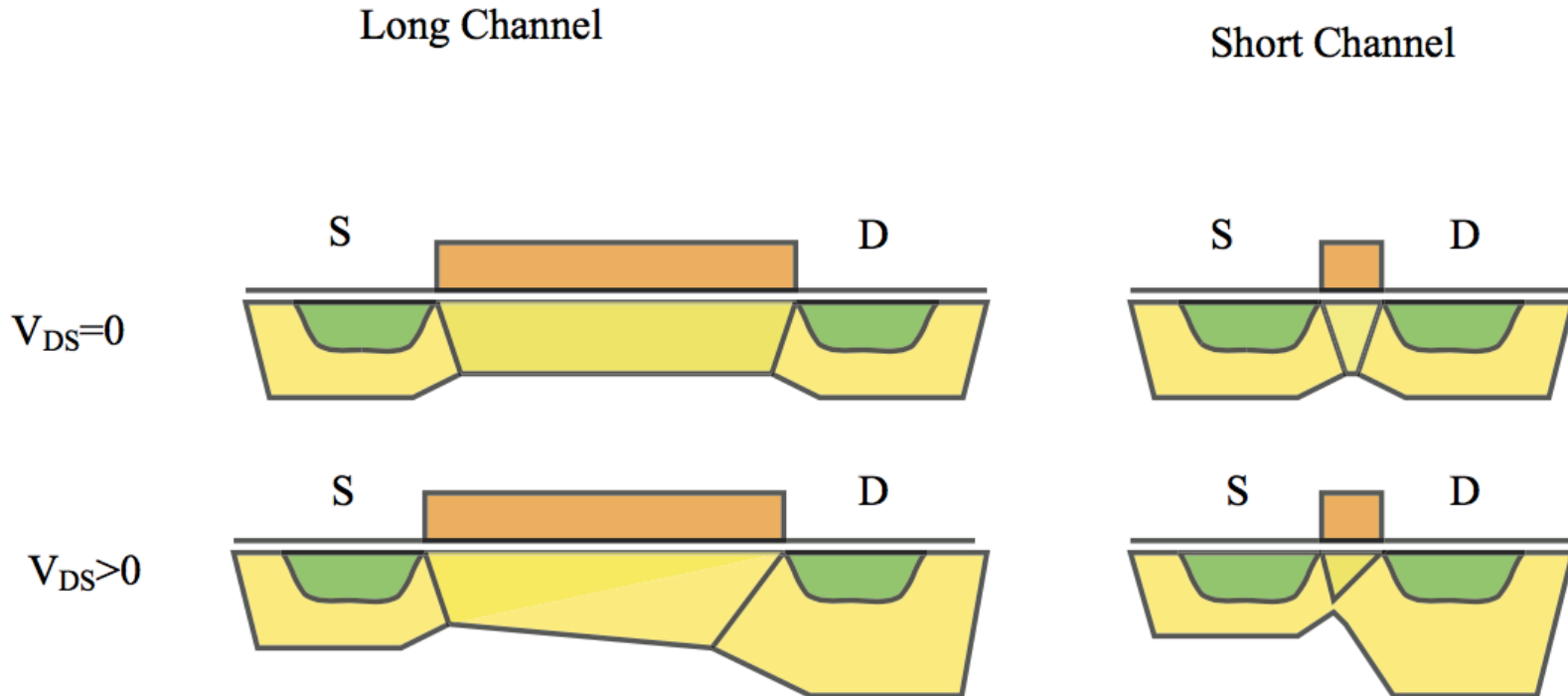
Short Channel Effects - DIBL

- Drain Induced Barrier Lowering
 - V_T Reduction with Drain Bias



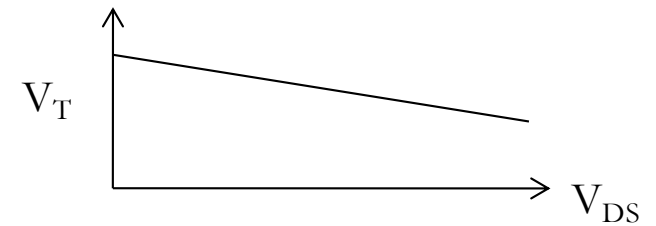
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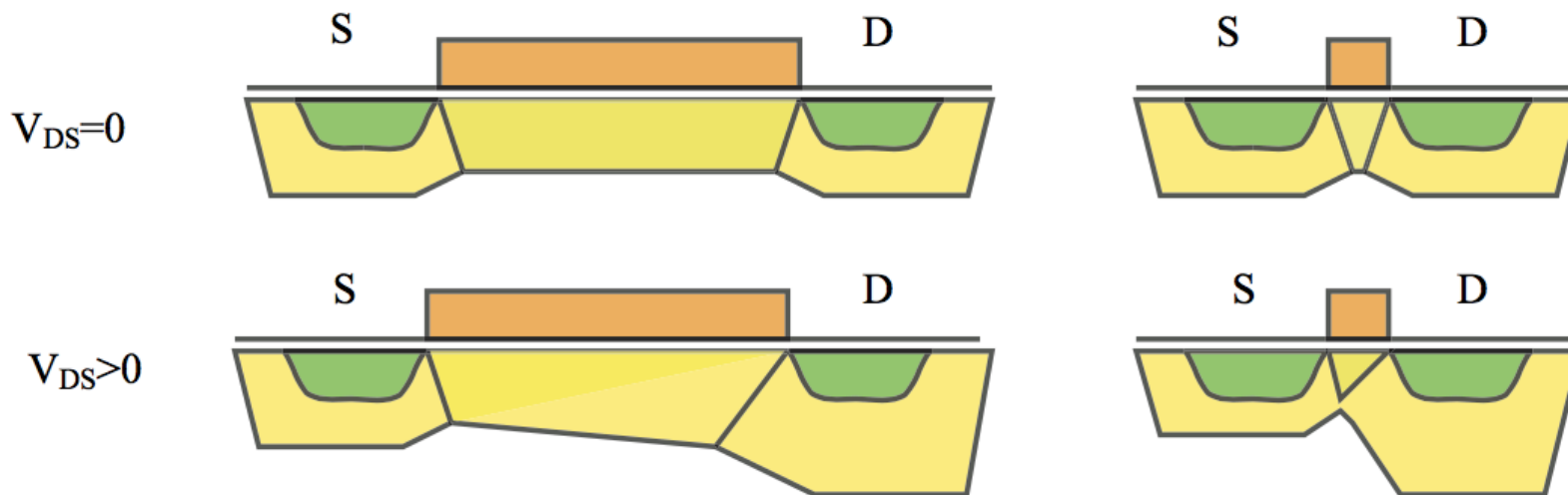
Short Channel Effects - DIBL

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Long Channel

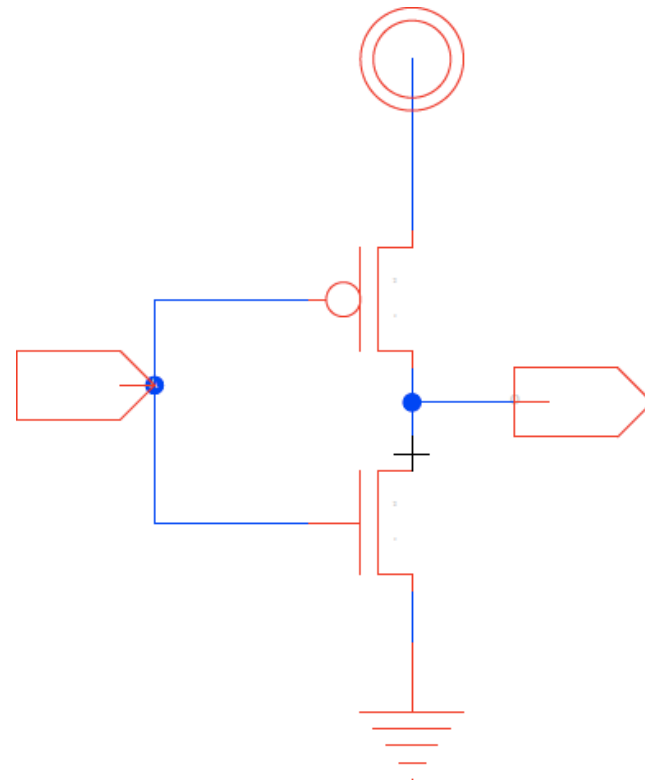
Short Channel



Threshold Reduction Impact

In a Gate?

- What does it impact most?
 - Which device, has large V_{ds} ?
 - How does this effect operation?
 - Speed of switching?
 - Leakage?



Capacitance



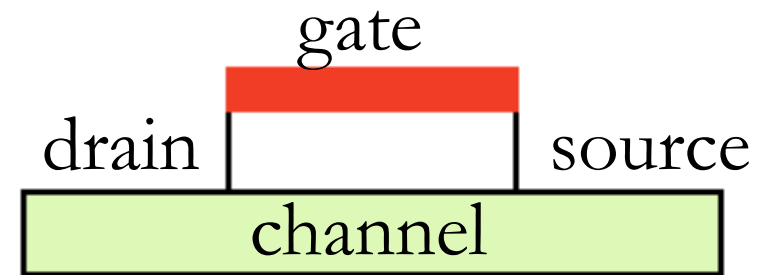
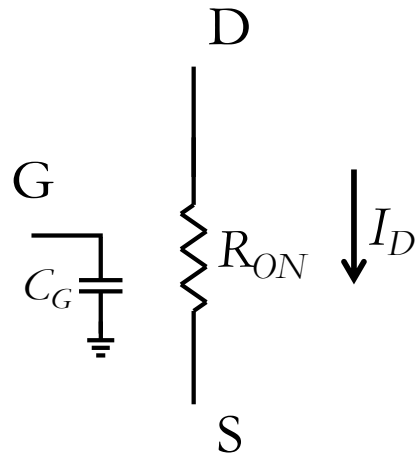


Simplified Design Flow

- ❑ Design a circuit to perform a function with specified minimum speed and optimized power (minimized with an upper bound)
 - Zero order model to design topology
 - First order model to meet speed spec
 - Rise/fall times, propagation delay, gate capacitance, output stage equivalent resistance
 - Transistor IV curves
 - Iterative SPICE simulation – tweak knobs to optimize for power (switching (dynamic), leakage (static), etc.)

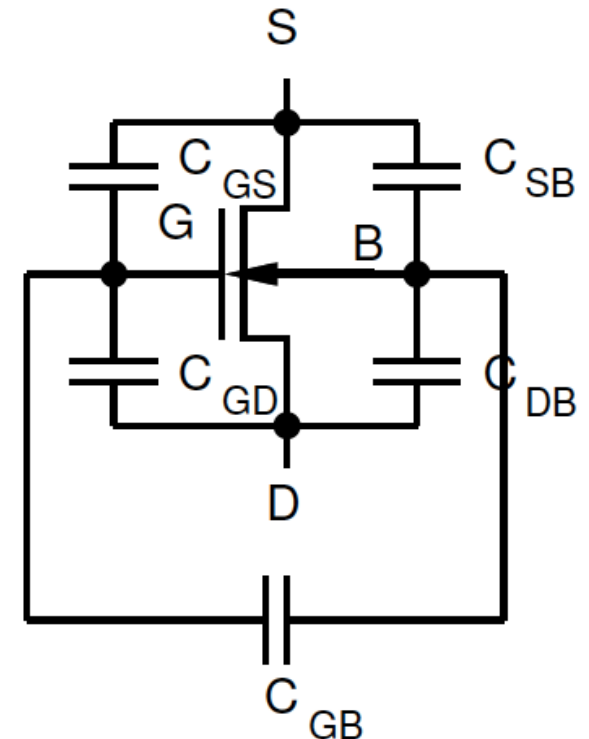
Capacitance

- First order: gate input looks like a capacitor



- Today:

- Capacitance is not constant
- Capacitance not physically to gnd
 - Modeled as such

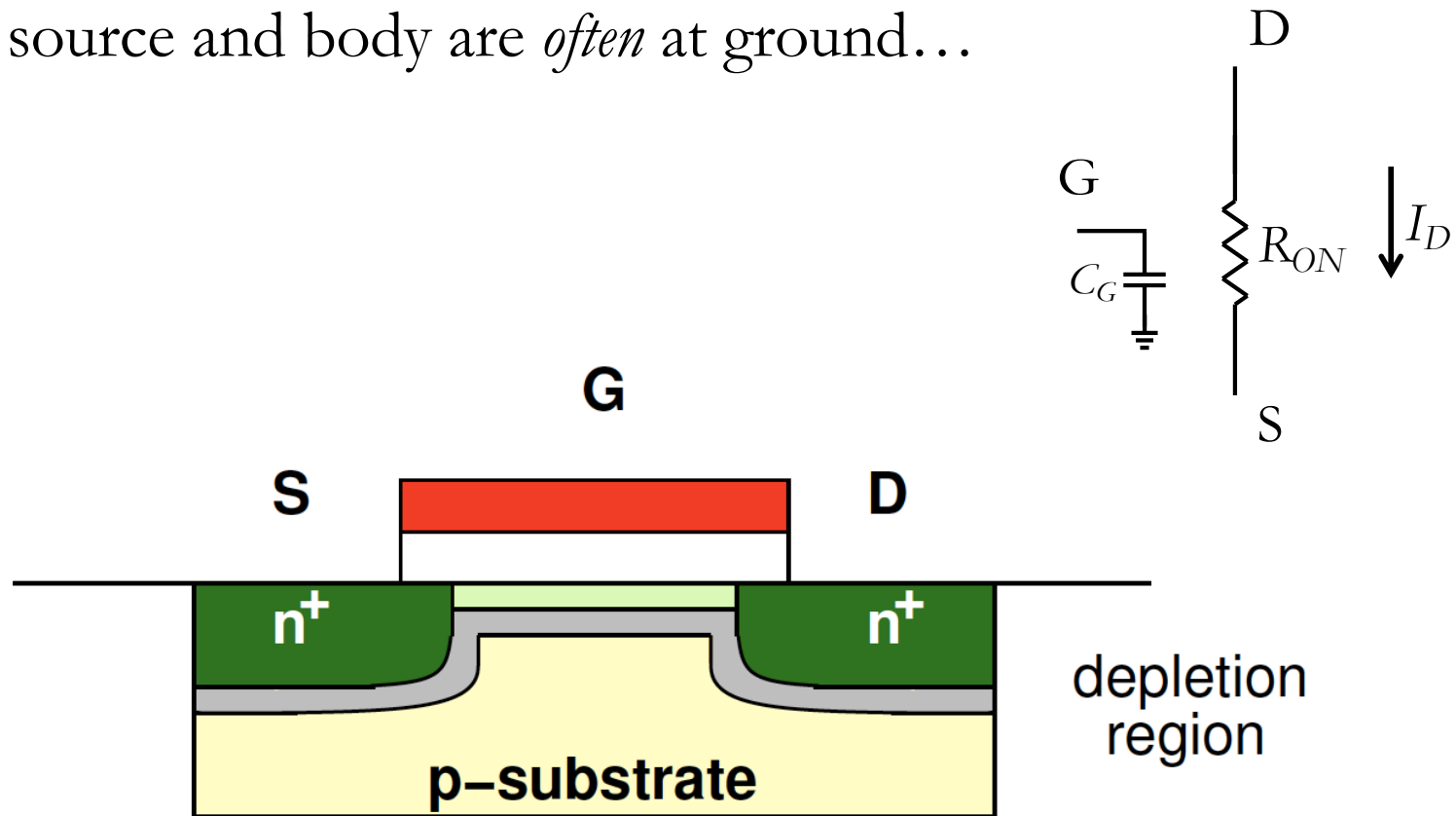


Capacitance Setup



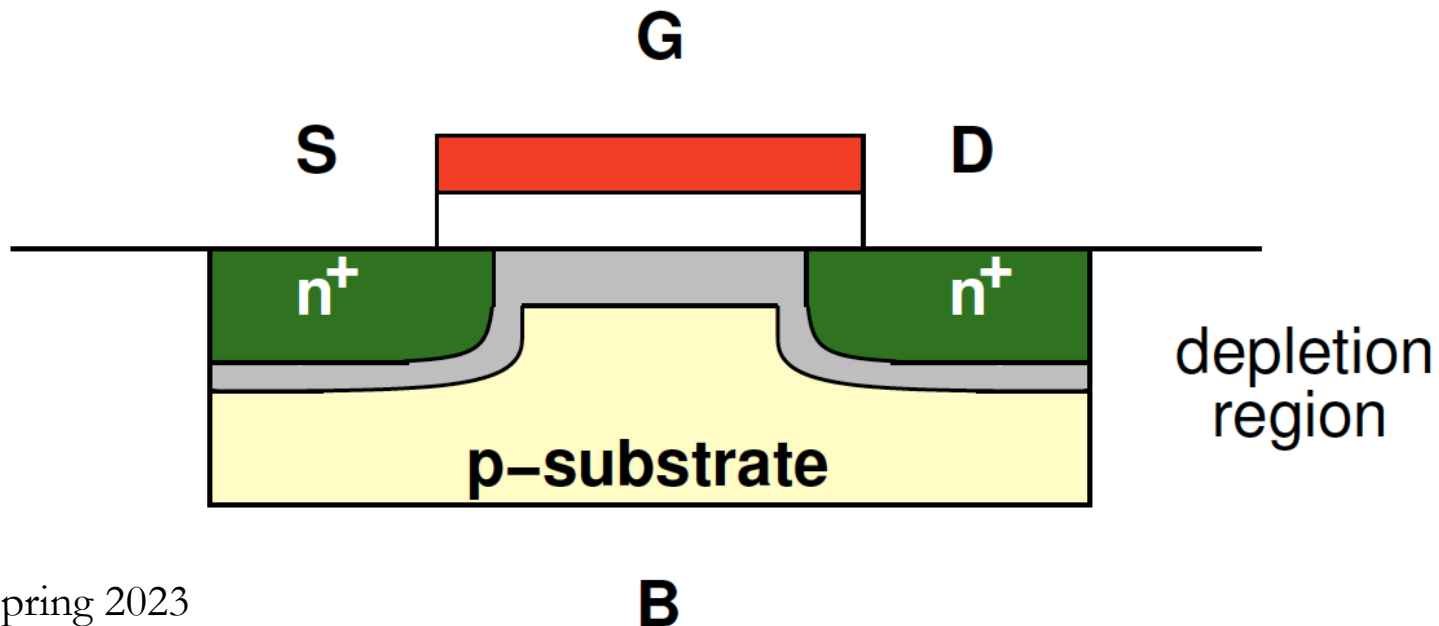
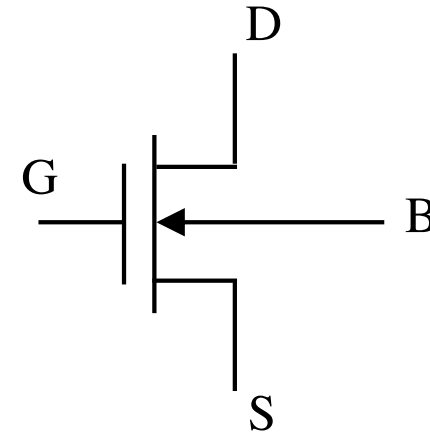
Capacitance

- ❑ Modeled gate with a capacitor to ground
- ❑ ...but ground isn't really one of our terminals
 - Don't connect directly to it
 - ...source and body are *often* at ground...



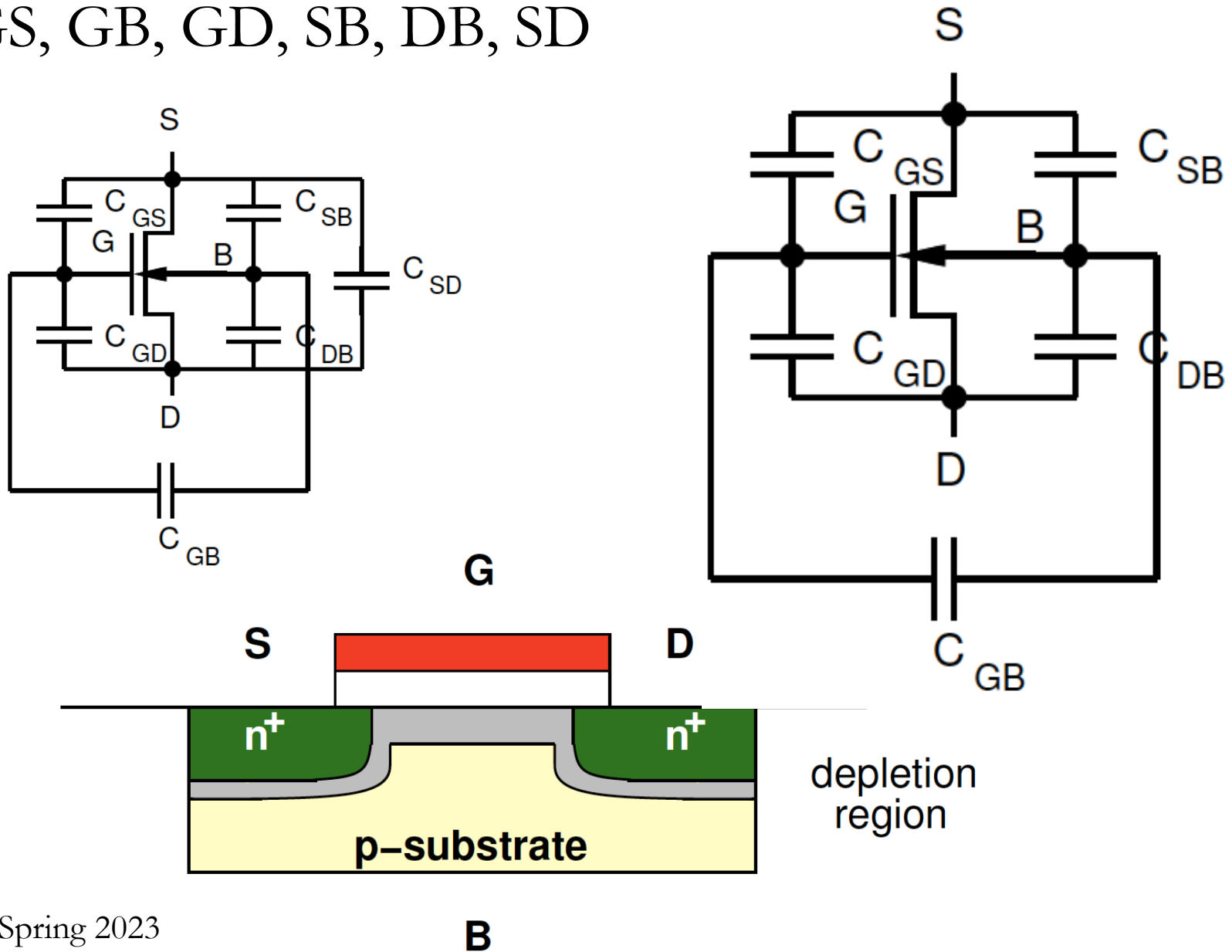
Capacitance (Preclass 2)

- ❑ Four Terminals
- ❑ How many combinations?
 - 4 things taken 2 at a time?



Capacitances

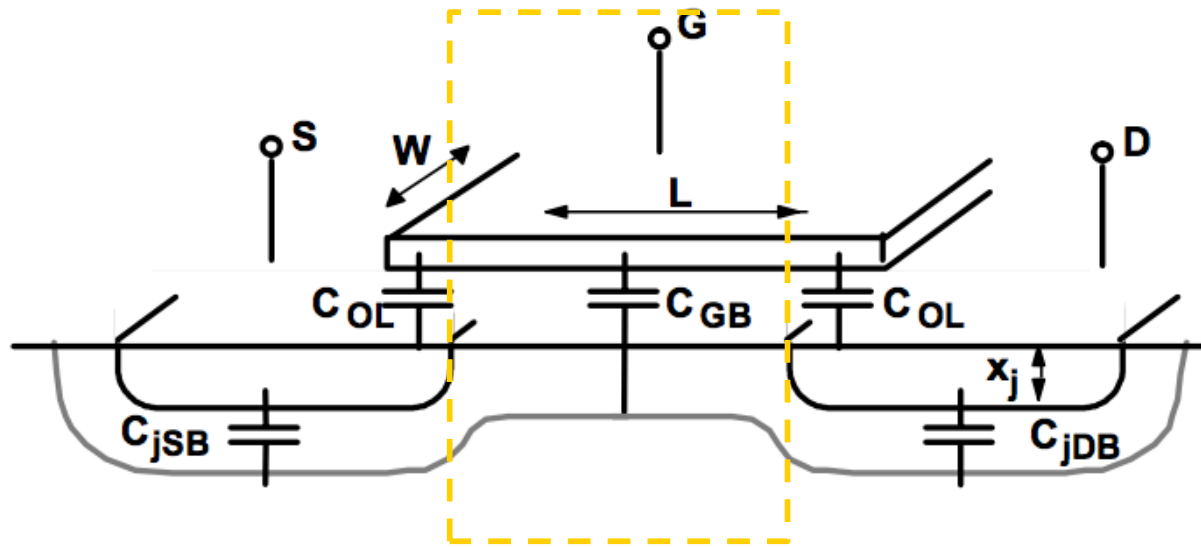
- GS, GB, GD, SB, DB, SD



Capacitance Decomposition



MOSFET Parasitic Capacitance



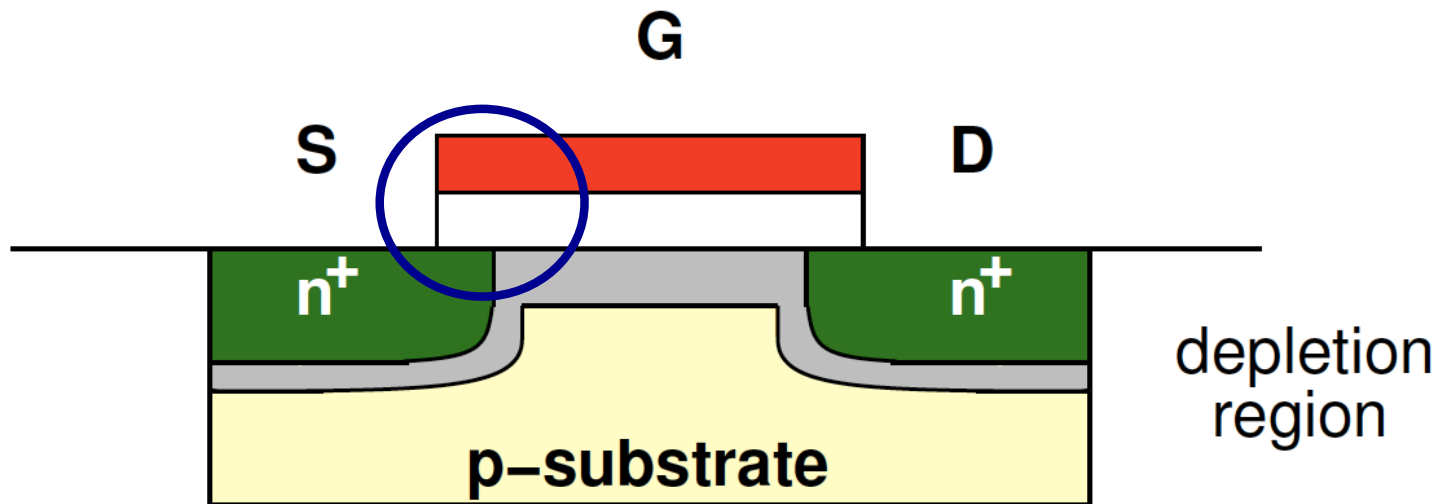
- Any two conductors separated by an insulator form a parallel-plate capacitor
- Two types
 - **Extrinsic** – Outside the box (e.g. junction, overlap)
 - **Intrinsic** – Inside the box (e.g. gate-to-channel)

Overlap Capacitance



Overlap

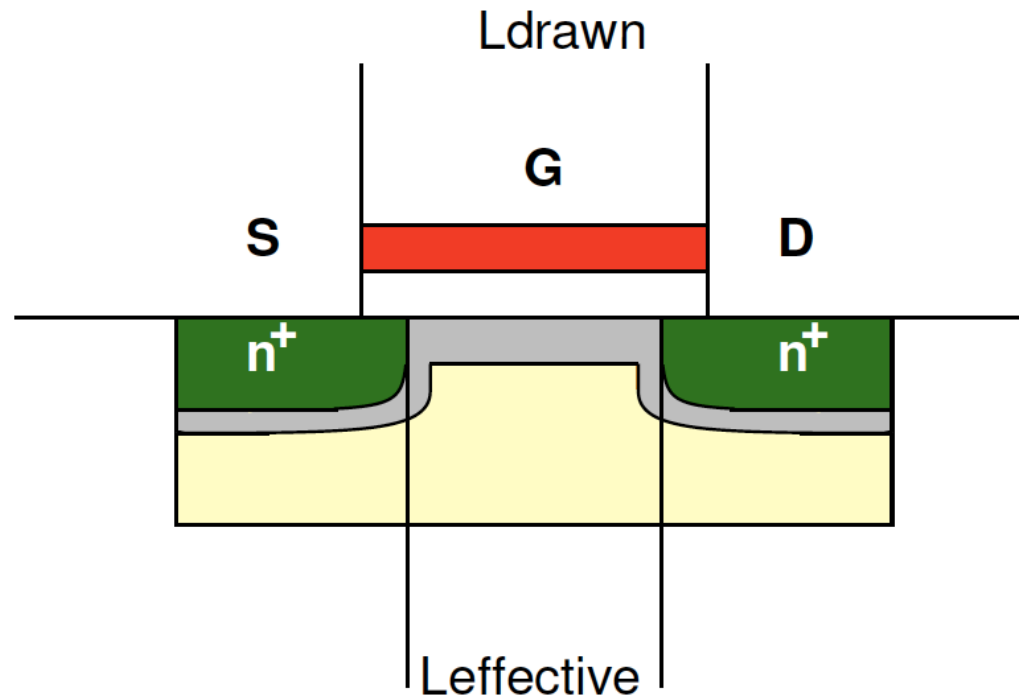
- What is the capacitive implication of gate/source and gate/drain overlap?



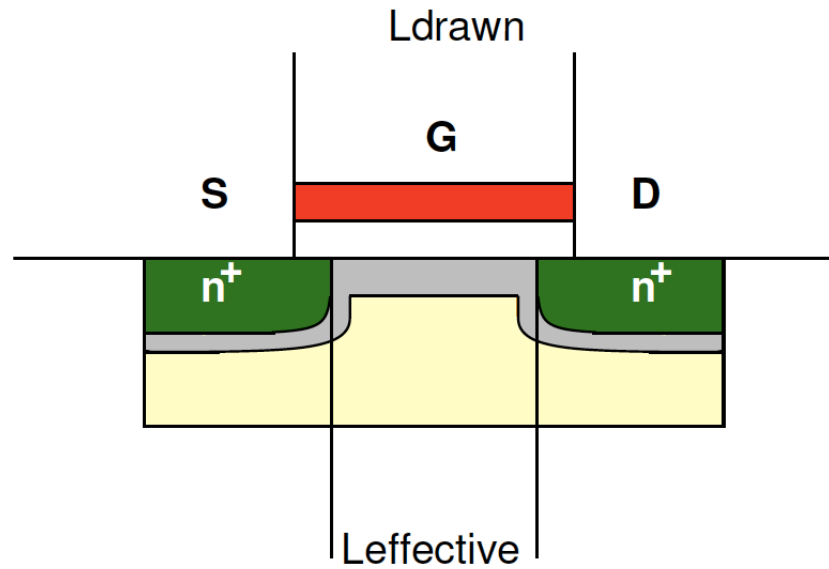


Overlap

- Length of overlap?



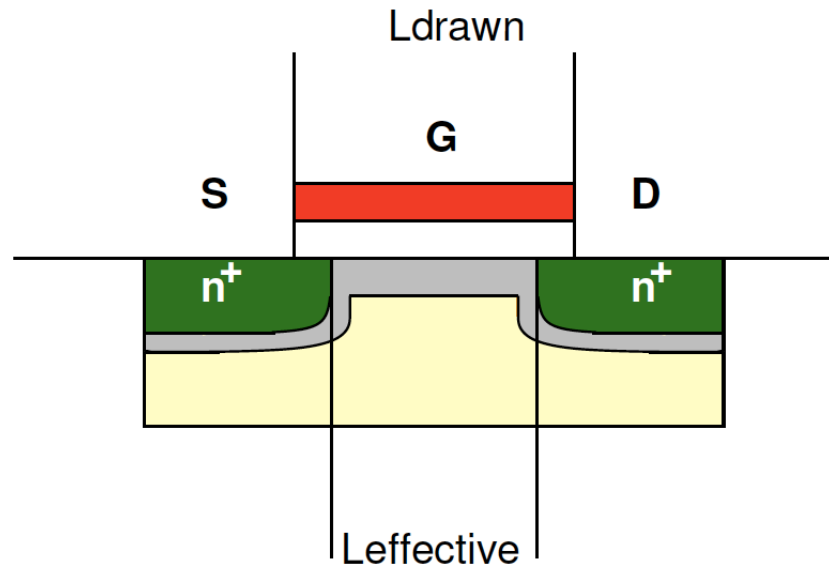
Overlap Capacitance



$$C = \epsilon_r \epsilon_0 \frac{A}{d}$$

$$C_o = \epsilon_{ox} \frac{W (L_{drawn} - L_{effective}) / 2}{t_{ox}}$$

Overlap Capacitance



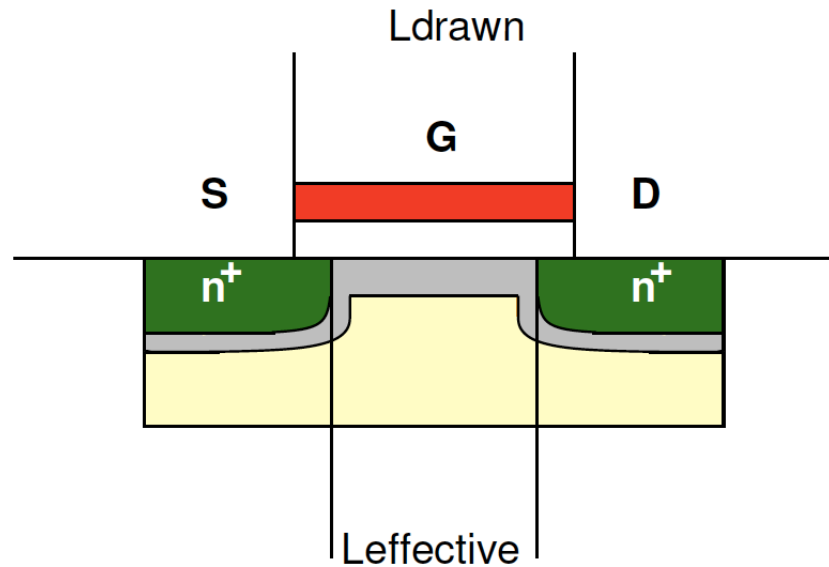
$$C = \epsilon_r \epsilon_0 \frac{A}{d}$$

$$C_{ox} = \frac{\epsilon_{ox}}{t_{ox}}$$

$$C_o = \epsilon_{ox} \frac{W (L_{drawn} - L_{effective}) / 2}{t_{ox}}$$

$$C_o = \frac{1}{2} C_{ox} W (L_{drawn} - L_{effective})$$

Overlap Capacitance



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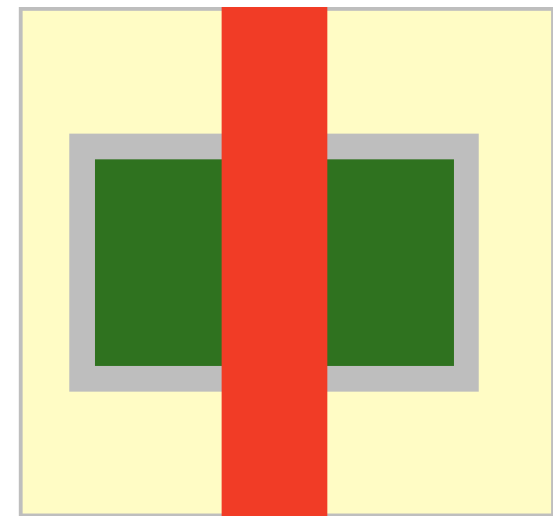
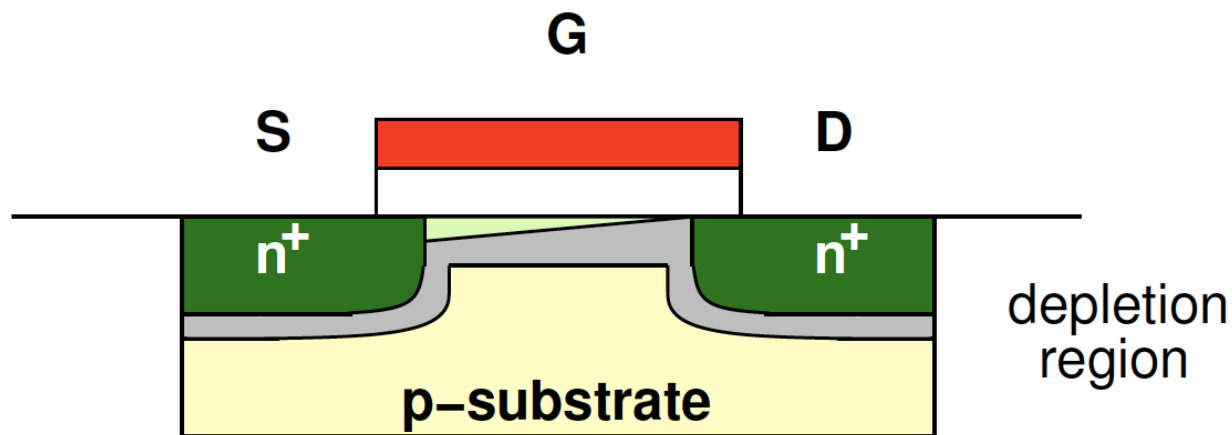
$$C_o = \epsilon_{ox} \frac{W (L_{drawn} - L_{effective}) / 2}{t_{ox}}$$

$$C_o = \frac{1}{2} C_{ox} W (L_{drawn} - L_{effective}) = C_{GSO} = C_{GDO}$$

Junction Capacitances

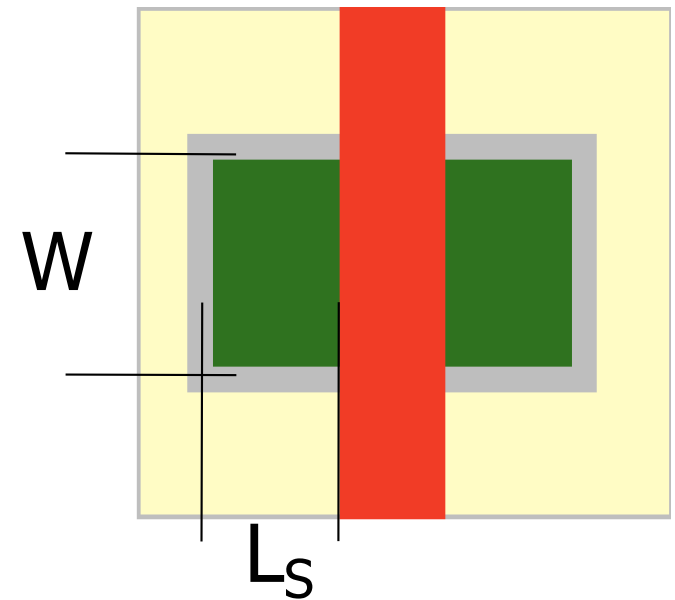
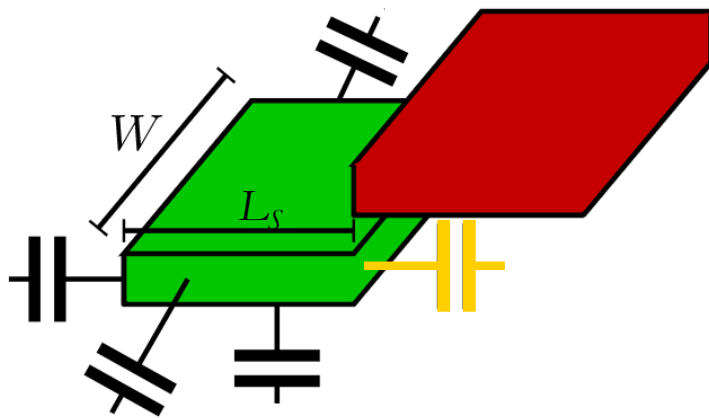
Junction (diffusion) Capacitance

- n^+ contacts are formed by doping = diffusion
- Depletion under diffusion region (bottom-plate)
 - Due to reverse biased PN junction
 - Bottom-plate junction capacitance, C_j
- Depletion around perimeter (sidewall) of diffusion region
 - Sidewall junction capacitance, C_{jsw}



Junction (Diffusion) Capacitance

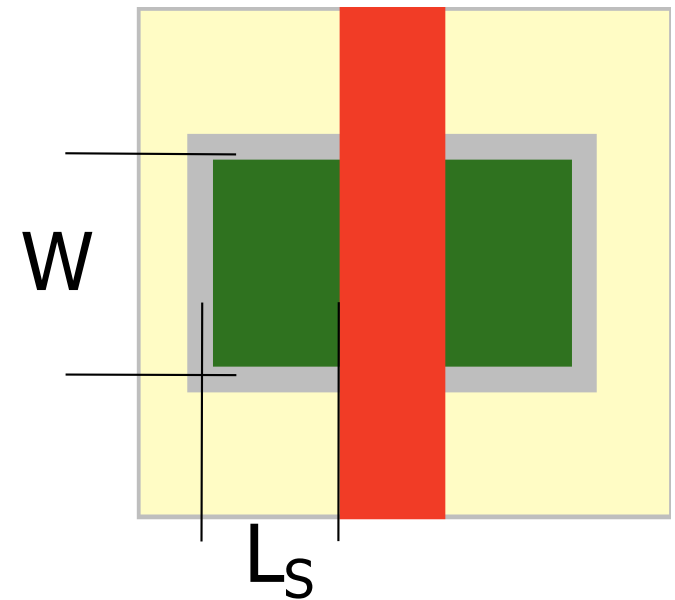
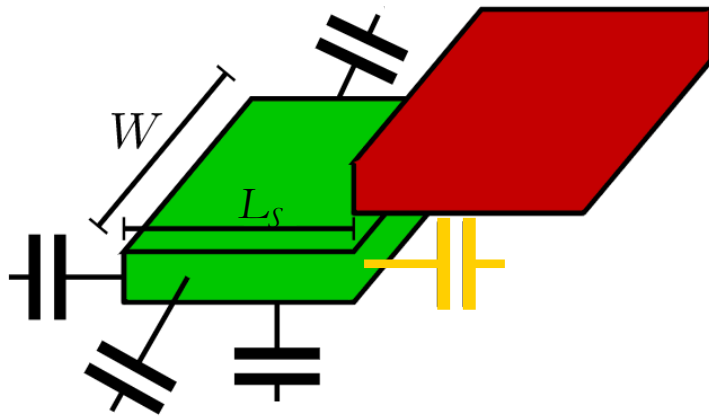
- ❑ C_j – Bottom-plate junction capacitance (F/Area)
- ❑ C_{jsw} – Sidewall junction capacitance (F/Length)
- ❑ L_S – length of diffusion region



$$C_{diff} = C_j L_S W +$$

Junction (Diffusion) Capacitance

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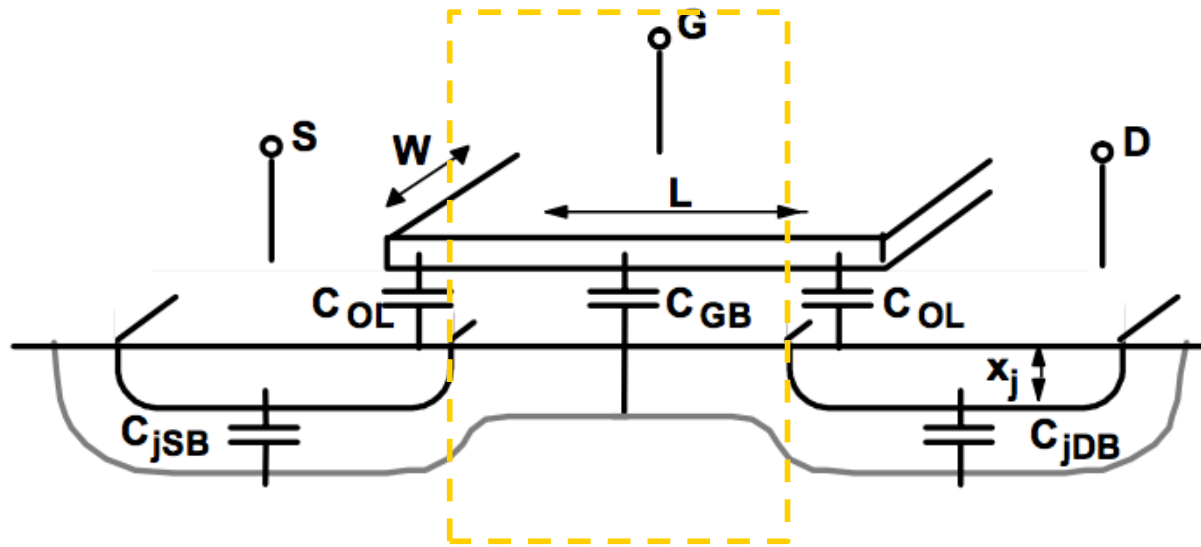


$$C_{diff} = C_j L_S W + C_{jsw} (2L_S + W)$$

Gate-to-channel



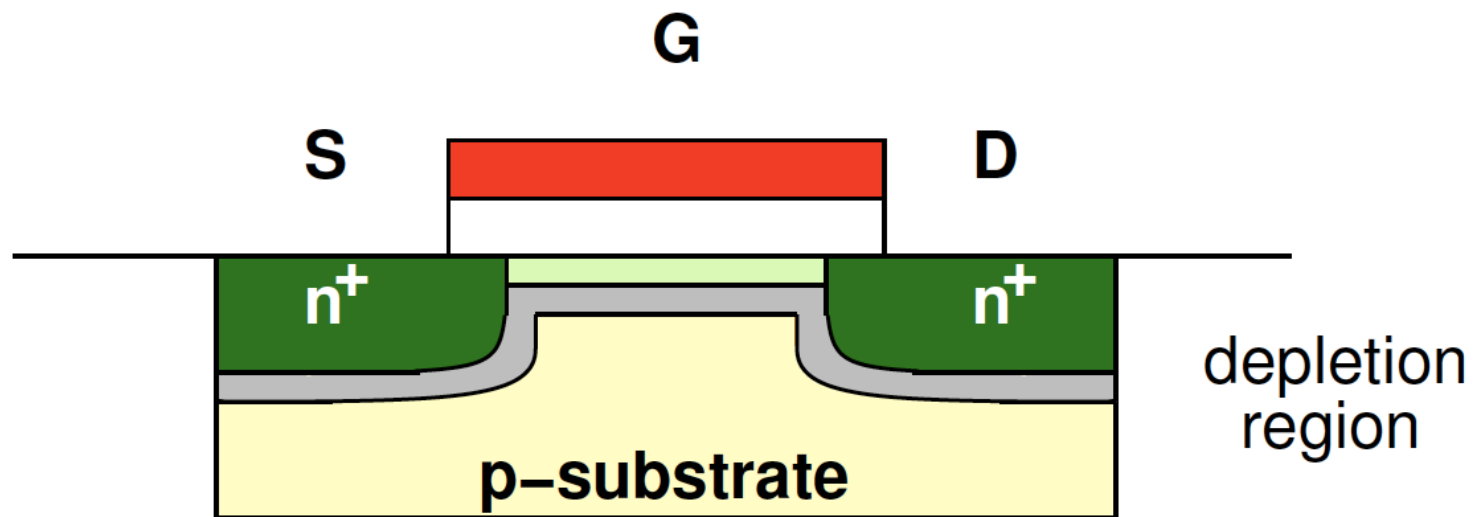
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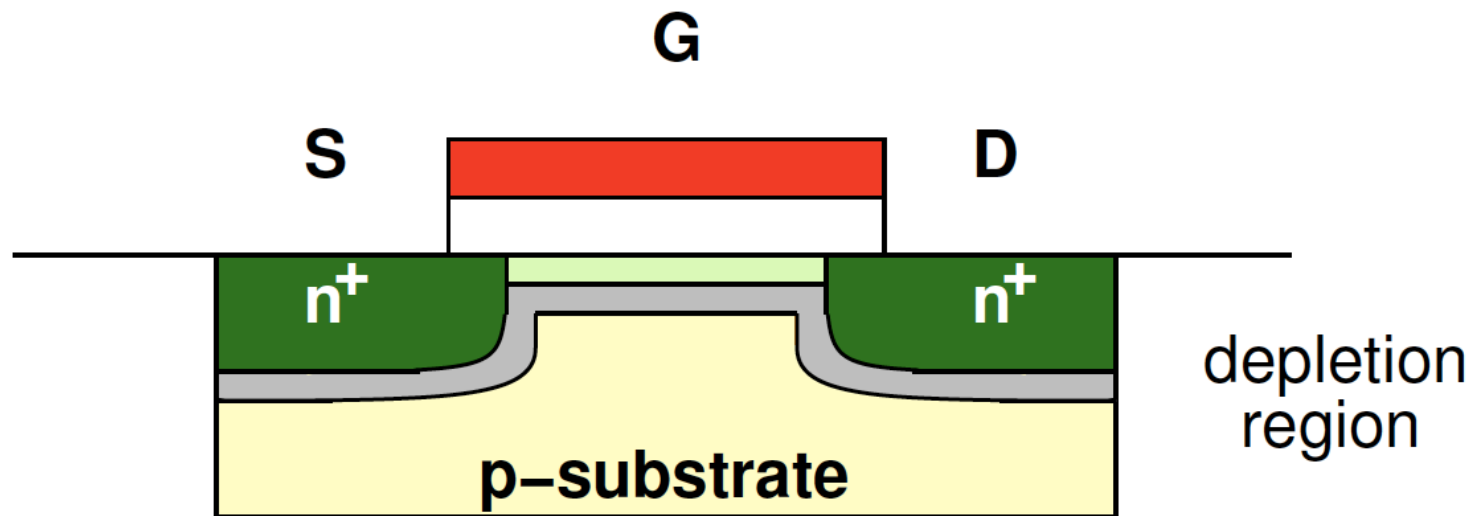
Gate-to-Bulk Capacitance

- Looks like parallel plate capacitance
- Two components:
 - What is C_{GC} ? (C_{GCS} , C_{GCD})
 - What is C_{GCB} ?



Gate-to-Channel Capacitance

- Looks like parallel plate capacitance
- Two components: **Case: Strong Inversion** (small V_{ds})
 - C_{GC}
 - C_{GCB}



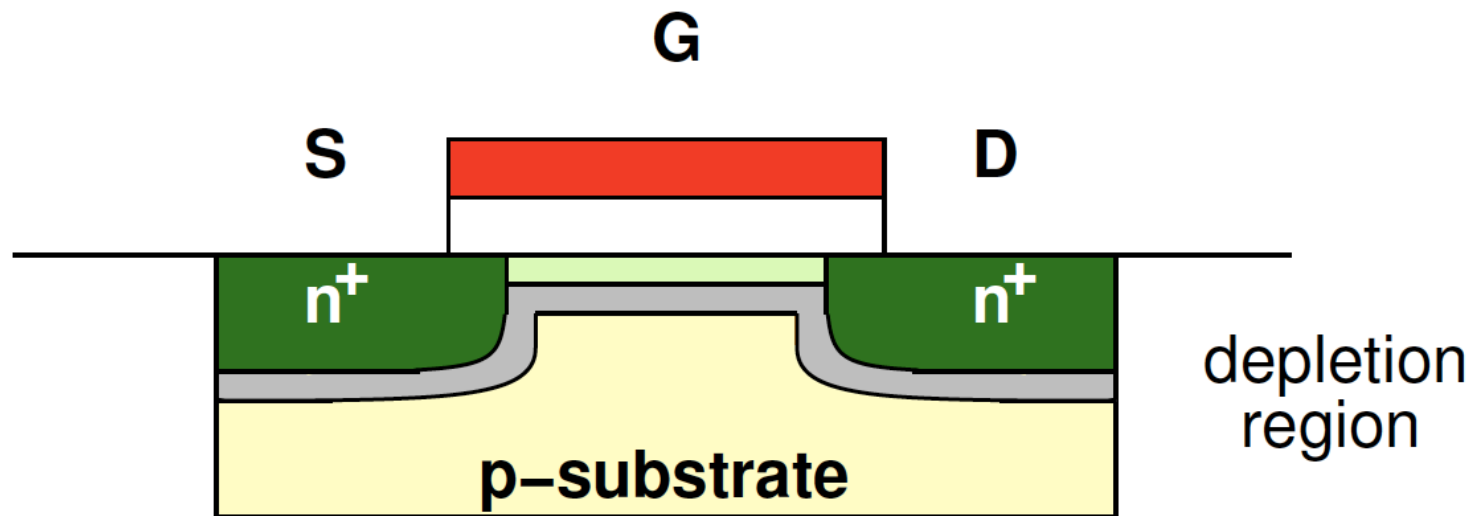
Gate-to-Channel Capacitance

- Looks like parallel plate capacitance
- Two components: **Case: Strong Inversion**

- C_{GC}

- $C_{GCB}=0$

$$C_{GC} = C_{ox}WL_{effective}$$



Gate-to-Channel Capacitance

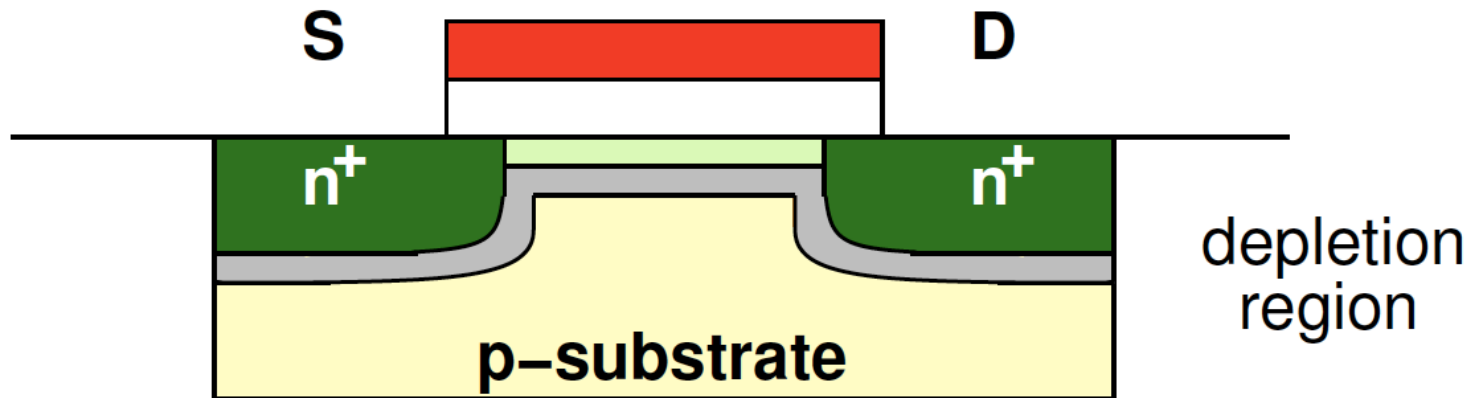
- Looks like parallel plate capacitance
- Two components: **Case: Strong Inversion**

- C_{GC} – Split evenly between S and D

- $C_{GB} = 0$

$$C_{GC} = C_{ox} W L_{effective}$$

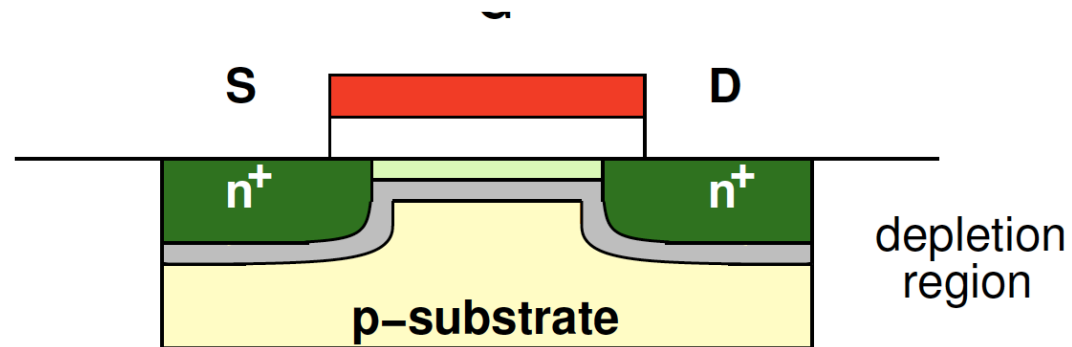
$$C_{GCS} = C_{GCD} = \frac{1}{2} C_{ox} W L_{effective}$$



Gate-to-Source Capacitance

- Channel + Overlap

$$C_{GS} = C_{GCS} + C_{GSO}$$



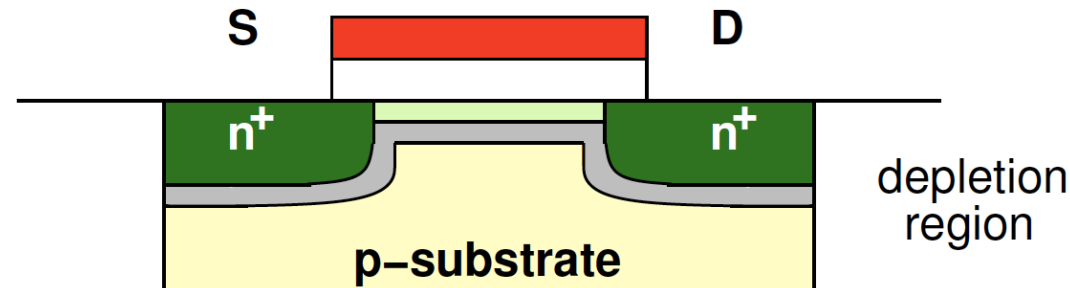
Gate-to-Source Capacitance

- Channel + Overlap

$$C_{GS} = C_{GCS} + C_{GSO}$$

$$C_{GS} = \frac{1}{2} C_{OX} W (L_{drawn} - L_{effective}) + \frac{1}{2} C_{OX} W L_{effective}$$

$$C_{GS} = \frac{1}{2} C_{OX} W L_{drawn}$$



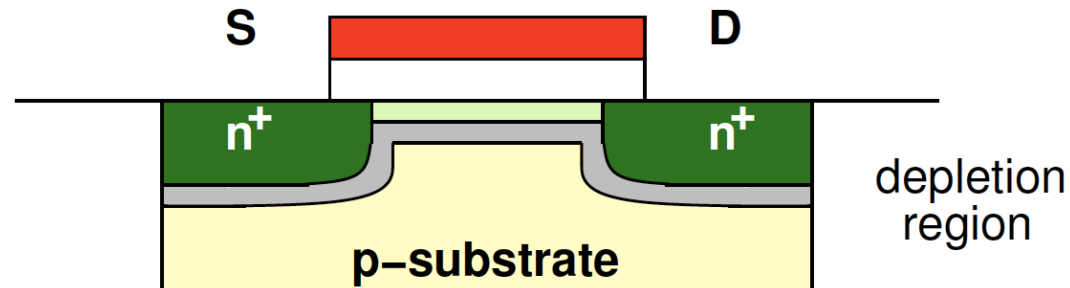
Gate-to-Drain Capacitance

- Channel + Overlap

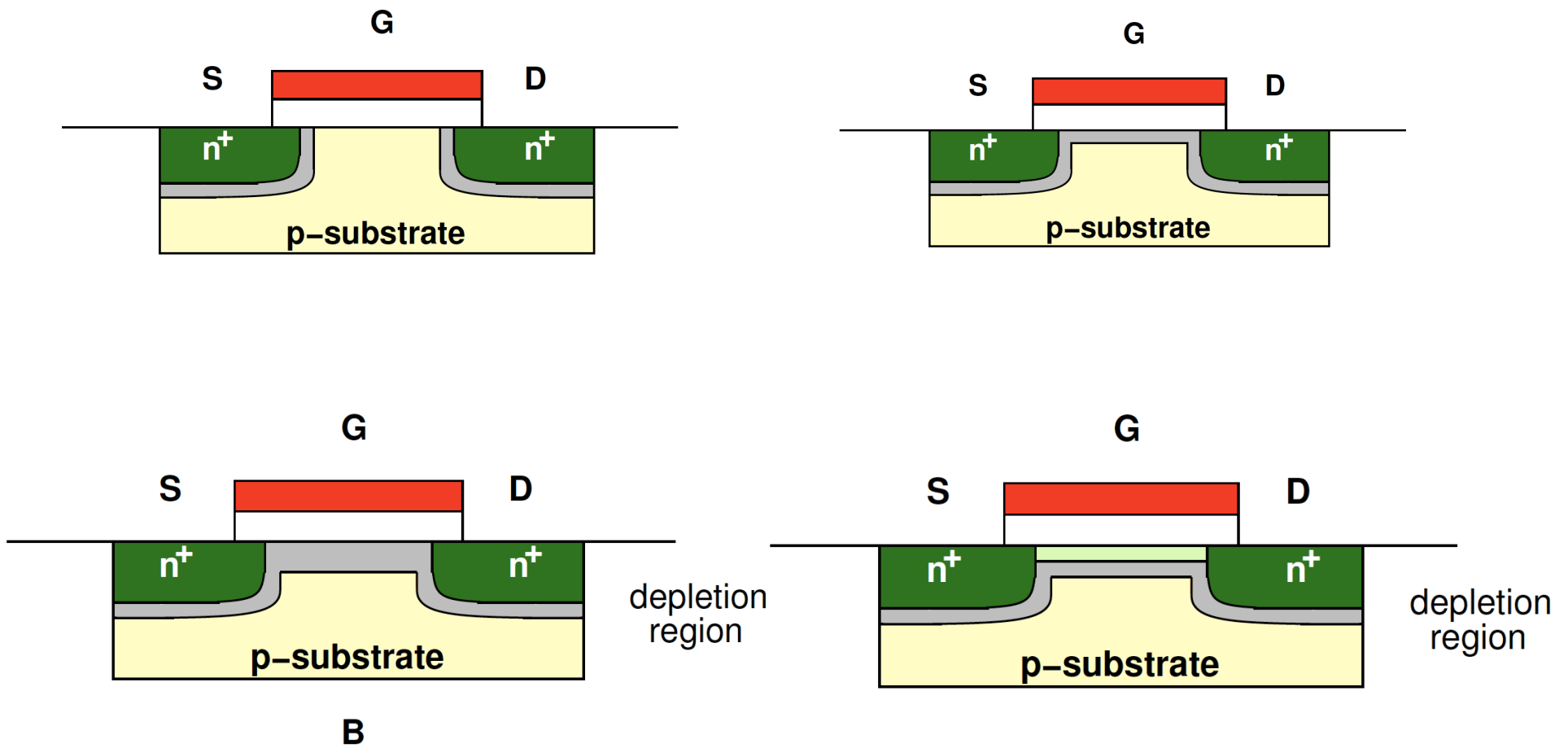
$$C_{GD} = C_{GCD} + C_{GDO}$$

$$C_{GD} = \frac{1}{2} C_{OX} W (L_{drawn} - L_{effective}) + \frac{1}{2} C_{OX} W L_{effective}$$

$$C_{GD} = \frac{1}{2} C_{OX} W L_{drawn}$$

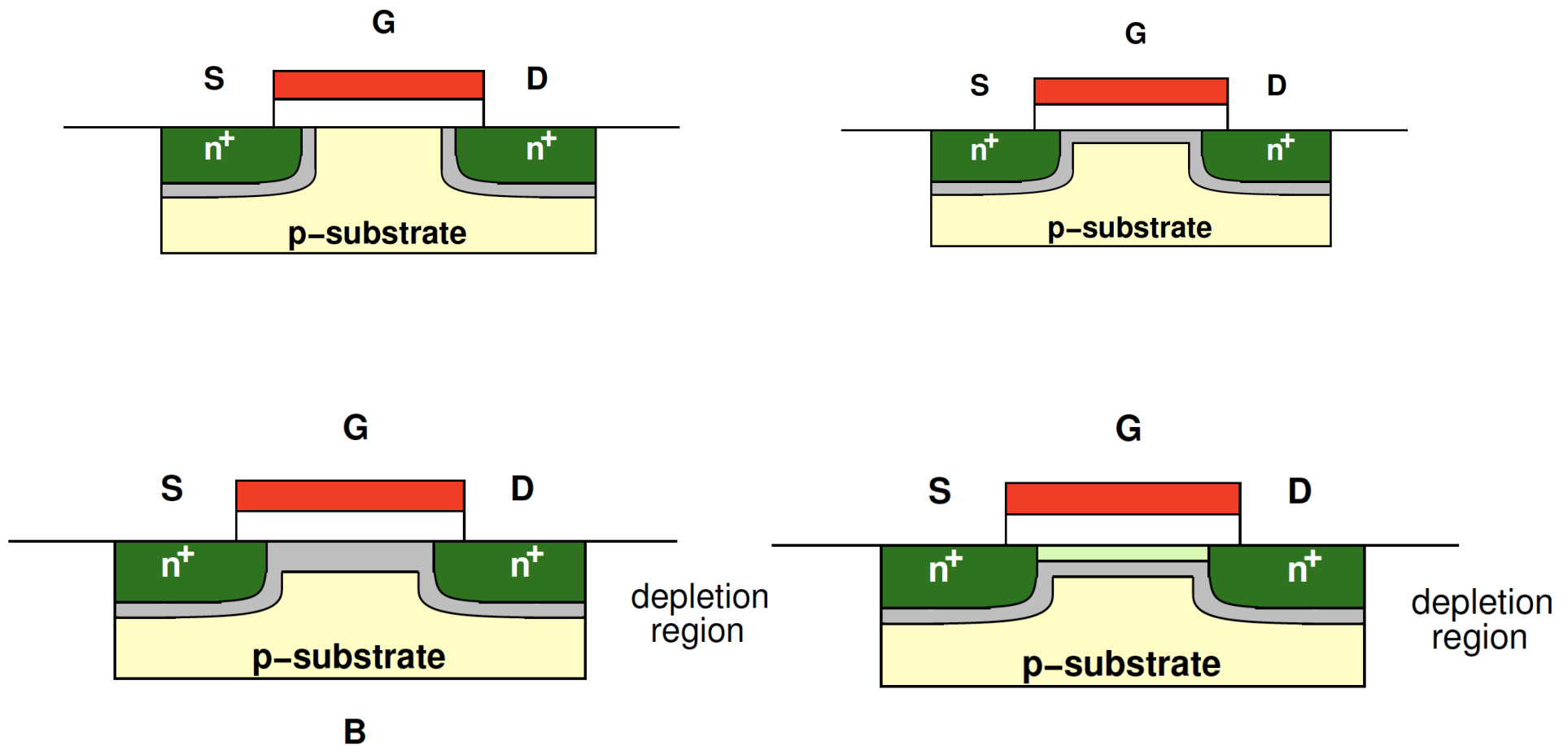


Channel Evolution: Weak Inversion



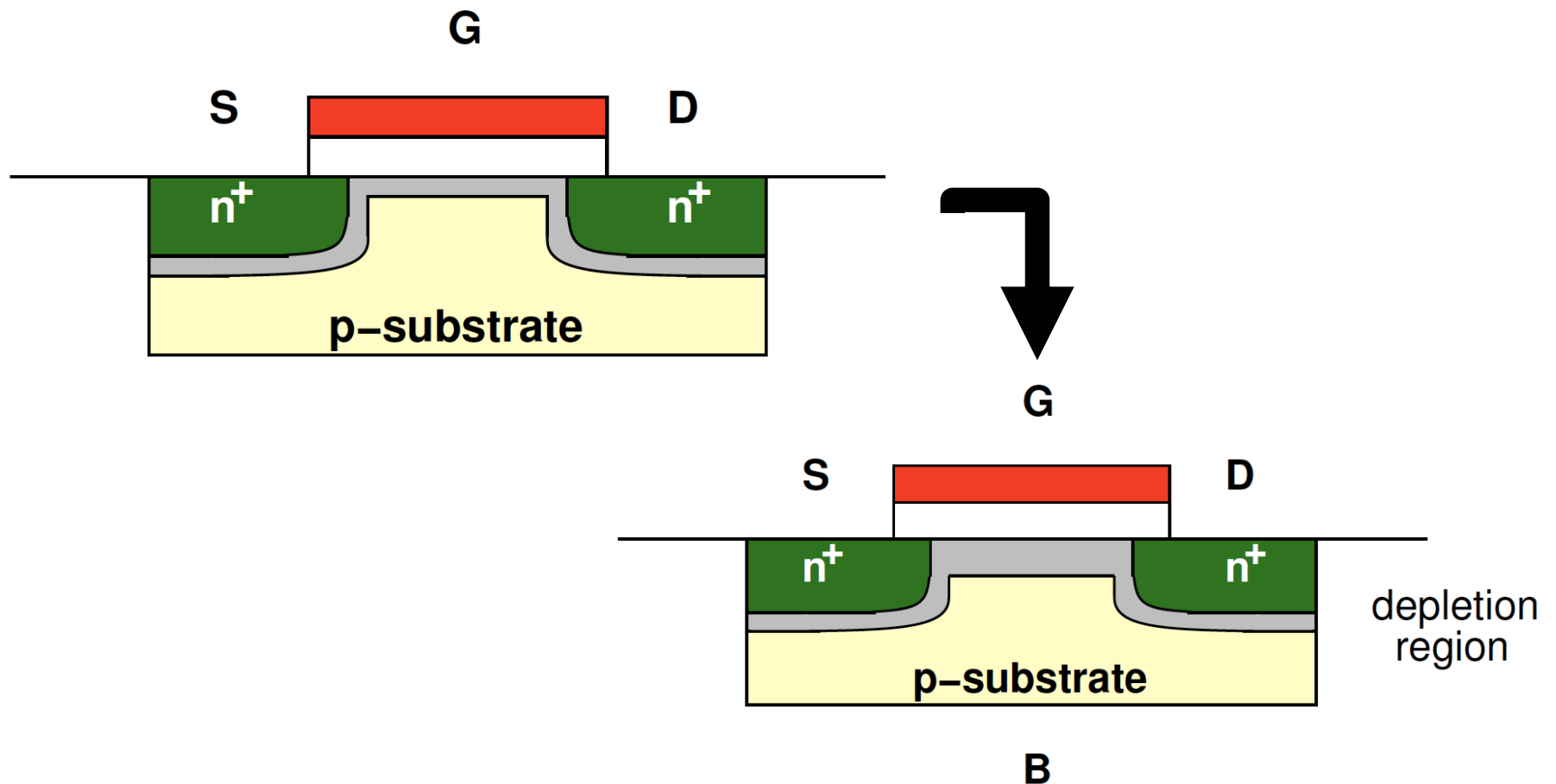
Channel Evolution: Weak Inversion

□ $V_{GS} = 0 \rightarrow C_{GC} = 0, C_{GCB} = WLC_{ox}$



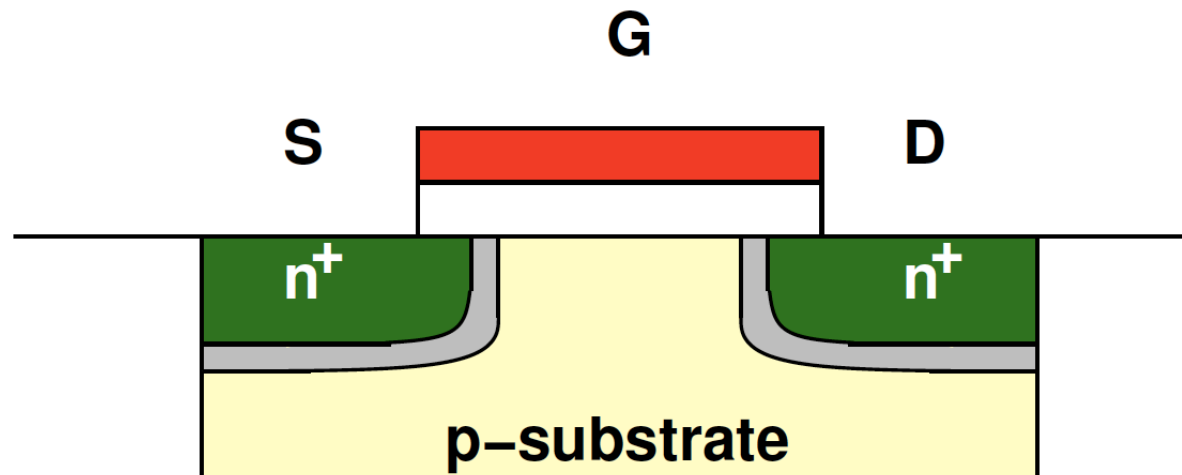
Channel Evolution: Weak Inversion

- What happens to capacitance here as V_{GS} increases?
 - Capacitor plate distance?

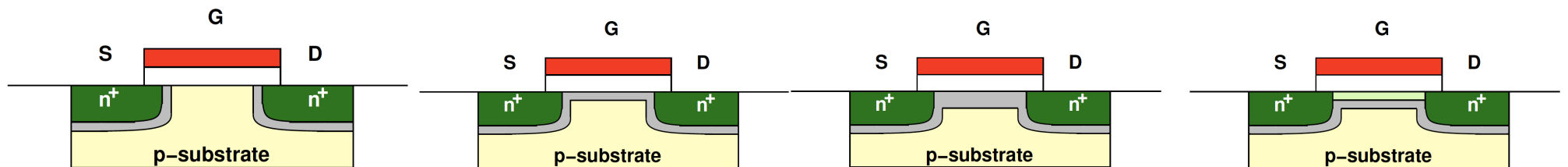
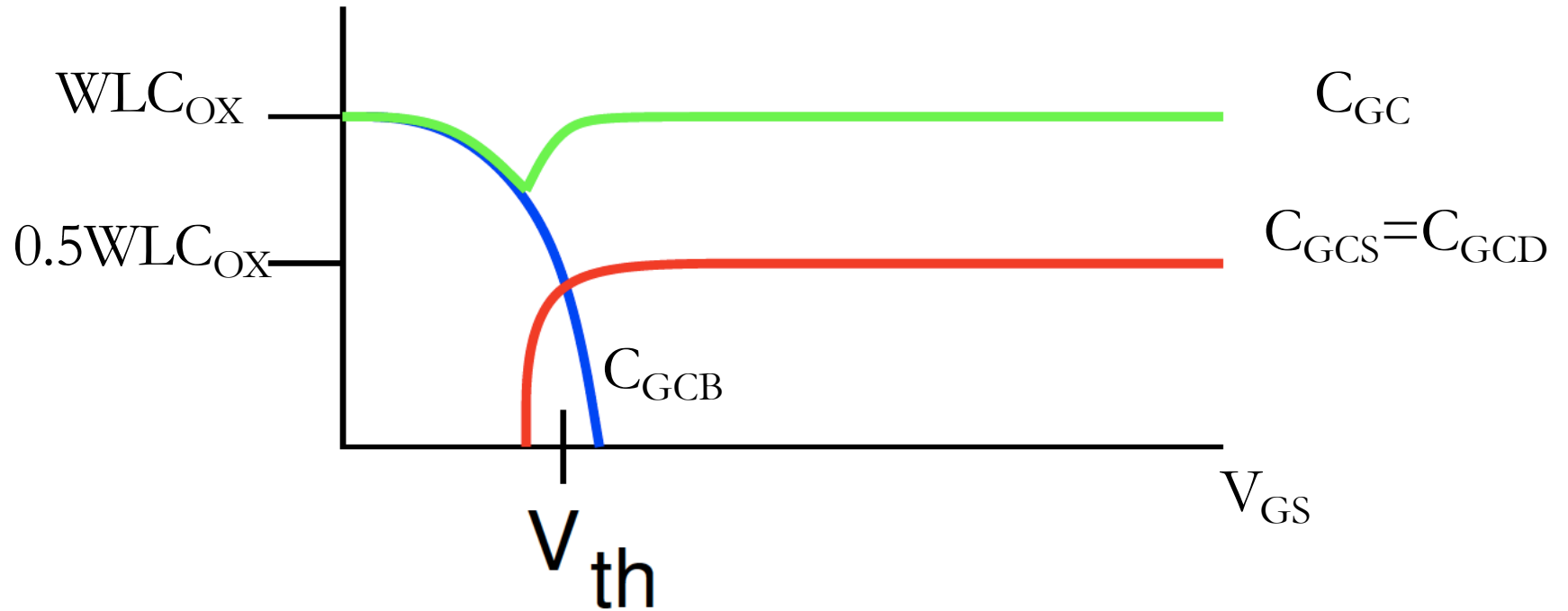


Channel Evolution: Weak Inversion

- ❑ Capacitance is initially dominated by Gate-to-bulk capacitance ($C_{GCS,D}=0$)
- ❑ Gate-to-bulk capacitance drops as V_{GS} increases toward V_{th}



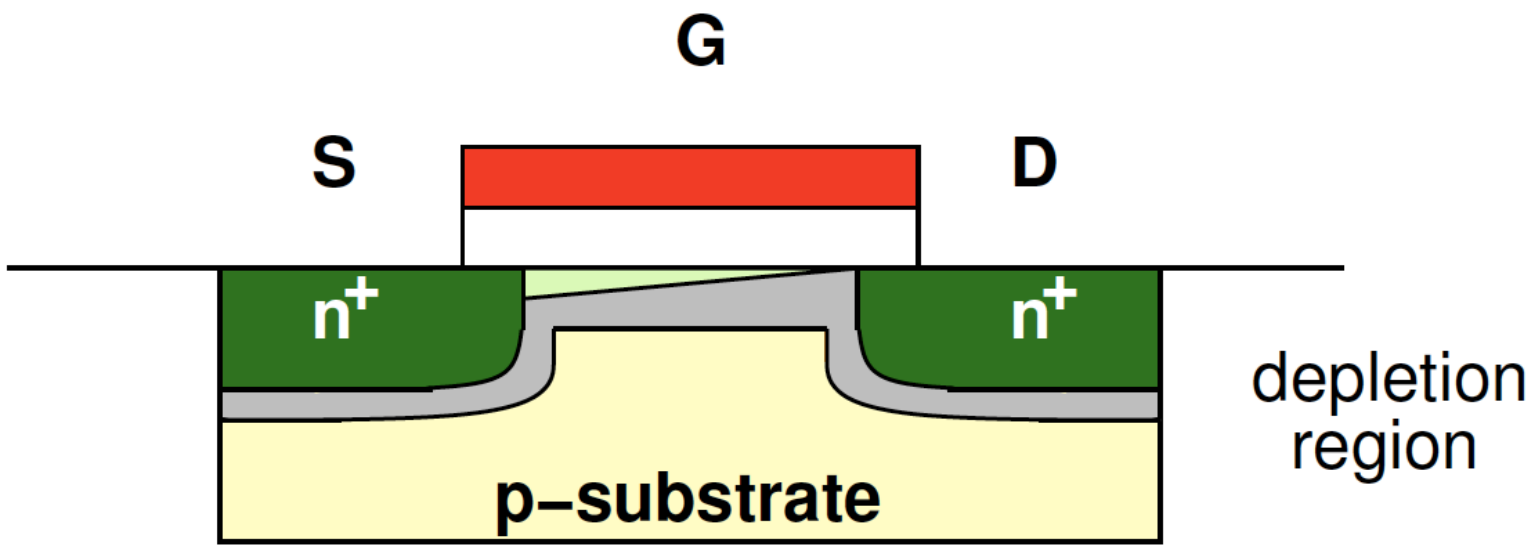
Capacitance vs V_{GS} ($V_{DS}=0$)



Increasing V_{GS} \longrightarrow

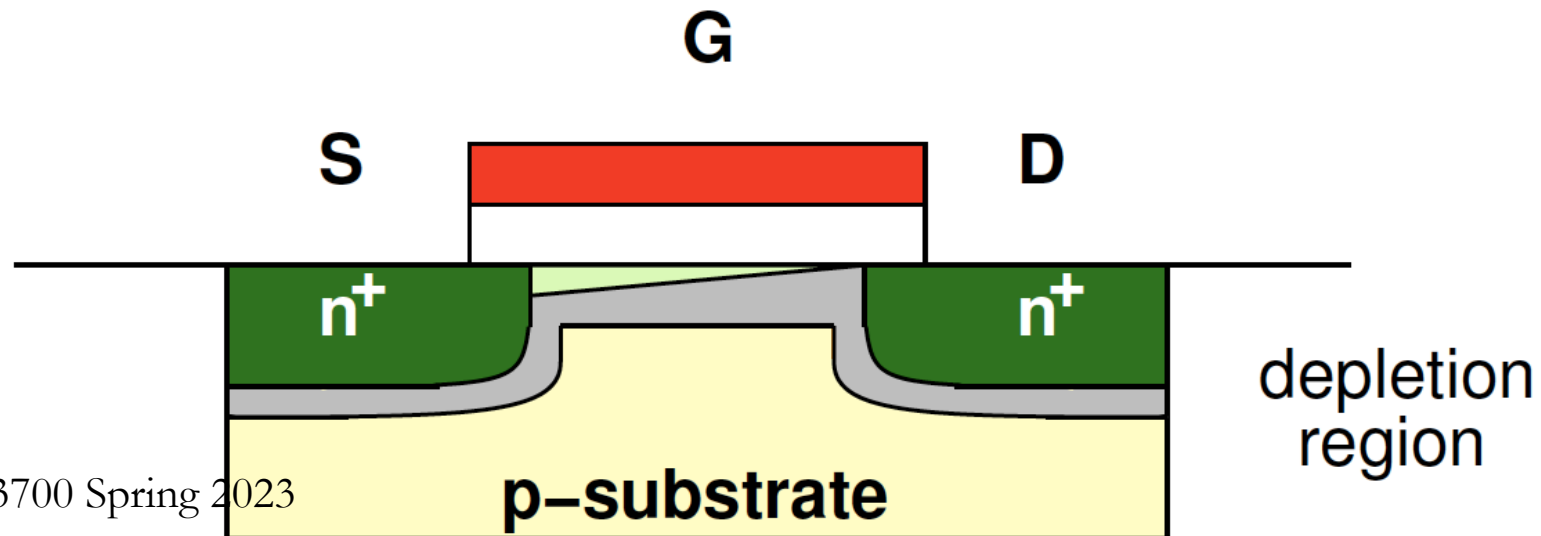


Saturation Capacitance?

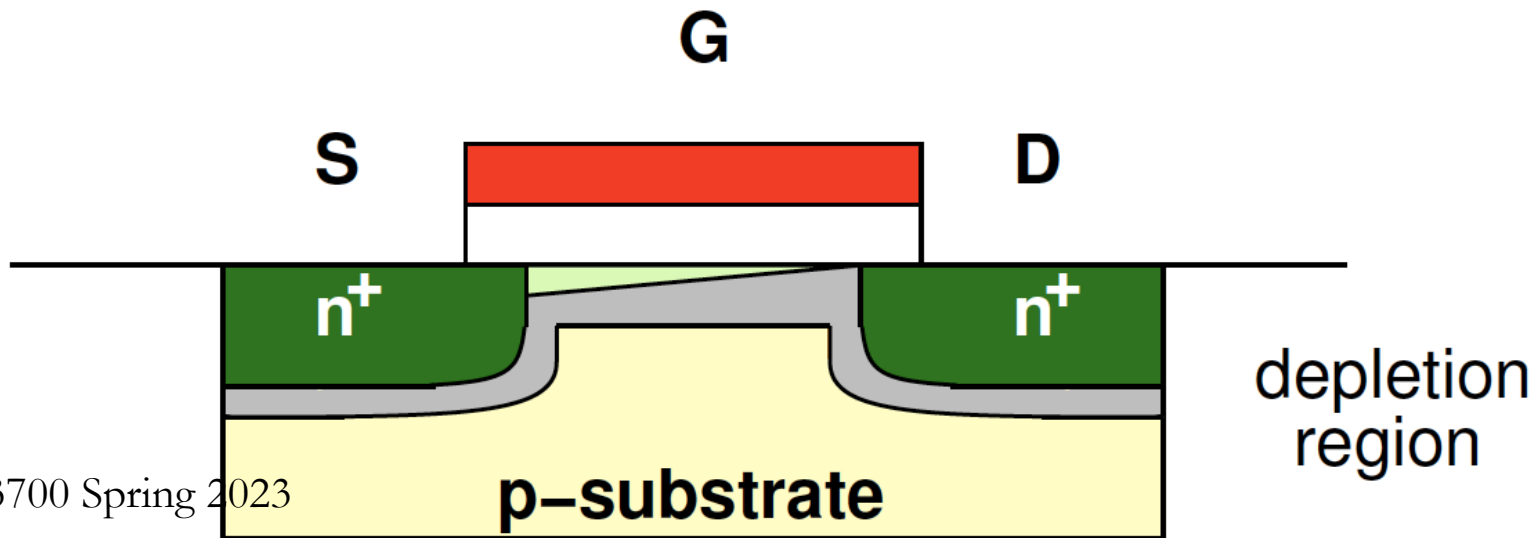
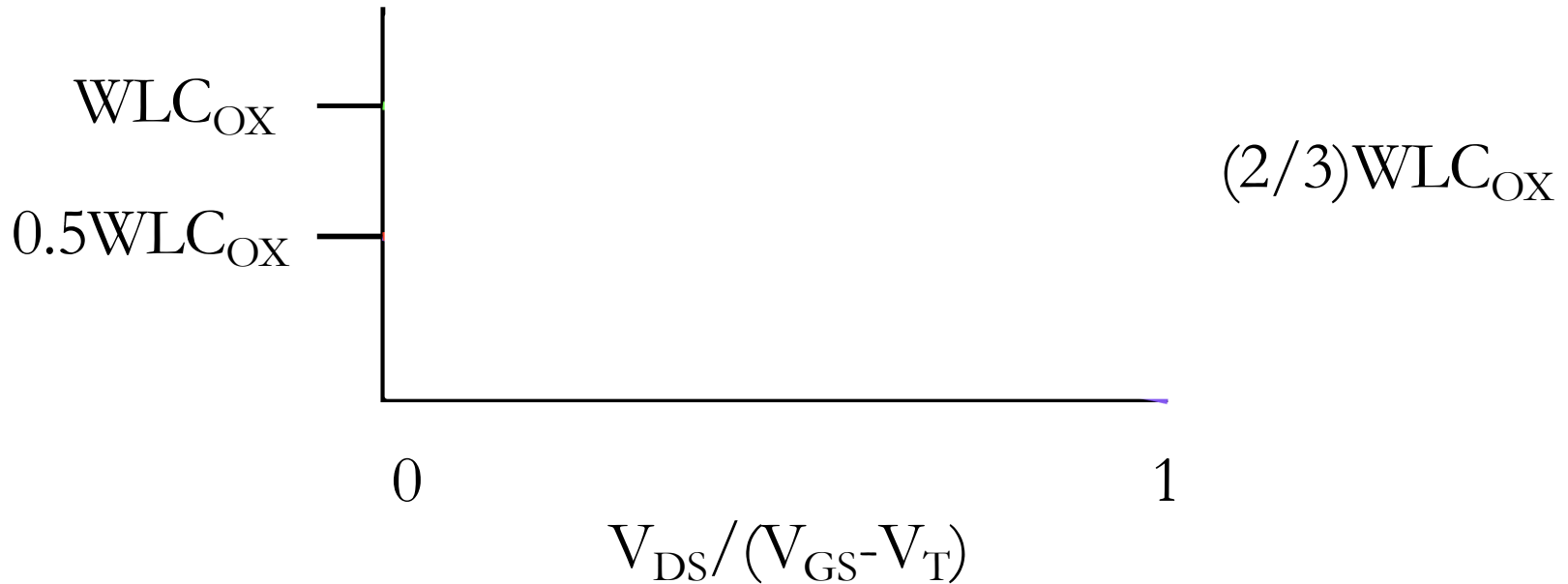


Saturation Capacitance?

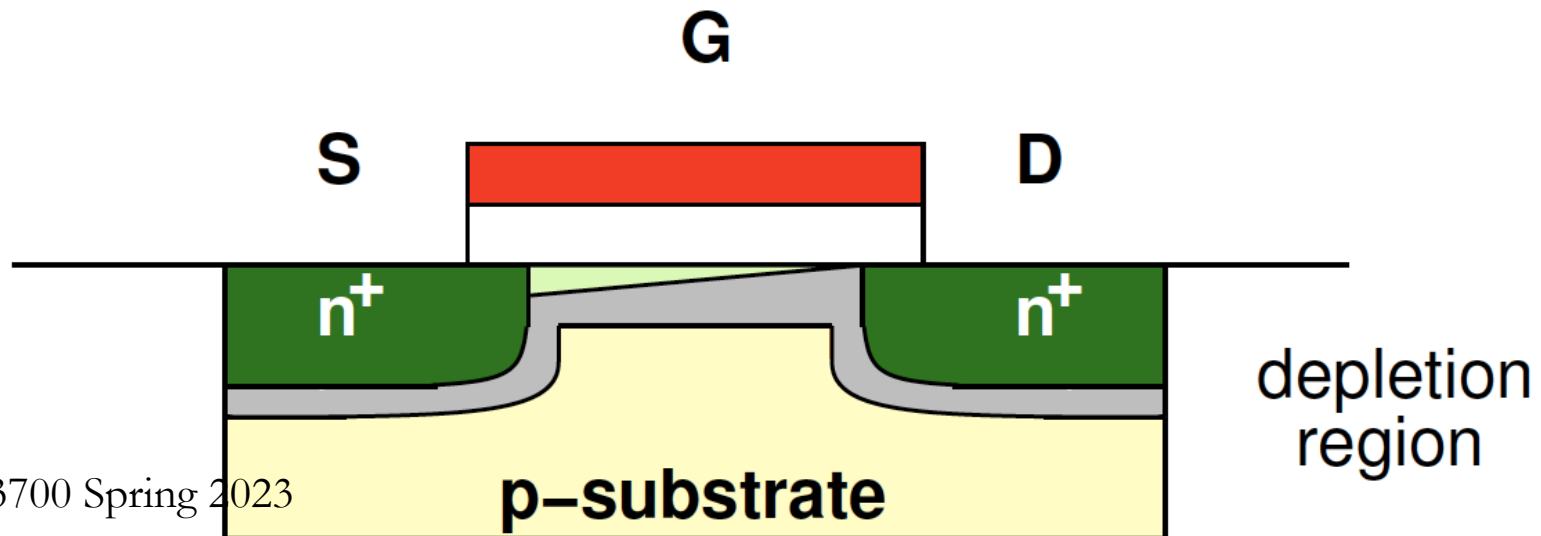
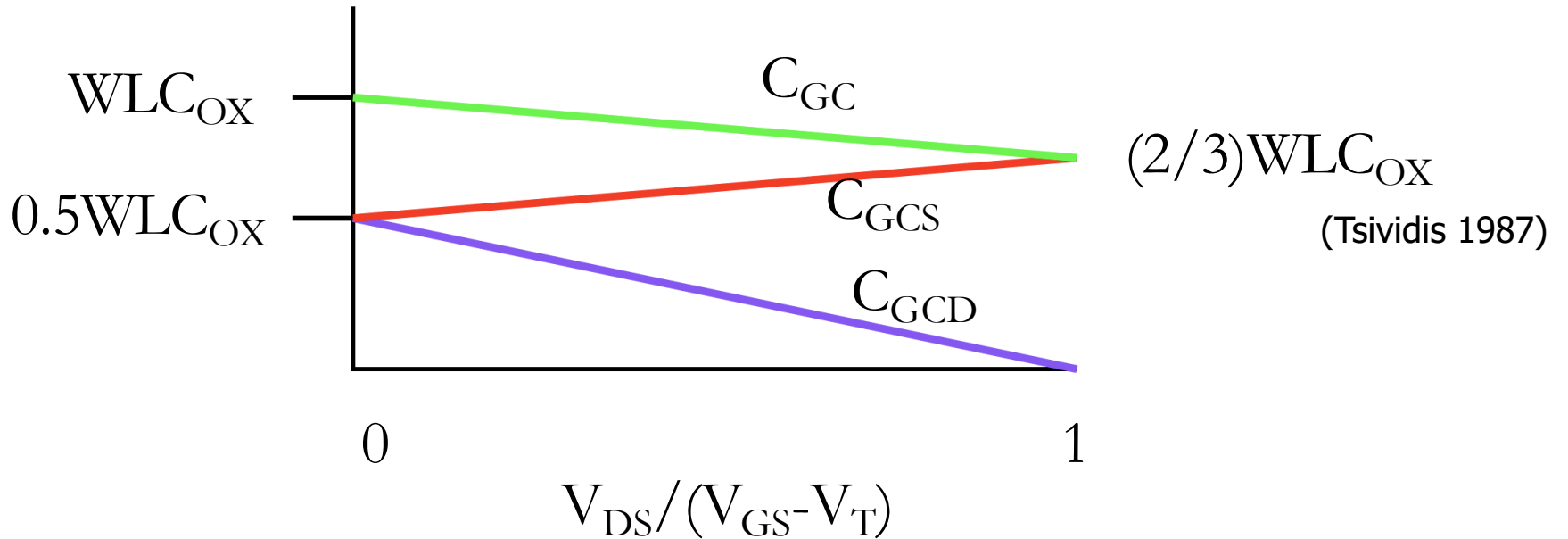
- ❑ Source end of channel in inversion
- ❑ Voltage at drain end of channel at or below threshold
- ❑ Capacitance shifts to source
 - Total capacitance reduced



Saturation Capacitance

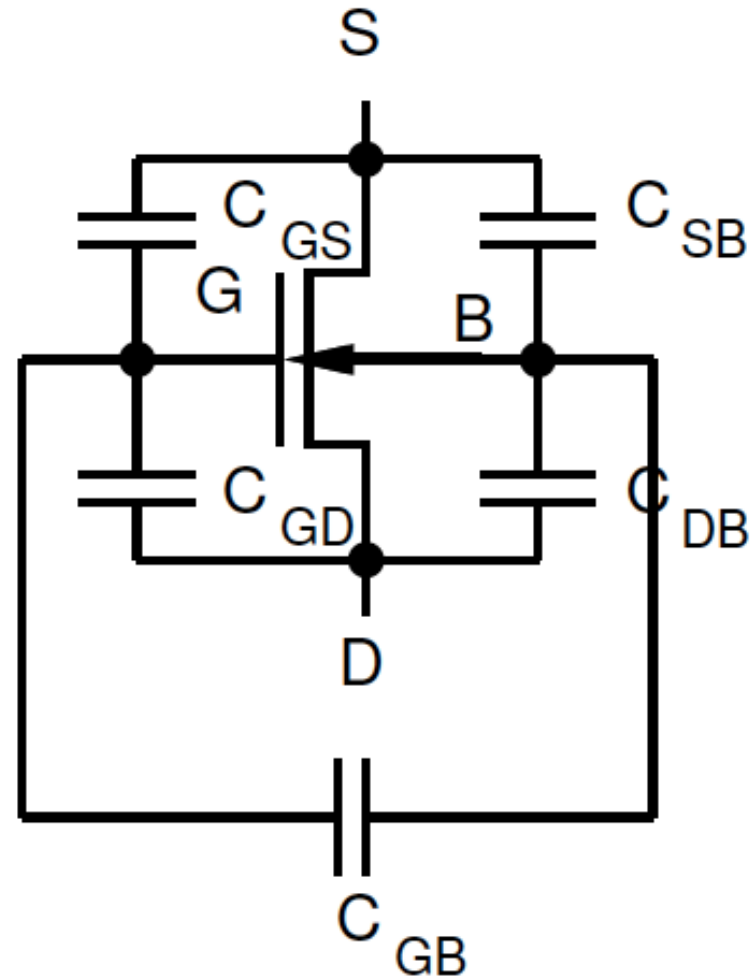


Saturation Capacitance



Capacitance Roundup

- $C_{GS} = C_{GCS} + C_{GSO}$
- $C_{GD} = C_{GCD} + C_{GDO}$
- $C_{GB} = C_{GCB}$
- $C_{SB} = C_{diff}$
- $C_{DB} = C_{diff}$





First Order Capacitance Summary

Operation Region	C_{GCB}	C_{GCS}	C_{GCD}	C_{GC}	C_G
Subthreshold					
Linear					
Saturation					



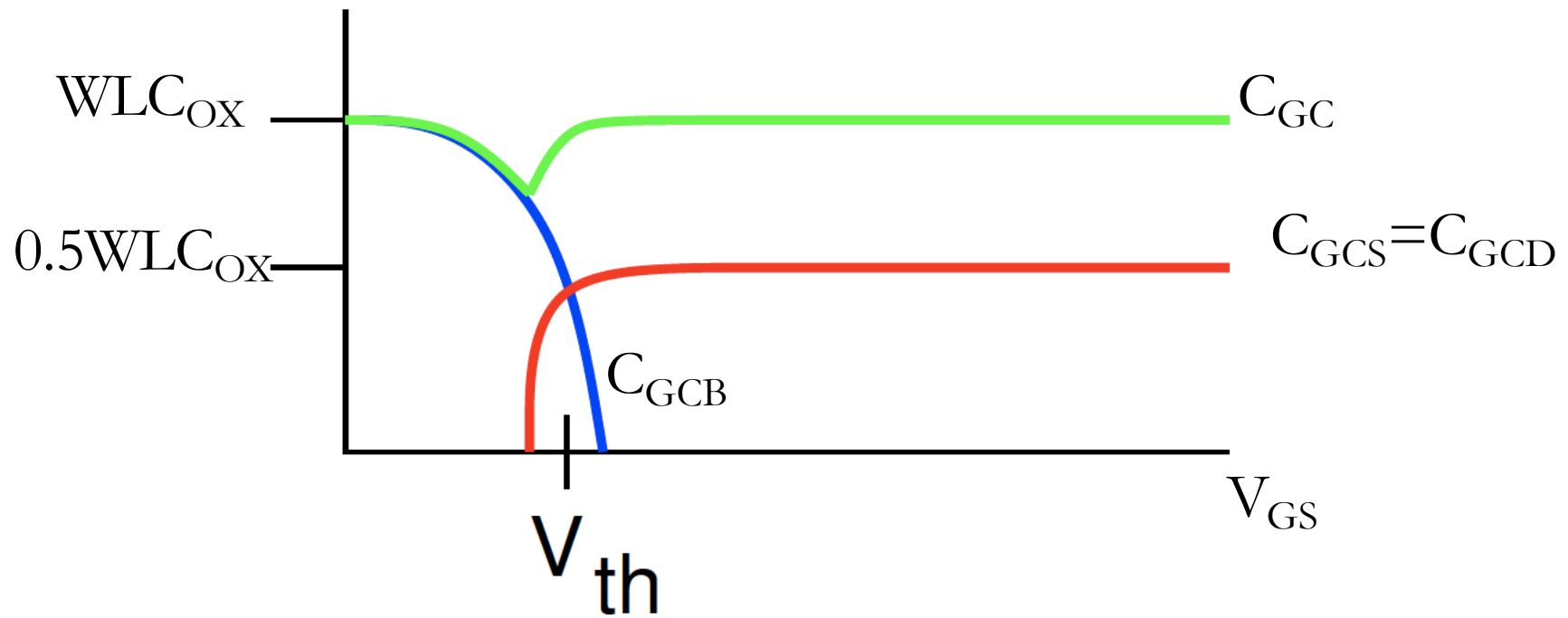
First Order Capacitance Summary

Operation Region	C_{GCB}	C_{GCS}	C_{GCD}	C_{GC}	C_G
Subthreshold					
Linear	0	$C_{OX}WL/2$	$C_{OX}WL/2$		
Saturation					

$$C_{GCS} = C_{GCD} = \frac{1}{2} C_{ox} WL_{effective}$$

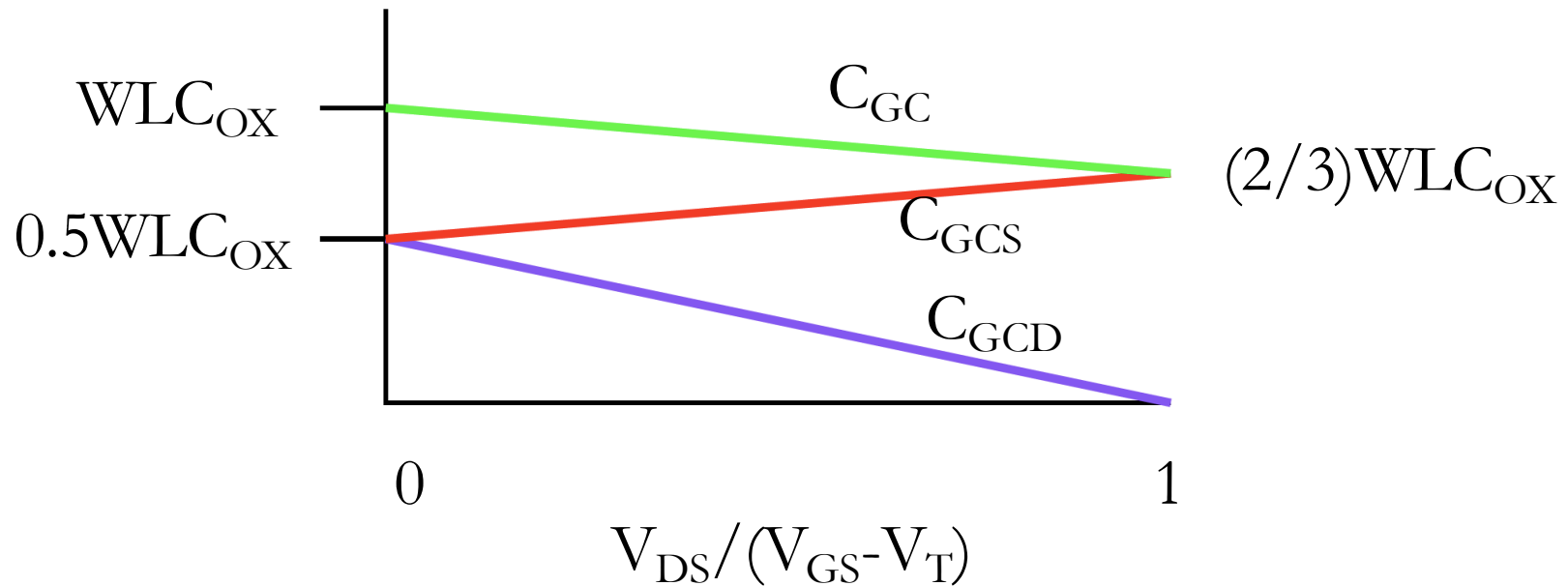
First Order Capacitance Summary

Operation Region	C_{GCB}	C_{GCS}	C_{GCD}	C_{GC}	C_G
Subthreshold	$C_{OX}WL$	0	0		
Linear	0	$C_{OX}WL/2$	$C_{OX}WL/2$		
Saturation					



First Order Capacitance Summary

Operation Region	C_{GCB}	C_{GCS}	C_{GCD}	C_{GC}	C_G
Subthreshold	$C_{OX}WL$	0	0		
Linear	0	$C_{OX}WL/2$	$C_{OX}WL/2$		
Saturation	0	$(2/3)C_{OX}WL$	0		





First Order Capacitance Summary

Operation Region	C_{GCB}	+	C_{GCS}	+	C_{GCD}	=	C_{GC}	C_G
Subthreshold	$C_{OX}WL$		0		0		$C_{OX}WL$	
Linear	0		$C_{OX}WL/2$		$C_{OX}WL/2$		$C_{OX}WL$	
Saturation	0		$(2/3)C_{OX}WL$		0		$(2/3)C_{OX}WL$	

First Order Capacitance Summary

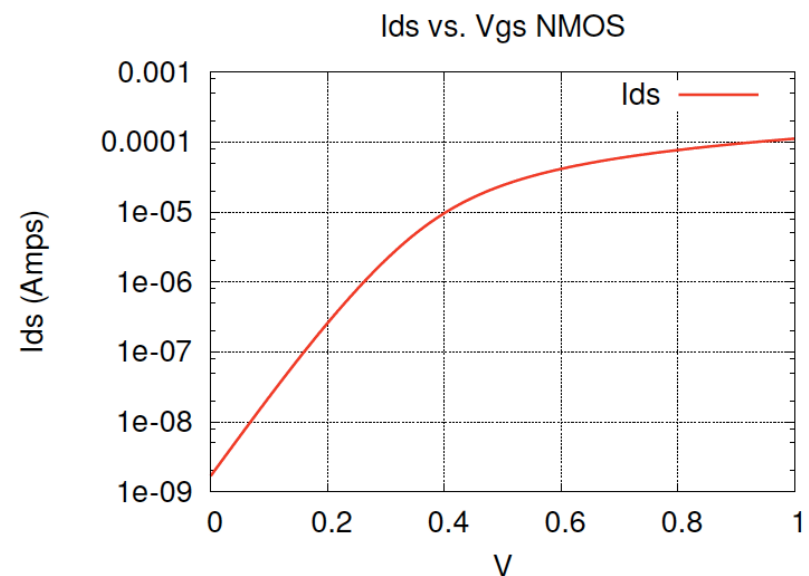
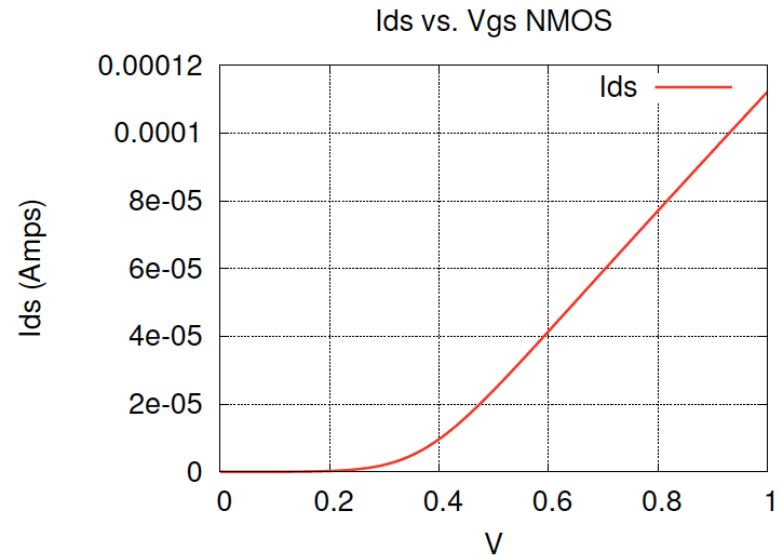
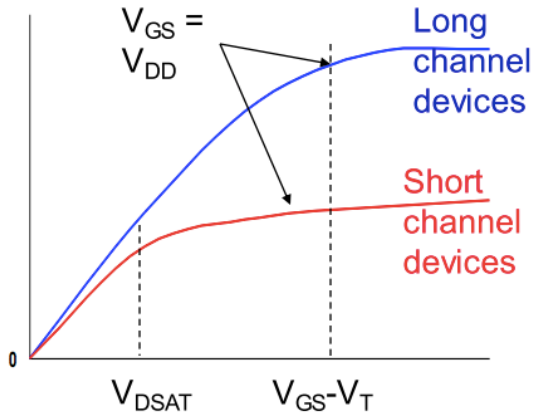
Operation Region	C_{GCB}	C_{GCS}	C_{GCD}	C_{GC}	C_G
Subthreshold	$C_{OX}WL$	0	0	$C_{OX}WL$	$C_{OX}WL+2C_O$
Linear	0	$C_{OX}WL/2$	$C_{OX}WL/2$	$C_{OX}WL$	$C_{OX}WL+2C_O$
Saturation	0	$(2/3)C_{OX}WL$	0	$(2/3)C_{OX}WL$	$(2/3)C_{OX}WL+2C_O$

$$C_o = \frac{1}{2} C_{ox} W (L_{drawn} - L_{effective}) = C_{GSO} = C_{GDO}$$

Big Idea

3+ Regions of operation for MOSFET

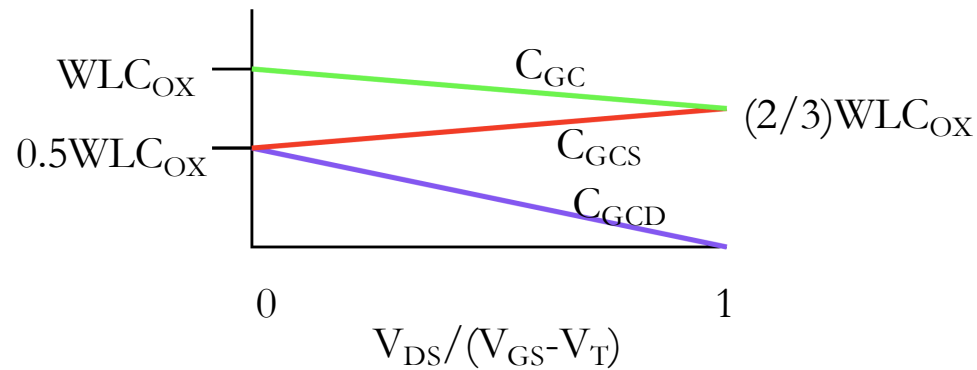
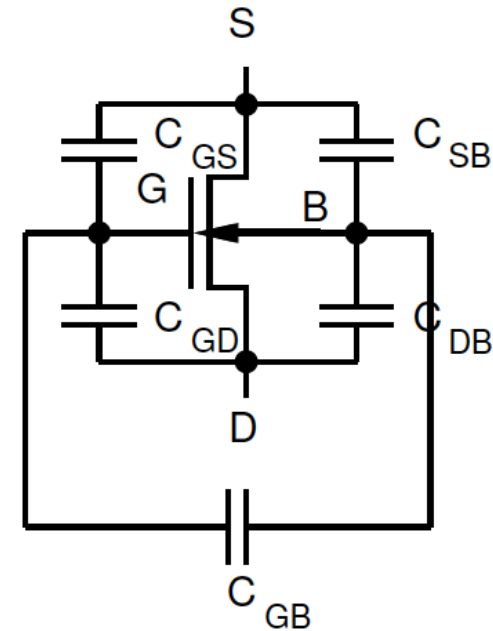
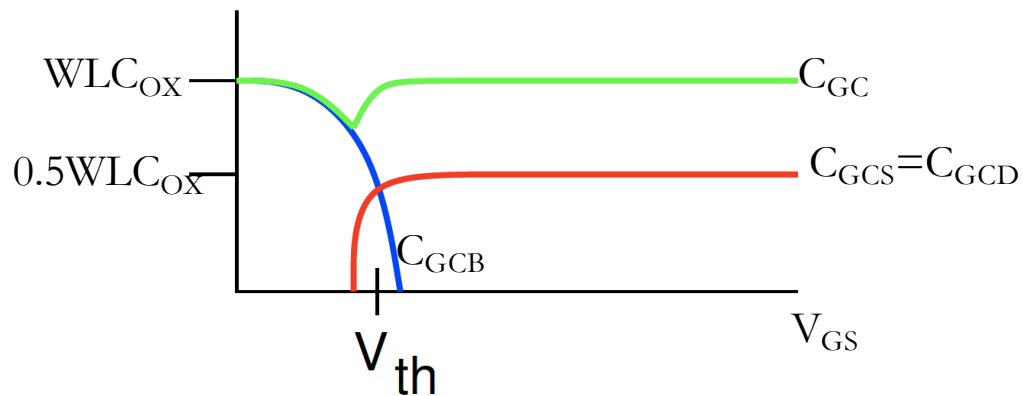
- Subthreshold
- Linear
- Saturation
 - Pinch Off
- Velocity Saturation, DIBL
 - Short channel



Big Idea

Capacitance

- To every terminal
- Voltage dependent





Admin

- ❑ HW3 out now – due 2/10 (Friday)
 - Takes time! Learning curve for how to debug
 - Don't forget the demo/video of SPICE workflow
- ❑ Monday Lecture Cancelled 2/13
- ❑ Midterm 1 Postponed to Wednesday 2/15
 - 1:30pm-3:30pm (Tentative) in LRSM 112B
 - See Ed Discussion
 - Midterm 1 Review session 2/8
 - See Ed Discussion



Acknowledgement

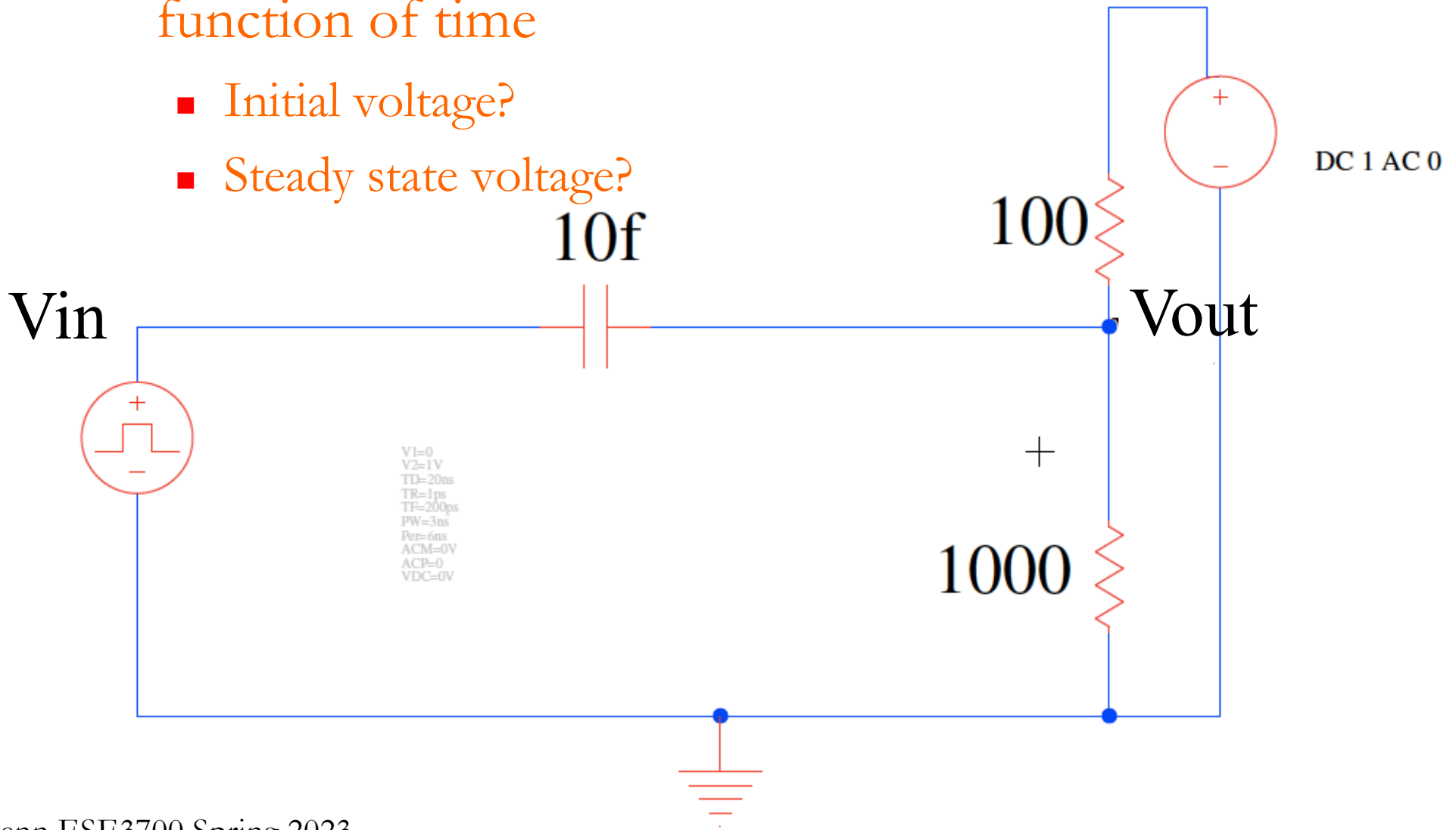
- ❑ Prof. André DeHon (University of Pennsylvania)
- ❑ Prof. Tania Li (University of Pennsylvania)

One Implication (Optional)

Feedback Capacitance C_{gd}

Step Response? (Preclass 3)

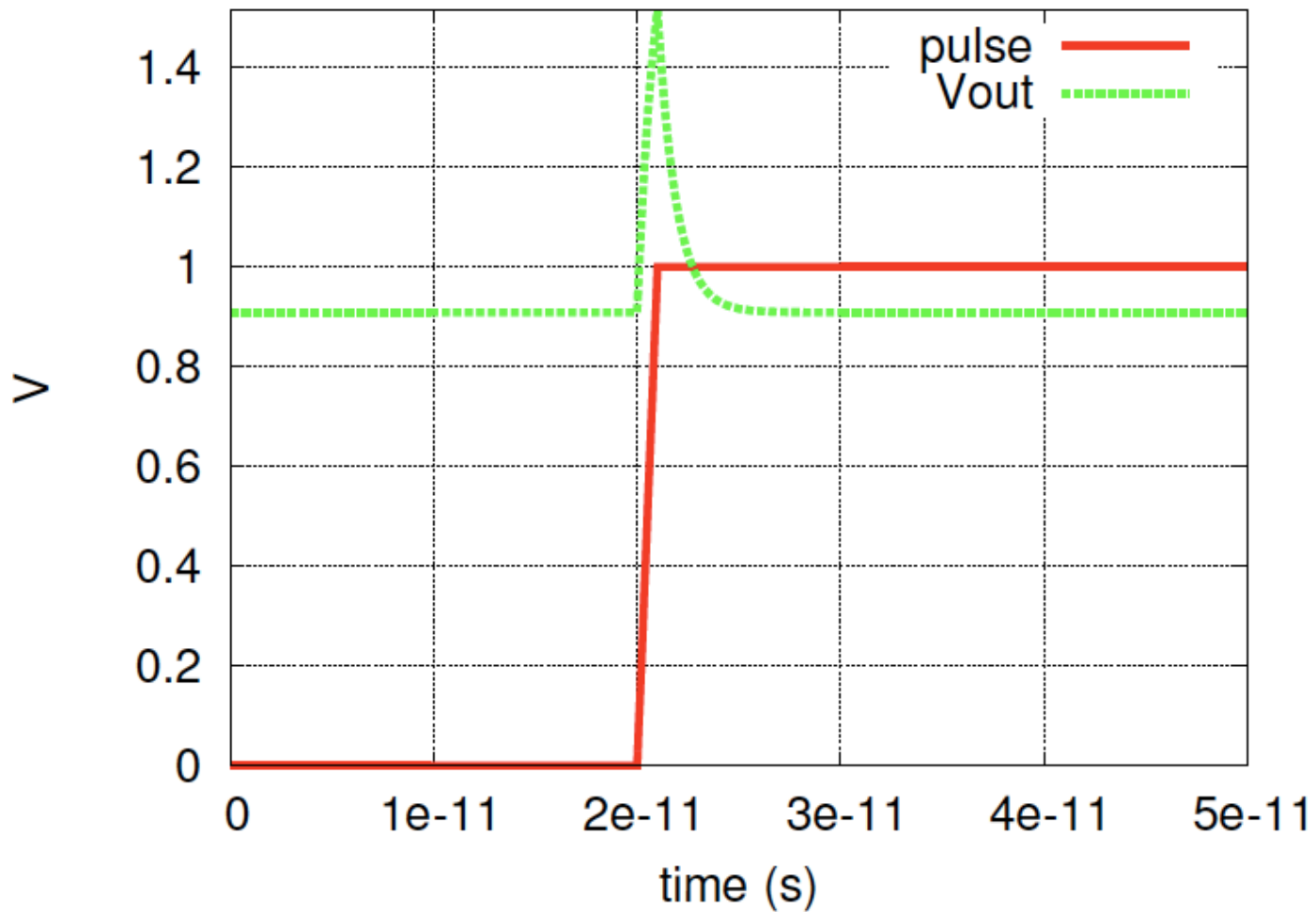
- V_{in} steps from 0 to 1, what does V_{out} look like as a function of time
 - Initial voltage?
 - Steady state voltage?





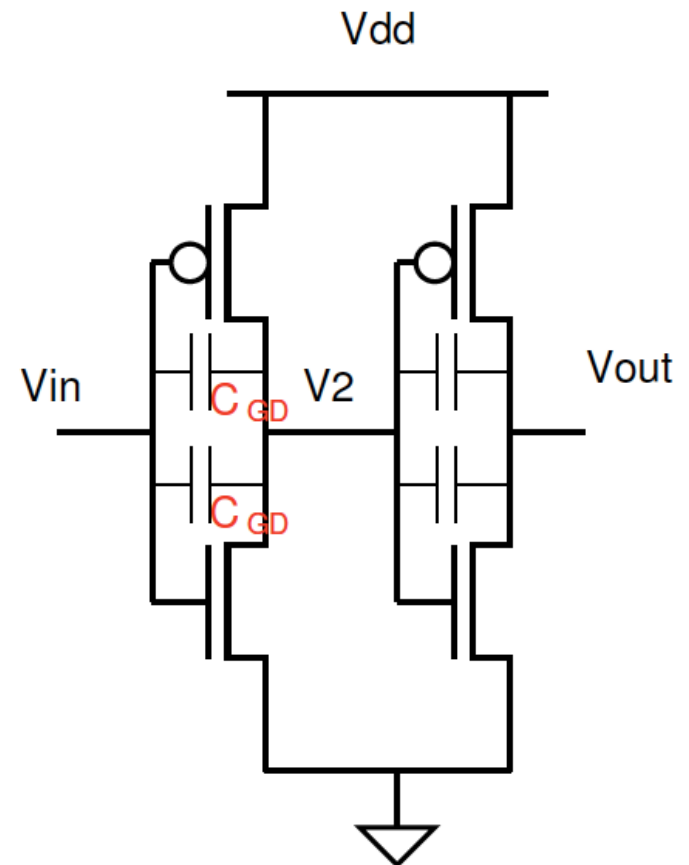
Step Response

Voltage peaking!



Impact of C_{GD}

- What does C_{GD} do to the switching response here?
 - V_2
 - V_{out}





Impact of C_{GD}

*** spice deck for cell flat_inv{sch} from library test

