

Lecture 12

CIS 341: COMPILERS

Announcements

- Midterm: March 3rd
 - In class
 - One-page, letter-sized, double-sided “cheat sheet” of notes permitted
 - Coverage: interpreters / program transformers / x86 / calling conventions / IRs / LLVM / Lexing / Parsing
 - See examples of previous exams on the web pages
- HW4: Compiling Oat v.1
 - released soon(ish)
 - due March 23rd

LL(1) GRAMMARS

Predictive Parsing

- Given an LL(1) grammar:
 - For a given nonterminal, the lookahead symbol uniquely determines the production to apply.
 - Top-down parsing = predictive parsing
 - Driven by a predictive parsing table:
nonterminal * input token \rightarrow production

$T \mapsto S\$$
 $S \mapsto ES'$
 $S' \mapsto \varepsilon$
 $S' \mapsto + S$
 $E \mapsto \text{number} \mid (S)$

	number	+	()	\$ (EOF)
T	$\mapsto S\$$		$\mapsto S\$$		
S	$\mapsto E S'$		$\mapsto E S'$		
S'		$\mapsto + S$		$\mapsto \varepsilon$	$\mapsto \varepsilon$
E	$\mapsto \text{num.}$		$\mapsto (S)$		

- Note: it is convenient to add a special *end-of-file* token \$ and a start symbol T (top-level) that requires \$.

How do we construct the parse table?

- Consider a given production: $A \rightarrow \gamma$
- Construct the set of all input tokens that may appear *first* in strings that can be derived from γ
 - Add the production $\rightarrow \gamma$ to the entry (A,token) for each such token.
- If γ can derive ε (the empty string), then we construct the set of all input tokens that may *follow* the nonterminal A in the grammar.
 - Add the production $\rightarrow \gamma$ to the entry (A, token) for each such token.
- Note: if there are two different productions for a given entry, the grammar is not LL(1)

Example

- $\text{First}(T) = \text{First}(S)$
- $\text{First}(S) = \text{First}(E)$
- $\text{First}(S') = \{ + \}$
- $\text{First}(E) = \{ \text{number}, '(' \}$

$T \mapsto S\$$
 $S \mapsto ES'$
 $S' \mapsto \epsilon$
 $S' \mapsto + S$
 $E \mapsto \text{number} \mid (S)$

- $\text{Follow}(S') = \text{Follow}(S)$
- $\text{Follow}(S) = \{ \$, ')' \} \cup \text{Follow}(S')$

Note: we want the *least* solution to this system of set equations... a *fixpoint* computation. More on these later in the course.

	number	+	()	\$ (EOF)
T	$\mapsto S\$$		$\mapsto S\$$		
S	$\mapsto E S'$		$\mapsto E S'$		
S'		$\mapsto + S$		$\mapsto \epsilon$	$\mapsto \epsilon$
E	$\mapsto \text{num.}$		$\mapsto (S)$		

Converting the table to code

- Define n mutually recursive functions
 - one for each nonterminal A : `parse_A`
 - The type of `parse_A` is `unit -> ast` if A is *not* an auxiliary nonterminal
 - Parse functions for auxiliary nonterminals (e.g. S') take extra `ast`'s as inputs, one for each nonterminal in the “factored” prefix.
- Each function “peeks” at the lookahead token and then follows the production rule in the corresponding entry.
 - Consume terminal tokens from the input stream
 - Call `parse_X` to create sub-tree for nonterminal X
 - If the rule ends in an auxiliary nonterminal, call it with appropriate `ast`'s. (The auxiliary rule is responsible for creating the `ast` after looking at more input.)
 - Otherwise, this function builds the `ast` tree itself and returns it.

	number	+	()	\$ (EOF)
T	$\mapsto S\$$		$\mapsto S\$$		
S	$\mapsto E S'$		$\mapsto E S'$		
S'		$\mapsto + S$		$\mapsto \epsilon$	$\mapsto \epsilon$
E	$\mapsto \text{num.}$		$\mapsto (S)$		

Hand-generated LL(1) code for the table above.

DEMO: HANDPARSER.ML

LL(1) Summary

- Top-down parsing that finds the leftmost derivation.
- Language Grammar \Rightarrow LL(1) grammar \Rightarrow prediction table \Rightarrow recursive-descent parser
- Problems:
 - Grammar must be LL(1)
 - Can extend to LL(k) (it just makes the table bigger)
 - Grammar cannot be left recursive (parser functions will loop!)
- Is there a better way?



LR GRAMMARS

Bottom-up Parsing (LR Parsers)

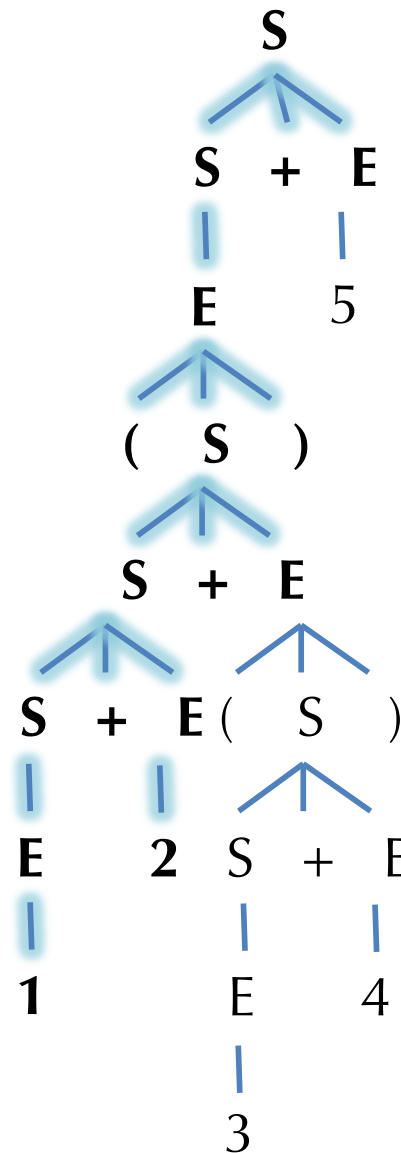
- LR(k) parser:
 - Left-to-right scanning
 - Rightmost derivation
 - k lookahead symbols
- LR grammars are more expressive than LL
 - Can handle left-recursive (and right recursive) grammars; virtually all programming languages
 - Easier to express programming language syntax (no left factoring)
- Technique: “Shift-Reduce” parsers
 - Work bottom up instead of top down
 - Construct right-most derivation of a program in the grammar
 - Used by many parser generators (e.g. yacc, CUP, ocamlyacc, merlin, etc.)
 - Better error detection/recovery

Top-down vs. Bottom up

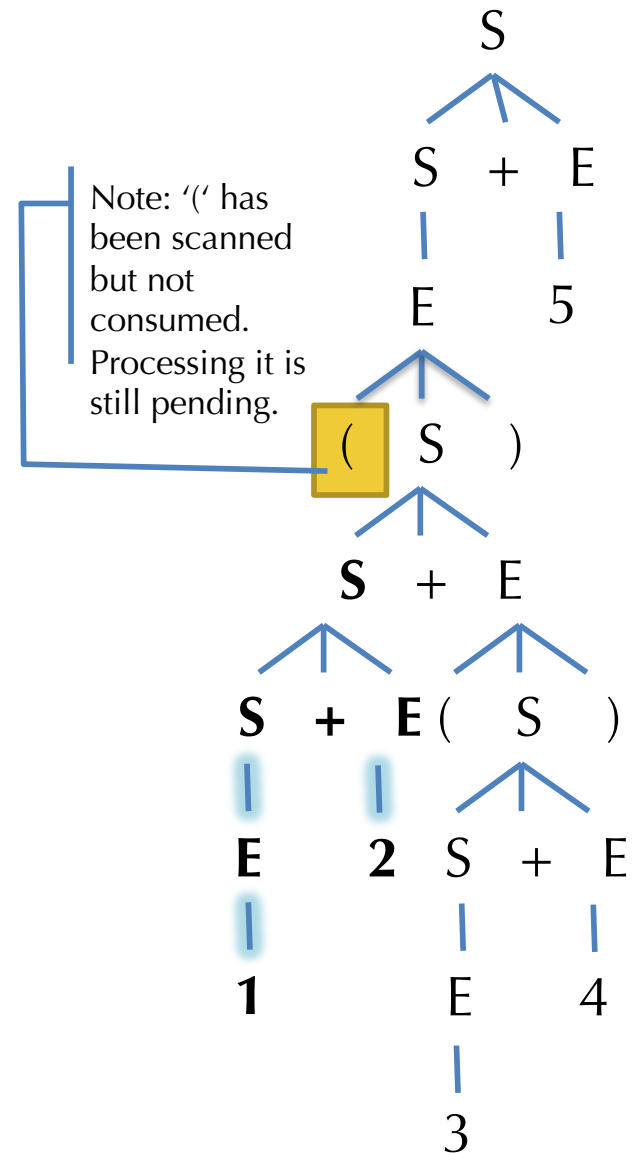
- Consider the left-recursive grammar:

$S \mapsto S + E \mid E$
 $E \mapsto \text{number} \mid (S)$

- $(1 + 2 + (3 + 4)) + 5$
- What part of the tree must we know after scanning just “ $(1 + 2$ ” ?
- In top-down, must be able to guess which productions to use...



Top-down



Note: ‘(’ has been scanned but not consumed. Processing it is still pending.

Bottom-up

Progress of Bottom-up Parsing

	Reductions	Scanned	Input Remaining
	$(1 + 2 + (3 + 4)) + 5 \leftarrow$		$(1 + 2 + (3 + 4)) + 5$
	$(\underline{\mathbf{E}} + 2 + (3 + 4)) + 5 \leftarrow$	$($	$1 + 2 + (3 + 4)) + 5$
	$(\underline{\mathbf{S}} + 2 + (3 + 4)) + 5 \leftarrow$	$(1$	$+ 2 + (3 + 4)) + 5$
	$(\mathbf{S} + \underline{\mathbf{E}} + (3 + 4)) + 5 \leftarrow$	$(1 + 2$	$+ (3 + 4)) + 5$
	$(\underline{\mathbf{S}} + (3 + 4)) + 5 \leftarrow$	$(1 + 2$	$+ (3 + 4)) + 5$
	$(\mathbf{S} + (\underline{\mathbf{E}} + 4)) + 5 \leftarrow$	$(1 + 2 + (3$	$+ 4)) + 5$
	$(\mathbf{S} + (\underline{\mathbf{S}} + 4)) + 5 \leftarrow$	$(1 + 2 + (3$	$+ 4)) + 5$
	$(\mathbf{S} + (\mathbf{S} + \underline{\mathbf{E}})) + 5 \leftarrow$	$(1 + 2 + (3 + 4$	$)) + 5$
	$(\mathbf{S} + (\underline{\mathbf{S}})) + 5 \leftarrow$	$(1 + 2 + (3 + 4$	$)) + 5$
	$(\mathbf{S} + \underline{\mathbf{E}}) + 5 \leftarrow$	$(1 + 2 + (3 + 4)$	$) + 5$
	$(\underline{\mathbf{S}}) + 5 \leftarrow$	$(1 + 2 + (3 + 4)$	$) + 5$
	$\underline{\mathbf{E}} + 5 \leftarrow$	$(1 + 2 + (3 + 4))$	$+ 5$
	$\underline{\mathbf{S}} + 5 \leftarrow$	$(1 + 2 + (3 + 4))$	$+ 5$
	$\mathbf{S} + \underline{\mathbf{E}} \leftarrow$	$(1 + 2 + (3 + 4)) + 5$	
	\mathbf{S}		

Rightmost derivation

$S \mapsto S + E \mid E$
 $E \mapsto \text{number} \mid (S)$

Shift/Reduce Parsing

- Parser state:
 - Stack of terminals and nonterminals.
 - Unconsumed input is a string of terminals
 - Current derivation step is $\text{stack} + \text{input}$
- Parsing is a sequence of *shift* and *reduce* operations:
- Shift**: move look-ahead token to the stack
- Reduce**: Replace symbols γ at top of stack with nonterminal X such that $X \mapsto \gamma$ is a production. (pop γ , push X)

$$S \mapsto S + E \mid E$$

$$E \mapsto \text{number} \mid (S)$$

Stack	Input	Action
	(1 + 2 + (3 + 4)) + 5	shift (
(1 + 2 + (3 + 4)) + 5	shift 1
(1	+ 2 + (3 + 4)) + 5	reduce: $E \mapsto \text{number}$
(E	+ 2 + (3 + 4)) + 5	reduce: $S \mapsto E$
(S	+ 2 + (3 + 4)) + 5	shift +
(S +	2 + (3 + 4)) + 5	shift 2
(S + 2	+ (3 + 4)) + 5	reduce: $E \mapsto \text{number}$

Simple LR parsing with no look ahead.

LR(0) GRAMMARS

LR Parser States

- Goal: know what set of reductions are legal at any given point.
- Idea: Summarize all possible stack prefixes α as a finite parser state.
 - Parser state is computed by a DFA that reads the stack σ .
 - Accept states of the DFA correspond to unique reductions that apply.
- Example: LR(0) parsing
 - Left-to-right scanning, Right-most derivation, zero look-ahead tokens
 - Too weak to handle many language grammars (e.g. the “sum” grammar)
 - But, helpful for understanding how the shift-reduce parser works.

Example LR(0) Grammar: Tuples

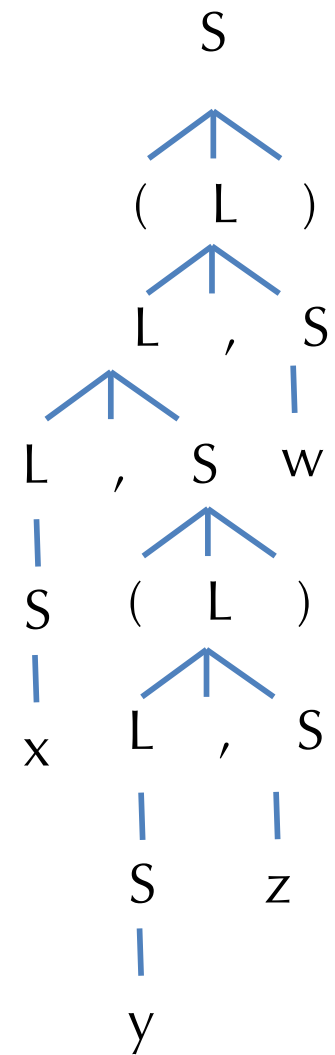
- Example grammar for non-empty tuples and identifiers:

$$\begin{aligned} S &\mapsto (L) \mid \text{id} \\ L &\mapsto S \mid L , S \end{aligned}$$

- Example strings:

- x
- (x,y)
- (((x))))
- (x, (y, z), w)
- (x, (y, (z, w)))

Parse tree for:
(x, (y, z), w)



Shift/Reduce Parsing

- Parser state:
 - Stack of terminals and nonterminals.
 - Unconsumed input is a string of terminals
 - Current derivation step is stack + input
- Parsing is a sequence of *shift* and *reduce* operations:
- Shift**: move look-ahead token to the stack: e.g.

$$S \mapsto (L) \mid id$$

$$L \mapsto S \mid L , S$$

Stack	Input	Action
	(x, (y, z), w)	shift (
(x, (y, z), w)	shift x

- Reduce**: Replace symbols γ at top of stack with nonterminal X such that $X \mapsto \gamma$ is a production. (pop γ , push X): e.g.

Stack	Input	Action
(x	, (y, z), w)	reduce $S \mapsto id$
(S	, (y, z), w)	reduce $L \mapsto S$

Example Run

Stack	Input	Action
	(x, (y, z), w)	shift (
(x, (y, z), w)	shift x
(x	, (y, z), w)	reduce $S \mapsto \text{id}$
(S	, (y, z), w)	reduce $L \mapsto S$
(L	, (y, z), w)	shift ,
(L,	(y, z), w)	shift (
(L, (y, z), w)	shift y
(L, (y	, z), w)	reduce $S \mapsto \text{id}$
(L, (S	, z), w)	reduce $L \mapsto S$
(L, (L	, z), w)	shift ,
(L, (L,	z), w)	shift z
(L, (L, z), w)	reduce $S \mapsto \text{id}$
(L, (L, S), w)	reduce $L \mapsto L, S$
(L, (L), w)	shift)
(L, (L)	, w)	reduce $S \mapsto (L)$
(L, S	, w)	reduce $L \mapsto L, S$
(L	, w)	shift ,

$S \mapsto (L) \mid \text{id}$
 $L \mapsto S \mid L, S$

Action Selection Problem

- Given a stack σ and a look-ahead symbol b , should the parser:
 - Shift b onto the stack (new stack is σb)
 - Reduce a production $X \mapsto \gamma$, assuming that $\sigma = \alpha\gamma$ (new stack is αX)?
- Sometimes the parser can reduce but shouldn't
 - For example, $X \mapsto \varepsilon$ can *always* be reduced
- Sometimes the stack can be reduced in different ways
- Main idea: decide what to do based on a *prefix* α of the stack plus the look-ahead symbol.
 - The prefix α is different for different possible reductions since in productions $X \mapsto \gamma$ and $Y \mapsto \beta$, γ and β might have different lengths.
- Main goal: know what set of reductions are legal at any point.
 - How do we keep track?

LR(0) States

- An LR(0) *state* is a *set of items* keeping track of progress on possible upcoming reductions.
- An LR(0) *item* is a production from the language with an extra separator “.” somewhere in the right-hand-side

$$\begin{array}{l} S \mapsto (L) \mid id \\ L \mapsto S \mid L , S \end{array}$$

- Example items: $S \mapsto .(L)$ or $S \mapsto (. L)$ or $L \mapsto S.$
- Intuition:
 - Stuff before the ‘.’ is already on the stack (beginnings of possible γ 's to be reduced)
 - Stuff after the ‘.’ is what might be seen next
 - The prefixes α are represented by the state itself

Constructing the DFA: Start state & Closure

- First step: Add a new production $S' \mapsto S\$$ to the grammar
- Start state of the DFA = empty stack, so it contains the item:
 $S' \mapsto .S\$$
- Closure of a state:
 - Adds items for all productions whose LHS nonterminal occurs in an item in the state just after the $'.'$
 - The added items have the $'.'$ located at the beginning (no symbols for those items have been added to the stack yet)
 - Note that newly added items may cause yet more items to be added to the state... keep iterating until a *fixed point* is reached.
- Example: $\text{CLOSURE}(\{S' \mapsto .S\$\}) = \{S' \mapsto .S\$, S \mapsto .(L), S \mapsto .id\}$
- Resulting “closed state” contains the set of all possible productions that might be reduced next.

$$\begin{array}{l} S' \mapsto S\$ \\ S \mapsto (L) \mid id \\ L \mapsto S \mid L , S \end{array}$$

Example: Constructing the DFA

$S' \mapsto .S\$$

$S' \mapsto S\$$

$S \mapsto (L) \mid \text{id}$

$L \mapsto S \mid L , S$

- First, we construct a state with the initial item $S' \mapsto .S\$$

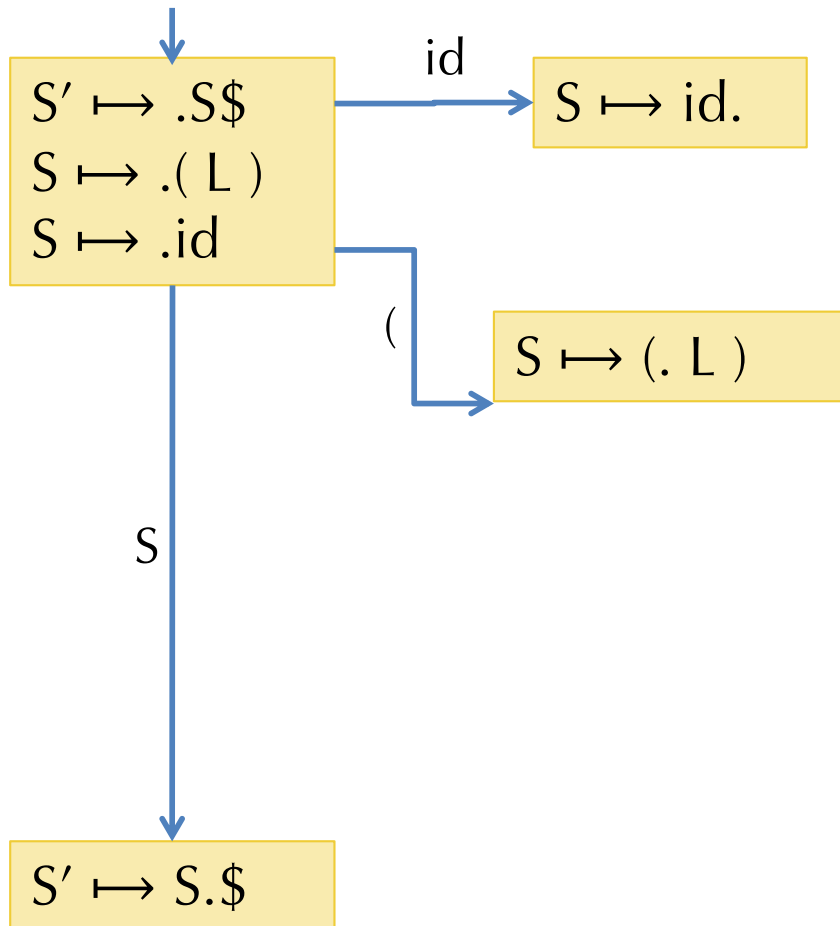
Example: Constructing the DFA

↓
 $S' \mapsto .S\$$
 $S \mapsto .(L)$
 $S \mapsto .id$

$S' \mapsto S\$$
 $S \mapsto (L) \mid id$
 $L \mapsto S \mid L , S$

- Next, we take the closure of that state:
 $\text{CLOSURE}(\{S' \mapsto .S\$\}) = \{S' \mapsto .S\$, S \mapsto .(L), S \mapsto .id\}$
- In the set of items, the nonterminal S appears after the $'.'$
- So we add items for each S production in the grammar

Example: Constructing the DFA



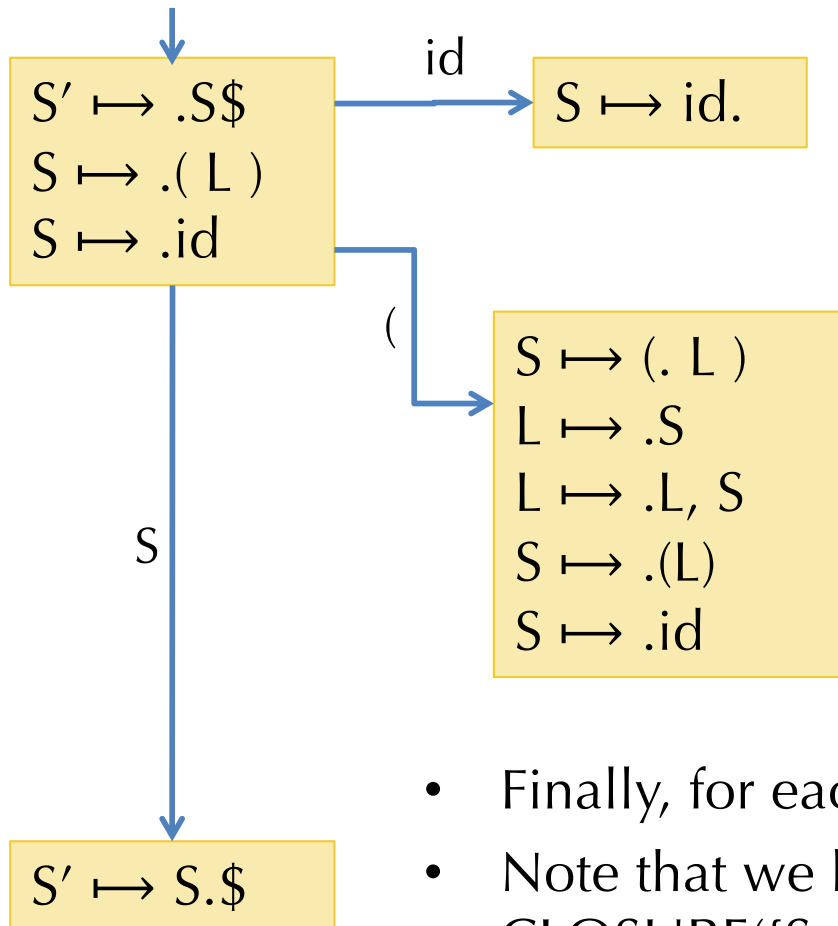
$S' \mapsto S\$$

$S \mapsto (L) \mid id$

$L \mapsto S \mid L , S$

- Next we add the transitions:
- First, we see what terminals and nonterminals can appear after the '.' in the source state.
 - Outgoing edges have those label.
- The target state (initially) includes all items from the source state that have the edge-label symbol after the '.', but we advance the '.' (to simulate shifting the item onto the stack)

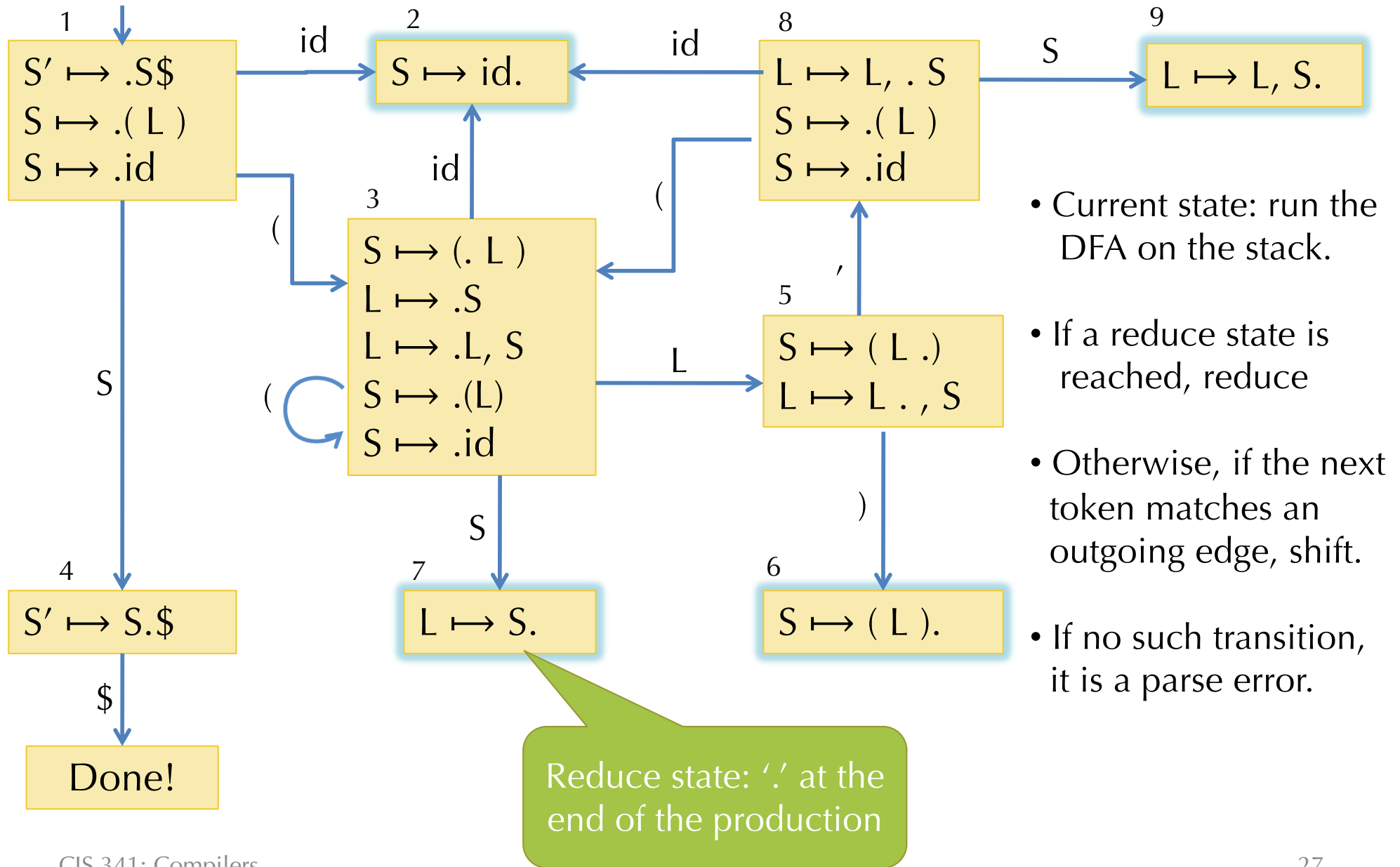
Example: Constructing the DFA



$S' \mapsto S\$$
 $S \mapsto (L) \mid id$
 $L \mapsto S \mid L, S$

- Finally, for each new state, we take the closure.
- Note that we have to perform two iterations to compute $CLOSURE(\{S \mapsto (.L)\})$
 - First iteration adds $L \mapsto .S$ and $L \mapsto .L, S$
 - Second iteration adds $S \mapsto .(L)$ and $S \mapsto .id$

Full DFA for the Example



- Current state: run the DFA on the stack.
- If a reduce state is reached, reduce
- Otherwise, if the next token matches an outgoing edge, shift.
- If no such transition, it is a parse error.

Using the DFA

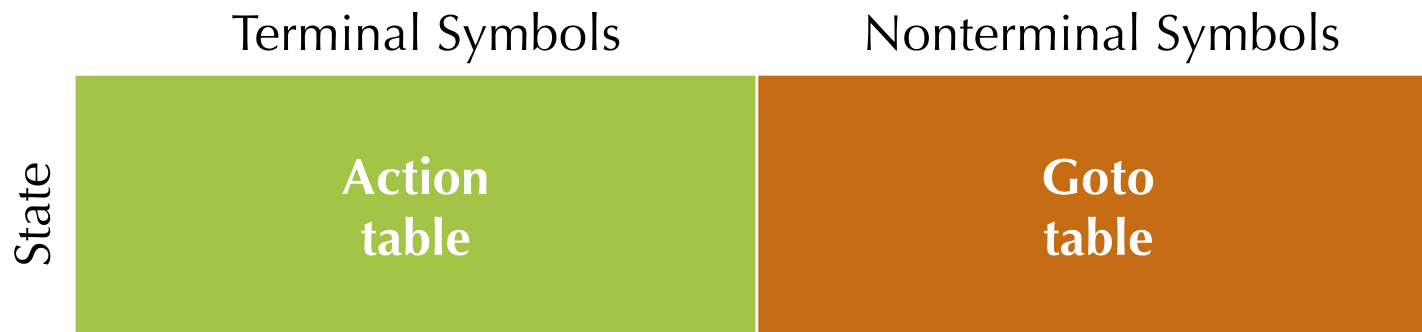
- Run the parser stack through the DFA.
- The resulting state tells us which productions might be reduced next.
 - If not in a reduce state, then shift the next symbol and transition according to DFA.
 - If in a reduce state, $X \mapsto \gamma$ with stack $\alpha\gamma$, pop γ and push X .
- Optimization: No need to re-run the DFA from beginning every step
 - Store the state with each symbol on the stack: e.g. $_1(3(3L_5)_6$
 - On a reduction $X \mapsto \gamma$, pop stack to reveal the state too:
e.g. From stack $_1(3(3L_5)_6$ reduce $S \mapsto (L)$ to reach stack $_1(3$
 - Next, push the reduction symbol: e.g. to reach stack $_1(3S$
 - Then take just one step in the DFA to find next state: $_1(3S_7$

Implementing the Parsing Table

Represent the DFA as a table of shape:

state * (terminals + nonterminals)

- Entries for the “action table” specify two kinds of actions:
 - Shift and goto state n
 - Reduce using reduction $X \mapsto \gamma$
 - First pop γ off the stack to reveal the state
 - Look up X in the “goto table” and goto that state



Example Parse Table

	()	id	,	\$	S	L
1	s3		s2			g4	
2	$S \mapsto id$	$S \mapsto id$	$S \mapsto id$	$S \mapsto id$	$S \mapsto id$		
3	s3		s2			g7	g5
4					DONE		
5		s6		s8			
6	$S \mapsto (L)$	$S \mapsto (L)$	$S \mapsto (L)$	$S \mapsto (L)$	$S \mapsto (L)$		
7	$L \mapsto S$	$L \mapsto S$	$L \mapsto S$	$L \mapsto S$	$L \mapsto S$		
8	s3		s2			g9	
9	$L \mapsto L,S$	$L \mapsto L,S$	$L \mapsto L,S$	$L \mapsto L,S$	$L \mapsto L,S$		

sx = shift and goto state x

gx = goto state x

Example

- Parse the token stream: $(x, (y, z), w)\$$

Stack	Stream	Action (according to table)
ϵ_1	$(x, (y, z), w)\$$	s3
$\epsilon_1(3$	$x, (y, z), w)\$$	s2
$\epsilon_1(3x_2$	$, (y, z), w)\$$	Reduce: $S \mapsto id$
$\epsilon_1(3S$	$, (y, z), w)\$$	g7 (from state 3 follow S)
$\epsilon_1(3S_7$	$, (y, z), w)\$$	Reduce: $L \mapsto S$
$\epsilon_1(3L$	$, (y, z), w)\$$	g5 (from state 3 follow L)
$\epsilon_1(3L_5$	$, (y, z), w)\$$	s8
$\epsilon_1(3L_{5,8}$	$(y, z), w)\$$	s3
$\epsilon_1(3L_{5,8}(3$	$y, z), w)\$$	s2

LR(0) Limitations

- An LR(0) machine only works if states with reduce actions have a *single* reduce action.
 - In such states, the machine *always* reduces (ignoring lookahead)
- With more complex grammars, the DFA construction will yield states with shift/reduce and reduce/reduce conflicts:

OK

$S \mapsto (L).$

shift/reduce

$S \mapsto (L).$
 $L \mapsto .L , S$

reduce/reduce

$S \mapsto L , S.$
 $S \mapsto , S.$

- Such conflicts can often be resolved by using a look-ahead symbol: LR(1)

Examples

- Consider the left associative and right associative “sum” grammars:

left

$$\begin{array}{l} S \mapsto S + E \mid E \\ E \mapsto \text{number} \mid (S) \end{array}$$

right

$$\begin{array}{l} S \mapsto E + S \mid E \\ E \mapsto \text{number} \mid (S) \end{array}$$

- One is LR(0) the other isn't... which is which and why?
- What kind of conflict do you get? Shift/reduce or Reduce/reduce?
- Ambiguities in associativity/precedence usually lead to shift/reduce conflicts.

LR(1) Parsing

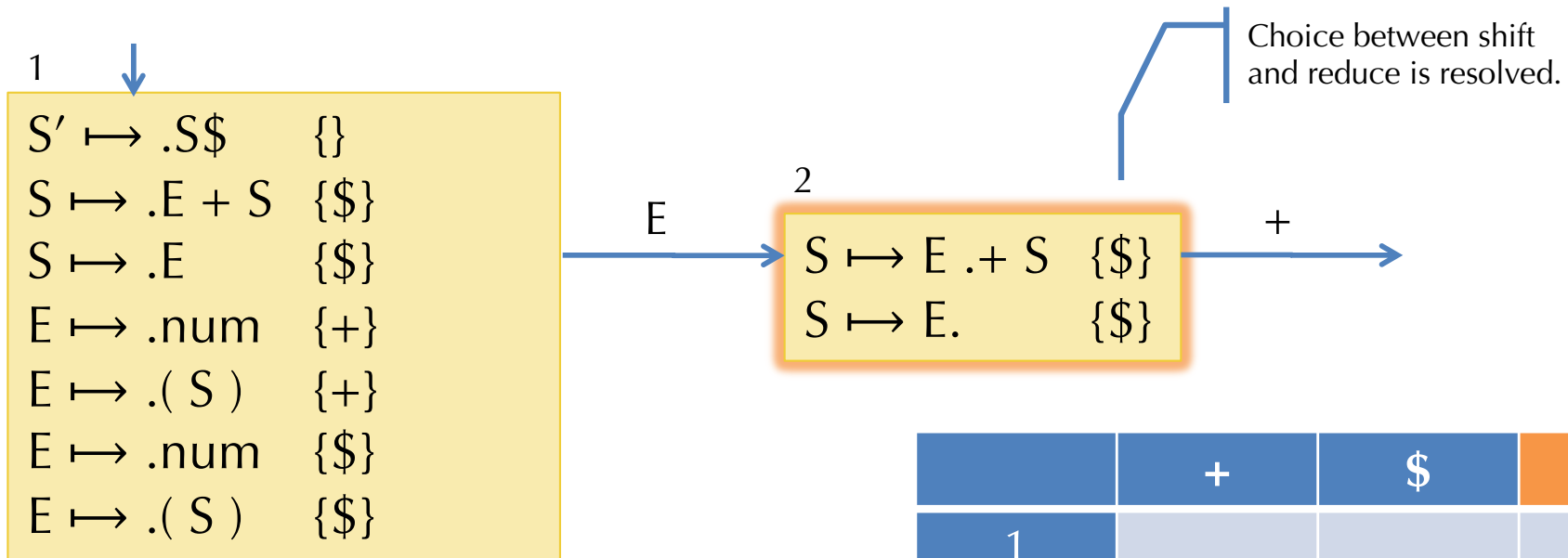
- Algorithm is similar to LR(0) DFA construction:
 - LR(1) state = set of LR(1) items
 - An LR(1) item is an LR(0) item + a set of look-ahead symbols:
 $A \mapsto \alpha.\beta, \mathcal{L}$
- LR(1) closure is a little more complex:
- Form the set of items just as for LR(0) algorithm.
- Whenever a new item $C \mapsto .\gamma$ is added because $A \mapsto \beta.C\delta, \mathcal{L}$ is already in the set, we need to compute its look-ahead set \mathcal{M} :
 1. The look-ahead set \mathcal{M} includes $\text{FIRST}(\delta)$
(the set of terminals that may start strings derived from δ)
 2. If δ is itself ϵ or can derive ϵ (i.e. it is nullable), then the look-ahead \mathcal{M} also contains \mathcal{L}

Example Closure

$$\begin{aligned} S' &\mapsto S\$ \\ S &\mapsto E + S \mid E \\ E &\mapsto \text{number} \mid (S) \end{aligned}$$

- Start item: $S' \mapsto .S\$$, $\{\}$
- Since S is to the right of a '.', add:
 $S \mapsto .E + S$, $\{\$ \}$ Note: $\{\$ \}$ is $\text{FIRST}(\$)$
 $S \mapsto .E$, $\{\$ \}$
- Need to keep closing, since E appears to the right of a '.' in ' $.E + S$ ':
 $E \mapsto .\text{number}$, $\{+\}$ Note: $+$ added for reason 1
 $E \mapsto .(S)$, $\{+\}$ $\text{FIRST}(+ S) = \{+\}$
- Because E also appears to the right of '.' in ' $.E$ ' we get:
 $E \mapsto .\text{number}$, $\{\$ \}$ Note: $\$$ added for reason 2
 $E \mapsto .(S)$, $\{\$ \}$ δ is ϵ
- All items are distinct, so we're done

Using the DFA



	+	\$	E
1			g2
2	s3	$S \mapsto E$	

Fragment of the Action & Goto tables

- The behavior is determined if:
 - There is no overlap among the look-ahead sets for each reduce item, and
 - None of the look-ahead symbols appear to the right of a '.'

LR variants

- LR(1) gives maximal power out of a 1 look-ahead symbol parsing table
 - DFA + stack is a push-down automaton (recall CIS 262)
- In practice, LR(1) tables are big.
 - Modern implementations (e.g. menhir) directly generate code

- LALR(1) = “Look-ahead LR”

- Merge any two LR(1) states whose items are identical except for the look-ahead sets:

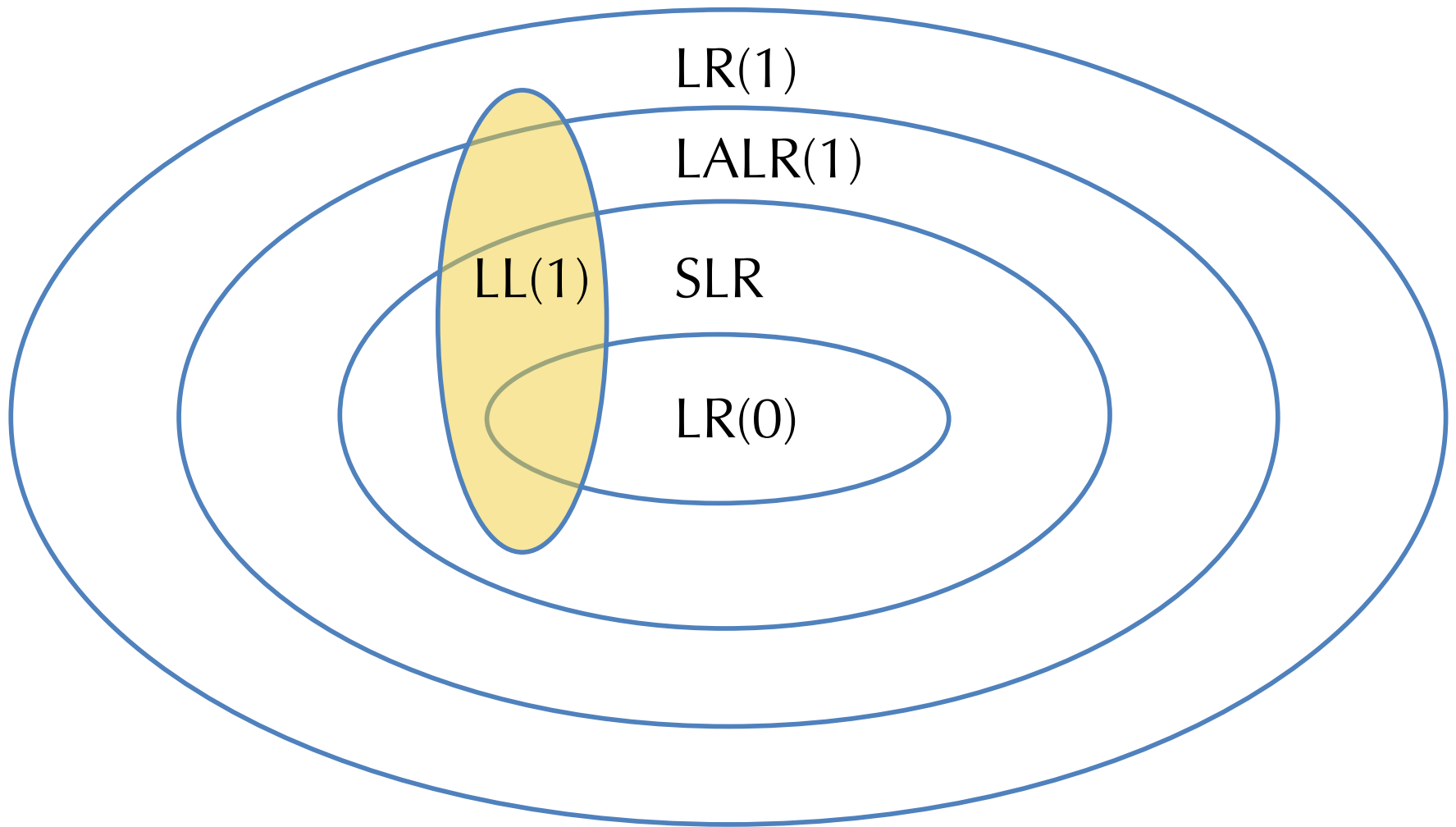
$S' \mapsto .S\$$	$\{\}$
$S \mapsto .E + S$	$\{\$ \}$
$S \mapsto .E$	$\{\$ \}$
$E \mapsto .num$	$\{+ \}$
$E \mapsto . (S)$	$\{+ \}$
$E \mapsto .num$	$\{\$ \}$
$E \mapsto . (S)$	$\{\$ \}$

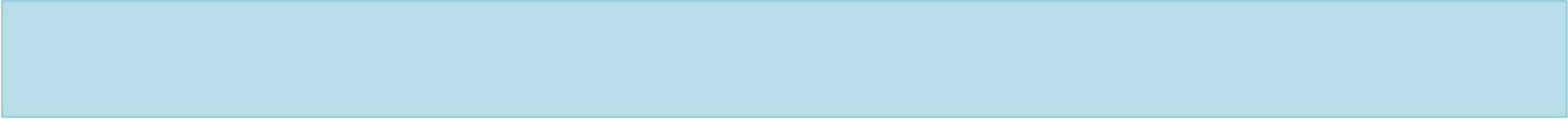


$S' \mapsto .S\$$	$\{\}$
$S \mapsto .E + S$	$\{\$ \}$
$S \mapsto .E$	$\{\$ \}$
$E \mapsto .num$	$\{+, \$ \}$
$E \mapsto . (S)$	$\{+, \$ \}$

- Such merging can lead to nondeterminism (e.g. reduce/reduce conflicts), but
 - Results in a much smaller parse table and works well in practice
 - This is the usual technology for automatic parser generators: yacc, ocamllyacc
- GLR = “Generalized LR” parsing
 - Efficiently compute the set of *all* parses for a given input
 - Later passes should disambiguate based on other context

Classification of Grammars





Debugging parser conflicts.
Disambiguating grammars.

MENHIR IN PRACTICE

Practical Issues

- Dealing with source file location information
 - In the lexer and parser
 - In the abstract syntax
 - See range.ml, ast.ml
- Lexing comments / strings

Menhir output

- You can get verbose ocaml yacc debugging information by doing:
 - `menhir --explain ...`
 - or, if using dune, adding this stanza:

```
(menhir  
  (modules parser)  
  (flags --explain))
```
- The result is a `<basename>.conflicts` file that contains a description of the error
 - The parser items of each state use the `'.'` just as described above
- The flag `--dump` generates a full description of the automaton
- Example: see `start-parser.mly`

Precedence and Associativity Declarations

- Parser generators, like menhir often support precedence and associativity declarations.
 - Hints to the parser about how to resolve conflicts.
 - See: `good-parser.mly`
- Pros:
 - Avoids having to manually resolve those ambiguities by manually introducing extra nonterminals (as seen in `parser.mly`)
 - Easier to maintain the grammar
- Cons:
 - Can't as easily re-use the same terminal (if associativity differs)
 - Introduces another level of debugging
- Limits:
 - Not always easy to disambiguate the grammar based on just precedence and associativity.

Example Ambiguity in Real Languages

- Consider this grammar:

$S \mapsto \text{if } (E) S$

$S \mapsto \text{if } (E) S \text{ else } S$

$S \mapsto X = E$

$E \mapsto \dots$

- Is this grammar OK?

- Consider how to parse:

$\text{if } (E_1) \text{ if } (E_2) S_1$
 $\text{else } S_2$

- This is known as the “dangling else” problem.
- What should the “right” answer be?
- How do we change the grammar?

How to Disambiguate if-then-else

- Want to rule out:

$$\text{if } (E_1) \left\{ \text{if } (E_2) S_1 \right\} \text{ else } S_2$$

- Observation: An un-matched 'if' should not appear as the 'then' clause of a containing 'if'.

$S \mapsto M \mid U$	// M = "matched", U = "unmatched"
$U \mapsto \text{if } (E) S$	// Unmatched 'if'
$U \mapsto \text{if } (E) M \text{ else } U$	// Nested if is matched
$M \mapsto \text{if } (E) M \text{ else } M$	// Matched 'if'
$M \mapsto X = E$	// Other statements

- See: `else-resolved-parser.mly`

Alternative: Use { }

- Ambiguity arises because the 'then' branch is not well bracketed:

```
if (E1) { if (E2) { S1 } } else S2      // unambiguous
if (E1) { if (E2) { S1 } else S2 }      // unambiguous
```

- So: could just require brackets
 - But requiring them for the else clause too leads to ugly code for chained if-statements:

```
if (c1) {
  ...
} else {
  if (c2) {

  } else {
    if (c3) {

    } else {

    }
  }
}
```

So, compromise? Allow unbracketed else block only if the body is 'if':

```
if (c1) {
} else if (c2) {

} else if (c3) {

} else {

}
```

Benefits:

- Less ambiguous
- Easy to parse
- Enforces good style