# University of Pennsylvania Department of Electrical and System Engineering System-on-a-Chip Architecture 

- Exam ends at 11:45Am; begin as instructed (target 10:15Am)

Do not open exam until instructed.

- Problems weighted as shown.
- Calculators allowed.
- Closed book $=$ No text or notes allowed.
- Show work for partial credit consideration. All answers here.
- Unless otherwise noted, answers to two significant figures are sufficient.
- Sign Code of Academic Integrity statement (see last page for code).

I certify that I have complied with the University of Pennsylvania's Code of Academic Integrity in completing this exam.

## Name:

Solution

| 1 | 2 a | 2 b | 3 | 4 | 5 | 6 | 7 | 8 | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | 5 | 5 | 10 | 10 | 20 | 10 | 10 | 20 | 100 |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |

Exam ended up being time constrained.
Mean: 57, Std. Dev. 12

Consider the following (very simplified) code to perform Deep Neural Network (DNN) Classification on a stream of matrix inputs.
Boundary conditions omitted for simplicity.)

```
#define DIM1 1024
#define WINDOW 64
#define STEP (WINDOW/2)
#define DIM2 (DIM1/STEP)
#define DIM3 (DIM2*DIM2)
#define STAGES 10
#define NORMALIZE 16
#define THRESH (1<<(NORMALIZE+1))
#include <stdint.h>
#include <stdlib.h>
#include <stdbool.h>
uint16_t in[DIM1][DIM1];
uint32_t mout[DIM1][DIM1];
uint16_t s2[DIM1][DIM1];
uint32_t cout[DIM2][DIM2];
uint16_t sinput[STAGES][DIM3];
uint32_t snorm[STAGES][DIM3];
uint16_t cm[DIM1][DIM1];
uint16_t cc[WINDOW][WINDOW];
uint16_t cweights[STAGES][DIM3][DIM3];
// static assignment to weights not shown for bevity
// assume these stream data in and out at the streaming rate
// as data is available
void read_input(uint16_t input[DIM1][DIM1]);
void write_output(uint16_t sout[STAGES][DIM3], uint16_t s);
void mvmpy(uint16_t a[STAGES][DIM3], uint16_t c[STAGES][DIM3][DIM3],
            uint16_t s, uint32_t o[STAGES][DIM3]) {
    for (int i=0;i<DIM3;i++) { // loop A
        o[s][i]=0;
        for (int x=0;x<DIM3;x++) // loop B
            o[s][i]+=a[s-1][x]*C[s][i][x];
        }
}
```

```
void conv2digest(uint16_t a[DIM1][DIM1], uint16_t w[WINDOW][WINDOW],
                    uint32_t o[DIM2][DIM2]) {
    for (int y=0;y<DIM2;y++) // loop C
        for (int x=0;x<DIM2;x++) // loop D
            {
                o[y][x]=0;
                    for (int wy=0;wy<WINDOW;wy++) // loop E
                    for (int wx=0;wx<WINDOW;wx++) // loop F
                    o[y][x]+=a[y*STEP+wy][x*STEP+wx]*w[wy][wx];
            }
}
void mmmpy(uint16_t a[DIM1][DIM1], uint16_t b[DIM1][DIM1],
                    uint32_t o[DIM1][DIM1]) {
    for (int y=0;y<DIM1;y++) // loop G
        for (int x=0;x<DIM1;x++) { // loop H
            o[y][x]=0;
            for (int k=0;k<DIM1;k++) // loop I
                o[y][x]+=a[y][k]*b[k][x];
            }
}
void nlmap2d (uint32_t i[DIM1][DIM1], uint16_t o[DIM1][DIM1]) {
    for (int y=0;y<DIM1;y++) // loop J
        for (int x=0;x<DIM1;x++) // look K
            if (i[y][x]<THRESH)
                o[y][x]=(i[y][x]>>NORMALIZE);
            else
                O[y][x]=0;
}
void nlmapflat (uint32_t i[DIM2][DIM2], uint16_t o[STAGES][DIM3], uint32_t s) {
    for (int y=0;y<DIM2;y++) // loop L
        for (int x=0;x<DIM2;x++) // loop M
            if (i[y][x]<THRESH)
                o[s][y*DIM2+x]=(i[y][x]>>NORMALIZE);
            else
                o[s][y*DIM2+x]=0;
}
void nlmap (uint32_t i[STAGES][DIM3], uint16_t o[STAGES][DIM3], uint32_t s) {
    for (int x=0;x<DIM3;x++) // loop N
            if (i[s][x]<THRESH)
                O[s][x]=(i[s][x]>>NORMALIZE);
            else
                o[s][x]=0;
}
int main(int argv, char **argc) {
    while (true) {
        read_input(in);
            mmmpy(in,cm,mout);
            nlmap2d(mout,s2);
            conv2digest(s2,cc,cout);
            nlmapflat(cout,sinput,0);
            for (int s=1;s<STAGES;s++) {
                mvmpy(sinput, cweights,s,snorm);
                nlmap(snorm,sinput,s);
            }
            write_output(sinput,(STAGES-1));
        }
}
```

We start with a baseline, single processor system as shown.


- For simplicity throughout, we will treat non-memory indexing adds (subtracts count as adds), compares, min, max, abs, divides, multiplies, shifts, and logical operations (binary and bitwise) as the only compute operations. We'll assume the other operations take negligible time or can be run in parallel (ILP) with the adds, multiplies, and memory operations. (Some consequences: You may ignore loop and conditional overheads in processor runtime estimates; you may ignore computations in array indecies.)
- Baseline processor can execute one multiply, divide, compare, min, max, shift, abs, or add per cycle and runs at 1 GHz .
- Data can be transfered from the 256 MB main memory at $32 \mathrm{~GB} / \mathrm{s}$ when streamed in chunks of at least 256B. Assume for loops that only copy data can be auto converted into streaming operations.
- Non-streamed access to the main memory takes 10 cycles.
- Baseline processor has a local scratchpad memory that holds 32 KB of data. Data can be streamed into the local scratchpad memory at $32 \mathrm{~GB} / \mathrm{s}$. Non-streamed accesses to the local scratchpad memory takes 1 cycle.
- By default, all arrays live in the main memory.
- Assume scalar (non-array) variables can live in registers.
- Assume all additions are associative.
- Assume comparisons, adds, min, max, divide and multiplies take 1 ns when implemented in hardware accelerator, so fully pipelined accelerators also run at 1 GHz .

1. Simple, Single Processor Resource Bounds

Give the single processor resource bound time for compute operations and memory access for each function directly inside the main loop and the total bound for the while loop in main.

| loop | Compute | Memory |
| :---: | :---: | :---: |
| read_input |  | $\frac{1024^{2} \times 2}{32}=65,536$ |
| mmmpy | $\begin{aligned} & 1024^{3} \times 2 \\ & =2.1 \times 10^{9} \end{aligned}$ | $\begin{gathered} 1024^{3} \times 3 \times 10 \\ (4 \text { instead of } 3 \text { if re-read o) } \\ =3.2 \times 10^{10} \end{gathered}$ |
| nlmap2d | $1024^{2} \times 2$ $2.1 \times 10^{6}$ | $1024^{2} \times 2 \times 10$ <br> 2 for read $\mathrm{i}[\mathrm{y}][\mathrm{x}]$ once <br> (alternately 3) $2.1 \times 10^{7}$ |
| conv2digest | $\begin{gathered} 32^{2} \times 64^{2} \times 2 \\ =8.4 \times 10^{6} \end{gathered}$ | $\begin{gathered} 32^{2} \times 64^{2} \times 3 \times 10 \\ =1.26^{8} \end{gathered}$ |
| nlmapflat | $\begin{aligned} & 32^{2} \times 2 \\ & =2,048 \end{aligned}$ | $\begin{gathered} 32^{2} \times 2 \times 10 \\ \text { (alternately } 3 \text { as above) } \\ =20,480 \end{gathered}$ |
| mvmpy (all STAGES) | $\begin{gathered} 9 \times 1024^{2} \times 2 \\ 1.9 \times 10^{7} \end{gathered}$ | $\begin{gathered} 9 \times 1024^{2} \times 3 \times 10 \\ 2.8 \times 10^{8} \end{gathered}$ |
| nlmap <br> (all STAGES) | $\begin{gathered} 9 \times 1024 \times 2 \\ =18,432 \end{gathered}$ | $\begin{gathered} 9 \times 1024 \times 3 \times 10 \\ =276,480 \end{gathered}$ |
| write_output |  | $\begin{aligned} & \frac{10 \times 32 \times 2}{32}=320 \\ & \text { or } 32 \times 10=320 \end{aligned}$ |
| main while | $\approx 2.1 \times 10^{9}$ | $\approx 3.2 \times 10^{10}$ |

2. Based on the simple, single processor mapping from Problem 1:
(a) What function is the bottleneck? Consider both compute and memory. (circle one)

# mmmpy <br> nlmap2d <br> conv2digest <br> mlmapflat <br> mvmpy (all STAGES) <br> nlmap (all STAGES) 

(b) What is the Amdahl's Law speedup if you only accelerate the identified function? Consider both compute and memory.
Compute except mmmpy: $29.5 \times 10^{6}$
Memory except mmmpy: $427 \times 10^{6}$
compute+memory except mmmpy: $456.5 \times 10^{6}$
$\frac{(2.1+32) \times 10^{9}+456.5 \times 10^{6}}{456.5 \times 10^{6}} \approx 76$
3. Parallelism in Loops
(a) Classify the following loops as data parallel or not? (loop bodies could be executed concurrently)
(b) Explain why or why not?

| Loop | Data <br> Parallel? | Why or why not? |
| :---: | :---: | :--- |
| A | Y |  |
| B | Reduce | Could say sequentialized on sum (not data <br> parallel); since associative add, we can <br> compute as a reduce, which we will iden- <br> tify as a separate category for final. For <br> credit, need to callout associative sum or <br> reduce as reason for calling this data par- <br> allel. |
| C | Y |  |
| E | Reduce | associative reduce like B |
| F | Reduce | associative reduce like B |
| G | Y |  |
| H | Y |  |
| I | Reduce | associative reduce like B |
| J | Y |  |
| K | Y |  |

4. What is the critical path for mmmpy function?

Perform all reads of $\mathrm{a}[\mathrm{y}][\mathrm{x}]$ and $\mathrm{b}[\mathrm{y}][\mathrm{x}]$ in parallel at beginning 10
Perform all multiplicies in parallel - 1
Perform loop I as add reduce - 10 cycles
(Alternately, perform adds in loop I sequentially for 1024 cycles)
Perform all writes of o[y][x] in parallel at end - 10 Total critical path is either 31 or 1045 .
(This page intentionally left mostly blank for answers.)
5. Revise the body of mmmpy to minimize the memory resource bound by exploiting the scratchpad memory and streaming memory operations.
(a) Identify the array or arrays whose memory operations account for most of the time in the loop.
a, b, o
(b) How would you rewrite mmmpy to use the scratchpad memory to reduce the time required to access memory? (show code)
Hint: an order of magnitude reduction in memory time is possible, but may be tricky. A little under $3 \times$ speedup is easier and will receive partial credit.

## - b won't fit in the scratchpad

- Cannot simply stream columns of b into a local column array since they will not be stored sequentially in memory.
- 20 pts for solution that makes it possible to stream a, b, and o while obeying scratchpad size constraints.
- 12 pts for solution that only streams a and o; done completely right, this should give about a $3 \times$ speedup since only reading b 10 cycles at a time.
- 7 pts for ignoring scratchpad size (and typically putting b in scratchpad.
- 7 pts for trying to stream b and treating it as streaming rather than random reads.
- Points further deducted from these baselines when details within the solution were missing or wrong.
code solution on next page

```
#define DIM1 1024
#include <stdint.h>
```

```
void mmmpy(uint16_t a[DIM1][DIM1], uint16_t b[DIM1][DIM1],
```

void mmmpy(uint16_t a[DIM1][DIM1], uint16_t b[DIM1][DIM1],
uint32_t o[DIM1][DIM1]) {
uint32_t o[DIM1][DIM1]) {
uint16_t arow[DIM1];
uint16_t arow[DIM1];
uint16_t orow[DIM1];
uint16_t orow[DIM1];
uint16_t b10rows[10][DIM1];
uint16_t b10rows[10][DIM1];
for (int y=0;y<DIM1;y++)
for (int y=0;y<DIM1;y++)
{
{
for (int x=0;x<DIM1;x++) arow[x]=a[y][x];
for (int x=0;x<DIM1;x++) arow[x]=a[y][x];
for (int }x=0;x<DIM1;x++) orow[x]=0
for (int }x=0;x<DIM1;x++) orow[x]=0
for (int k=0;k<DIM1;k+=10)
for (int k=0;k<DIM1;k+=10)
{
{
for (int kl=0;kl<10;kl++)
for (int kl=0;kl<10;kl++)
for (int x=0;x<DIM1;x++)
for (int x=0;x<DIM1;x++)
b10rows[kl][x]=b[k+kl][x];
b10rows[kl][x]=b[k+kl][x];
for (int x=0;x<DIM1;x++) {
for (int x=0;x<DIM1;x++) {
for (int kl=0;kl<10;kl++)
for (int kl=0;kl<10;kl++)
orow[x]+=arow[k+kl]*b10rows[kl][x];
orow[x]+=arow[k+kl]*b10rows[kl][x];
}
}
}
}
for (int x=0;x<DIM1;x++) o[y][x]=orow[x];
for (int x=0;x<DIM1;x++) o[y][x]=orow[x];
}
}
}

```
(c) Account for total memory usage in the local scratchpad (use provided table).
\begin{tabular}{|l|r|}
\hline Variable & Size (Bytes) \\
\hline \hline arow & \(2 \times 1024=2048\) \\
\hline orow & \(4 \times 1024=4096\) \\
\hline b10rows & \(10 \times 2 \times 1024=20,480\) \\
\hline & \\
\hline & \\
\hline & \\
\hline & \\
\hline
\end{tabular}
could push to 12 or 13 rows of \(b\)
(d) Estimate the new memory resource bound for your optimized mmmpy.

1024 iterations
stream in arow \(\frac{2 \times 1024}{32}\)
clear orow \(\frac{4 \times 1024}{32}\)
iterate \(1024 / 10=103\) times
stream in 10 brows \(\frac{10 \times 2 \times 1024}{32}\)
local reads and writes of arow, b10row, orow
\(10 \times 1024 \times 3\)
stream out orow \(\frac{4 \times 1024}{32}\)
\(=1024 \times(64+128+128)+1024 \times 103 \times(640+30720)\)
\(=3.3 \times 10^{9}\)
6. Identify concurrency opportunities between loops.

Which functions can run concurrently, as separate processes, to increase the throughput for the while loop in main. If they cannot, explain what prevents concurrency. If they can, explain why and what conditions need to be met for the concurrency to work.
\begin{tabular}{|c|c|c|}
\hline & \multicolumn{2}{|l|}{Concurfeat?or Why not?} \\
\hline mmmpy + nlmap2d & Y & As soon as each o[y][x] is produced in mmpy, nlmap2d can compute on it. \\
\hline nlmap2d + conv2digest & Y & As soon as nlmap2d finishes a value, it can be used in first window in conv2digest; conv2digest just needs to make sure o[y][x] values are ready as used in conv2digest; computation will be mostly overlapped. \\
\hline conv2digest + nlmapflat & Y & As soon as each o[y][x] is produced in conv2digest, nlmapflat can compute on it. \\
\hline nlmapflat + mvmpy & Y & As soon as nlmapflat produces each value, it can be used in the first dot product (loop B, \(\mathrm{i}=0\) ) in mvmpy. \\
\hline mvmpy + nlmap & Y & As soon as each o \([\mathrm{s}][\mathrm{i}]\) is produced in mvmpy, it can be used in nlmap. \\
\hline
\end{tabular}
(This page intentionally left mostly blank for answers.)
7. Consider building an accelerator for mmmpy. Target a throughput of completing one iteration of loop I on each cycle.
- Assume we've pre-loaded the \(\mathrm{b}(\mathrm{cm})\) matrix into a memory in the accelerator before the application starts, and this memory is wide and can supply the b (cm) data needed for one iteration of loop I on each cycle.
- Assume a (in) data is streamed in from read_input at the streaming memory rate.
(a) What compute operations must be performed in parallel on every cycle to complete loop I? (give number and type as well as computation being performed) 1024 multiplies and 1024 adds
(b) What needs to be read from the local b memory on every cycle? 1024 values; a column from b.
(c) How do we need to handle the a input stream to support this rate of operation?
i. Describe why the a input streaming rate is adequate to maintain the throughput required by this accelerator.
Operate on each row of a at a time for 1024 cycles (loop H). Can stream in next row of a in \(\frac{2 \times 1024}{32}=64\) cycles. So, have time to bring in each row while computing on previous row.
ii. How can the input reception be treated to overlap the collection of input data with the computation?
Shift values of a into row-wide shift register as the come. When accelerator is ready for next a row, transfer from the input shift register into the register used to supply the a row into the computation.
(d) How can this accelerator be extended to also include the nlmap2d computation that follows it while maintaining the same throughput?
Add the threshold computation to the end of the accumulation pipeline since each \(\mathrm{o}[\mathrm{y}][\mathrm{x}]\) value thresholded independently.
(e) Assuming this accelerator runs concurrently with the rest of the computation on a processor, what is the new throughput for the while loop in the main function? (how many cycles per iteration of the while loop?)
\(460 \times 10^{6}(\) from 2 b\()\)
8. Map the main while loop computation to a system composed of:
- four simple processors ( 1 GHz as previously outlined),
- two fast processors ( 2 GHz , with everything running \(2 \times\) as fast except data transfer from main memory),
- one vector processor that can perform \(816 \mathrm{~b} \times 16 \mathrm{~b}\) multiplies or 832 b adds on each cycle as well as performing 8 vector loads of 16 b or 32 b data from its scratchpad, and
- the accelerator from Problem 7.

Assume each processor has its own scratchpad and has a separate path to the large memory so they can all simultaneously stream at full rate. \({ }^{1}\)
(Hint: can you map the problem to match the throughput provided by the mmmpy accelerator?)
(a) Describe how you would map the computation onto these heterogeneous computing resources. Where is each computation run? What computations share compute units?

\footnotetext{
\({ }^{1}\) Probably not realistic, but we'll use to simplify this problem.
}
\begin{tabular}{|c|c|c|}
\hline loop & Where Run & Throughput \\
\hline mmmpy & Problem 7 Accelerator & \(\frac{1}{1024^{2}}\) cycles \\
\hline nlmap2d & with above & \\
\hline conv2digest & vector unit & \[
\frac{1}{\frac{32^{2} \times 64^{2} \times(2+2)}{8}+32^{2} \times(2+2)+\frac{1024^{2} \times 2+666^{2} \times 2+10}{32}}
\] \\
\hline nlmapflat & (with above) & \\
\hline mvmpy & \begin{tabular}{l}
2 Fast +4 simple
\[
\frac{9 \times 1024^{2} \times(2+2)+9 \times 10}{8}
\] \\
split by outputs
\end{tabular} & \begin{tabular}{l}
\[
\frac{1}{\frac{24 \times(2+2)}{1}+\frac{1024^{2} \times 2}{32 \times 4}+\frac{32 \times 10}{4}+\frac{1024 \times 2}{32}}
\] \\
\(1 / 4\) of outputs on each fast processor; cweights also split by output; but all processors need all a/sinputs values
\end{tabular} \\
\hline nlmap & (with above) & \\
\hline write_output & (with above) & \\
\hline
\end{tabular}
(b) Describe how you would use the scratchpad memories as necessary beyond what you've already answered in Problems 5 and 7 to achieve your target performance. [no further change is a possible answer here.] (Hint: can you make sure the throughput of each function is limited by computation or time streaming data from memory?)
Store cm in scratchpad for vector unit. Stream in inputs and outputs. Merge nlmapflat at end of o[y[x] accumulation so does not require writes to or reads from memory. mvmpy, nlmap. Similarly merge nlmap at end of o[s] [i] accumulation to avoid reads/writes. Keep current and next a in scratchpads on processors. Stream in cweights one row at a time.
(c) Estimate the throughput your mapping achieves in cycles per main while loop iteration.
Limit now is on mvmpy+nlmap+write_output computation at: one iteration every \(4.7 \times 10^{6}\) cycles

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