Consider the B+ tree index shown in Figure 1, which stores data entries at leaf nodes in the index. Each intermediate node can hold up to five pointers and four key values. Each leaf node can hold up to four records (indicated as a key value plus a “*”), and leaf nodes are doubly linked to their predecessor and successor nodes in the index (this is not shown in the figure). The order of the tree, i.e., the minimum number of keys allowed in an intermediate node, is two, and the minimum number of records allowed in a leaf node is also two. Underscores (“___”) indicate unallocated (free) entries.

1. Insert a record with search key 53 into the tree.
Problem 2 [50 points]: For this part of the assignment, you will need to run Oracle on eniac, using the sql command, as in previous assignments. The goal is to see the benefits of indexing in action.

The Oracle setup on eniac has a series of sample tables created for running database benchmarks — the so-called TPC-H benchmark. Additionally, each of these tables may have several alternative index structures. We will be comparing performance depending on which indices are used. To do this assignment, you will need to first enter the Oracle command set timing on, which will cause Oracle to report an “elapsed” time in seconds. You should run each query.

The lineitem table has nearly 300,000 rows and takes approximately 37MB of space. We have two indices in lineitem, each with a name: sys_C001480 is an index over the attribute pair (l_orderkey, l_linenumber) and lineno is on the singleton attribute (l_linenumber).

1. Start by running the query:

```sql
select avg(l_linenumber)
from zives.lineitem
where l_linenumber < 4;
```

which uses whatever indices Oracle prefers. Time the run and repeat it 5 times, averaging the total. What is that value?

2. Next, repeat the query with a special optimizer hint that says you want to scan the full table and avoid indices:

```sql
select /*+ full(l) */ avg(l_linenumber)
from zives.lineitem l
where l_linenumber < 4;
```

Average the running time for 5 runs and report the result. What can you say about the difference between the two runs? Do these results suggest that Oracle uses an index by default?

3. Try another hint, which makes use of the first index:

```sql
select /*+ index(l SYS_C001480) */ avg(l_linenumber)
from zives.lineitem l
where l_linenumber < 4;
```
Run 5 times and report the result. How did this compare to the first two cases? Did that particular index offer any benefits?

4. Which index, or indices, might have been used in the default, un-hinted Oracle query? Generalizing from the Oracle SQL hints shown above, what is the query hint that is equivalent to that default query?

5. For each of the two indices and for the non-indexed case, explain how what data and/or index structures will be examined in answering the query.

6. Run the two queries:

   ```sql
   select /*+ index(l SYS_C001480) */ count(distinct l_suppkey)
   from zives.lineitem l
   where l_linenumber <= 450;
   ```

   ```sql
   select /*+ full(l) */ count(distinct l_suppkey)
   from zives.lineitem l
   where l_linenumber <= 450;
   ```

   Report the averaged running times over 5 runs. Explain the relative differences (or lack thereof) in performance, based on your knowledge of index and data layout characteristics, as well as your knowledge of “covering” indices.

Problem 3 [25 points]: Now we will have you specify query plans using the TPC-H benchmark data set, using Oracle. To do this assignment, you will need to repeat each query 5 times. Time it by using the Oracle command “set timing on” and reading the elapsed time. Remember to repeat the query 5 times and average the results, in order to get more consistent results.

Start with the query:

```sql
select count(*)
from zives.lineitem, zives.orders
where l_orderkey = o_orderkey
and o_totalprice <= 1500;
```

1. What index or indices would be most useful on the lineitem and orders tables?

2. As with before, we are going to use Oracle’s hints to tell the optimizer how to run the query. Time the query:
select /*+ USE_HASH(l o) */ count(*)
from zives.lineitem l, zives.orders o
where l_orderkey = o_orderkey
and o_totalprice <= 1500;

3. Replace “USE_HASH” with “USE_MERGE” and repeat.

4. Replace with “USE_NL” and repeat.

5. Was there any substantive difference? Which plan or plans seemed to perform best? Explain why.