All machine learning is optimization

\[ \hat{y} = f(x; \theta) \]

\[ \arg\min_\theta \| y - \hat{y} \| \]

So what’s new?

(Slightly) different loss functions
(Slightly) different optimization methods
CPU/GPU; SAAS/full stack
Different, flexible, functional forms for \( f \)
which require regularization
Loss functions

\[ \hat{y} = f(x; \theta) \]

\[ \text{argmin}_\theta ||y - \hat{y}|| \]

\[ ||y - \hat{y}||_2 \quad ||y - \hat{y}||_1 \quad ||y - \hat{y}||_0 \]

log-likelihood
logistic/softmax
hinge
exponential
Flexible model forms

\[ \hat{y} = f(x; \theta) \]

\begin{align*}
X & \quad y \\
Web page, ad & \quad \text{Click on ad?} \\
Past purchases & \quad \text{NPV} \\
Facebook posts & \quad \text{Age, Sex, Personality, ...}
\end{align*}
Flexible model forms

\[ X \rightarrow y \]

biopsy image  Cancer present?
Flexible model forms

X
Camera image

y
Objects in it
<table>
<thead>
<tr>
<th>X</th>
<th>y</th>
</tr>
</thead>
<tbody>
<tr>
<td>English sentence</td>
<td>Translation</td>
</tr>
<tr>
<td>I love machine learning</td>
<td>'uhibb taelam alala</td>
</tr>
</tbody>
</table>
Neural Networks: Deep Learning
Deep learning is taking over

- **Machine vision**
  - Face/Object/Scene recognition
  - Self driving cars

- **Speech recognition (“speech to text”)**
  - Siri, Alexa …

- **Machine translation**
  - Google translate
Artificial Neural Nets

- **Semi-parametric**
  - Flexible model form

- **Used when there are vast amounts of data**
  - Hence popular (again) now
  - But recently with smaller training sets.

- **Deep networks**
  - Idea: representation should have *many* different levels of abstraction
Neural Nets can be

- **Supervised**
  - Generalizes *logistic regression* to a semi-parametric form
- **Unsupervised**
  - Generalizes *PCA* to a semi-parametric form
- **Semi-supervised**
- **Reinforcement**
- **Adversarial**

*Neural nets often have built in structure*
“Real” and Artificial neuron

One neuron does logistic regression

\[ h_{w,b}(x) = f(w^T x + b) \]

\[ f(z) = \frac{1}{1 + e^{-z}} \]
Neural nets stack logistic regressions

Every line represents a parameter in the model
Neural nets stack logistic regressions

Every line represents a parameter in the model
Training

- Mini-batch gradient descent
- “Backpropagate” error derivatives through the model = chain rule
ANNs do pattern recognition

- Map input “percepts” to output categories or actions
  - Image of an object → what it is
  - Image of a person → who it is
  - Picture → caption describing it
  - Board position → probability of winning
  - A word → the sound of saying it
  - Sound of a word → the word
  - Sequence of words in English → their Chinese translation
## MNIST

- Classify 28x28 images of handwritten digits
- **Train:** 50,000
- **Test:** 10,000

<table>
<thead>
<tr>
<th>Error (%)</th>
<th>Method</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>5.0</td>
<td>KNN</td>
<td>Lecun et al. (1998)</td>
</tr>
<tr>
<td>3.6</td>
<td>1k RBF + linear classifier</td>
<td>Lecun et al. (1998)</td>
</tr>
<tr>
<td>1.6</td>
<td>2-layer NN</td>
<td>Simard et al. (2003)</td>
</tr>
<tr>
<td>1.53</td>
<td>boosted stumps</td>
<td>Kegl et al. (2009)</td>
</tr>
<tr>
<td>1.4</td>
<td>SVM</td>
<td>Lecun et al. (1998)</td>
</tr>
<tr>
<td>0.79</td>
<td>DNN</td>
<td>Srivastava (2013)</td>
</tr>
<tr>
<td>0.45</td>
<td>conv-DNN</td>
<td>Goodfellow et al. (2013)</td>
</tr>
<tr>
<td>0.21</td>
<td>conv-DNN</td>
<td>Wi et al. (2013)</td>
</tr>
</tbody>
</table>
Street View House Numbers

- Classify 32x32 color images of digits
- Digits taken from house numbers in Google Street View
- **Train**: 604,388
- **Test**: 26,032

<table>
<thead>
<tr>
<th>Error (%)</th>
<th>Method</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>36.7</td>
<td>WDCH</td>
<td>Netzer et al. (2011)</td>
</tr>
<tr>
<td>15</td>
<td>HOG</td>
<td>Netzer et al. (2011)</td>
</tr>
<tr>
<td>9.4</td>
<td>KNN</td>
<td>Netzer et al. (2011)</td>
</tr>
<tr>
<td>2.47</td>
<td>conv-DNN</td>
<td>Goodfellow et al. (2013)</td>
</tr>
<tr>
<td>2</td>
<td>Human</td>
<td>Netzer et al. (2013)</td>
</tr>
<tr>
<td>1.92</td>
<td>conv-DNN</td>
<td>Lee et al. (2015)</td>
</tr>
</tbody>
</table>
## CIFAR-100

- Classify 32x32 color images into 100 classes
- Images taken from TinyImages dataset at MIT
- **Train:** 50,000
- **Test:** 10,000

<table>
<thead>
<tr>
<th>Error (%)</th>
<th>Method</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>43.77</td>
<td>SVM</td>
<td>Jia et al. (2012)</td>
</tr>
<tr>
<td>39.20</td>
<td>OMP</td>
<td>Lin and Kung (2014)</td>
</tr>
<tr>
<td>38.57</td>
<td>conv-DNN</td>
<td>Goodfellow et al. (2013)</td>
</tr>
<tr>
<td>36.18</td>
<td>DNN</td>
<td>Srivastava and Alakhudtinov (2015)</td>
</tr>
<tr>
<td>34.57</td>
<td>conv-DNN</td>
<td>Lee et al. (2015)</td>
</tr>
</tbody>
</table>
ImageNet Classification with Deep Convolutional Neural Networks

Alex Krizhevsky
Ilya Sutskever
Geoffrey Hinton

University of Toronto
Canada

“AlexNet” 2012
Neural networks

- A neuron

A neuron computes a simple differentiable function of its input, represented as:

\[ x = w_1 f(z_1) + w_2 f(z_2) + w_3 f(z_3) \]

where

- \( x \) is the total input to the neuron,
- \( f(x) \) is the output of the neuron,
- \( z_1, z_2, z_3 \) are intermediate calculations,
- \( w_1, w_2, w_3 \) are weights.

- A neural network

A neural network computes a differentiable function of its input. For example, ours computes:

\[ p(\text{label} | \text{an input image}) \]
Neurons

Traditional: sigmoidal e.g. logistic function
\[ f(x) = \tanh(x) \]

Hyperbolic tangent
Very bad (slow to train)

But one can use any nonlinear function
\[ f(x) = \max(0, x) \]

Rectified Linear Unit (ReLU)
Very good (quick to train)

\[ x = w_1 f(z_1) + w_2 f(z_2) + w_3 f(z_3) \]
\[ x \text{ is called the total input to the neuron, and } f(x) \text{ is its output} \]
Overview of our model

- **Deep**: 7 hidden “weight” layers
- **Learned**: all feature extractors initialized at white Gaussian noise and learned from the data
- Entirely supervised
- More data = good

**Convolutional layer**: convolves its input with a bank of 3D filters, then applies point-wise non-linearity

**Fully-connected layer**: applies linear filters to its input, then applies point-wise non-linearity
Local receptive fields

In vision, a neuron may only get inputs from a limited set of “nearby” neurons.
Local receptive fields

- spatial extent $F = 3$
- stride $S = 1$

- spatial extent $F = 3$
- stride $S = 2$

http://cs231n.github.io/convolutional-networks/
Local receptive fields

Input Volume (+pad 1) (7x7x3)  Filter W0 (3x3x3)  Filter W1 (3x3x3)  Output Volume (3x3x2)

http://cs231n.github.io/convolutional-networks/
Local pooling

**Max-pooling** partitions the input image into local regions and outputs the maximum value for each.

Reduces the computational complexity
Provides translation invariance.
Max pooling

- **Spatial extent** $F=2$
- **Stride** $S=2$

http://cs231n.github.io/convolutional-networks/
Our model

- Max-pooling layers follow first, second, and fifth convolutional layers
- The number of neurons in each layer is given by 253440, 186624, 64896, 64896, 43264, 4096, 4096, 1000
Overview of our model

- Trained with stochastic gradient descent on two NVIDIA GPUs for about a week
- 650,000 neurons
- 60,000,000 parameters
- 630,000,000 connections
- **Final feature layer**: 4096-dimensional

**Convolutional layer**: convolves its input with a bank of 3D filters, then applies point-wise non-linearity

**Fully-connected layer**: applies linear filters to its input, then applies point-wise non-linearity
Using stochastic gradient descent and the *backpropagation algorithm* (just repeated application of the chain rule)

One output unit per class

\[ x_i = \text{total input to output unit } i \]

\[ f(x_i) = \frac{\exp(x_i)}{\sum_{j=1}^{1000} \exp(x_j)} \]

We maximize the log-probability of the correct label, \( \log f(x_t) \)
Data augmentation

- Our neural net has 60M real-valued parameters and 650,000 neurons
- It overfits a lot. Therefore we train on 224x224 patches extracted randomly from 256x256 images, and also their horizontal reflections.
Validation classification
Validation classification

- lens cap
- abacus
- slug
- hen
- reflex camera
- typewriter keyboard
- slug
- hen
- Polaroid camera
- space bar
- zucchini
- cock
- pencil sharpener
- computer keyboard
- ground beetle
- cocker spaniel
- switch
- accordion
- common newt
- partridge
- combination lock
- water snake
- English setter
- tiger
- chambered nautilus
- tape player
- planetarium
- tiger
- lampshade
- cellular telephone
- planetarium
- tiger cat
- throne
- slot
- dome
- tabby
- goblet
- mosque
- boxer
- table lamp
- radio telescope
- Saint Bernard
- hamper
- dial telephone
- steel arch bridge
Validation localizations
Retrieval experiments
First column contains query images from ILSVRC-2010 test set, remaining columns contain retrieved images from training set.
Now used for image search; Benefit: Good Generalization

Both recognized as “meal”

Jeff Dean, google
Sensible Errors (sometimes)

“snake”

“dog”

Jeff Dean, google
Now used for image search

Works in practice… for real users

Wow.
The new Google plus photo search is a bit insane.
I didn’t tag those...)
Now used for image search

Works in practice… for real users

Google Plus photo search is awesome. Searched with keyword 'Drawing' to find all my scribbles at once :D

Jeff Dean, google
Modern deep nets

- Often use rectified linear units (ReLUs)
  - Less problems of saturation than logistic
- Use a variety of loss functions
  - Log likelihood (uses softmax)
- Can be very deep
- Solved with mini-batch gradient descent
- Regularized using $L_2$ penalty plus “dropout”
  - and partial convergence and ..

\[
\sigma(z)_j = \frac{e^{z_j}}{\sum_{k=1}^{K} e^{z_k}} \quad \text{for } j = 1, \ldots, K.
\]
Regularization

![Diagram showing accuracy over epochs with different levels of overfitting.](http://cs231n.github.io/neural-networks-3/)
Regularization

- $L_2$
- Max norm ($L_\infty$)
- Early stopping
- Dropout
Dropout

- Randomly (temporarily) remove a fraction $p$ of the nodes (with replacement)
  - Usually $p = 1/2$
- Repeatedly doing this samples (in theory) over exponentially many networks
  - Bounces the network out of local minima
- For the final network use all the weights but shrink them by $p$
Gradient descent

- **Gradient descent**
  - stochastic
  - gradient clipping
- **Minibatch**
- **Momentum**
- **Learning rate adaptation**
  - See the wiki

\[
\frac{\delta \text{Err}}{\delta w} = \frac{\text{Err}(w+h) - \text{Err}(w-h)}{2h}
\]

\[
\Delta w^t = \eta \frac{\delta \text{Err}}{\delta w} + m \Delta w^{t-1}
\]
Learning rate

Learning rate adaption

- Adjust the learning rate over time

\[ \Delta w^t = \eta(t) \frac{\delta Err}{\delta w} \]

- Adagrad: make the learning rate depend on previous changes in each weight
  - increases the learning rate for more sparse parameters and decreases the learning rate for less sparse ones.

\[ \Delta w^t_j = \frac{\eta}{||\delta w^t_j||_2} \frac{\delta Err}{\delta w_j} \]
Semi-supervised learning

- How do you learn a model with only a few hundred labeled examples?
New AI can guess whether you're gay or straight from a photograph

An algorithm deduced the sexuality of people on a dating site with up to 91% accuracy, raising tricky ethical questions
Deep neural networks are more accurate than humans at detecting sexual orientation from facial images.

Michal Kosinski & Yilun Wang

We show that faces contain much more information about sexual orientation than can be perceived and interpreted by the human brain. We used deep neural networks to extract features from 35,326 facial images. These features were entered into a logistic regression aimed at classifying sexual orientation. Given a single facial image, a classifier could correctly distinguish between gay and heterosexual men in 81% of cases, and in 74% of cases for women. Human judges achieved much lower accuracy: 61% for men and 54% for women. The accuracy of the algorithm increased to 91% and 83%, respectively, given five facial images per person. Facial features employed by the classifier included both fixed (e.g., nose shape) and transient facial features (e.g., grooming style). Consistent with the prenatal hormone theory of sexual orientation, gay men and women tended to have gender-atypical facial morphology, expression, and grooming styles. .... Additionally, given that companies and governments are increasingly using computer vision algorithms to detect people’s intimate traits, our findings expose a threat to the privacy and safety of gay men and women.

https://osf.io/fk3xr/ 2017
Deep learning case study

- Download images and labels from a dating site where people declare their sexual orientation
  - Only keep images with a single “good” face
    - Use Face++ to identify faces -- yielded 35,000 faces
- Use M-turkers to QC & restrict to Caucasians
- Use pretrained CNN to compute ~ 4,000 ‘scores’/image
  - VGG-Face was trained on 2.6 million faces
- Use logistic regression on SVD of the 4,000 scores
  - report cross-validation error predicting gay/straight
What you should know

- CNN
  - local receptive field
- Rectified Linear Unit (RLU)
- Dropout
- Back-propagation
- Mini-batch
- At least four kinds of regularization
Visualizing networks

- Display pattern of hidden unit activations
  - Just shows they are sparse
- **Show** input that maximizes a node’s output
  - Over all inputs in the training set
  - Over the entire range of possible inputs
  - Early layers do feature detection
  - Later layers do object detection
- **Show how occluding parts of an image affect classification accuracy**

http://cs231n.github.io/understanding-cnn/
Lots of fancy network structures

Convolutional (different sizes)
Or fully connected
Maxpool
Concatenation
Softmax

Some layers use dropout

googlenet
AutoML learns network structure

Human built

Learned by RL

https://research.googleblog.com/2017/05/using-machine-learning-to-explore.html
What do you like best about the class? What can I improve on?