

CIS 194

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# TYPES

**EVERYTHING THAT IS SYNTACTICALLY LEGAL, THAT THE COMPILER WILL ACCEPT, WILL EVENTUALLY WIND UP IN YOUR CODEBASE. AND THAT'S WHY I THINK STATIC TYPING IS SO VALUABLE BECAUSE IT CUTS DOWN ON WHAT CAN MAKE IT PAST THOSE HURDLES THERE.**

**John Carmack**

## A WORLD WITHOUT TYPES

```
def double(x):  
    return 2 * x
```

Maybe `double(5) == 10`? Wrong.

How about `double("hello") == "hellohello"`?

Actually the correct answer is (obviously):

```
double([5, "a"]) == [5, "a", 5, "a"].
```

## HW1 CONTINUED...

{-

Replace `undefined` with your phone number.

-}

phoneNumber = undefined

## HW1 CONTINUED...

- ▶ `phoneNumber` = `2158985000`
- ▶ `phoneNumber'` = `"2158985000"`
- ▶ `phoneNumber''` = `(2,1,5,8,9,8,5,0,0,0)`
- ▶ `phoneNumber''''` = `[0,0,0,5,8,9,8,5,1,2]`

## HW1 CONTINUED...

{-

Replace `undefined` with your phone number.

-}

```
phoneNumber :: Int
```

```
phoneNumber = undefined
```

Clearly should be `phoneNumber = 2158985000`

**TYPE ANNOTATIONS**

# WHAT TYPES HAVE WE SEEN SO FAR?

- ▶ Int
- ▶ Char
- ▶ String
- ▶ Maybe String
- ▶ etc.



### WHAT TYPES HAVE WE SEEN SO FAR?

```
favoriteNumber :: Int  
favoriteNumber = 194
```

```
firstLetterOfName :: Char  
firstLetterOfName = head "Palmer"
```

```
hello194 :: String  
hello194 = hello "194"
```

```
githubUsername :: Maybe String  
githubUsername = Just "pzp1997"
```

**GENERICS**

## LENGTH OF A LIST

```
lengthIntList :: [Int] -> Int
```

```
lengthIntList xs =
```

```
  if null xs then
```

```
    0
```

```
  else
```

```
    1 + lengthIntList (tail xs)
```

```
lengthIntList [1,2,3] -> 3
```

```
lengthIntList "abc" -> WON'T COMPILE!
```

## LENGTH OF A LIST

```
lengthString :: String -> Int
lengthString xs =
  if null xs then
    0
  else
    1 + lengthString (tail xs)
```

```
lengthString "abc" -> 3
```

## LENGTH OF A LIST

```
lengthIntList :: [Int] -> Int
```

```
lengthIntList xs =
```

```
  if null xs then 0
```

```
  else 1 + lengthIntList (tail xs)
```

```
lengthString :: String -> Int
```

```
lengthString xs =
```

```
  if null xs then 0
```

```
  else 1 + lengthString (tail xs)
```

## LENGTH OF A LIST

lengthIntList :: [Int] -> Int

lengthIntList xs =  
 if null xs then 0  
 else 1 + lengthIntList (tail xs)

lengthString :: String -> Int

lengthString xs =  
 if null xs then 0  
 else 1 + lengthString (tail xs)

## LENGTH OF A LIST

```
length :: [???] -> Int
length xs =
  if null xs then
    0
  else
    1 + length (tail xs)
```

The ??? could be replaced by ANY type.

How can we use the type system to express that?

# ANSWER: DAILY DOUBLE

`length :: [a] -> Int`

- ▶ `a` is a placeholder
- ▶ `a` is bound when we apply the function
- ▶ No restrictions on which types that can be bound to `a`
- ▶ `b` or `aLexTrebek` would work too



## WHAT IS BINDING ANYWAY?

Suppose we have a definition

```
twoOfAKind :: a -> a -> (a, a)
```

```
twoOfAKind x y = (x, y)
```

```
twoOfAKind 1 2 -> (1, 2)
```

```
twoOfAKind 'a' 'b' -> ('a', 'b')
```

```
twoOfAKind 'a' 1 -> WON'T COMPILE! WHY?
```

## APPLY THE ARGUMENTS ONE AT A TIME

```
twoOfAKind :: a -> a -> (a, a)
```

```
twoOfAKind x y = (x, y)
```

```
partial = twoOfAKind 'a'
```

```
partial' :: Char -> (Char, Char)
```

```
partial' y = ('a', y)
```

```
partial 1
```

BUT 1 is not a Char!

# PARAMETERIZED TYPES

## MAYBE VS. MAYBE INT

```
maybeAdd mx my =  
  if isJust mx && isJust my then  
    Just (fromJust mx + fromJust my)  
  else  
    Nothing
```

What should the type of `maybeAdd` be?

How about `Maybe -> Maybe -> Maybe`?

## MAYBE VS. MAYBE INT

`maybeAdd :: Maybe -> Maybe -> Maybe`

But then we could do

`maybeAdd (Just 1) (Just "hello")`

which doesn't make sense...

### MAYBE VS. MAYBE INT

- ▶ Knowing that a value is a Maybe is not enough.
- ▶ We need to be able to specify the type of value stored inside of the Maybe too.
- ▶ In other words how can we differentiate between Maybe of an Int and a Maybe of a String at the type level?!
- ▶ **Solution: Maybe Int**

### BREAKING DOWN MAYBE INT

- ▶ Maybe is a “type constructor”
- ▶ Maybe is parameterized by type of value stored inside it  

```
myFavoriteNumber :: Maybe Int  
myFavoriteNumber = Just 194
```
- ▶ In the case above Int is the parameter to Maybe  

```
myLeastFavoriteNumber :: Maybe a  
myLeastFavoriteNumber = Nothing
```
- ▶ In the case above the parameter could be anything!

# SO IS MAYBE A TYPE?

- ▶ Is `Int` a type?
- ▶ Is `Maybe Int` a type?
- ▶ How about `Maybe` by itself?



# TYPE OF A FUNCTION

# WHAT IS THE TYPE OF A FUNCTION?

- ▶ Let's make a type called `Function`

```
isEven :: Function
```

```
isEven x = x `mod` 2 == 0
```

- ▶ Good first attempt
- ▶ Not a lot of type safety

# WHAT IS THE TYPE OF A FUNCTION?

- ▶ We need to add more information to our type
- ▶ Let's add type of argument and return value as parameters
- ▶ Our type is now `Function arg ret`

```
isEven :: Function Int Bool  
isEven x = x `mod` 2 == 0
```

# DYADIC FUNCTIONS

Maybe Function arg1 arg2 ret?

```
repeatIt :: Function Int String String  
repeatIt timesToRepeat snippet = ...
```

Actually Function arg1 (Function arg2 ret)

```
repeatIt :: Function Int (Function String String)  
repeatIt timesToRepeat snippet = ...
```

# SYNTACTIC SUGAR FTW

- ▶ `Function arg ret` is not the clearest syntax
- ▶ Haskell defines an infix type constructor `(->)` which is synonymous to `Function`
- ▶ `Function arg ret` becomes `arg -> ret`
- ▶ `isEven :: Int -> Bool`

### SYNTACTIC SUGAR FTW

- ▶ Function `arg1 (Function arg2 ret)` becomes `arg1 -> (arg2 -> ret)`
- ▶ Or since `(->)` is right associative, `arg1 -> arg2 -> ret`
- ▶ `repeatIt :: Int -> String -> String`