

Database and Information Systems

Solutions to Homework 1

Due on September 26, 2007

The first two problems concern the Penn Ebay (PBAY) System, which is represented by the following schema:

Sellers(*sellerID*:int, *rating*:char, *email*:string)
 Items(*itemID*:int, *type*:string)
 Buyers(*buyerID*:int, *email*:string, *city*:string, *state*:string)
 Stock(*itemID*:int, *sellerID*:int, *startBid*:float, *quantity*:int, *endTime*:int)
 Purchase(*itemID*:int, *buyerID*:int, *sellerID*:int, *price*:float, *purchaseQuantity*:int, *bidTime*:int)

Problem 1 [60 points]: Express the following queries in (a) the relational algebra, (b) the tuple relational calculus, and (c) the domain relational calculus:

Note: in problems where wording proved unclear, answers correct with respect to some reasonable interpretation of the problem were accepted.

- Find the **IDs** of items purchased for price < \$50.

RA: $\pi_{itemID}(\sigma_{price < 50}(Purchase))$
TRC: $\{Q \mid \exists P \in Purchase (P.price < 50 \wedge P.itemID = Q.itemID)\}$
DRC: $\{ \langle i \rangle \mid \exists b, s, p, u, m (\langle i, b, s, p, u, m \rangle \in Purchase \wedge p < 50) \}$

- Find the **emails** of buyers from PA who buy items with purchaseQuantity > 3.

RA: $\pi_{email}(\sigma_{state = \text{"PA"}}(Buyers) \bowtie \pi_{buyerID}(\sigma_{purchaseQuantity > 3}(Purchase)))$
TRC: $\{Q \mid \exists B \in Buyers, \exists P \in Purchase (B.state = \text{"PA"} \wedge B.buyerID = P.buyerID \wedge P.purchaseQuantity > 3 \wedge Q.email = B.email)\}$
DRC: $\{ \langle e \rangle \mid \exists b, c, a (\langle b, e, c, a \rangle \in Buyers \wedge a = \text{"PA"} \wedge \exists i, s, p, u, m (\langle i, b, s, p, u, m \rangle \in Purchase \wedge u > 3)) \}$

- Find the **IDs** of buyers who purchased items of purchaseQuantity less than 10% of the quantity provided by the same seller the buyer purchased from in the stock.

RA: $\pi_{buyerID}(\pi_{itemID, sellerID, quantity}(Stock) \bowtie \sigma_{purchaseQuantity < 0.1 * quantity}(\pi_{itemID, buyerID, sellerID, purchaseQuantity}(Purchase)))$
TRC: $\{Q \mid \exists T \in Stock, \exists P \in Purchase (T.itemID = P.itemID \wedge T.sellerID = P.sellerID \wedge P.purchaseQuantity < 0.1 * T.quantity \wedge Q.buyerID = P.buyerID)\}$
DRC: $\{ \langle b \rangle \mid \exists i, s, q, u (\exists d, n (\langle i, s, d, q, n \rangle \in Stock) \wedge \exists p, m (\langle i, b, s, p, u, m \rangle \in Purchase) \wedge u < 0.1 * q) \}$

- Find the **IDs** of buyers who purchased items with type "furniture" for over 10% of the startBid price of the items they bought.

RA: $\pi_{buyerID}(\pi_{itemID}(\sigma_{type = \text{"furniture"}}(Items)) \bowtie \pi_{itemID, sellerID, startBid}(Stock) \bowtie \sigma_{price > 1.1 * startBid}(\pi_{itemID, buyerID, sellerID, price}(Purchase)))$
TRC: $\{Q \mid \exists I \in Items, \exists T \in Stock, \exists P \in Purchase (I.itemID = T.itemID \wedge T.itemID = P.itemID \wedge T.sellerID = P.sellerID \wedge P.price > 1.1 * T.startBid \wedge I.type = \text{"furniture"}) \}$

$Q.buyerID = P.buyerID)\}$

DRC: $\{ \langle b \rangle \mid \exists i(\exists t(\langle i, t \rangle \in Items \wedge t = \text{"furniture"}) \wedge \exists s, p, d(\exists q, n(\langle i, s, d, q, n \rangle \in Stock) \wedge \exists u, m(\langle i, b, s, p, u, m \rangle \in Purchase) \wedge (p > 1.1 * d)))\}$

5. Find the IDs of buyers who either always make purchases with purchaseQuantity < 5 or haven't made any purchases.

RA: $\pi_{buyerID}(Buyers) - \pi_{buyerID}(\sigma_{purchaseQuantity \geq 5}(Purchase))$

TRC: $\{Q \mid \exists B \in Buyers (\forall P \in Purchase (P.purchaseQuantity < 5 \vee P.buyerID \neq B.buyerID) \wedge Q.buyerID = B.buyerID)\}$

DRC: $\{ \langle b \rangle \mid \exists e, c, a(\langle b, e, c, a \rangle \in Buyers \wedge \neg \exists i, s, p, u, m(\langle i, b, s, p, u, m \rangle \in Purchase) \wedge (u \geq 5))\}$

(You can either have:

DRC: $\{ \langle b \rangle \mid \exists e, c, a(\langle b, e, c, a \rangle \in Buyers \wedge \forall i, s, p, u, m(\neg(\langle i, b, s, p, u, m \rangle \in Purchase) \vee (u < 5)))\}$, but remember that is is an unsafe plan.)

6. Find the types of items stocked by ≥ 2 sellers or bought by ≥ 2 buyers.

RA: $\pi_{type}(\sigma_{s1 \neq s2}(\rho_{sellerID \rightarrow s1}(\pi_{sellerID, type}(Items \bowtie Stock)) \bowtie \rho_{sellerID \rightarrow s2}(\pi_{sellerID, type}(Items \bowtie Stock))))$

\cup

$\pi_{type}(\sigma_{b1 \neq b2}(\rho_{buyerID \rightarrow b1}(\pi_{buyerID, type}(Items \bowtie Purchase)) \bowtie \rho_{buyerID \rightarrow b2}(\pi_{buyerID, type}(Items \bowtie Purchase))))$

TRC: $\{Q \mid (\exists P_1, P_2 \in Purchases, \exists I_1, I_2 \in Items (P_1.itemID = I_1.itemID \wedge P_2.itemID = I_2.itemID \wedge I_1.type = I_2.type \wedge P_1.buyerID \neq P_2.buyerID \wedge I_1.type = Q.type)) \vee (\exists S_1, S_2 \in Stocks, \exists I_1, I_2 \in Items (S_1.itemID = I_1.itemID \wedge S_2.itemID = I_2.itemID \wedge I_1.type = I_2.type \wedge S_1.sellerID \neq S_2.sellerID \wedge I_1.type = Q.type))\}$

DRC: $\{ \langle t \rangle \mid \exists i_1, s_1, d_1, q_1, n_1, i_2, s_2, d_2, q_2, n_2(\langle i_1, t \rangle \in Items \wedge \langle i_1, s_1, d_1, q_1, n_1 \rangle \in Stock \wedge \langle i_2, t \rangle \in Items \wedge \langle i_2, s_2, d_2, q_2, n_2 \rangle \in Stock \wedge s_1 \neq s_2) \vee \exists i_3, b_3, s_3, p_3, u_3, m_3, i_4, b_4, s_4, p_4, u_4, m_4(\langle i_3, t \rangle \in Items \wedge \langle i_3, b_3, s_3, p_3, u_3, m_3 \rangle \in Purchase \wedge \langle i_4, t \rangle \in Items \wedge \langle i_4, b_4, s_4, p_4, u_4, m_4 \rangle \in Purchase \wedge b_3 \neq b_4)\}$

Problem 2 [30 points]: State in English what the following queries compute:

- $\{Q \mid \exists P \in Purchase, \exists S \in Sellers (S.rating = \text{"A"} \wedge P.sellerID = S.sellerID \wedge P.purchaseQuantity = 2 \wedge Q.buyerID = P.buyerID)\}$
IDs of buyers who have bought 2 of the same items from a seller with rating "A".
- $\{ \langle e \rangle \mid \exists i, s(\exists r(\langle s, r, e \rangle \in Sellers) \wedge \exists d, q, n(\langle i, s, d, q, n \rangle \in Stock \wedge (d < 20) \wedge (q = 5)) \wedge \exists b, p, u, m(\langle i, b, s, p, u, m \rangle \in Purchase \wedge (p > 50)))\}$
Emails of sellers who have 5 of the same stock items, all with start bid price < 20, and who have sold at least 1 item with price > 50.
- $\pi_{email}(\sigma_{city = \text{"Philadelphia"}}(Buyers) \bowtie \pi_{buyid}(\sigma_{price < 2 * startBid}(\sigma_{type = \text{"book"}} \wedge purchaseQuantity = 2)(Items \bowtie Purchase) \bowtie Stock))$
Emails of the buyers living in Philadelphia who have bought 2 same books with price less than twice of the start bid price.
- $\pi_{rating}(\pi_{s1}(\sigma_{i1 \neq i2 \wedge s1 = s2}(\rho_{itemID \rightarrow i1, sellerID \rightarrow s1}(Stock) \bowtie \rho_{itemID \rightarrow i2, sellerID \rightarrow s2}(\sigma_{quantity \geq 3}(Stock)))) \bowtie_{s1 = sellerID} Sellers)$
Ratings of sellers with 2 different items in stock where the seller stocks at least 3 of one of those items.

Problem 3 [10 points]: Explain how Codd's points of access path dependence and indexing dependence relate to today's Java objects. (Assume the goal is to return all instances of a particular member variable of a particular object, which might be linked to by other objects.)

Java has all of the same "shortcomings," i.e., access path dependencies, as the languages of Codd's time. For instance, a programmer must know: (1) data ordering for files serialized to disk; (2) what indices are available, and what they point to (and in fact this requires a special library like BerkeleyDB); (3) how references between files are represented (one can serialize object references in a single file but not across files).