

ESE5320: System-on-a-Chip Architecture

Day 8: September 27, 2023
Spatial Computations

Preclass 2 physical pages



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Today

- Accelerator Pipelines (Part 1)
- FPGAs (Part 2)
- Computational Capacity (Part 3)
 - Zynq

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Message

- Custom accelerators efficient for large computations
 - Exploit Instruction-level parallelism
 - Run many low-level operations in parallel
- Field-Programmable Gate Arrays (FPGAs)
 - Allow post-fabrication configuration of custom accelerator pipelines
 - Can offer high computational capacity

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Accelerator Datapaths

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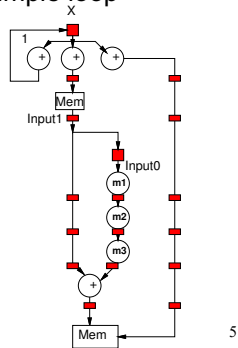
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Pipeline Graph

- Last time: pipelined simple loop

```

unsigned char Input0, Input1;
Input1=Input[Y * INPUT_WIDTH + X + 0];
for (int X = 0; X < OUTPUT_WIDTH; X++)
{
    unsigned int Sum;
    Input0=Input1;
    Input1=Input[Y * INPUT_WIDTH + X + 1];
    Sum = Coefficients_0 * Input0 + Input1;
    Output[Y * OUTPUT_WIDTH + X] = Sum;
}
    
```

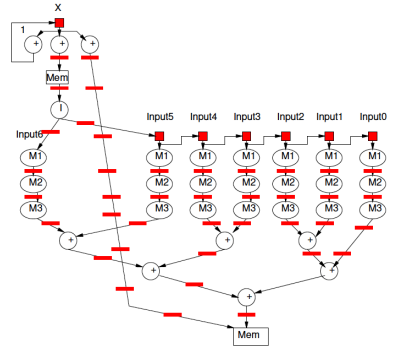


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Pipeline for Unrolled Loop



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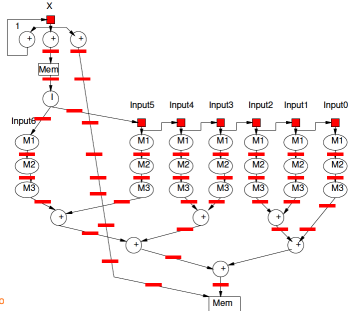
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Preclass 1

- For fully unrolled loop shown, how many instructions per pipeline cycle?

- Add
- Mpy
- Load
- Store



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Spatial Pipeline

- Can compute equivalent of tens of “instructions” in a cycle
- Wire up primitive operators
 - No indirection through register file, memory
- Pipeline for operator latencies
- Any dataflow graph of computational operations

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Operators

- Can assemble any custom operators
 - Ones may not have in generic processor
- Processor
 - Add, bitwise-xor/and/or
 - Maybe: floating-point add, multiply
- Less likely
 - Square-root, exponent, cosine, encryption (AES) step, polynomial evaluate, log-number-system

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Accelerators

- Compression/decompression
- Encryption/decryption
- Encoding (ECC, Checksum)
- Discrete Cosine Transform (DCT)
- Sorter
- Taylor Series Approximation of function
- Transistor evaluator
- Tensor or Neural Network evaluator

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Streaming Dataflow

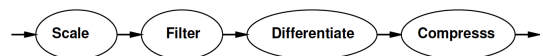
- Replace operator with custom accelerator
- Stream data to/from it

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Streaming Dataflow Example



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Application-Specific SoCs

- For dedicated applications may build custom hardware for accelerators
 - Layout VLSI, fab unique chips
 - ESE3700, 5700
- Video-encoder – include custom DCT, motion-estimation engines

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Apple A16 Bionic

- ? 110+mm², 4nm
- 16 Billion Tr.
- iPhone 14
- 6 ARM cores
 - 2 fast (3.5GHz)
 - 4 low energy (2GHz)
- 5 custom GPUs (1.4GHz)
- 16 Neural Engines
 - 17 Trillion ops/s?



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https://en.wikipedia.org/wiki/Apple_A16

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Customizable Accelerators

- With post-fabrication configurability can exploit without unique fabrication
- Need programmable substrate that allows us to wire-up computations

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Field-Programmable Gate Arrays

FPGAs
Part 2

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FPGA

- Idea: Can wire up programmable gates in the “field”
 - After fabrication
 - At your desk
 - When part “boots”
- Like a “Gate Array”
 - But not hardwired

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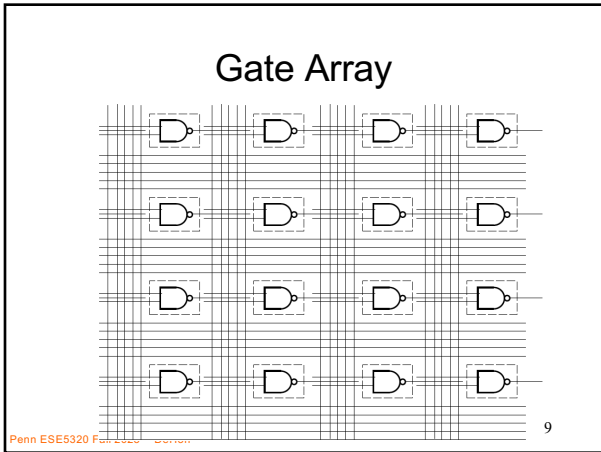
Gate Array

- Idea: Provide a collection of uncommitted gates
- Create your “custom” logic by wiring together the gates
- Less layout, fewer masks than full custom IC Chip
 - Since only wiring together pre-fab gates
 - lower cost (fewer masks)
 - lower manufacturing delay

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GA → FPGA

- Remove the need to even fabricate the wiring mask
- Make “customization” soft
- Key trick:
 - Use reprogrammable configuration bits
 - Typically: static-RAM bits
 - Like SRAM cells or latches in memory
 - Hold a configuration value
 - Configuration bits define gates, wiring

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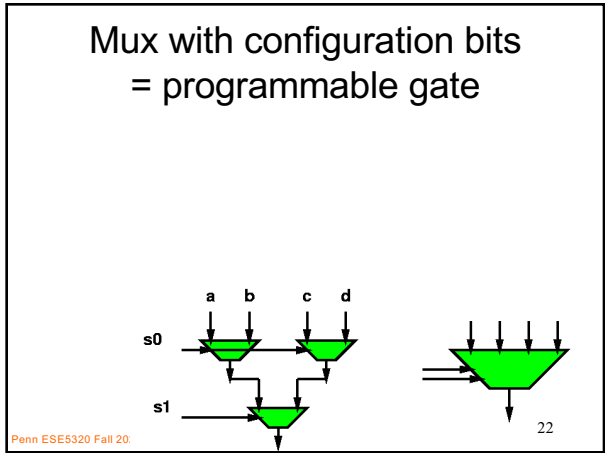
Multiplexer Gate

- MUX
 - When S=0, output=i0
 - When S=1, output=i1

$$\text{Out} = \overline{s} \cdot i_0 + s \cdot i_1$$

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Preclass 4a

- How do we program to behave as and2?

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Preclass 4b

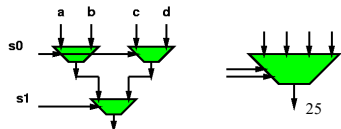
- How do we program to behave as xor2?

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Mux as Logic

- Just by “configuring” data into this mux4,
 - Can select **any** two input function

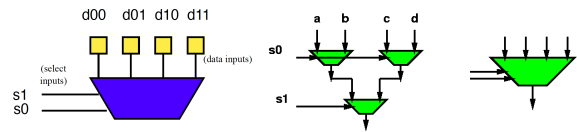


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LUT – LookUp Table

- When use a mux as programmable gate
 - Call it a **LookUp Table (LUT)**
 - Implementing the Truth Table for small # of inputs
 - k-LUT: # of inputs =k (need mux- 2^k)
 - Just lookup the output result in the table

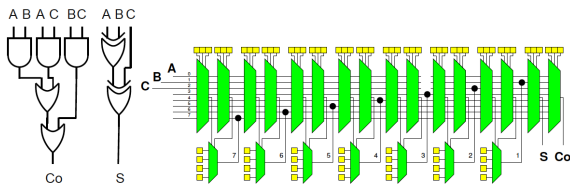


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Preclass 6

- How do we program full adder?



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[Switch Google Doc]

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FPGA

- Programmable gates + wiring
 - (both built from muxes w/ config. bits)
- Can wire up any collection of gates
 - Like a gate array

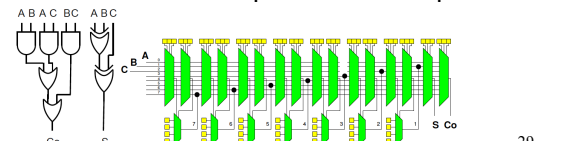
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Simplistic FPGA (illustrate possibility)

- Every LUT input has a mux
- Every such mux has $m=(N+1)$ inputs
 - An input for each LUT output (N 2-LUTs)
 - An input for each Circuit Input (I Circuit inputs)
- Each Circuit Output has an m-input mux



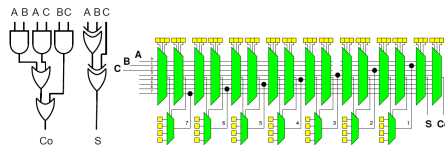
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Simplistic FPGA (illustrate possibility)

- N 2-LUTs, I Circuit Inputs, O Circuit Outputs
- $2N+O$ muxes to connect
- Can build **any** combinational logic circuit that doesn't need more than N 2-input gates, I inputs, O outputs



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Preclass 3

How big is an m-input mux?

- In terms of 2-input muxes?
 - Warmup: how many for 4-input (Preclass 2)
 - Warmup: how many for 8-input (below)

m inputs – what we are selecting from

$\log_2(m)$ bits to select which input routed to output

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Math: Series Sums

- $A_0(1+r+r^2+r^3+r^4+\dots)$
- $A_0(1+r+r^2+r^3+r^4+\dots)*(1-r)$

$$= A_0 + A_0 r + A_0 r^2 + A_0 r^3 + A_0 r^4 + \dots$$

$$- A_0 r - A_0 r^2 - A_0 r^3 - A_0 r^4 - \dots$$

$$= A_0 \quad (\text{when } r < 1)$$
- $A_0(1+r+r^2+r^3+r^4+\dots)*(1-r) = A_0$
- $A_0(1+r+r^2+r^3+r^4+\dots) = A_0/(1-r)$

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Receding Sum

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Preclass 3

How big is an m-input mux?

- m-input mux will require m-1 2-input muxes

m inputs – what we are selecting from

$\log_2(m)$ bits to select which input routed to output

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Simplistic FPGA

(illustrate possibility...and expense)

- $2N+O$ m-input muxes; $m=N+1$
- Each m-input mux is m-1 2-input muxes
- Requires: $(2N+O)*(N+1-1)$ 2-input muxes
- Mux area grows as $\sim N^2$
 - when gate (LUT) area grows as N

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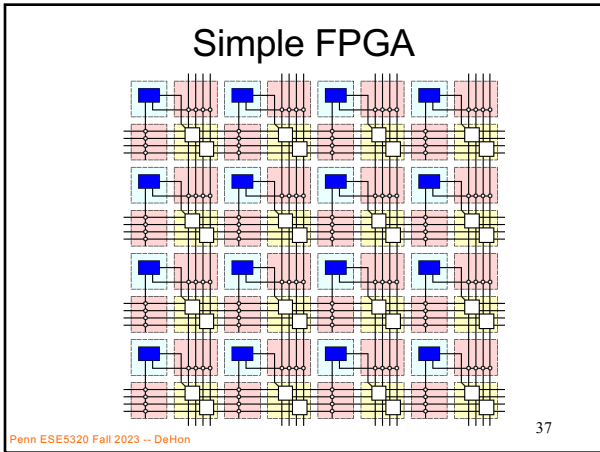
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Interconnect

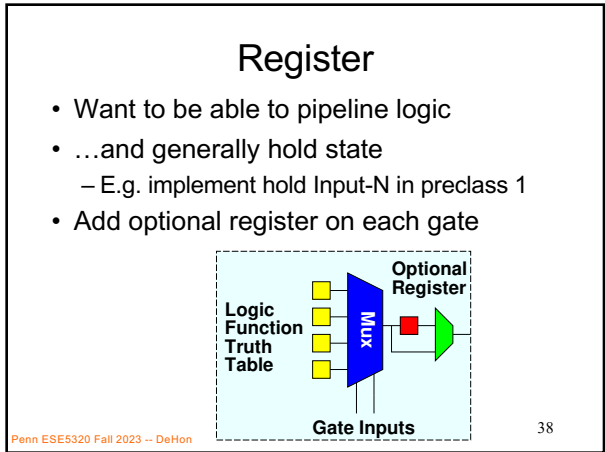
- Fully connected mux input is too expensive, growing as N^2
 - ...and not necessary
- Want
 - To be able to wire up gates
 - Economical with wires and muxes
 - ...and configuration bits
 - Exploit locality (keep wires short)

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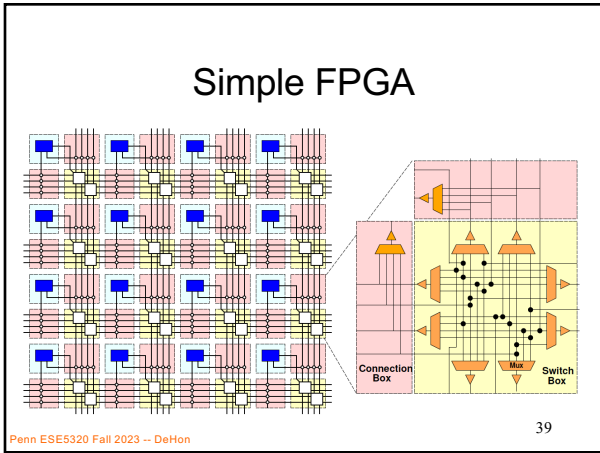
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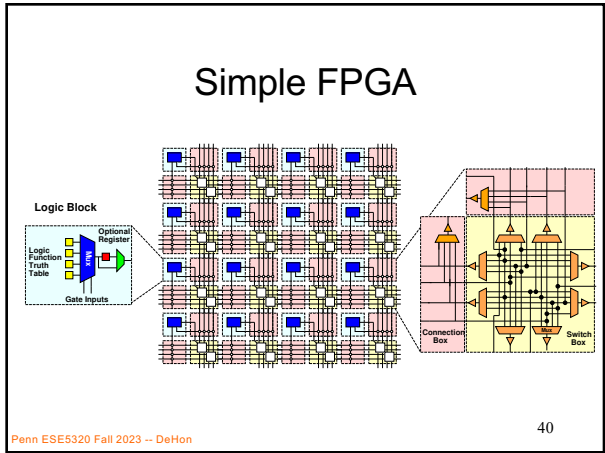
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FPGA Design

- Raises many architectural design questions
 - How big (many inputs) should the gates have? (what k should use for k-LUTs?)
 - Are LUTs really the right thing...
 - How rich is the interconnect?
 - Wires/channel
 - Wire length
 - Switching options

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Modern FPGAs

- Logic Blocks
 - hardwired fast-carry logic
 - Can implement adder bit in single "LUT"
 - Speed optimized: 6-LUTs
 - Energy, Cost optimization: 4-LUTs
 - Clusters many LUTs into a tile
- Interconnect
 - Mesh, segments of length 4 and longer

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More than LUTs

- Should there be more than LUTs in the “array” fabric?
- What else might we want?

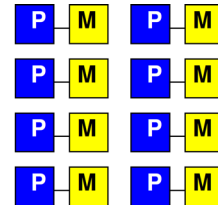
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Embedded Memory

- One flip-flop per LUT doesn't store state densely
- Want memory close to logic



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Embed Memory in Array

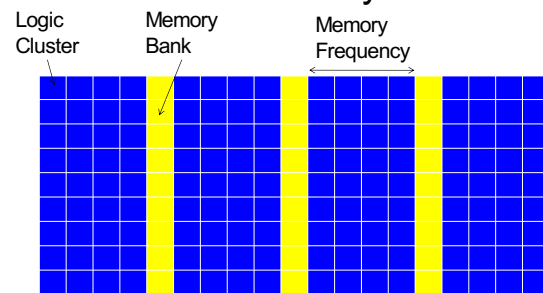
- Replace logic clusters
- Convenient to replace columns
 - Since area of memory may not match area of logic cluster

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Embedded Memory in FPGA



Memory banks on AMD/Xilinx called BRAMs (Block RAMs)

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Hardwired Multipliers

- Can build multipliers out of LUTs
 - Just as can implement multiplies on processor out of adds
- But, custom multiplier is smaller than LUT-configured multiplier
 - ...and multipliers common in signal processing, scientific/engineering compute

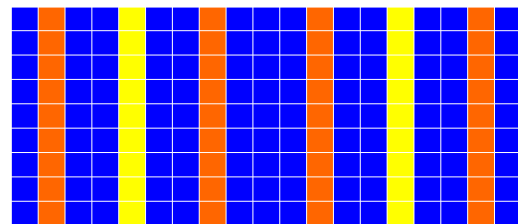
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Multiplier Integration

- Integrate like memories
 - Replace columns



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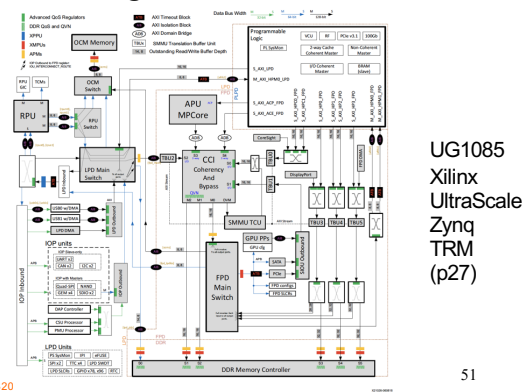
More FPGA Architecture Design Questions

- Size of Memories? Multipliers?
- Mix of LUTs, Memories, Multipliers?
- Add processors? Floating-point?
- Other hardwired blocks?
- How manage configuration?

Zynq MPSoC

Part 3

Programmable SoC



ZU3EG (Ultra96)

- 6-LUTs: 70,560
- DSP Blocks: 360
 - 18x27 multiply, 48b accumulate
- Block RAMs (BRAMs): 216
 - 36Kb
 - Dual port
 - Up to 72b wide (512x72)

DSP48

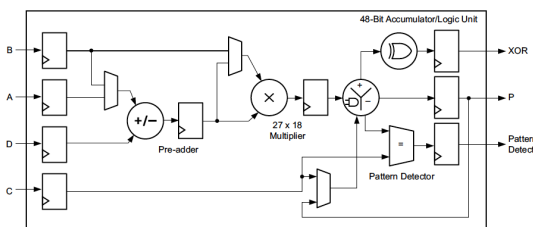


Figure 1-1: Basic DSP48E2 Functionality

Xilinx UG579 UltraScale DSP Slice User's Guide 53

Preclass 5

Approximating	Resources	Cycle	Per second
Zynq LUTs	70,000 adder bits	0.5 GHz	
4x ARM Scalar	4x2x64 adder bits	1.2 GHz	
4x ARM Neon	4x1x64 adder bits	1.2 GHz	
Zynq DSP	360 multiply-accumulates	0.5 GHz	
4x ARM Scalar	4x(1 mpy+1add)	1.2 GHz	
4x ARM Neon	4x1x4 multiply-accumulates	1.2 GHz	

- How compare between ARM scalar, ARM NEON and FPGA array?

– Adder-bits/second?

– Multiply-accumulators/second?

Capacity → Density

- Says Zynq has high computational capacity in FPGA
- More broadly
 - FPGA can have more compute/area than processor
 - E.g., more adder bits in some fixed area
 - SIMD can have more compute/area than processor (Day 6)
 - How wide SIMD can you exploit?

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FPGA Potential

- FPGA Array has high raw capacity
- Exploitable when computation has high regularity
 - Uses the same computation over-and-over
 - High throughput on a computation
 - Build customized accelerator pipeline to match the computation
- Low-hanging fruit
 - Operator/function takes most of the compute time

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90/10 Rule

- Observation that code is not used uniformly
- 90% of the time is spent in 10% of the code
- Knuth: 50% of the time in 2% of the code
- Opportunity
 - Build custom datapath in FPGA (hardware) for that 10% (or 2%) of the code

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Big Ideas

- Custom accelerators efficient for large computations
 - Exploit Instruction-level parallelism
 - Run many low-level operations in parallel
- Field Programmable Gate Arrays (FPGAs)
 - Allow post-fabrication configuration of custom accelerator pipelines
 - Can offer high computational capacity

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Admin

- Reading for Day 9 on canvas
- HW4 due on Friday
- HW5 out soon
 - Heavier – start early...
 - Vivado HLS synthesis slow (plan for it)

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