Programming Languages and Techniques (CIS1200)

Lecture 8

Generics & First-class functions Chapters 8 and 9

Announcements

- Homework 2 due tomorrow night at 11:59pm
- Complete the intro survey (link on Ed) when available
- Homework 3 available Wednesday
 - Practice with BSTs, generic functions, first-class functions and abstract types
 - Start early!
- Read: Chapters 8, 9, and 10 of the lecture notes
- Midterm 1: Friday, September 27th
 - Covers chapters 1-10 in the lecture notes
 - Details posted on Ed later this week

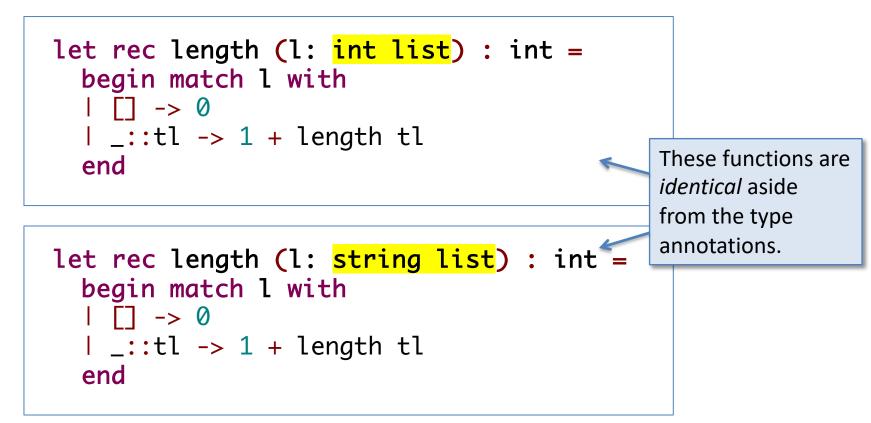
Generic Functions and Data

Wow, implementing BSTs took quite a bit of typing... Do we have to do it all again if we want to use BSTs containing strings, and again for characters, and again for floats, and...?

> or How not to repeat yourself, Part I.

Structurally Identical Functions

- Observe: Many functions on lists don't depend on the contents of the list, only on the list structure
- Compare:



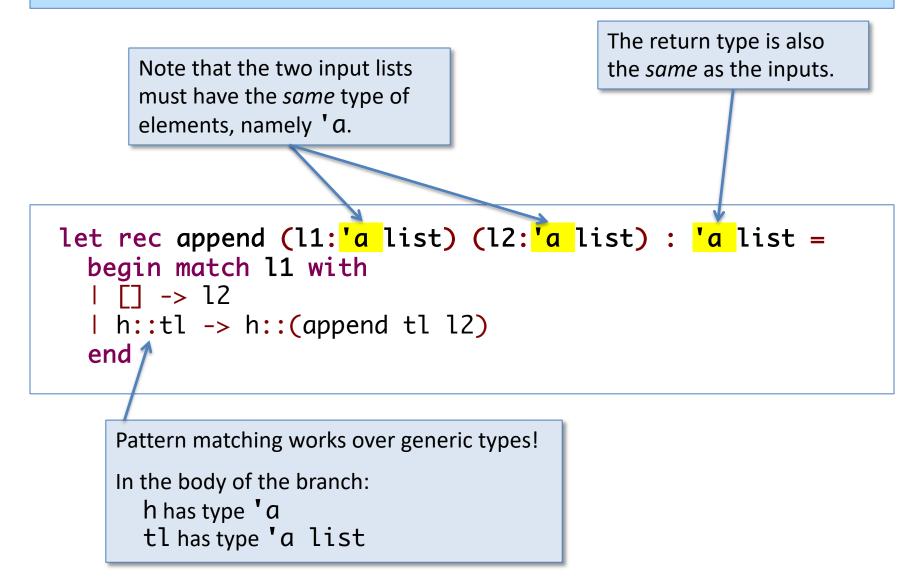
Notation for Generic Types

• In OCaml, functions can have *generic* types

```
let rec length (l:'a list) : int =
  begin match 1 with
  | [] -> 0
  | ::tl \rightarrow 1 + (length tl)
  end
```

- Notation: 'a is a type variable, indicating that the function length can be used on a t list for any type t
- Examples:
 - length [1;2;3]
 - length ["a"; "b"; "c"] use length on a string list
- use length on an int list
- Idea: OCaml chooses an appropriate type for 'a whenever length is used

Generic List Append



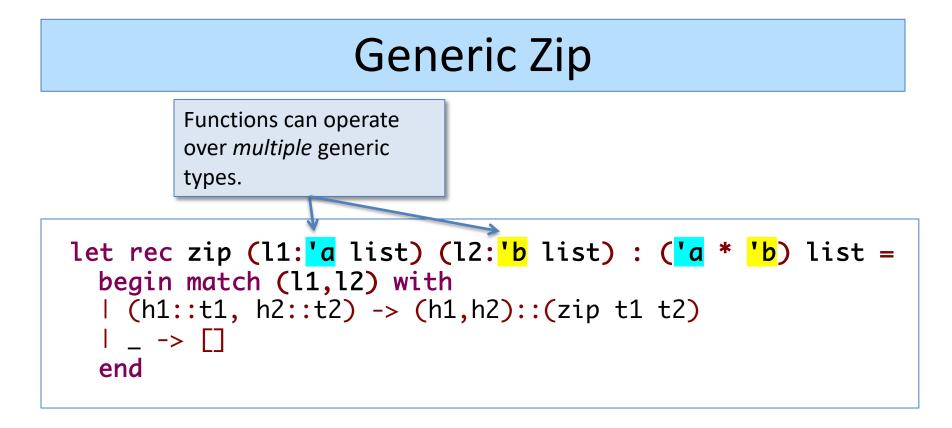
Zip function

- Combine two lists into one list
 - ignore elements from longer list if they are not the same length

```
zip [1;2;3] ["a";"b";"c"]

→[(1,"a"); (2,"b"); (3,"c")]
```

• Does it matter what type of elements are in these lists?



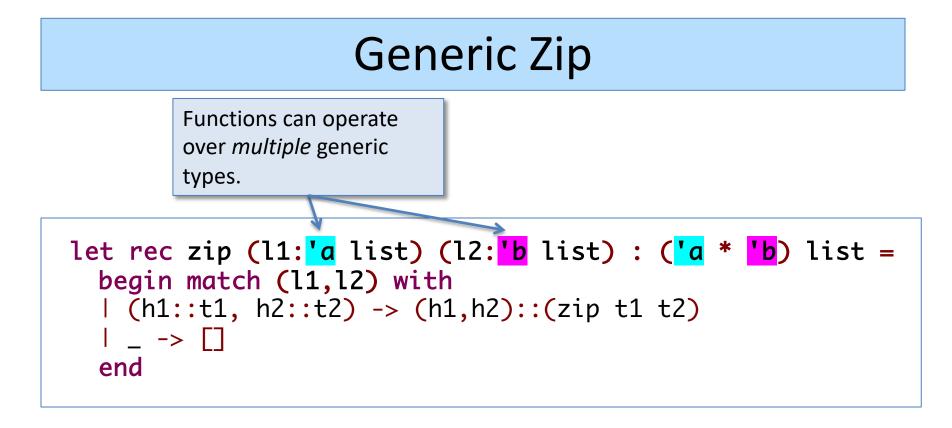
• *Distinct* type variables *can* be instantiated differently:

zip [1;2;3] ["a";"b";"c"] Here, 'a is instantiated to int, 'b to string

• Result is

٠

[(1,"a");(2,"b");(3,"c")] oftype(int * string) list



• Distinct type variables *do not need to be* instantiated differently:

zip <mark>[1;2;3] [4;5;6]</mark>

- Here, 'a is instantiated to int, 'b to int
- Result is

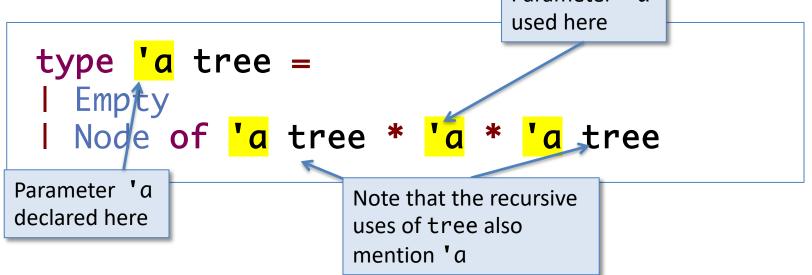
[(1,4);(2,5);(3,6)] oftype(int * int) list Intuition: OCaml tracks instantiations of type variables ('a and 'b) and makes sure they are used consistently.

User-Defined Generic Datatypes

• Recall our integer tree type:

```
type tree =
   Empty
   Node of tree * int * tree
```

 We can define a generic version by adding a type parameter, like this:



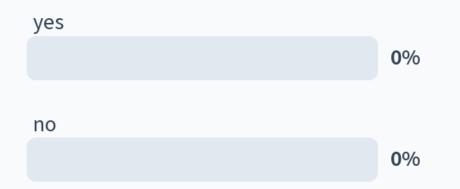
User-Defined Generic Datatypes

BST operations can be generic too; the only change is to the type annotations

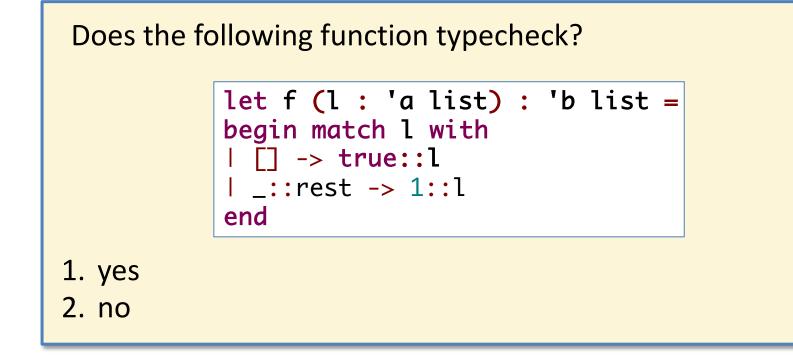
```
(* Insert n into the BST t *)
let rec insert (t:'a tree) (n:'a) : 'a tree =
  begin match t with
  I Empty -> Node(Empty, n, Empty)
  | Node(lt,x,rt) ->
      if x = n then t
       else if n < x then Node(insert lt n, x, rt)
       else Node(lt, x, insert rt n)
  end
```

Equality and comparison are *generic* — they work for *any* type of data, even strings, lists, and tuples!

8: Does the following function typecheck?

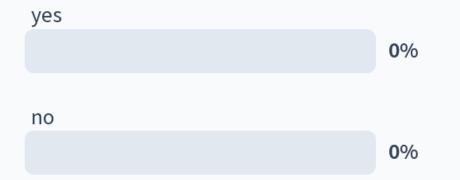


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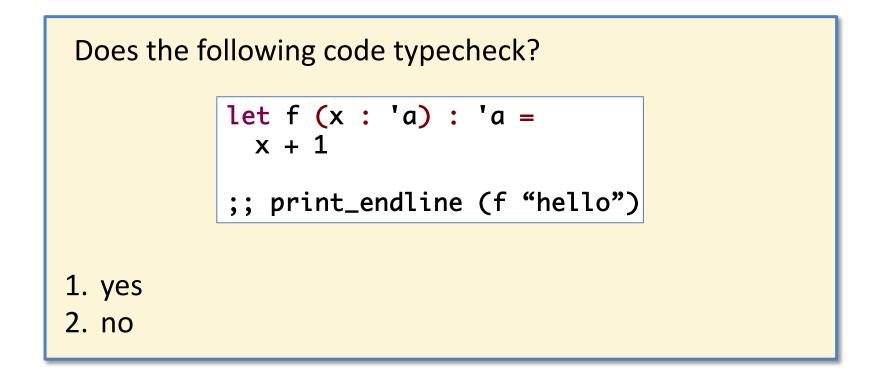


Answer: no: even though the return type is generic, the two branches must agree (so that 'b can be consistently instantiated).

8: Does the following code typecheck?



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Answer: no, the type annotations and uses of f aren't consistent.

However, it is a bit subtle: without the use (f "hello") the code *would* be correct - so long as all uses of f provide only 'int' the code is consistent! Despite the "generic" type annotation, f really has type int -> int.

First-class Functions

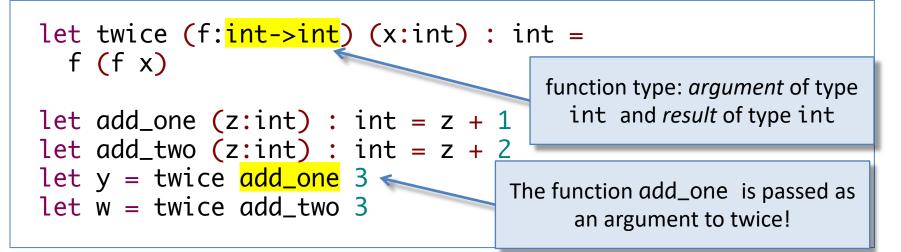
Higher-order Programs

or

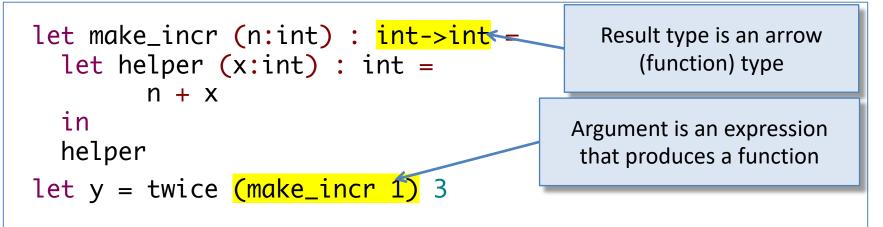
How not to repeat yourself, Part II.

First-class Functions

• You can pass a function as an *argument* to another function

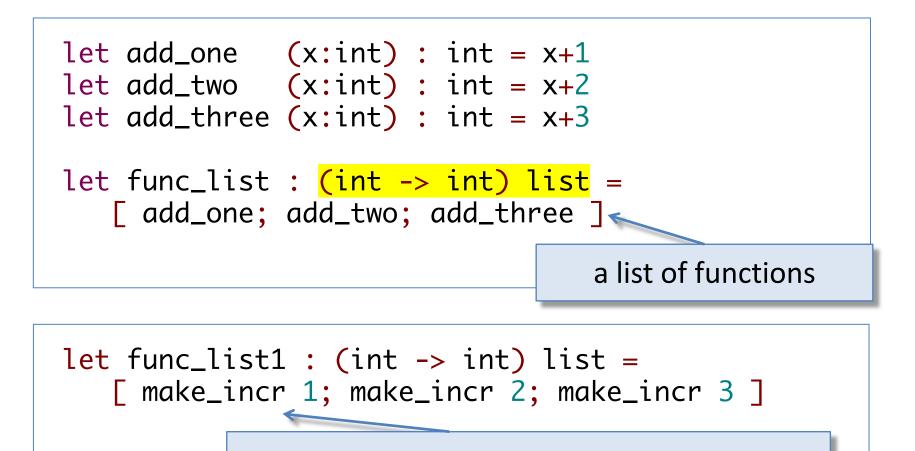


• You can *return* a function as the result of another function



Functions as Data

You can store functions in data structures!



a list of expressions that produce functions

Simplifying First-Class Functions

```
let twice (f:int->int) (x:int) : int =
  f (f x)
let add_one (z:int) : int = z + 1
```

```
twice add_one 3

\mapsto add_one (add_one 3)

\mapsto add_one (3 + 1)

\mapsto add_one 4

\mapsto 4 + 1

\mapsto 5
```

substitute add_one for f, 3 for x substitute 3 for z in add_one $3+1 \Rightarrow 4$ substitute 4 for z in add_one $4+1 \Rightarrow 5$

Simplifying First-Class Functions

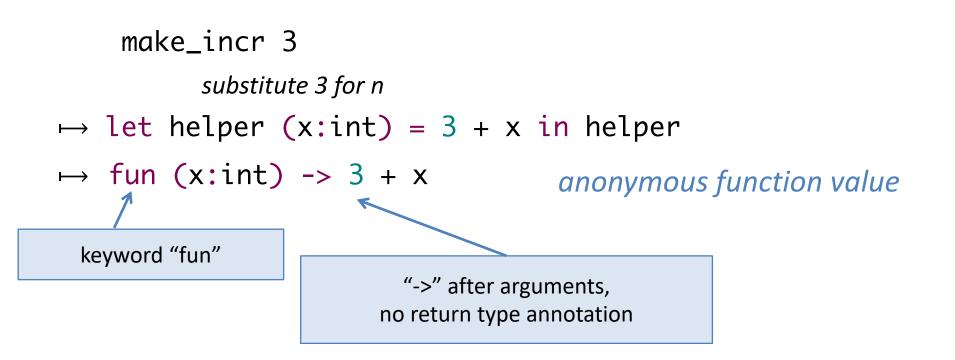
```
let make_incr (n:int) : int->int =
   let helper (x:int) : int = n + x in
   helper
```

make_incr 3
 substitute 3 for n

 Het helper (x:int) = 3 + x in helper
 Helper ???

Simplifying First-Class Functions

```
let make_incr (n:int) : int->int =
   let helper (x:int) : int = n + x in
   helper
```

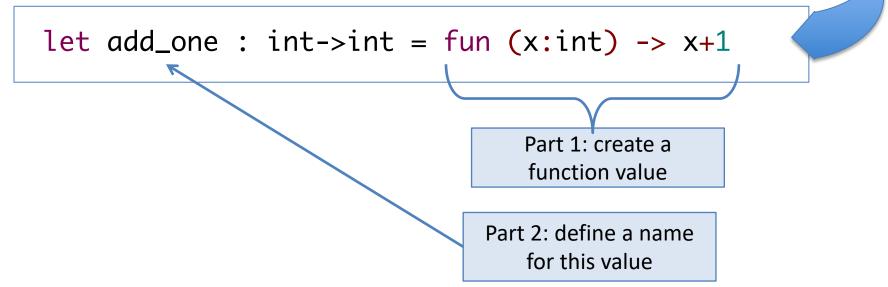


Function values

A standard function definition...

```
let add_one (x:int) : int = x+1
```

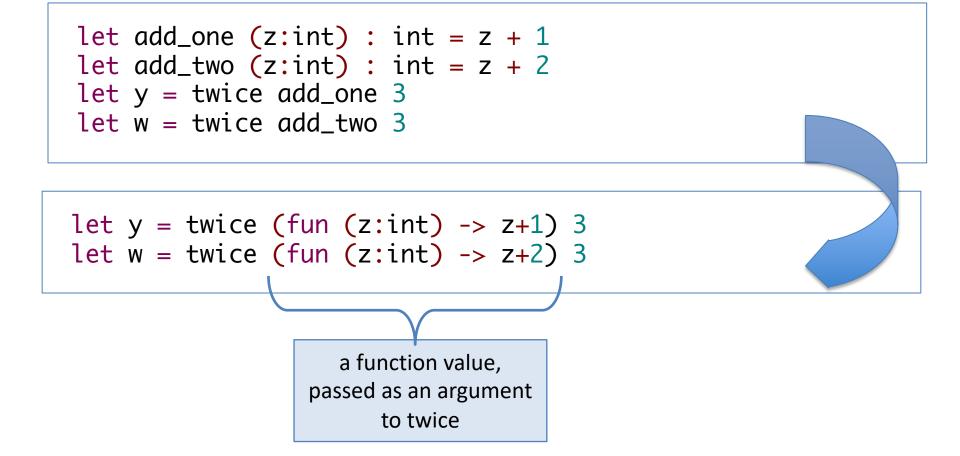
... is really an abbreviation for this:



The two definitions of add_one have exactly the same type and behave exactly the same. (The first is just an abbreviation* for the second.)

*computer scientists like to use the term "syntactic sugar" for such abbreviations. Such abbreviations make it "sweeter "to write simpler, tastier code, which "desugars" into more complex stuff

Anonymous functions



Function Types

• Functions have types that look like this:

• Examples:

int -> int int -> bool * int int -> int -> int (int -> int) -> int Parentheses matter! int -> int -> int = int -> (int -> int) ≠ (int -> int) -> int

int input

function input

Function Types

Yes!

Hang on... did we just say that

and

mean the same thing??

$$2 = 1 + 1$$

A function that takes *two* arguments...

has the same type as a function that takes one argument and returns a function that takes one argument

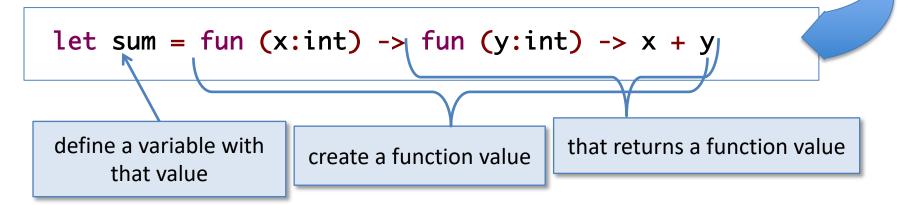
This is actually useful!

Multiple Arguments

We can decompose a standard function definition

```
let sum (x : int) (y:int) : int = x + y
```

into parts:

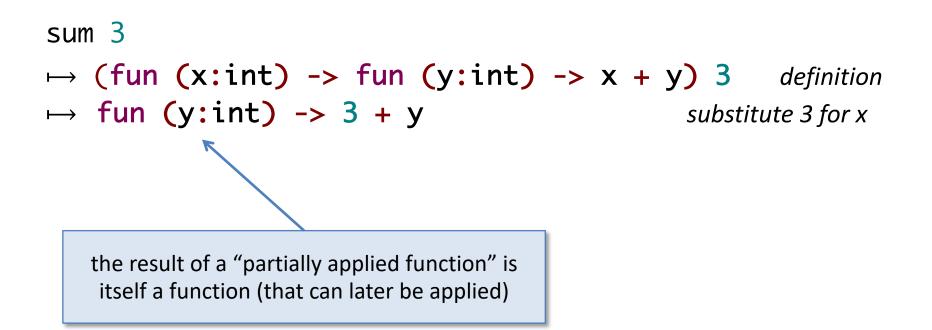


The two definitions of sum have the same type and behave the same!

let sum : int -> int -> int

Partial Application

let sum (x : int) (y:int) : int = x + y



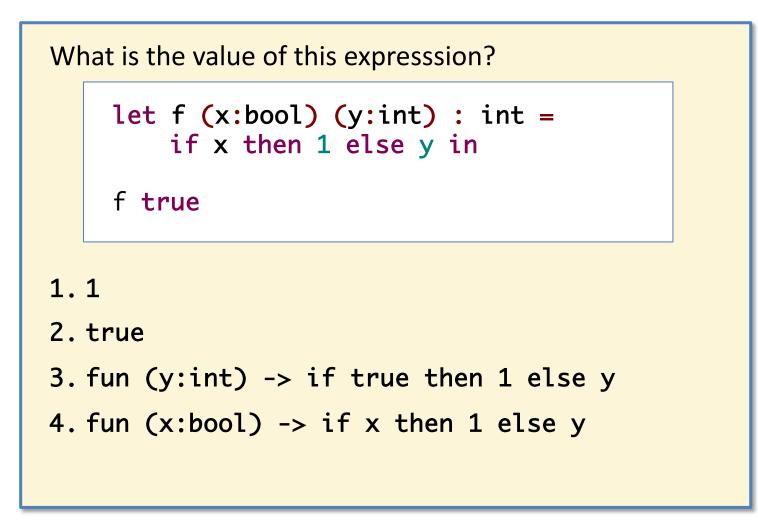
What good is partial application?

Consider this *filter* function:

let rec filter (p:'a -> bool) (l:'a list) : 'a list = begin match 1 with | [] -> [] 1 x::xs -> if p_x then x :: (filter p xs) else (filter p xs) end filter selects elements of a list based on a predicate p. let larger = filter (fun $x \rightarrow x > 10$) let smaller = filter (fun x -> x <= 10) We can create specialized "instances" by partial application... larger $[1;17;120;4;10] \Rightarrow [17;120]$ smaller $[1;17;120;4;10] \Rightarrow [1;4;10]$ Upshot: higher-order functions like filter are a very useful way and use them as ordinary list-processing functions. to structure library interfaces...

A. 1	
	0%
B. True	
	0%
C. fun (y:int) -> if true then 1 else y	
	0%
D. fun (x:bool) -> if x then 1 else y	
	0%

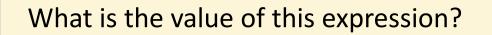
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8: What is the value of this expression?



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```
let f (g : int->int) (y: int) : int =
    g 1 + y in
```

f (fun (x:int) -> x + 1) 3

1.1 2.2

3.3 4.4

5.5

8: What is the type of this expression?

1. int	
	0%
2. int -> int	0%
	0,0
3. int -> int -> int	0%
4. (int -> int) -> int -> int	0%
5. Ill-typed	
5. ht typed	0%

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```
What is the type of this expression?
```

```
let f (g : int->int) (y: int) : int =
    g 1 + y in
```

```
f (fun (x:int) -> x + 1)
```

```
1. int
2. int -> int
3. int -> int -> int
4. (int -> int) -> int -> int
5. ill-typed
```