# CIS 500 Software Foundations Fall 2006

September 11

Administrivia

### Recitations

Recitations start this week.

Thursday, 10:30-12:00Location TBAReviewFriday, 10:30-12:00Location TBAAdvanced



Anybody still want help forming a group?

# Homework 2

Homework 1 was due at noon today. Homework 2 will be available by this evening and will be due next Monday at noon.

Read Chapter 6 of Jason Hickey's "Introduction to the Objective Caml Programming Language" before starting

# Class mailing list

If you have not been receiving messages for the class, please send me an email and I will add you.

### Questions from last time...

Are there any?

# On With OCaml...

Recursive functions on lists tend to have a standard shape: we test whether the list is empty, and if it is not we do something involving the head element and the tail.

```
# let rec listSum (l:int list) =
    if l = [] then 0
    else List.hd l + listSum (List.tl l);;
```

OCaml provides a convenient *pattern-matching* construct that bundles the emptiness test and the extraction of the head and tail into a single syntactic form:

```
# let rec listSum (l: int list) =
    match l with
    [] -> 0
    | x::y -> x + listSum y;;
```

Pattern matching can be used with types other than lists. For example, here it is used on integers:

```
# let rec fact (n:int) =
    match n with
        0 -> 1
        | _ -> n * fact(n-1);;
```

The \_ pattern here is a *wildcard* that matches any value.

The basic elements (constants, variable binders, wildcards, [], ::, etc.) may be combined in arbitrarily complex ways in match expressions:

```
# let silly 1 =
   match 1 with
     [_;_;_] -> "three elements long"
    | _::x::y::_::rest ->
        if x>y then "foo" else "bar"
    _ -> "dunno";;
val silly : int list -> string = <fun>
# silly [1;2;3];;
- : string = "three elements long"
# silly [1;2;3;4];;
- : string = "dunno"
# silly [1;2;3;4;5];;
- : string = "bar"
```

# Type Inference

One pleasant feature of OCaml is a powerful *type inference* mechanism that allows the compiler to calculate the types of variables from the way in which they are used.

```
# let rec fact n =
    match n with
        0 -> 1
        | _ -> n * fact(n-1);;
val fact : int -> int = <fun>
```

The compiler can tell that fact takes an integer argument because n is used as an argument to the integer \* and - functions.

Similarly:

```
# let rec listSum l =
    match l with
    [] -> 0
    | x::y -> x + listSum y;;
val listSum : int list -> int = <fun>
```

# Polymorphism (first taste)

```
# let rec length l =
    match l with
    [] -> 0
    | _::y -> 1 + length y;;
val length : 'a list -> int = <fun>
```

The 'a in the type of length, pronounced "alpha," is a *type variable* standing for an arbitrary type.

The inferred type tells us that the function can take a list with elements of *any* type (i.e., a list with elements of type alpha, for any choice of alpha).

We'll come back to polymorphism in more detail a bit later.

### **Tuples**

Items connected by commas are "tuples." (The enclosing parens are optional.)

```
# "age", 44;;
- : string * int = "age", 44
# "professor", "age", 33;;
 : string * string * int = "professor", "age", 33
# ("children", ["bob";"ted";"alice"]);;
- : string * string list =
        "children", ["bob"; "ted"; "alice"]
# let g (x,y) = x*y;;
val g : int * int -> int = <fun>
```

How many arguments does g take?

Please do not confuse them!

```
# List.hd tuple;;
This expression has type string * string * string
but is here used with type 'a list
```

```
# let tup2 = 1, "cow";;
val tup2 : int * string = 1, "cow"
# let l2 = [1; "cow"];;
This expression has type string but is here
used with type int
```

# Tuples and pattern matching

Tuples can be "deconstructed" by pattern matching:

```
# let lastName name =
    match name with
        (n,_,_) -> n;;
# lastName ("Pierce", "Benjamin", "Penn");;
- : string = "Pierce"
```

# Example: Finding words

Suppose we want to take a list of characters and return a list of lists of characters, where each element of the final list is a "word" from the original list.

(Character constants are written with single quotes.)

# An implementation of split

```
# let rec loop w l =
    match 1 with
       [] -> [w]
    | (' '::ls) -> w :: (loop [] ls)
    | (c::ls) -> loop (w @ [c]) ls;;
val loop : char list
        -> char list
        -> char list list
         = \langle f_{11} n \rangle
# let split l = loop [] l;;
val split : char list -> char list list = <fun>
```

Note the use of both tuple patterns and nested patterns. The @ operator is shorthand for List.append.

# Aside: Local function definitions

The loop function is completely local to split: there is no reason for anybody else to use it — or even for anybody else to be able to see it! It is good style in OCaml to write such definitions as *local bindings*:

```
# let split l =
    let rec loop w l =
    match l with
    [] -> [w]
    | (' '::ls) -> w :: (loop [] ls)
    | (c::ls) -> loop (w @ [c]) ls in
    loop [] l;;
```

In general, any let definition that can appear at the top level

```
# let ...;;
# e;;;
```

can also appear in a let...in... form.

# let ... in e;;;

# A Better Split

Our split function worked fine for the example we tried it on. But here are some other tests:

```
# split ['a';' ';' ';'b'];;
- : char list list = [['a']; []; ['b']]
# split ['a';' '];;
- : char list list = [['a']; []]
```

Could we refine split so that it would leave out these spurious empty lists in the result?

Sure. First rewrite the pattern match a little (without changing its behavior):

```
# let split l =
    let rec loop w l =
    match w,l with
    _, [] -> [w]
    | _, (' '::ls) -> w :: (loop [] ls)
    | _, (c::ls) -> loop (w @ [c]) ls in
    loop [] l;;
```

Then add a couple of clauses:

```
# let better_split 1 =
    let rec loop w l =
      match w,l with
        [], [] -> []
      |_,[] -> [w]
      | [], (' '::ls) -> loop [] ls
      | _, (' '::ls) -> w :: (loop [] ls)
      | _, (c::ls) -> loop (w @ [c]) ls in
    loop [] l;;
# better_split ['a';'b';' ';' ';'c';' ';'d';' '];;
- : char list list = [['a'; 'b']; ['c']; ['d']]
# better_split ['a';' '];;
- : char list list = [['a']]
# better_split [' ';' '];;
- : char list list = []
```

OCaml's exception mechanism is roughly similar to that found in, for example, Java.

We begin by defining an exception:

```
# exception Bad;;
```

Now, encountering raise Bad will immediately terminate evaluation and return control to the top level:

```
# let rec fact n =
    if n<0 then raise Bad
    else if n=0 then 1
    else n * fact(n-1);;
# fact (-3);;
Exception: Bad.</pre>
```

# (Not) catching exceptions

Naturally, exceptions can also be caught within a program (using the try...with... form), but let's leave that for another day.

# Defining New Types of Data

# Predefined types

We have seen a number of data types:

int
bool
string
char
[x;y;z] lists
(x,y,z) tuples

Ocaml has a number of other built-in data types — in particular, float, with operations like +., \*., etc.

One can also create completely new data types.

# The need for new types

The ability to construct new types is an essential part of most programming languages.

For example, suppose we are building a (very simple) graphics program that displays circles and squares. We can represent each of these with three real numbers...

A circle is represented by the co-ordinates of its center and its radius. A square is represented by the co-ordinates of its bottom left corner and its width. So we can represent *both* shapes as elements of the type:

float \* float \* float

However, there are two problems with using this type to represent circles and squares. First, it is a bit long and unwieldy, both to write and to read. Second, because their types are identical, there is nothing to prevent us from mixing circles and squares. For example, if we write

# let areaOfSquare (\_,\_,d) = d \*. d;;

we might accidentally apply the areaOfSquare function to a circle and get a nonsensical result.

(Recall that numerical operations on the float type are written differently from the corresponding operations on int — e.g., +. instead of +. See the OCaml manual for more information.)

# Data Types

We can improve matters by defining square as a new type:

# type square = Square of float \* float \* float;;

This does two things:

- It creates a *new* type called square that is different from any other type in the system.
- It creates a constructor called Square (with a capital S) that can be used to create a square from three floats. For example:

```
# Square(1.1, 2.2, 3.3);;
```

- : square = Square (1.1, 2.2, 3.3)

# Taking data types apart

We take types apart with (surprise, surprise...) pattern matching.

```
# let areaOfSquare s =
    match s with
        Square(_, _, d) -> d *. d;;
val areaOfSquare : square -> float = <fun>
# let bottomLeftCoords s =
    match s with
        Square(x, y, _) -> (x,y);;
val bottomLeftCoords : square -> float * float
        = <fun>
```

So we can use constructors like Square both as *functions* and as *patterns*.

These functions can be written a little more concisely by combining the pattern matching with the function header:

# let areaOfSquare (Square(\_, \_, d)) = d \*. d;; # let bottomLeftCoords (Square(x, y, \_)) = (x,y);;

```
Continuing, we can define a data type for circles in the same way.
# type circle = Circle of float * float * float;;
# let c = Circle (1.0, 2.0, 2.0);;
# let areaOfCircle (Circle(_, _, r)) =
     3.14159 *. r *. r;;
# let centerCoords (Circle(x, y, _)) = (x,y);;
# areaOfCircle c;;
 - : float = 12.56636
```

We *cannot* now apply a function intended for type square to a value of type circle:

```
# areaOfSquare c;;
This expression has type circle but is here used
with type square.
```

Going back to the idea of a graphics program, we obviously want to have several shapes on the screen at once. For this we'd probably want to keep a list of circles and squares, but such a list would be *heterogenous*. How do we make such a list?

Answer: Define a type that can be *either* a circle *or* a square.

#	type	shape	=	Circle	of	float	*	float	*	float
				Square	of	float	*	float	*	float;;

Now *both* constructors Circle and Square create values of type shape. For example:

```
# Square (1.0, 2.0, 3.0);;
```

```
- : shape = Square (1.0, 2.0, 3.0)
```

A type that can have more than one form is often called a *variant* type.

### Pattern matching on variants

We can also write functions that do the right thing on all forms of a variant type. Again we use pattern matching:

```
# let area s =
    match s with
    Circle (_, _, r) -> 3.14159 *. r *. r
    | Square (_, _, d) -> d *. d;;
# area (Circle (0.0, 0.0, 1.5));;
- : float = 7.0685775
```

Here is a heterogeneous list:

```
# let l = [Circle (0.0, 0.0, 1.5);
    Square (1.0, 2.0, 1.0);
    Circle (2.0, 0.0, 1.5);
    Circle (5.0, 0.0, 2.5)];;
```

```
# area (List.hd l);;
```

- : float = 7.0685775

### Mixed-mode Arithmetic

Many programming languages (Lisp, Basic, Perl, database query languages) use variant types internally to represent numbers that can be either integers or floats. This amounts to *tagging* each numeric value with an indicator that says what kind of number it is.

```
# type num = Int of int | Float of float;;
 let add r1 r2 =
#
    match (r1,r2) with
      (Int i1, Int i2) -> Int (i1 + i2)
    | (Float r1, Int i2) -> Float (r1 +. float i2)
    | (Int i1, Float r2) -> Float (float i1 +. r2)
    | (Float r1, Float r2) \rightarrow Float (r1 +. r2);;
  add (Int 3) (Float 4.5);;
    num = Float 7.5
```

### More Mixed-Mode Functions

```
# let unaryMinus n =
    match n with Int i -> Int (- i)
               | Float r -> Float (-. r);;
# let minus n1 n2 = add n1 (unaryMinus n2);;
 let rec fact n =
#
    if n = Int 0 then Int 1
    else mult n (fact (minus n (Int 1)));;
# fact (Int 7);;
  : num = Int 5040
```

What will happen if we write fact 7?

# A Data Type for Optional Values

Suppose we are implementing a simple lookup function for a telephone directory. We want to give it a string and get back a number (say an integer). We expect to have a function lookup whose type is

lookup: string -> directory -> int

where directory is a (yet to be decided) type that we'll use to represent the directory.

However, this isn't quite enough. What happens if a given string isn't in the directory? What should lookup return?

There are several ways to deal with this issue. One is to raise an exception. Another uses the following data type:

# type optional\_int = Absent | Present of int;;

To see how this type is used, let's represent our directory as a list of pairs:

```
# let directory = [("Joe", 1234); ("Martha", 5672);
                     ("Jane", 3456); ("Ed", 7623)]::
# let rec lookup s l =
    match 1 with
      [] -> Absent
    | (k,i)::t \rightarrow if k = s then Present(i)
                            else lookup s t;;
# lookup "Jane" directory;;
 : optional_int = Present 3456
# lookup "Karen" directory;;
 : optional_int = Absent
```

Because options are often useful in functional programming, OCaml provides a built-in type t option for each type t. Its constructors are None (corresponding to Absent) and Some (for Present).

# Enumerations

The option type has one variant, None, that is a "constant" constructor carrying no data values with it. Data types in which *all* the variants are constants can actually be quite useful...

# A Boolean Data Type

A simple data type can be used to replace the built-in booleans. We use the constant constructors True and False to represent *true* and *false*. We'll use different names as needed to avoid confusion between our booleans and the built-in ones:

```
# type myBool = False | True;;
# let myNot b =
    match b with False -> True | True -> False;;
# let myAnd b1 b2 =
    match (b1,b2) with
    (True, True) -> True
    | (True, False) -> False
    | (False, True) -> False
    | (False, False) -> False;;
```

Note that the behavior of myAnd is not quite the same as the built-in &&!

# **Recursive Types**

Consider the tiny language of arithmetic expressions defined by the following (BNF-like) grammar:

exp ::= number ( exp + exp ) ( exp - exp ) ( exp \* exp )

(We'll come back to these grammars in more detail next week...)

We can translate this grammar directly into a datatype definition:

```
type ast =
    ANum of int
    APlus of ast * ast
    AMinus of ast * ast
    ATimes of ast * ast;;
```

Notes:

- ► This datatype (like the original grammar) is *recursive*.
- The type ast represents abstract syntax trees, which capture the underlying tree structure of expressions, suppressing surface details such as parentheses

### An evaluator for expressions

Goal: write an evaluator for these expressions.

```
val eval : ast -> int = <fun>
# eval (ATimes (APlus (ANum 12, ANum 340), ANum 5));
- : int = 1760
```

The solution uses a recursive function plus a pattern match.

```
let rec eval e =
match e with
ANum i -> i
| APlus (e1,e2) -> eval e1 + eval e2
| AMinus (e1,e2) -> eval e1 - eval e2
| ATimes (e1,e2) -> eval e1 * eval e2;;
```