

**University of Pennsylvania**  
**Department of Electrical and System Engineering**  
**System-on-a-Chip Architecture**

ESE5320, Fall 2022

Midterm

Wednesday, October 5

- Exam ends at 11:45AM; begin as instructed (target 10:15AM)  
Do not open exam until instructed.
- Problems weighted as shown.
- Calculators allowed.
- Closed book = No text or notes allowed.
- Show work for partial credit consideration. All answers here.
- Unless otherwise noted, answers to two significant figures are sufficient.
- Sign Code of Academic Integrity statement (see last page for code).

I certify that I have complied with the University of Pennsylvania's Code of Academic Integrity in completing this exam.

<b>Name:</b>
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1	2a	2b	3	4	5	6	7	8	Total
10	5	5	10	10	20	10	10	20	100

Consider the following (very simplified) code to find paths in a grid with obstacles.

```

#define MAX_TARGETS 100
#define MAX_TIMESTEPS 100
#define WIDTH 1000
#define HEIGHT 1000
#include <stdint.h>
#include <stdlib.h>
#include <stdbool.h>

#define BLOCKED (1<<15)-1
#define USED (1<<14)
#define SOURCE 0
#define TARGET ((1<<14)|2)
#define NOPATH (MAX_TIMESTEPS+1)
#define FREE NOPATH

#define MASK16 ((1<<16)-1)

typedef struct pair_xy
{
    uint16_t y;
    uint16_t x;
} pair_xy;

uint16_t min(uint16_t a, uint16_t b); // assume single instruction
uint16_t max(uint16_t a, uint16_t b); // assume single instruction
void read_obstacles(uint16_t g[HEIGHT][WIDTH]);
    // marks obstacles BLOCKED in g
void read_sources_and_targets(uint16_t g[HEIGHT][WIDTH],
    pair_xy source[MAX_TARGETS],
    pair_xy target[MAX_TARGETS]);
    // loads targets into target, sources into source
    // marks target in g
void share_paths(pair_xy paths[MAX_TARGETS][MAX_TIMESTEPS]);
    // reports out results
void reset_tgrid(uint16_t tgrid[MAX_TIMESTEPS][HEIGHT][WIDTH],
    pair_xy path[MAX_TARGETS][MAX_TIMESTEPS],
    pair_xy target[MAX_TARGETS], pair_xy source[MAX_TARGETS],
    int targ) {
    // Need to know when path done to stop following
    bool pdone[MAX_TARGETS];
    for (int t=0;t<MAX_TARGETS;t++) { pdone[t]=false; } // loop F

    for (int step=0;t<MAX_TIMESTEPS;t++) { // loop G
        for (int y=0;y<HEIGHT;y++) // loop H
            for (int x=0;x<WIDTH;x++) // loop I
                { tgrid[step][y][x]=NOPATH; }
        if (t==0)
            for (int s=0;s<MAX_TARGETS;s++) // loop J
                { tgrid[0][source[s].y][source[s].x]=0; }
        for (int t=0;t<targ;t++) // loop K
            if (!pdone[t]) {
                tgrid[step][path[t][step].y][path[t][step].x]=USED;
                if ((path[t][step].x==target[t].x)
                    && (path[t][step].y==target[t].y)) // end of path
                    { pdone[t]=true; }
            }
    }
}

```

```

uint16_t new_cost(uint16_t grid[HEIGHT][WIDTH],
                 uint16_t tgrid[MAX_TIMESTEPS][HEIGHT][WIDTH],
                 uint16_t t, uint16_t y, uint16_t x){
    uint16_t below=max(grid[y-1][x],tgrid[t][y-1][x]);
    uint16_t above=max(grid[y+1][x],tgrid[t][y+1][x]);
    uint16_t left=max(grid[y][x-1],tgrid[t][y][x-1]);
    uint16_t right=max(grid[y][x+1],tgrid[t][y][x+1]);
    return(min(min(below,above),min(left,right))+1);
}

uint32_t predecessor(uint16_t tgrid[MAX_TIMESTEPS][HEIGHT][WIDTH],
                    uint16_t t, uint16_t y, uint16_t x) {
    if (tgrid[t-1][y-1][x]==t-1) { return((y-1)<<16 | x); }
    if (tgrid[t-1][y+1][x]==t-1) { return((y+1)<<16 | x); }
    if (tgrid[t-1][y][x-1]==t-1) { return(y<<16 | (x-1)); }
    if (tgrid[t-1][y][x+1]==t-1) { return(y<<16 | (x+1)); }
    abort(); // inconsistency: predecessor not find match
}

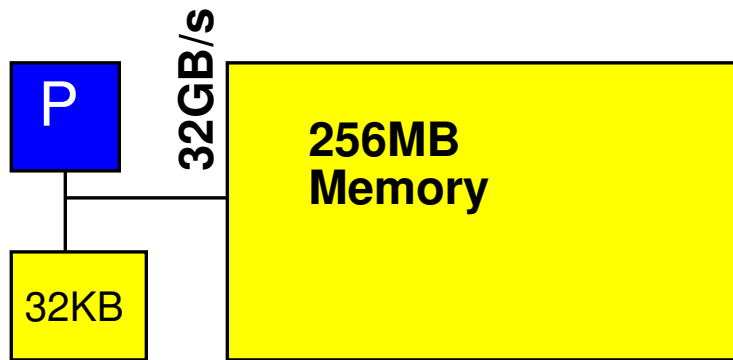
void find_paths () {
    uint16_t grid[HEIGHT][WIDTH];
    uint16_t tgrid[MAX_TIMESTEPS][HEIGHT][WIDTH];
    pair_xy target[MAX_TARGETS];
    pair_xy source[MAX_TARGETS];
    pair_xy path[MAX_TARGETS][MAX_TIMESTEPS];
    bool found;
    int found_time;

    read_obstacles(grid);
    read_sources_and_targets(grid, source, target);
    reset_tgrid(tgrid, path, target, source, 0);

    for(int targ=0;targ<MAX_TARGETS;targ++) { // loop A
        found=false;
        for (int t=0; ((!found) || (t<MAX_TIMESTEPS));t++) // loop B
            for (int y=0;y<HEIGHT;y++) // loop C
                for (int x=0;x<WIDTH;x++) { // loop D
                    uint16_t cost=new_cost(grid,tgrid,t,y,x);
                    if (grid[y][x]==FREE) { tgrid[t+1][y][x]=cost; }
                    bool found_now=((target[targ].x==x)&&(target[targ].y==y)
                                     &&(cost<NOPATH));
                    found|=found_now;
                    if (found_now) { found_time=t; }
                }
        path[targ][found_time].x=target[targ].x;
        path[targ][found_time].y=target[targ].y;
        for(int it=found_time;it>0;it--) { // loop E
            uint32_t pxy=predecessor(tgrid,it,path[targ][it].y,path[targ][it].x);
            path[targ][it-1].y=pxy>>16;
            path[targ][it-1].x=(pxy&MASK16);
        }
        reset_tgrid(tgrid, path, target, source, targ); // loop F-K inside
    }
    share_paths(path);
}

```

We start with a baseline, single processor system as shown.



## local scratchpad memory

- For simplicity throughout, we will treat non-memory indexing adds (subtracts count as adds), compares, min, max, abs, divides, multiplies, shifts, and logical operations (binary and bitwise) as the only compute operations. We'll assume the other operations take negligible time or can be run in parallel (ILP) with the adds, multiplies, and memory operations. (Some consequences: You may ignore loop and conditional overheads in processor runtime estimates; you may ignore computations in array indices.)
- Baseline processor can execute one multiply, divide, compare, min, max, abs, or add per cycle and runs at 1 GHz.
- Data can be transferred from the 256 MB main memory at 32 GB/s when streamed in chunks of at least 256B. Assume for loops that only copy data can be auto converted into streaming operations.
- Non-streamed access to the main memory takes 20 cycles.
- Baseline processor has a local scratchpad memory that holds 32KB of data. Data can be streamed into the local scratchpad memory at 32 GB/s. Non-streamed accesses to the local scratchpad memory takes 1 cycle.
- By default, all arrays live in the main memory.
- Arrays `source`, `target`, and `pdone` live in local scratchpad memory.
- Assume scalar (non-array) variables can live in registers.
- Assume all additions are associative.

## 1. Simple, Single Processor Resource Bounds

Give the single processor resource bound time for compute operations and memory access for each loop directly inside loop A and the total bound for loop A.

loop	Compute	Memory
B		
E		
F		
G		
A		

2. Based on the simple, single processor mapping from Problem 1:

(a) What loop is the bottleneck? Consider both compute and memory.  
(circle one)

B

E

F

G

(b) What is the Amdahl's Law speedup if you only accelerate the identified function?  
Consider both compute and memory.

## 3. Parallelism in Loops

- (a) Classify the following loops as data parallel or not? (loop bodies could be executed concurrently)
- (b) Explain why or why not?

Loop	Data Parallel?	Why or why not?
A		
B		
C		
D		
E		
F		
G		
H		
I		
K		

4. What is the critical path for the body of loop A?



(This page intentionally left mostly blank for answers.)

5. Revise the body of `loop B` to minimize the memory resource bound by exploiting the scratchpad memory and streaming memory operations.

(a) Identify the array or arrays whose memory operations account for most of the time in the loop.

(b) How would you use the scratchpad memory to reduce the time required to access memory? (You don't need to give code, but you need to describe clearly how the code would change. You may show code if that is the most efficient way to communicate your changes.)

(c) Account for total memory usage in the local scratchpad (use provided table)

Variable	Size (Bytes)
source	
target	
pdone	

(d) Estimate the new memory resource bound for your optimized `loop B`.

(This page intentionally left mostly blank for answers.)

6. Assume you have a vector processor that can provide 16 vector lanes for 16b (including uint16\_t) operations. The vector processor can read or write 256b from its local scratchpad memory in one cycle using a vector read or vector write operation. Build on your memory optimizations in the previous question. If necessary, describe any additional memory optimizations you may do beyond the previous question for this vector case. Assuming perfect vectorization, what is the impact on the compute and memory resource bounds for `loop B`? (state new bounds; show work.)

## 7. Identify concurrency opportunities between loops.

Which loops can run concurrently, as separate processes, to increase the **throughput** for loop A? If they cannot, explain what prevents concurrency. If they can, explain why and what conditions need to be met for the concurrency to work.

	Concurrent?	How or Why not?
B + E		
E + F		
F + B	Y	

Hint: we're giving you that there is concurrency between F and B. Note that they both iterate over timesteps. Identify the constraints required for them to run concurrently.

8. Map the `loop A` computation to a system composed of two simple processors (1 GHz as previously outlined), two fast processors (2 GHz, with everything running  $2\times$  as fast except data transfer from main memory), and four vector processors (Problem 6). Assume each processor has its own scratchpad and has a separate path to the large memory so they can all simultaneously stream at full rate.<sup>1</sup>

(a) Describe how you would map the computation onto these heterogeneous computing resources.

(b) As necessary, describe how you would use the scratchpad memories as necessary beyond what you've already answered in Problems 5 and 6. [no further change is a possible answer here.]

(c) Estimate the performance your mapping achieves in cycles per `loop A` iteration.

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<sup>1</sup>Probably not realistic, but we'll use to simplify this problem.

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## Code of Academic Integrity

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**C. Fabrication** Submitting contrived or altered information in any academic exercise. Example: making up data for an experiment, fudging data, citing nonexistent articles, contriving sources, etc.

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\* If a student is unsure whether his action(s) constitute a violation of the Code of Academic Integrity, then it is that student's responsibility to consult with the instructor to clarify any ambiguities.