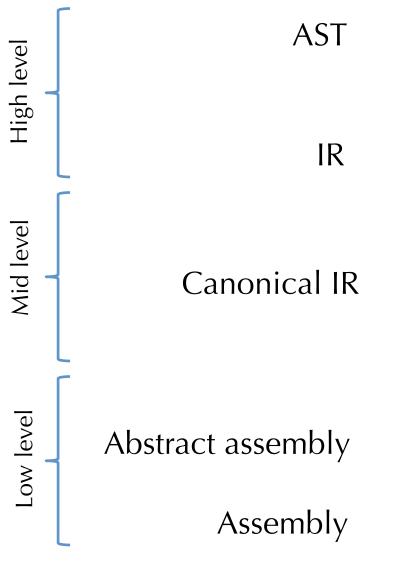
Lecture 22
CIS 341: COMPILERS

Announcements / Plan

- HW5: OAT typechecking, structs, function pointers
 Due: TONIGHT!
- HW6: LLVM Optimization: analysis and register allocation
 - Available soon
 - Due: Wednesday, April 26
- FINAL EXAM: Thursday, May 4th noon 2:00p.m.

When to apply optimization



- Inlining
 - Function specialization
 - Constant folding
 - Constant propagation
 - Value numbering
 - Dead code elimination
 - Loop-invariant code motion
 - Common sub-expression elimination
 - Strength Reduction
 - Constant folding & propagation
 - Branch prediction / optimization
 - Register allocation
 - Loop unrolling
 - Cache optimization

Constant Propagation

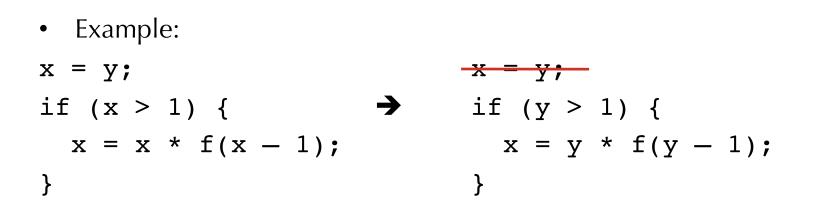
- If the value is known to be a constant, replace the use of the variable by the constant
- Value of the variable must be propagated forward from the point of assignment
 - This is a substitution operation

Example:
int x = 5;
int y = x * 2; → int y = 5 * 2; → int y = 10; →
int z = a[y]; int z = a[y]; int z = a[10];

• To be most effective, constant propagation should be interleaved with constant folding

Copy Propagation

- If one variable is assigned to another, replace uses of the assigned variable with the copied variable.
- Need to know where copies of the variable propagate.
- Interacts with the scoping rules of the language.



• Can make the first assignment to x *dead* code (that can be eliminated).

Dead Code Elimination

• If a side-effect free statement can never be observed, it is safe to eliminate the statement.

- A variable is *dead* if it is never used after it is defined.
 - Computing such *definition* and *use* information is an important component of compiler
- Dead variables can be created by other optimizations...

Unreachable/Dead Code

- Basic blocks not reachable by any trace leading from the starting basic block are *unreachable* and can be deleted.
 - Performed at the IR or assembly level
 - Improves cache, TLB performance
- Dead code: similar to unreachable blocks.
 - A value might be computed but never subsequently used.
- Code for computing the value can be dropped
- But only if it's *pure*, i.e. it has *no* externally visible side effects
 - Externally visible effects: raising an exception, modifying a global variable, going into an infinite loop, printing to standard output, sending a network packet, launching a rocket
 - Note: Pure functional languages (e.g. Haskell) make reasoning about the safety of optimizations (and code transformations in general) easier!

Inlining

- Replace a call to a function with the body of the function itself with arguments rewritten to be local variables:
- Example in OAT code:

```
int g(int x) { return x + pow(x); }
int pow(int a) { var b = 1; var n = 0;
while (n < a) {b = 2 * b}; return b; }</pre>
```

→

```
int g(int x) { var a = x; var b = 1; var n = 0;
while (n < a) {b = 2 * b}; var tmp = b;
return x + tmp;
```

- }
- May need to rename variable names to avoid *name capture*
 - Example of what can go wrong?
- Best done at the AST or relatively high-level IR.
- When is it profitable?
 - Eliminates the stack manipulation, jump, etc.
 - Can increase code size.
 - Enables further optimizations

Code Specialization

- Idea: create specialized versions of a function that is called from different places with different arguments.
- Example: specialize function **f** in:

```
class A implements I { int m() {...} }
class B implements I { int m() {...} }
int f(I x) { x.m(); } // don't know which m
A a = new A(); f(a); // know it's A.m
B b = new B(); f(b); // know it's B.m
```

- **f_A** would have code specialized to dispatch to **A.m**
- **f_B** would have code specialized to dispatch to **B.m**
- You can also inline methods when the run-time type is known statically
 - Often just one class implements a method.

Common Subexpression Elimination

- In some sense it's the opposite of inlining: fold redundant computations together
- Example:

a[i] = a[i] + 1 compiles to:

[a + i*4] = [a + i*4] + 1

Common subexpression elimination removes the redundant add and multiply:

t = a + i*4; [t] = [t] + 1

• For safety, you must be sure that the shared expression always has the same value in both places!

Unsafe Common Subexpression Elimination

```
    Example: consider this OAT function:
    unit f(int[] a, int[] b, int[] c) {
        var j = ...; var i = ...; var k = ...;
        b[j] = a[i] + 1; c[k] = a[i]; return;
    }
```

• The following optimization that shares the expression a[i] is unsafe... why?

```
unit f(int[] a, int[] b, int[] c) {
  var j = ...; var i = ...; var k = ...;
  t = a[i];
  b[j] = t + 1; c[k] = t; return;
}
```

LOOP OPTIMIZATIONS

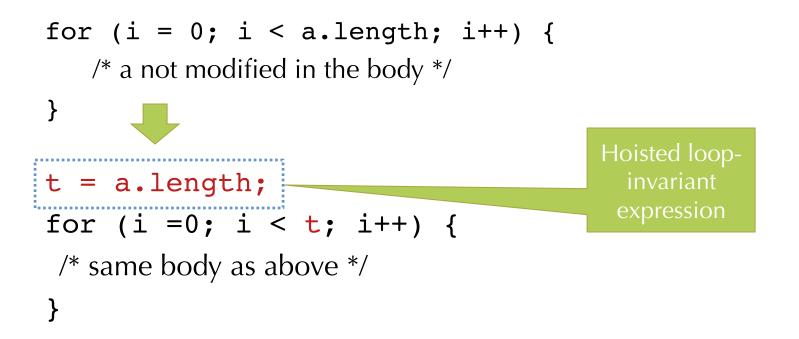
Zdancewic CIS 341: Compilers

Loop Optimizations

- Program hot spots often occur in loops.
 - Especially inner loops
 - Not always: consider operating systems code or compilers vs. a computer game or word processor
- Most program execution time occurs in loops.
 - The 90/10 rule of thumb holds here too. (90% of the execution time is spent in 10% of the code)
- Loop optimizations are very important, effective, and numerous
 - Also, concentrating effort to improve loop body code is usually a win

Loop Invariant Code Motion

- Another form of redundancy elimination.
- If the result of a statement or expression does not change during the loop *and* it's pure, it can be hoisted outside the loop body.
- Often useful for array element addressing code
 - Invariant code not visible at the source level



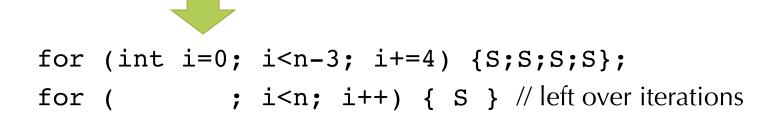
Strength Reduction (revisited)

- Strength reduction can work for loops too
- Idea: replace expensive operations (multiplies, divides) by cheap ones (adds and subtracts)
- For loops, create a dependent induction variable:

```
• Example:
for (int i = 0; i<n; i++) { a[i*3] = 1; }
     // stride by 3
     int j = 0;
for (int i = 0; i<n; i++) {
     a[j] = 1;
     j = j + 3; // replace multiply by add
}
```

Loop Unrolling (revisited)

Branches can be expensive, unroll loops to avoid them.
 for (int i=0; i<n; i++) { S }

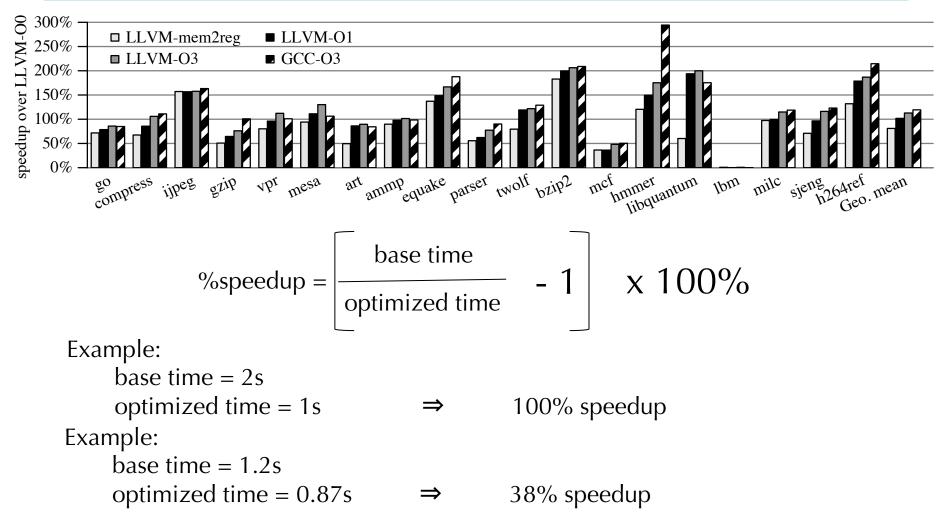


- With k unrollings, eliminates (k-1)/k conditional branches
 - So for the above program, it eliminates ³/₄ of the branches
- Space-time tradeoff:
 - Not a good idea for large S or small n
- Interacts with instruction caching, branch prediction

EFFECTIVENESS?

Zdancewic CIS 341: Compilers

Optimization Effectiveness?



Graph taken from:

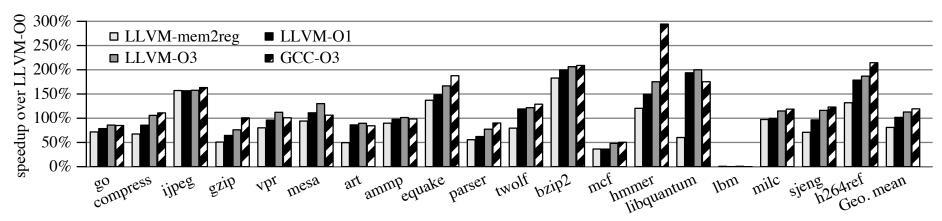
Jianzhou Zhao, Santosh Nagarakatte, Milo M. K. Martin, and Steve Zdancewic.

Formal Verification of SSA-Based Optimizations for LLVM.

In Proc. 2013 ACM SIGPLAN Conference on Programming Languages Design and Implementation (PLDI), 2013

Zdancewic CIS 341: Compilers

Optimization Effectiveness?



- mem2reg: promotes alloca'ed stack slots to temporaries to enable register allocation
- Analysis:
 - mem2reg alone (+ back-end optimizations like register allocation) yields ~78% speedup on average
 - O1 yields ~100% speedup (so all the rest of the optimizations combined account for ~22%)
 - -O3 yields ~120% speedup
- Hypothetical program that takes 10 sec. (base time):
 - Mem2reg alone: expect ~5.6 sec
 - - O1: expect ~5 sec
 - - O3: expect ~4.5 sec

CODE ANALYSIS

Zdancewic CIS 341: Compilers

Motivating Code Analyses

- There are lots of things that might influence the safety/applicability of an optimization
 - What algorithms and data structures can help?
- How do you know what is a loop?
- How do you know an expression is invariant?
- How do you know if an expression has no side effects?
- How do you keep track of where a variable is defined?
- How do you know where a variable is used?
- How do you know if two reference values may be aliases of one another?

Moving Towards Register Allocation

- The OAT compiler currently generates as *many* temporary variables as it needs
 - These are the **%uids** you should be very familiar with by now.
- Current compilation strategy:
 - Each %uid maps to a stack location.
 - This yields programs with many loads/stores to memory.
 - Very inefficient.
- Ideally, we'd like to map as many **%uid**'s as possible into registers.
 - Eliminate the use of the alloca instruction?
 - Only 16 max registers available on 64-bit X86
 - %rsp and %rbp are reserved and some have special semantics, so really only 10 or 12 available
 - This means that a register must hold more than one slot
- When is this safe?

Liveness

- Observation: **%uid1** and **%uid2** can be assigned to the same register if their values will not be needed at the same time.
 - What does it mean for an **%uid** to be "needed"?
 - Ans: its contents will be used as a source operand in a later instruction.
- Such a variable is called "*live*"
- Two variables can share the same register if they are *not* live at the same time.

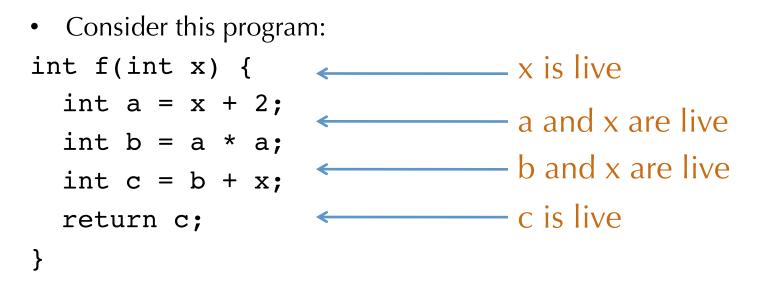
Scope vs. Liveness

- We can already get some coarse liveness information from variable scoping.
- Consider the following OAT program:

```
int f(int x) {
   var a = 0;
   if (x > 0) {
      var b = x * x;
      a = b + b;
   }
   var c = a * x;
   return c;
}
```

- Note that due to OAT's scoping rules, variables **b** and **c** can never be live at the same time.
 - c's scope is disjoint from b's scope
- So, we could assign b and c to the same alloca'ed slot and potentially to the same register.

But Scope is too Coarse



- The scopes of a,b,c,x all overlap they're all in scope at the end of the block.
- But, a, b, c are never live at the same time.
 - So they can share the same stack slot / register

Live Variable Analysis

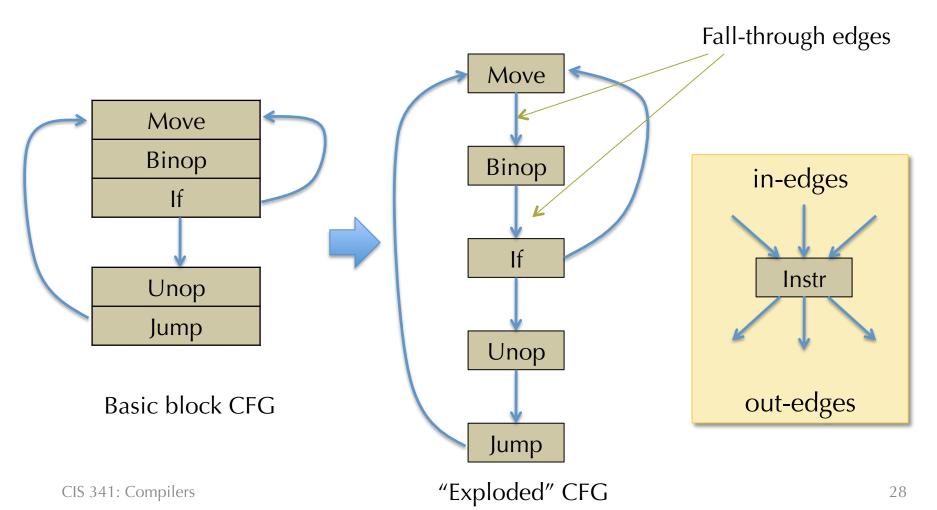
- A variable v is *live* at a program point if v is defined before the program point and used after it.
- Liveness is defined in terms of where variables are *defined* and where variables are *used*
- Liveness analysis: Compute the live variables between each statement.
 - May be *conservative* (i.e. it may claim a variable is live when it isn't) so because that's a safe approximation
 - To be useful, it should be more *precise* than simple scoping rules.
- Liveness analysis is one example of *dataflow analysis*
 - Other examples: Available Expressions, Reaching Definitions, Constant-Propagation Analysis, ...

Control-flow Graphs Revisited

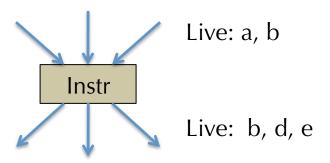
- For the purposes of dataflow analysis, we use the *control-flow graph* (CFG) intermediate form.
- Recall that a basic block is a sequence of instructions such that:
 - There is a distinguished, labeled entry point (no jumps into the middle of a basic block)
 - There is a (possibly empty) sequence of non-control-flow instructions
 - The block ends with a single control-flow instruction (jump, conditional branch, return, etc.)
- A control flow graph
 - Nodes are blocks
 - There is an edge from B1 to B2 if the control-flow instruction of B1 might jump to the entry label of B2
 - There are no "dangling" edges there is a block for every jump target.
- Note: the following slides are intentionally a bit ambiguous about the exact nature of the code in the control flow graphs:
 - at the x86 assembly level
 - an "imperative" C-like source level
 - at the LLVM IR level
 - Same general idea, but the exact details will differ
 - e.g. LLVM IR doesn't have "imperative" update of %uid temporaries.
 - In fact, the SSA structure of the LLVM IR makes some of these analyses simpler.

Dataflow over CFGs

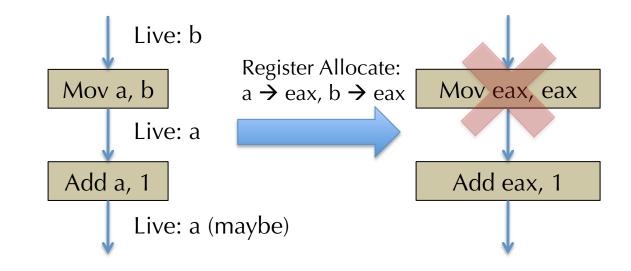
- For precision, it is helpful to think of the "fall through" between sequential instructions as an edge of the control-flow graph too.
 - Different implementation tradeoffs in practice...



Liveness is Associated with Edges



- This is useful so that the same register can be used for different temporaries in the same statement.
- Example: a = b + 1
- Compiles to:



Uses and Definitions

- Every instruction/statement *uses* some set of variables
 - i.e. reads from them
- Every instruction/statement *defines* some set of variables
 - i.e. writes to them
- For a node/statement s define:
 - use[s] : set of variables used by s
 - def[s] : set of variables defined by s
- Examples:

-a = b + c	$use[s] = \{b,c\}$	$def[s] = \{a\}$
- a = a + 1	$use[s] = \{a\}$	$def[s] = \{a\}$

Liveness, Formally

- A variable v is *live* on edge e if: There is
 - a node n in the CFG such that use[n] contains v, and
 - a directed path from e to n such that for every statement s' on the path, def[s'] does not contain v
- The first clause says that v will be used on some path starting from edge e.
- The second clause says that v won't be redefined on that path before the use.
- Questions:
 - How to compute this efficiently?
 - How to use this information (e.g. for register allocation)?
 - How does the choice of IR affect this? (e.g. LLVM IR uses SSA, so it doesn't allow redefinition ⇒ simplify liveness analysis)

Simple, inefficient algorithm

- "A variable v is live on an edge e if there is a node n in the CFG using it *and* a directed path from e to n pasing through no def of v."
- Backtracking Algorithm:
 - For each variable v...
 - Try all paths from each use of v, tracing backwards through the controlflow graph until either v is defined or a previously visited node has been reached.
 - Mark the variable v live across each edge traversed.

• Inefficient because it explores the same paths many times (for different uses and different variables)

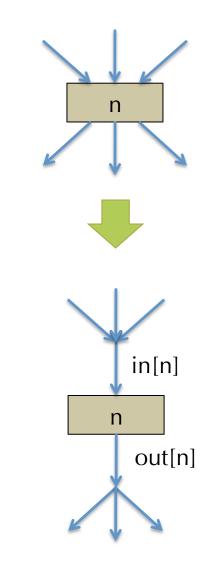
Dataflow Analysis

- *Idea*: compute liveness information for all variables simultaneously.
 - Keep track of sets of information about each node
- Approach: define *equations* that must be satisfied by any liveness determination.
 - Equations based on "obvious" constraints.
- Solve the equations by iteratively converging on a solution.
 - Start with a "rough" approximation to the answer
 - Refine the answer at each iteration
 - Keep going until no more refinement is possible: a *fixpoint* has been reached
- This is an instance of a general framework for computing program properties: dataflow analysis

Dataflow Value Sets for Liveness

- Nodes are program statements, so:
- use[n] : set of variables used by n
- def[n] : set of variables defined by n
- in[n] : set of variables live on entry to n
- out[n] : set of variables live on exit from n
- Associate in[n] and out[n] with the "collected" information about incoming/outgoing edges
- For Liveness: what constraints are there among these sets?
- Clearly:

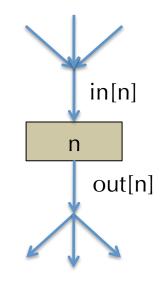
 $in[n] \supseteq use[n]$



• What other constraints?

Other Dataflow Constraints

- We have: $in[n] \supseteq use[n]$
 - "A variable must be live on entry to n if it is used by n"
- Also: $in[n] \supseteq out[n] def[n]$
 - "If a variable is live on exit from n, and n doesn't define it, it is live on entry to n"
 - Note: here '-' means "set difference"
- And: $out[n] \supseteq in[n']$ if $n' \in succ[n]$
 - "If a variable is live on entry to a successor node of n, it must be live on exit from n."



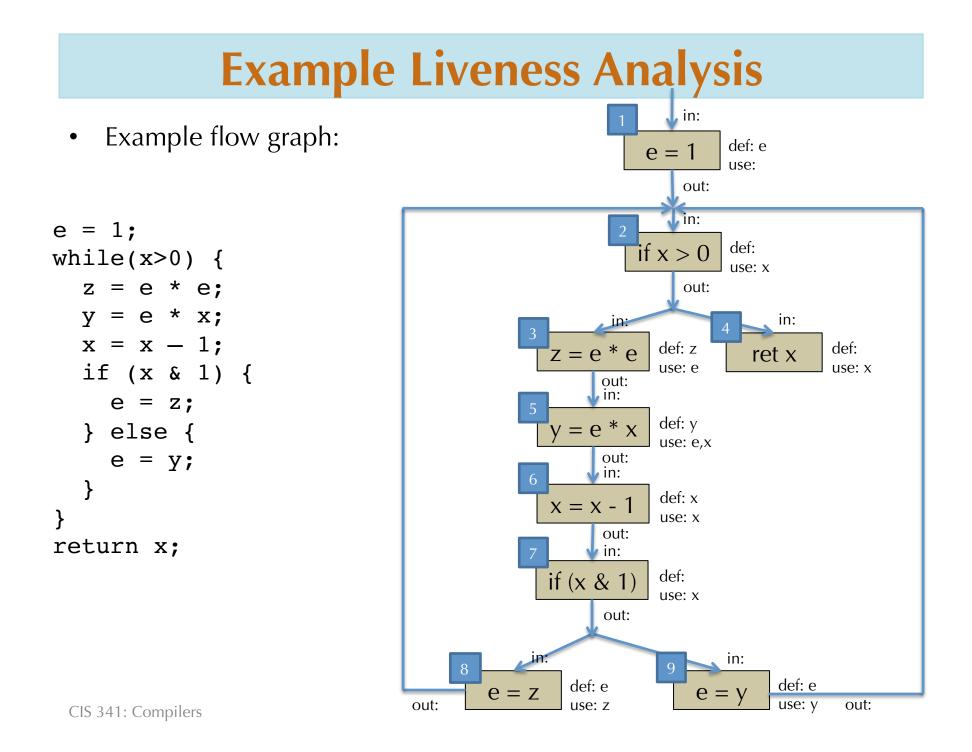
Iterative Dataflow Analysis

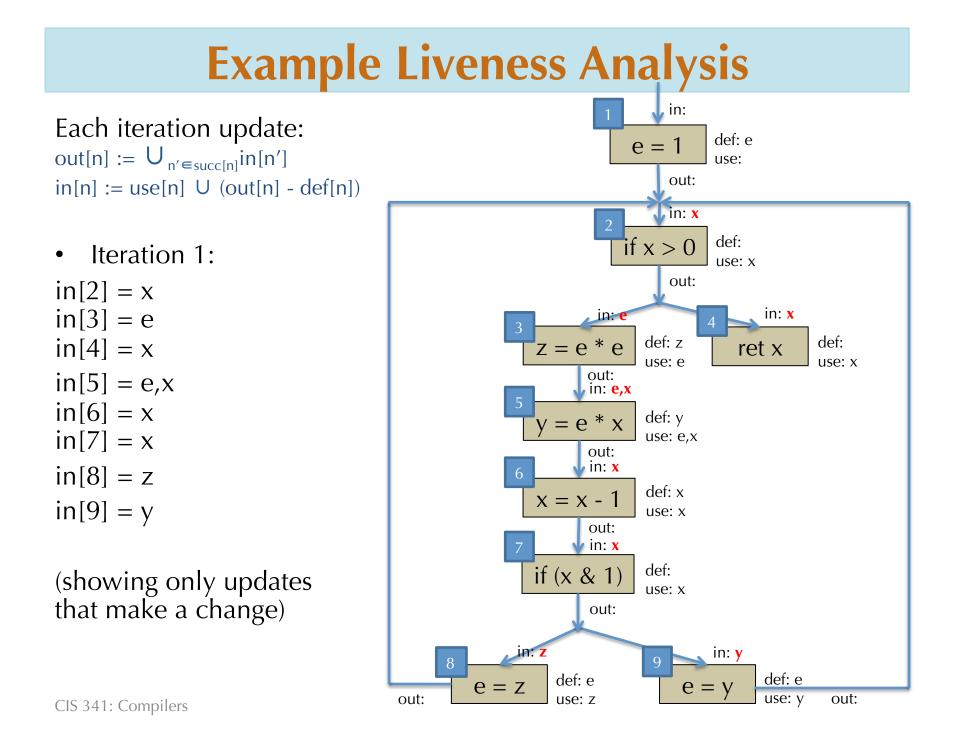
- Find a solution to those constraints by starting from a rough guess.
- Start with: $in[n] = \emptyset$ and $out[n] = \emptyset$
- They don't satisfy the constraints:
 - in[n] ⊇ use[n]
 - in[n] ⊇ out[n] def[n]
 - out[n] ⊇ in[n'] if n' ∈ succ[n]
- Idea: iteratively re-compute in[n] and out[n] where forced to by the constraints.
 - Each iteration will add variables to the sets in[n] and out[n] (i.e. the live variable sets will increase monotonically)
- We stop when in[n] and out[n] satisfy these equations: (which are derived from the constraints above)
 - in[n] = use[n] U (out[n] def[n])
 - out[n] = $U_{n' \in succ[n]}in[n']$

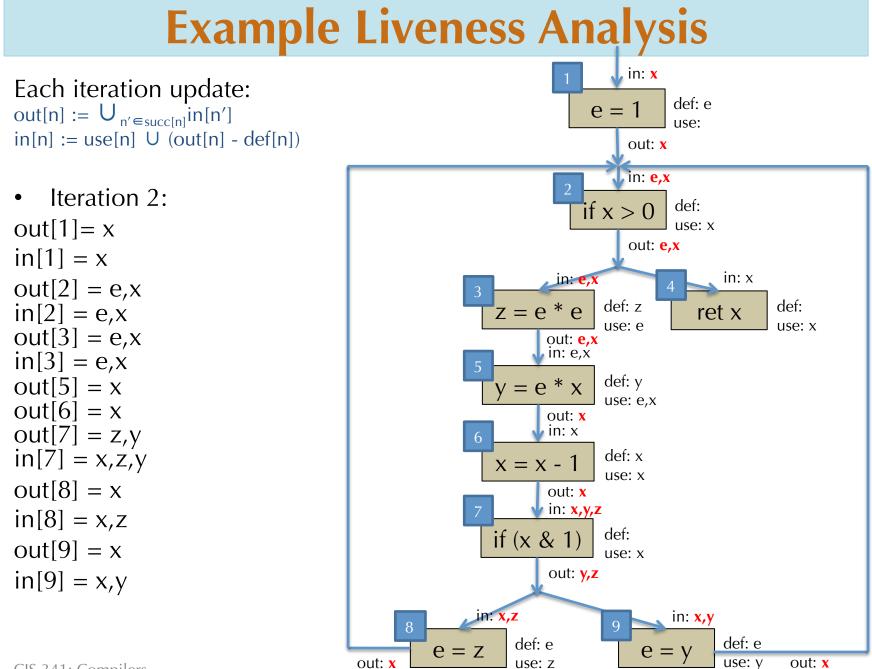
Complete Liveness Analysis Algorithm

```
for all n, in[n] := Ø, out[n] := Ø
repeat until no change in 'in' and 'out'
for all n
out[n] := U_{n' \in succ[n]}in[n']
in[n] := use[n] \cup (out[n] - def[n])
end
end
```

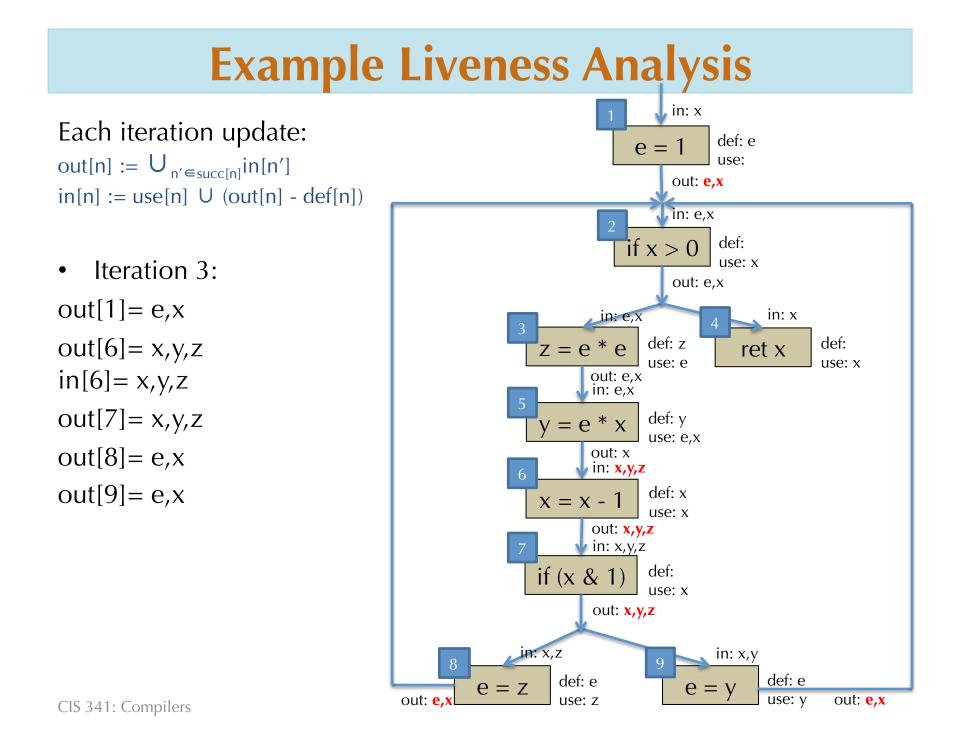
- Finds a *fixpoint* of the in and out equations.
 - The algorithm is guaranteed to terminate... Why?
- Why do we start with Ø?

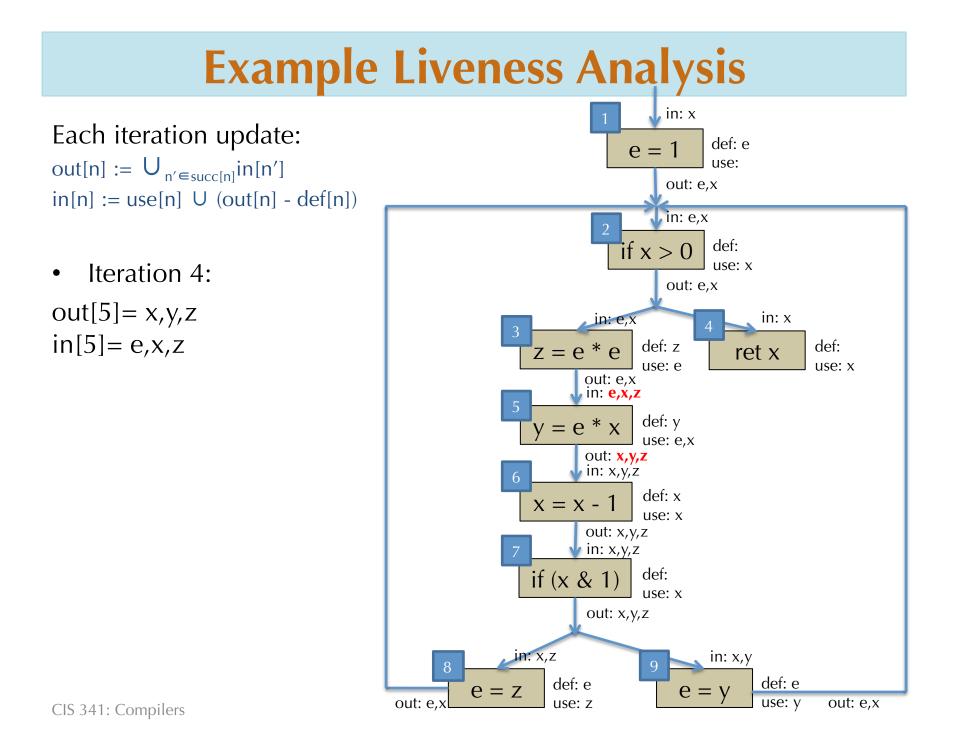


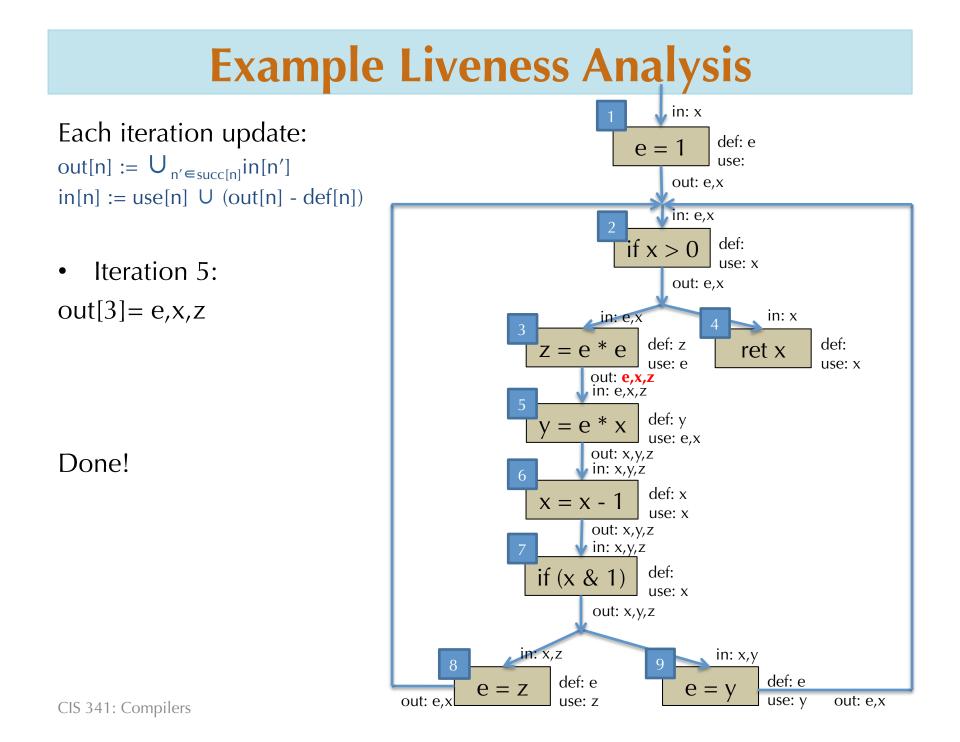




CIS 341: Compilers







Improving the Algorithm

- Can we do better?
- Observe: the only way information propagates from one node to another is using: out[n] := U_{n'∈succ[n]}in[n']
 - This is the only rule that involves more than one node
- If a node's successors haven't changed, then the node itself won't change.
- Idea for an improved version of the algorithm:
 - Keep track of which node's successors have changed

A Worklist Algorithm

• Use a FIFO queue of nodes that might need to be updated.

```
for all n, in[n] := Ø, out[n] := Ø

w = new queue with all nodes

repeat until w is empty

let n = w.pop() // pull a node off the queue

old_in = in[n] // remember old in[n]

out[n] := \bigcup_{n' \in succ[n]} in[n']

in[n] := use[n] U (out[n] - def[n])

if (old_in != in[n]), // if in[n] has changed

for all m in pred[n], w.push(m)// add to worklist

end
```