Problem 1 [24 points]: Consider a relational algebra expression of the form $\sigma_c(\pi_l(R \bowtie S))$. Suppose that the equivalent expression with selections and projections pushed as much as possible, taking into account only relational algebra equivalences, is in one of the following forms. In each case list the attributes of $R$ and $S$, list an original relational algebra expression – filling in selection conditions and projection lists (instead of $c, l, c_1, l_1,$ etc.) – and show the relational algebra expression in the form shown below.

Example of a similar problem:
Given relations: $R(a, b), S(b, c)$
Suppose we have an original expression of the form $\sigma_c(R \bowtie S)$, for instance $\sigma_{b<5}(R \bowtie S)$. A final expression of the form $\sigma_{c_1}(R) \bowtie \sigma_{c_2}(S)$ would be $\sigma_{b<5}(R) \bowtie \sigma_{b<5}(S)$.

1. **Equivalent maximally pushed form:** $\sigma_{c_1}(\pi_{l_2}(R)) \times S$.
   - Relations: $R(a, b, d), S(b, c)$
   - Original expression: $\sigma_{a<5}(\pi_{a,b,c}(R \bowtie S))$.
   - Maximal pushed form: $(\sigma_{a<5}(\pi_{a,b}(R)) \bowtie S)$.

2. **Equivalent maximally pushed form:** $\sigma_{c_1}(\pi_{l_1}(\pi_{l_2}(\sigma_{c_2}(R)) \bowtie S))$.
   - Relations: $R(a, b), S(b, c, d)$
   - Original expression: $\sigma_{c<b \land b<5}(\pi_{b,c}(R \bowtie S))$.
   - Maximal pushed form: $\sigma_{c<b}(\pi_{b,c}(\pi_b(\sigma_{b<5}(R) \bowtie S)))$.

Problem 2 [26 points]: Using Oracle on eniac (the `sql` command), we will have you specify query plans using the TPC-H benchmark data set of Homework 6. To do this assignment, you will need to repeat each query 5 times. Time it by using the Oracle command “set timing on” and reading the elapsed time.

Start with the query:

```sql
select count(*)
from zives.lineitem, zives.orders
where l_orderkey = o_orderkey
and o_totalprice < 1500.65
```
1. What index or indices would be most useful on the lineitem and orders tables?

Certainly, an index on the o_orderkey attribute would be highly useful. Possibly useful might be one on o_totalprice, but that depends on how many answers have a value less than 1500.65.

2. As with before, we are going to use Oracle’s hints to tell the optimizer how to run the query. Time the query:

```sql
select /*+ USE_HASH(l o) */ count(*)
from zives.lineitem l, zives.orders o
where l_orderkey = o_orderkey
and o_totalprice < 1500.65
```

I got about 7.5 sec.

3. Replace “USE_HASH” with “USE_MERGE” and repeat.

I got about 8.5 sec.

4. Replace with “USE_NL” and repeat.

I got about 6.2 sec.

5. Was there any substantive difference? Which plan or plans seemed to perform best? Explain why.

The nested loops join is the only one that makes use of the (default) index on o_orderkey, which is a clustered index; it’s the fastest.