

## 5. The TOY Machine II



Laboratory Instrument Computer (LINC)

Introduction to Computer Science: An Interdisciplinary Approach Robert Sedgewick and Kevin Wayne Copyright © 2002-2011 12/11/2012 11:19:46

### What We've Learned About TOY

#### TOY machine.

- Box with switches and lights.
- 16-bit memory locations, 16-bit registers, 8-bit pc.
- 4,328 bits =  $(255 \times 16) + (15 \times 16) + (8) = 541$  bytes!
- von Neumann architecture.

#### TOY programming.

- TOY instruction set architecture: 16 instruction types.
- Variables, arithmetic, loops.



### What We Do Today

Data representation. Negative numbers.

Input and output. Standard input, standard output.

Manipulate addresses. References (pointers) and arrays.

TOY simulator in Java.



## Data Representation

### Digital World

Data is a sequence of bits. (interpreted in different ways)

- Integers, real numbers, characters, strings, ...
- Documents, pictures, sounds, movies, Java programs, ...

Ex. 01110101

- As binary integer:  $1 + 4 + 16 + 32 + 64 = 117_{10}$ .
- As character: 117<sup>th</sup> Unicode character = 'u'.
- As music: 117/256 position of speaker.
- As grayscale value: 45.7% black.



```
public class HelloWorld {
    public static void main(String[] args) {
        System.out.println("Hello, World!");
    }
}
```



### Adding and Subtracting Binary Numbers

Decimal and binary addition.

$$\begin{array}{r}
 1 \\
 013 \\
 + 092 \\
 \hline
 105
 \end{array}
 \qquad
 \begin{array}{r}
 \text{carries} \\
 11 \\
 00001101 \\
 + 01011100 \\
 \hline
 01101001
 \end{array}$$

Subtraction. Add a negative integer.

e.g.,  $6 - 4 = 6 + (-4)$

Q. How to represent negative integers?

### Representing Negative Integers

TOY words are 16 bits each.

- We could use 16 bits to represent 0 to  $2^{16} - 1$ .
- We want negative integers too.
- Reserving half the possible bit-patterns for negative seems fair.

Highly desirable property. If  $x$  is an integer, then the representation of  $-x$ , when added to  $x$ , is zero.


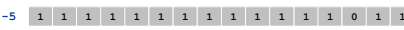

$$\begin{array}{r} x \quad \quad 00110100 \\ +(-x) \quad +???????? \\ \hline 0 \quad \quad 00000000 \end{array}$$

$$\begin{array}{r} x \quad \quad 00110100 \\ +(-x) \quad +11001011 \\ \hline 11111111 \\ + \quad \quad 1 \\ \hline 0 \quad \quad 00000000 \end{array}$$

flip bits and add 1

### Two's Complement Integers

To compute  $-x$  from  $x$ :

- Start with  $x$ .  leading bit
- Flip bits. 
- Add one. 

### Two's Complement Integers

dec	hex	binary
+32767	7FFF	0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
+4	0004	0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0
+3	0003	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 1 0
+2	0002	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0
+1	0001	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0
+0	0000	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
-1	FFFF	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
-2	FFFE	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0
-3	FFFD	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0
-4	FFFC	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0
-32768	8000	1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0

### Properties of Two's Complement Integers

- Properties.
- Leading bit (bit 15) signifies sign.
  - Addition and subtraction are easy.
  - 0000000000000000 represents zero.
  - Checking for arithmetic overflow is easy.
  - Negative integer  $-x$  represented by  $2^{16} - x$ .
  - Not symmetric: can represent  $-32,768$  but not  $32,768$ .
- Java. Java's `int` data type is a 32-bit two's complement integer.  
 Ex.  $2147483647 + 1$  equals  $-2147483648$ .



<http://xkcd.com/571>

### Representing Other Primitive Data Types in TOY

Bigger integers. Use two 16-bit TOY words per 32-bit Java `int`.

Real numbers.

- Use IEEE floating point (like scientific notation).
- Use four 16-bit TOY words per 64-bit Java `double`.

Characters. Use one 16-bit TOY word per 16-bit Java Unicode `char`.

0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F
0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F
1	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...
2	!	"	#	\$	%	&	'	(	)	*	+	,	-	.	/
3	0	1	2	3	4	5	6	7	8	9	:	<	=	>	?@
4	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
5	P	Q	R	S	T	U	V	W	X	Y	Z	[	\	]	^_
6	a	b	c	d	e	f	g	h	i	j	k	l	m	n	o
7	p	q	r	s	t	u	v	w	x	y	z	{		}	~



M = 01001101<sub>2</sub> = 4D<sub>16</sub>  
 O = 01001111<sub>2</sub> = 4F<sub>16</sub>  
 M = 01001101<sub>2</sub> = 4D<sub>16</sub>

Note. Real microprocessors add hardware support for `int` and `double`.

### Standard Input and Output

### Standard Output

#### Standard output.

- Writing to memory location `FF` sends one word to TOY stdout.
- Ex. `9AFF` writes the integer in register `a` to stdout.

```

00: 0000 0
01: 0001 1

10: 8A00 RA ← mem[00]    a = 0
11: 8B01 RB ← mem[01]    b = 1
                               do {
12: 9AFF write RA to stdout print a
13: 1AAB RA ← RA + RB     a = a + b
14: 2BAB RB ← RA - RB     b = a - b
15: DA12 if (RA > 0) goto 12 } while (a > 0)
16: 0000 halt
    
```

fibonacci.toy

```

0000
0001
0001
0001
0002
0002
0003
0005
0008
0008
0000
0015
0022
0022
0037
0059
0090
00E9
0179
0262
0308
0630
0A18
1055
1A6D
2AC2
452F
6FF1
    
```

### Standard Input

#### Standard input.

- Loading from memory address `FF` loads one word from TOY stdin.
- Ex. `8AFF` reads an integer from stdin and store it in register `a`.

Ex: read in a sequence of integers and print their sum.

- In Java, stop reading when EOF.
- In TOY, stop reading when user enters 0000.

```

while (!StdIn.isEmpty()) {
    a = StdIn.readInt();
    sum = sum + a;
}
StdOut.println(sum);
    
```

```

00: 0000 0
10: 8C00 RC ← mem[00]
11: 8AFF read RA from stdin
12: CA15 if (RA == 0) pc ← 15
13: 1CCA RC ← RC + RA
14: C011 pc ← 11
15: 9CFF write RC
16: 0000 halt
    
```

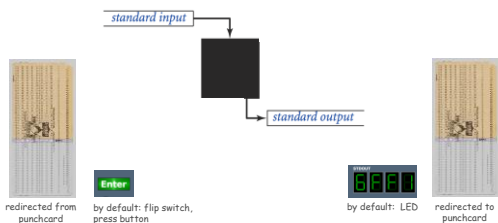
```

00AE
0046
0003
0000
00F7
    
```

### Standard Input and Output: Implications

#### Standard input and output enable you to:

- Get information out of machine.
- Put information from real world into machine.
- Process more information than fits in memory.
- Interact with the computer while it is running.



### Pointers

### Load Address (a.k.a. Load Constant)

#### Load address. [opcode 7]

- Loads an 8-bit integer into a register.
- `7A30` means load the value 30 into register `a`.

#### Applications.

- Load a small **constant** into a register.
- Load a 8-bit **memory address** into a register.

```
a = 0x30;
```

Java code

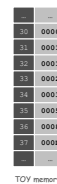
register stores "pointer" to a memory cell

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
0	1	1	1	1	0	1	0	0	0	1	1	0	0	0	0
7 <sub>16</sub>				A <sub>16</sub>				3 <sub>16</sub>				0 <sub>16</sub>			
opcode				dest d				addr							

### Arrays in TOY

#### TOY main memory is a giant array.

- Can access memory cell 30 using load and store.
- `8c30` means load `mem[30]` into register `c`.
- Goal: access memory cell `i` where `i` is a variable.



#### Load indirect. [opcode A]

- `ac06` means load `mem[R6]` into register `c`.

#### Store indirect. [opcode B]

- `bc06` means store contents of register `c` into `mem[R6]`.

```

for (int i = 0; i < N; i++)
    a[i] = StdIn.readInt();

for (int i = 0; i < N; i++)
    StdOut.println(a[N-i-1]);
    
```

### TOY Implementation of Reverse

TOY implementation of reverse.

- Read in a sequence of integers and store in memory 30, 31, 32, ... until reading 0000.
- Print sequence in reverse order.

```

10: 7101 R1 ← 0001      constant 1
11: 7A30 RA ← 0030      a[]
12: 7B00 RB ← 0000      n

13: 8CFF read RC          while(true) {
14: CC19 if (RC == 0) goto 19   c = StdIn.readInt();
15: 16AB R6 ← RA + RB         if (c == 0) break;
16: BC06 mem[R6] ← RC         address of a[n]
17: 1BB1 RB ← RB + R1         memory address of
18: C013 goto 13             a[n] = c;
                                n++;
                                }
                                read in the data
    
```

### TOY Implementation of Reverse

TOY implementation of reverse.

- Read in a sequence of integers and store in memory 30, 31, 32, ... until reading 0000.
- Print sequence in reverse order.

```

19: CB20 if (RB == 0) goto 20   while (n > 0) {
1A: 16AB R6 ← RA + RB         address of a[n]
1B: 2661 R6 ← R6 - R1         address of a[n-1]
1C: AC06 RC ← mem[R6]         c = a[n-1];
1D: 9CFF write RC             StdOut.println(c);
1E: 2BB1 RB ← RB - R1         n--;
1F: C019 goto 19              }
20: 0000 halt
    
```

print in reverse order

### Unsafe Code at any Speed

Q. What happens if we make array start at 00 instead of 30?  
 A. Self modifying program; can overflow buffer and run arbitrary code!

```

10: 7101 R1 ← 0001      constant 1
11: 7A00 RA ← 0000      a[]
12: 7B00 RB ← 0000      n

13: 8CFF read RC          while(true) {
14: CC19 if (RC == 0) goto 19   c = StdIn.readInt();
15: 16AB R6 ← RA + RB         if (c == 0) break;
16: BC06 mem[R6] ← RC         address of a[n]
17: 1BB1 RB ← RB + R1         a[n] = c;
18: C013 goto 13             n++;
                                }
                                % more crazy8.txt
                                1 1 1 1 1 1 1 1
                                1 1 1 1 1 1 1 1
                                8888 8810
                                98FF C011
    
```

### What Can Happen When We Lose Control (in C or C++)?

Buffer overflow.

- Array `buffer[]` has size 100.
- User might enter 200 characters.
- Might lose control of machine behavior.

```


#include <stdio.h>
int main(void) {
    char buffer[100];
    scanf("%s", buffer);
    printf("%s\n", buffer);
    return 0;
}
    
```

unsafe C program

Consequences. Viruses and worms.

Java enforces security.

- Type safety.
- Array bounds checking.
- Not foolproof.




shine 50W bulb at DRAM  
 [Appel-Govindaraj@holo 03]

### Buffer Overflow Attacks

Stuxnet worm. [July 2010]

- Step 1. Natanz centrifuge fuel-refining plant employee plugs in USB flash drive.
- Step 2. Data becomes code by exploiting Window buffer overflow; machine is Owned.
- Step 3. Uranium enrichment in Iran stalled.



More buffer overflow attacks: Morris worm, Code Red, SQL Slammer, iPhone unlocking, Xbox softmod, JPEG of death, ...


Lesson.

- Not easy to write error-free software.
- Embrace Java security features.
- Keep your OS patched.

### Buffer Overflow Example: JPEG of Death

Microsoft Windows JPEG bug. [September, 2004]

- Step 1. User views malicious JPEG in IE or Outlook.
- Step 2. Machine is Owned.
- Data becomes code by exploiting buffer overrun in GDI+ library.



Fix. Update old library with patched one.

but many applications install independent copies of GDI library

Moral.

- Not easy to write error-free software.
- Embrace Java security features.
- Don't try to maintain several copies of the same file.
- Keep your OS patched.

### Dumping

Q. Work all day to develop operating system in mem[10] to mem[FF]. How to save it?

A. Write short program dump.toy and run it to dump contents of memory onto tape.

```

00: 7001 R1 ← 0001
01: 7210 R2 ← 0010
02: 73FF R3 ← 00FF
                                i = 10
                                do {
03: AA02 RA ← mem[R2]           a = mem[i]
04: 9AFF write RA                print a
05: 1221 R2 ← R2 + R1           i++
06: 2432 R4 ← R3 - R2
07: D403 if (R4 > 0) goto 03    } while (i < 255)
08: 0000 halt
    
```

dump.toy

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### Booting

Q. How do you get it back?

A. Write short program boot.toy and run it to read contents of mem[10] to mem[FF] from tape.

```

00: 7001 R1 ← 0001
01: 7210 R2 ← 0010
02: 73FF R3 ← 00FF
                                i = 10
                                do {
03: 8AFF read RA                read a
04: BA02 mem[R2] ← RA          mem[i] = a
05: 1221 R2 ← R2 + R1           i++
06: 2432 R4 ← R3 - R2
07: D403 if (R4 > 0) goto 03    } while (i < 255)
08: 0000 halt
    
```

boot.toy

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### Extra Slides

### Two's Complement Arithmetic

Addition is carried out as if all integers were positive.

- It usually works.

```

-3  1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 1
+
 4  0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0
=
 1  0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1
    
```

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### Two's Complement Arithmetic

Addition is carried out as if all integers were positive.

- It usually works.
- But overflow can occur.

carry into sign (left most) bit with no carry out  
or carry out out of sign bit with no carry in

```

+32,767 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
+
 2      0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0
=
-32,767 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1
    
```

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### Java and TOY

Correspondence between Java constructs and TOY mechanisms.

Java	TOY
assignment	load, store
arithmetic expressions	add, subtract
logical expressions	xor, and, shifts
loops (for, while)	jump absolute, branch
branches (if-else, switch)	branch if zero, positive
arrays, linked lists	indirect addressing
function call	jump and link, jump indirect
recursion	implement stack with arrays
whitespace	no-op 1000
...	...

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