# Programming Languages and Techniques (CIS120)

Lecture 10

Feb 10, 2014

First-class functions

#### **Announcements**

- HW #3 due Tuesday at midnight
- Read Ch 10 of the lecture notes
- Midterm 1
  - Scheduled in class on Friday, February 21st
  - Review session Wednesday, February 19<sup>th</sup>,
     7-9PM in Wu & Chen
  - More details to follow!

# Abstracting with first-class functions

# Motivating design problem

 Suppose you are given an association list from students to majors, but you wanted a list that includes only students in the engineering school? Or only students in wharton?

```
type student = string
type major = string
type school = SEAS | WHARTON | SAS | NURSING
type roster = (student * major) list
let to_school (m : major) : school = ...
let is_engr (m : major) : bool = to_school m = SEAS
let is_wharton (m : major) : bool = to_school m = WHARTON
let only_engr (m : roster) : roster = ???
let only_wharton (m : roster) : roster = ???
```

# Demo: majors.ml

## **First Class Functions**

Functions are values

#### First-class Functions

• You can pass a function as an *argument* to another function:

```
let twice (f:int -> int) (x:int) : int =
  f (f x)

let add_one (z:int) : int = z + 1
let z = twice add_one 3
```

You can return a function as the result of another function.

#### First-class Functions

You can store functions in data structures

```
let add_one (x:int) : int = x+1
let add_two (x:int) : int = x+2
let add_three (x:int) : int = x+3

let func_list : (int -> int) list =
  [ add_one; add_two; add_three ]
```

```
let func_list1 : (int -> int) list =
  [ make_incr 1; make_incr 2; make_incr 3 ]
```

# Simplifying First-Class Functions

```
let twice (f:int -> int) (x:int) : int =
  f (f x)

let add_one (z:int) : int = z + 1
```

```
twice add_one 3

\mapsto add_one (add_one 3) substitute add_one for f, 3 for x

\mapsto add_one (3 + 1) substitute 3 for z in add_one

\mapsto add_one 4 3+1\Rightarrow 4

\mapsto 4 + 1 substitute 4 for z in add_one

\mapsto 5
```

# **Evaluating First-Class Functions**

```
let make_incr (n:int) : int -> int =
  let helper (x:int) : int = n + x in
  helper
```

# **Evaluating First-Class Functions**

```
let make_incr (n:int) : int -> int =
  let helper (x:int) : int = n + x in
  helper
```

keyword "fun"

"->" after arguments no return type annotation

#### **Function values**

A standard function definition:

```
let is_engr (m : major) : bool = to_school m = SEAS
```

really has two parts:

```
let is_engr = fun (m:major) -> to_school m = SEAS
```

define a variable with that value

create a function value

Both definitions have the same type and behave exactly the same:

```
val is_engr : major -> bool
```

# Anonymous functions

```
let is_engr (m : major) : bool = to_school m = SEAS
let is_sas (m : major) : bool = to_school m = SAS

let rec only (f : major -> bool) (r: roster) = ...
let only_engr (r : roster) : roster =
   only is_engr r
let only_sas (r : roster) : roster =
   only is_sas r
```

```
let only_engr (r : roster) : roster =
  only
     (fun (m:major) -> to_school m = SEAS) r
let only_sas (r : roster) : roster =
  only
     (fun (m:major) -> to_school m = SAS) r
```

# Multiple Arguments

We can decompose a standard function definition:

```
let sum (x : int) (y:int) : int : x + y
```

into two parts:

```
let sum = fun (x:int) \rightarrow fun (y:int) \rightarrow x + y
```

define a variable with that value

create a function value

Both definitions have the same interface and behave exactly the same:

```
val sum : int -> int -> int
```

# **Partial Application**

```
let sum (x:int) (y:int) : int = x + y
```

What is the value of this expresssion?

```
let f (x:bool) (y:int) : int =
   if x then 1 else y in
f true
```

- 1.1
- 2. true
- 3. fun (y:int) -> if true then 1 else y
- 4. fun (x:bool) -> if x then 1 else y

#### What is the value of this expresssion?

```
let f (g : int -> int) (y: int) :int =
    g 1 + y in

f (fun (x:int) -> x + 1) 3
```

- 1.1
- 2.2
- 3.3
- 4.4
- 5.5

What is the type of this expresssion?

```
let f (g : int -> int) (y: int) : int =
    g 1 + y in

f (fun (x:int) -> x + 1)
```

- 1. int
- 2. int -> int
- 3. int -> int -> int
- 4.(int -> int) -> int -> int
- 5. ill-typed

What is the type of this expresssion?

```
[ (fun (x:int) -> x + 1);
 (fun (x:int) -> x - 1) ]
```

- 1. int
- 2. int -> int
- 3.(int -> int) list
- 4. int list -> int list
- 5. ill typed

### List transformations

A fundamental design pattern using first-class functions

# Refactoring code: Keys and Values

Can we use first-class functions to refactor code to share common structure?

# Keys and Values

The argument f controls what happens with the binding at the head of the list

```
fst and snd are functions that
access the parts of a tuple:
let fst (x,y) = x
let snd (x,y) = y
```

# Going even more generic

```
let rec helper (f:('k*'v) -> 'b) (m: ('k*'v) list)
    : 'b list =
    begin match m with
    | [] -> []
    | h::t -> f h :: helper f t
    end

let keys    (m:('k,'v) map) : 'k list = helper fst m
let values (m:('k,'v) map) : 'v list = helper snd m
```

Now let's make it work for *all* lists, not just lists of tuples...

# Going even more generic

```
let rec helper (f:'a -> 'b) (m:'a list)
   : 'b list =
   begin match m with
   | [] -> []
   | h::t -> (f h) :: helper f t
   end

let keys   (m:('k,'v) list) : 'k list = helper fst m
   let values (m:('k,'v) list) : 'v list = helper snd m
```

'a stands for ('k\*'v)
'b stands for 'k

fst: ('k\*'v) -> 'k

# **Transforming Lists**

List transformation (a.k.a. "mapping a function across a list"\*)

- foundational function for programming with lists
- occurs over and over again
- part of OCaml standard library (called List.map)

#### Example of using transform:

```
transform is_engr ["FNCE";"CIS";"ENGL";"DMD"] =
    [false;true;false;true]
```

<sup>\*</sup>confusingly, many languages (including OCaml) use the terminology "map" for the function that transforms a list by applying a function to each element. Don't confuse List.map with "finite map".

#### What is the value of this expresssion?

```
transform String.uppercase ["a";"b";"c"]
```

- 1. []
- 2. ["a"; "b"; "c"]
- 3. ["A"; "B"; "C"]
- 4. runtime error

What is the value of this expresssion?

```
transform (fun (x:int) -> x > 0)
[0; -1; 1; -2]
```

- 1. [0; -1; 1; -2]
- 2. [1]
- 3. [0; 1]
- 4. [false; false; true; false]
- 5. runtime error

# List processing

The fold design pattern

# Refactoring code, again

Is there a pattern in the definition of these two functions?

```
let rec exists (l : bool list) : bool =
   begin match 1 with
      [] -> false <__
                                                     base case:
     h :: t -> h || exists t
                                                     Simple answer when
   end
                                                     the list is empty
let rec acid_length (l : acid list) : int =
   begin match 1 with
                                                     combine step:
      [] -> 0 4
                                                     Do something with
     x :: t \rightarrow 1 + acid length t
                                                     the head of the list
   end
                                                     and the recursive call
```

Can we factor out that pattern using first-class functions?

#### List Fold

#### Fold (aka Reduce)

- Another foundational function for programming with lists
- Captures the pattern of recursion over lists
- Also part of OCaml standard library (List.fold\_right)
- Similar operations for other recursive datatypes (fold\_tree)

#### **Functions as Data**

- We've seen a number of ways in which functions can be treated as data in OCaml
- Present-day programming practice offers many more examples at the "small scale":
  - objects bundle "functions" (a.k.a. methods) with data
  - iterators ("cursors" for walking over data structures)
  - event listeners (in GUIs)
  - etc.
- The idiom is useful at the "large scale": Google's MapReduce
  - Framework for mapping across sets of key-value pairs
  - Then "reducing" the results per key of the map
  - Easily distributed to 10,000 machines to execute in parallel!