

Introduction to Syntactic Parsing

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Some slides were provided by Michael Collins (MIT) and Dan Moldovan (UT Dallas)

Overview

- An introduction to the parsing problem
- Context free grammars
- A brief(!) sketch of the syntax of English
- Examples of ambiguous structures
- PCFGs, their formal properties
- Weaknesses of PCFGs
- Heads in CFGs
- Chart parsing – algorithm and an example

Syntactic Parsing

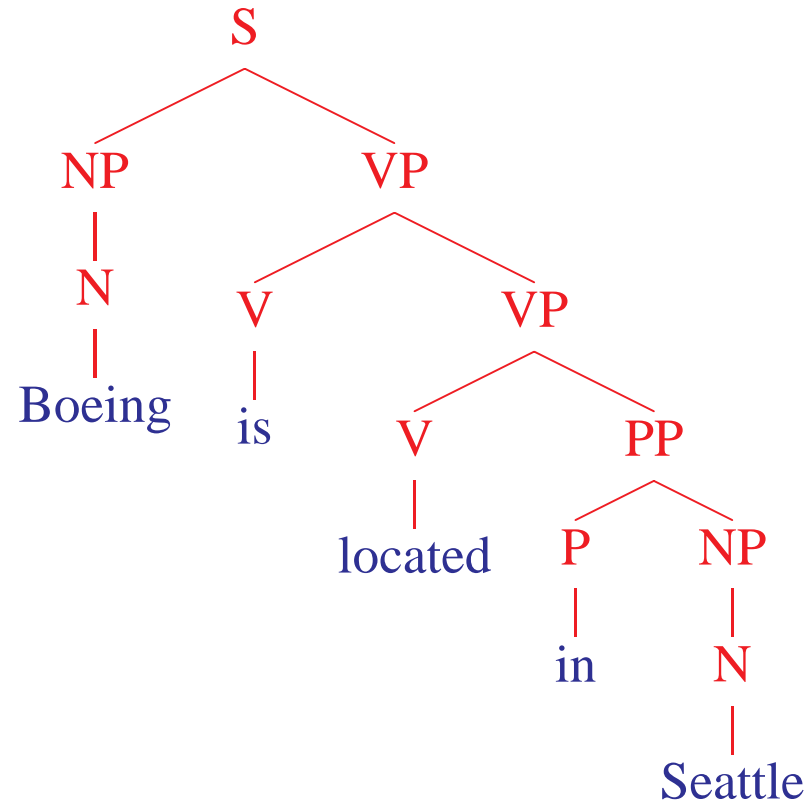
- **Syntax**: provides rules to put together words to form components of sentence and to put together these components to form sentences.
- Knowledge of syntax is useful for:
 - Parsing
 - QA
 - IE
 - Generation
 - Translation, etc.
- **Grammar** is the formal specification of rules of a language.
- **Parsing** is a method to perform syntactic analysis of a sentence.

Parsing (Syntactic Structure)

INPUT:

Boeing is located in Seattle.

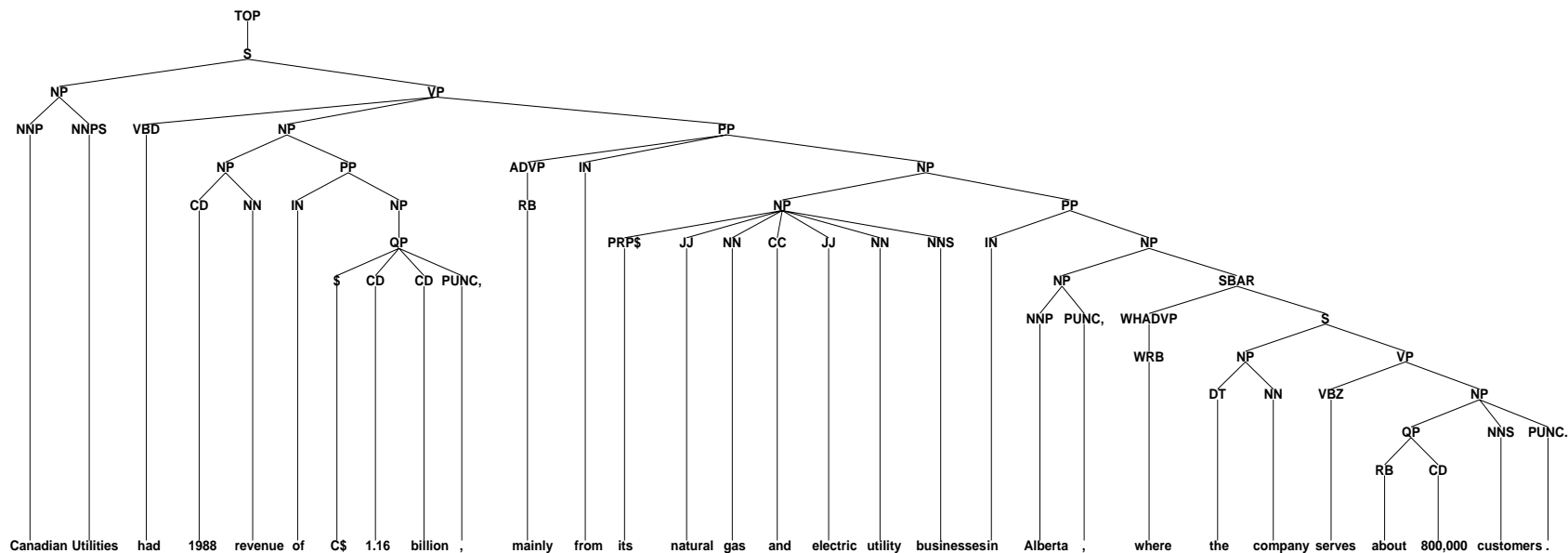
OUTPUT:



Data for Parsing Experiments

- Penn WSJ Treebank = 50,000 sentences with associated trees
- Usual set-up: 40,000 training sentences, 2400 test sentences

An example tree:

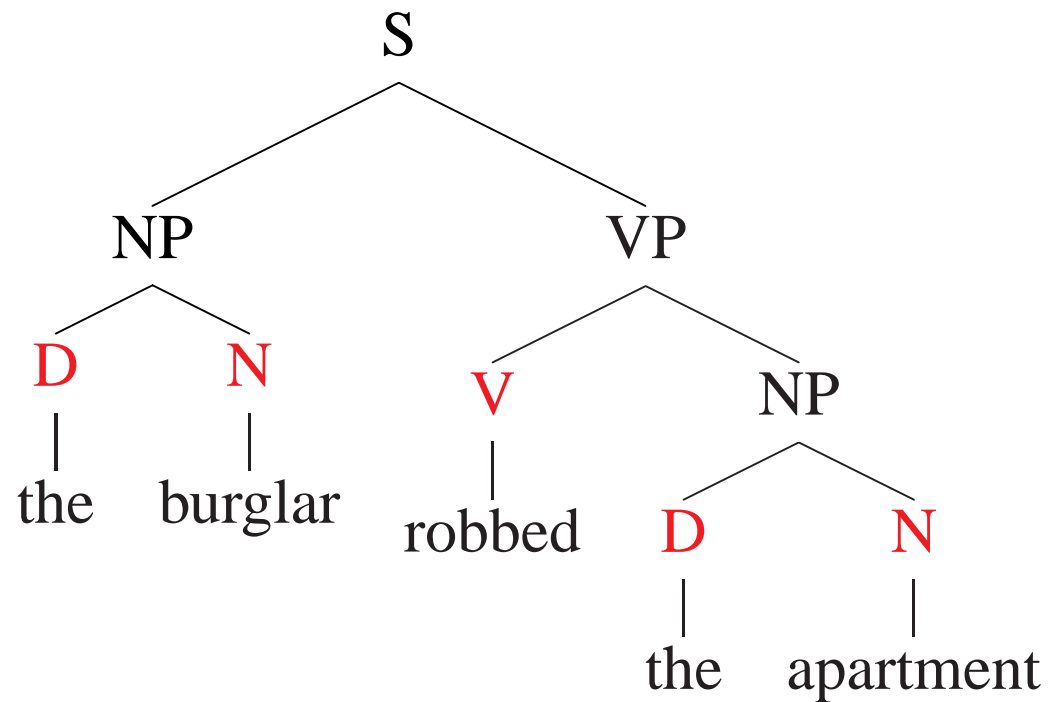


Canadian Utilities had 1988 revenue of C\$ 1.16 billion , mainly from its natural gas and electric utility businesses in Alberta , where the company serves about 800,000 customers .

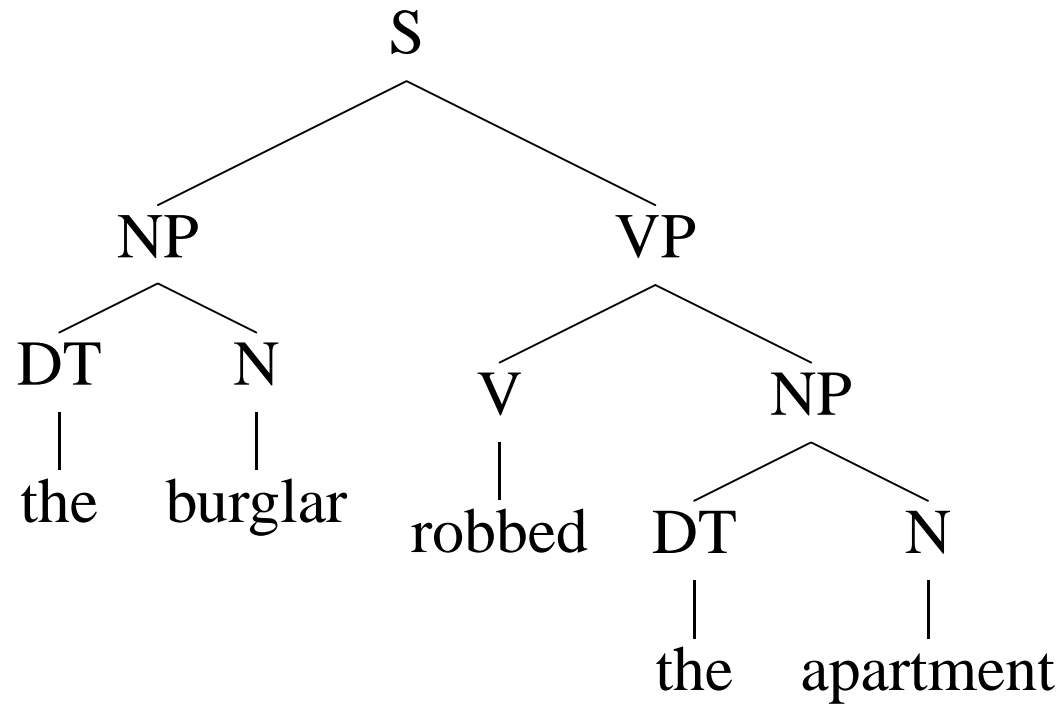
The Information Conveyed by Parse Trees

1) Part of speech for each word

(N = noun, V = verb, D = determiner)



2) Phrases

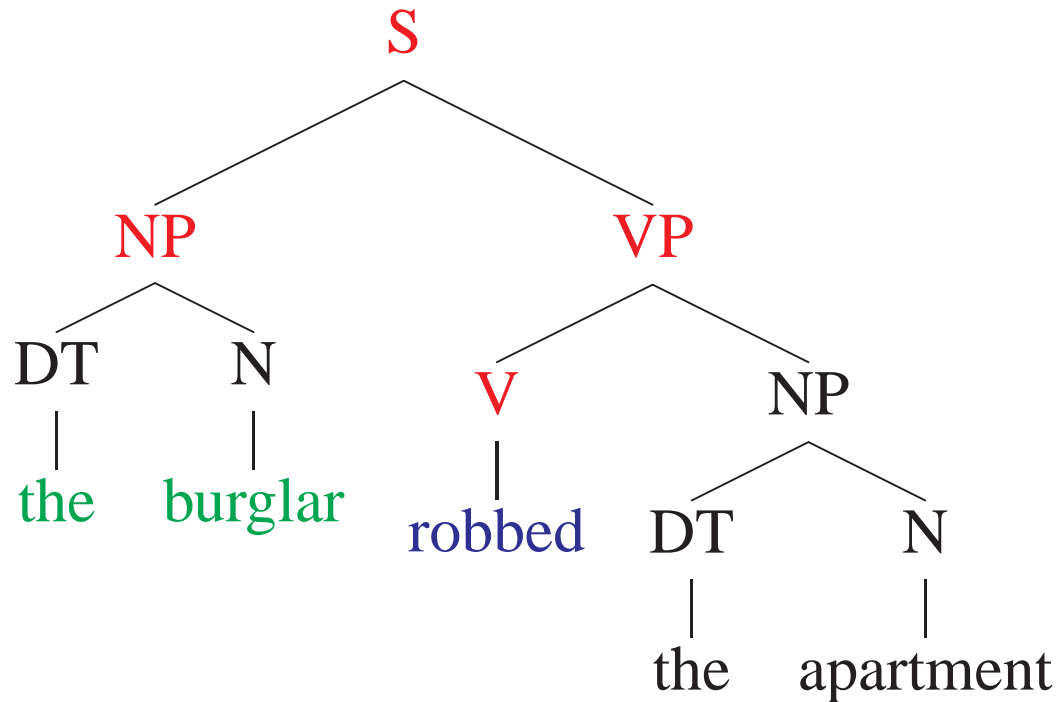
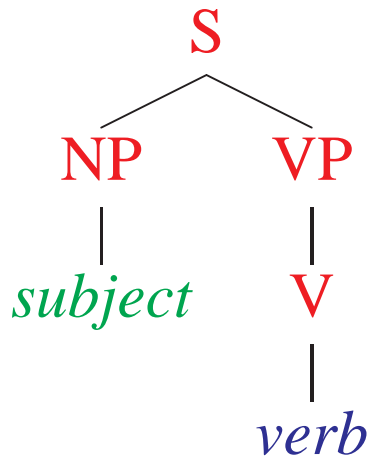


Noun Phrases (NP): “the burglar”, “the apartment”

Verb Phrases (VP): “robbed the apartment”

Sentences (S): “the burglar robbed the apartment”

3) Useful Relationships



⇒ “the burglar” is the subject of “robbed”

An Example Application: Machine Translation

- English word order is *subject – verb – object*
- Japanese word order is *subject – object – verb*

English: IBM bought Lotus

Japanese: *IBM Lotus bought*

English: Sources said that IBM bought Lotus yesterday

Japanese: *Sources yesterday IBM Lotus bought that said*

Context-Free Grammars

[Hopcroft and Ullman 1979]

A context free grammar $G = (N, \Sigma, R, S)$ where:

- N is a set of non-terminal symbols
- Σ is a set of terminal symbols
- R is a set of rules of the form $X \rightarrow Y_1 Y_2 \dots Y_n$
for $n \geq 0$, $X \in N$, $Y_i \in (N \cup \Sigma)$
- $S \in N$ is a distinguished start symbol

A Context-Free Grammar for English

$N = \{S, NP, VP, PP, DT, Vi, Vt, NN, IN\}$

$S = S$

$\Sigma = \{\text{sleeps, saw, man, woman, telescope, the, with, in}\}$

$R =$

S	\Rightarrow	NP	VP
VP	\Rightarrow	Vi	
VP	\Rightarrow	Vt	NP
VP	\Rightarrow	VP	PP
NP	\Rightarrow	DT	NN
NP	\Rightarrow	NP	PP
PP	\Rightarrow	IN	NP

Vi	\Rightarrow	sleeps
Vt	\Rightarrow	saw
NN	\Rightarrow	man
NN	\Rightarrow	woman
NN	\Rightarrow	telescope
DT	\Rightarrow	the
IN	\Rightarrow	with
IN	\Rightarrow	in

Note: S=sentence, VP=verb phrase, NP=noun phrase, PP=prepositional phrase, DT=determiner, Vi=intransitive verb, Vt=transitive verb, NN=noun, IN=preposition

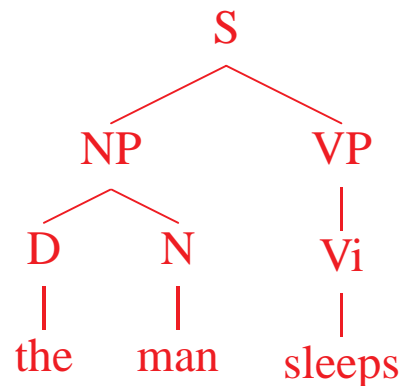
Left-Most Derivations

A left-most derivation is a sequence of strings $s_1 \dots s_n$, where

- $s_1 = S$, the start symbol
- $s_n \in \Sigma^*$, i.e. s_n is made up of terminal symbols only
- Each s_i for $i = 2 \dots n$ is derived from s_{i-1} by picking the left-most non-terminal X in s_{i-1} and replacing it by some β where $X \rightarrow \beta$ is a rule in R

For example: [S], [NP VP], [D N VP], [the N VP], [the man VP], [the man Vi], [the man sleeps]

Representation of a derivation as a tree:



DERIVATION

RULES USED

S

DERIVATION

S

NP VP

RULES USED

$S \rightarrow NP VP$

DERIVATION

S

NP VP

DT N VP

RULES USED

$S \rightarrow NP VP$

$NP \rightarrow DT N$

DERIVATION

S

NP VP

DT N VP

the N VP

RULES USED

$S \rightarrow NP VP$

$NP \rightarrow DT N$

$DT \rightarrow \text{the}$

DERIVATION

S

NP VP

DT N VP

the N VP

the dog VP

RULES USED

$S \rightarrow NP VP$

$NP \rightarrow DT N$

$DT \rightarrow \text{the}$

$N \rightarrow \text{dog}$

DERIVATION

S

NP VP

DT N VP

the N VP

the dog VP

the dog VB

RULES USED

$S \rightarrow NP VP$

$NP \rightarrow DT N$

$DT \rightarrow \text{the}$

$N \rightarrow \text{dog}$

$VP \rightarrow VB$

DERIVATION

S

NP VP

DT N VP

the N VP

the dog VP

the dog VB

the dog laughs

RULES USED

$S \rightarrow NP VP$

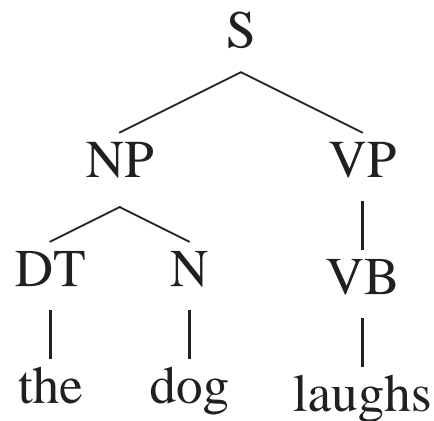
$NP \rightarrow DT N$

$DT \rightarrow \text{the}$

$N \rightarrow \text{dog}$

$VP \rightarrow VB$

$VB \rightarrow \text{laughs}$



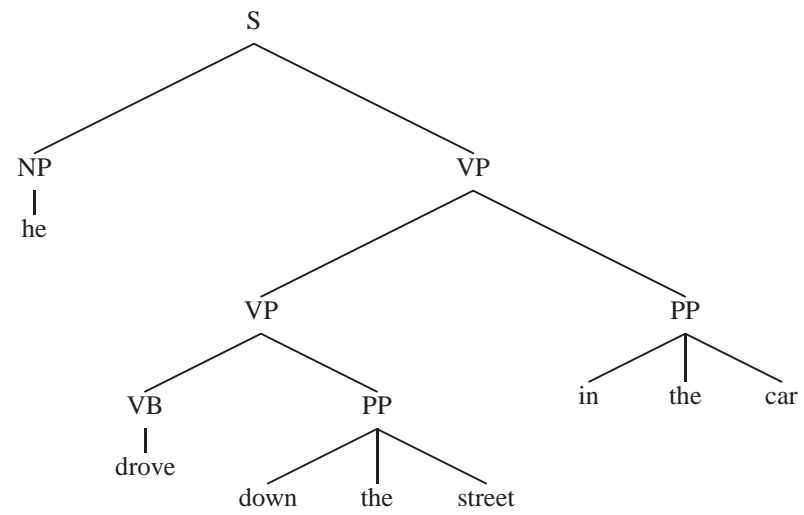
Properties of CFGs

- A CFG defines a set of possible derivations
- A string $s \in \Sigma^*$ is in the *language* defined by the CFG if there is at least one derivation which yields s
- Each string in the language generated by the CFG may have more than one derivation (“ambiguity”)

DERIVATION

S

RULES USED



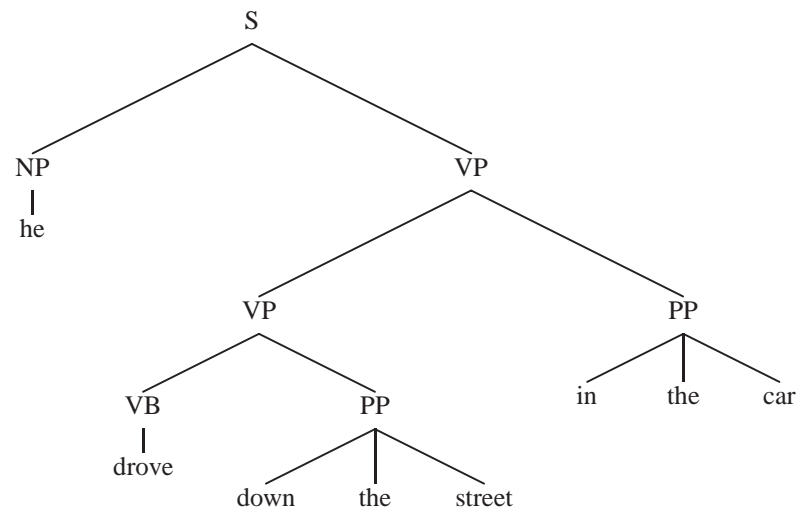
DERIVATION

S

NP VP

RULES USED

$S \rightarrow NP VP$



DERIVATION

S

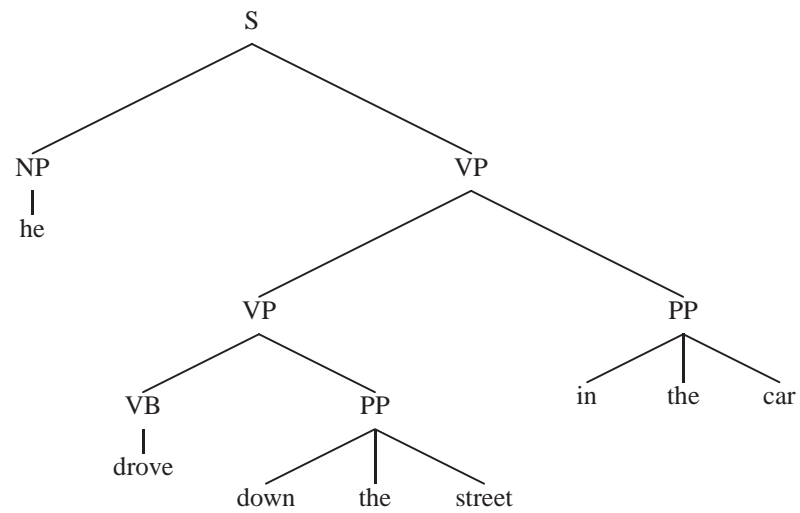
NP VP

he VP

RULES USED

$S \rightarrow NP VP$

$NP \rightarrow he$



DERIVATION

S

NP VP

he VP

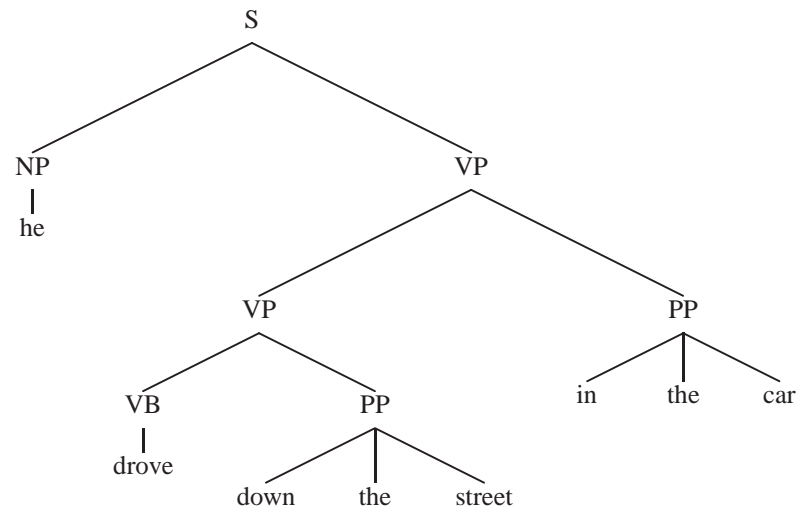
he VP PP

RULES USED

$S \rightarrow NP VP$

$NP \rightarrow he$

$VP \rightarrow VP PP$



DERIVATION

S

NP VP

he VP

he VP PP

he VB PP PP

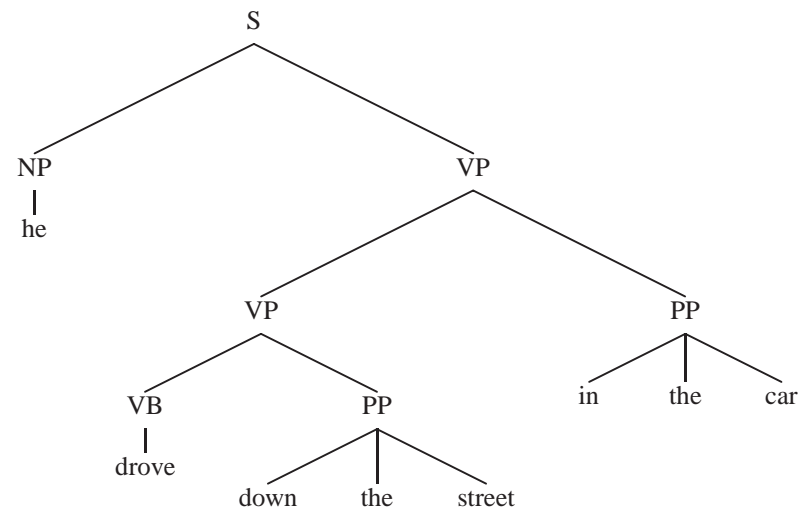
RULES USED

$S \rightarrow NP VP$

$NP \rightarrow he$

$VP \rightarrow VP PP$

$VP \rightarrow VB PP$



DERIVATION

S

NP VP

he VP

he VP PP

he VB PP PP

he drove PP PP

RULES USED

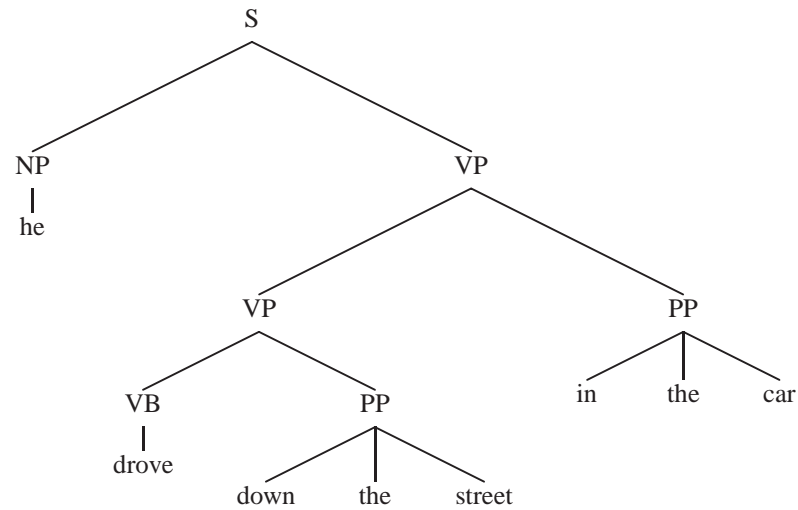
$S \rightarrow NP VP$

$NP \rightarrow he$

$VP \rightarrow VP PP$

$VP \rightarrow VB PP$

$VB \rightarrow drove$



DERIVATION

S

NP VP

he VP

he VP PP

he VB PP PP

he drove PP PP

he drove down the street PP

RULES USED

$S \rightarrow NP VP$

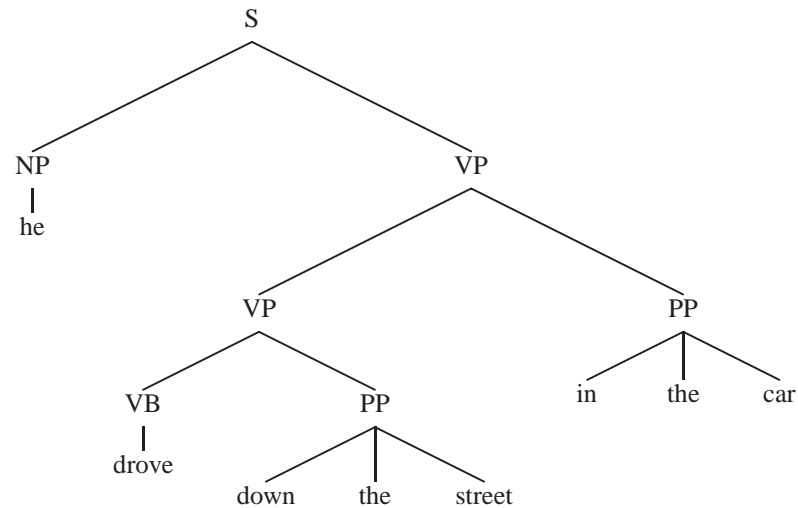
$NP \rightarrow he$

$VP \rightarrow VP PP$

$VP \rightarrow VB PP$

$VB \rightarrow drove$

$PP \rightarrow down\ the\ street$



DERIVATION

S

NP VP

he VP

he VP PP

he VB PP PP

he drove PP PP

he drove down the street PP

he drove down the street in the car

RULES USED

$S \rightarrow NP VP$

$NP \rightarrow he$

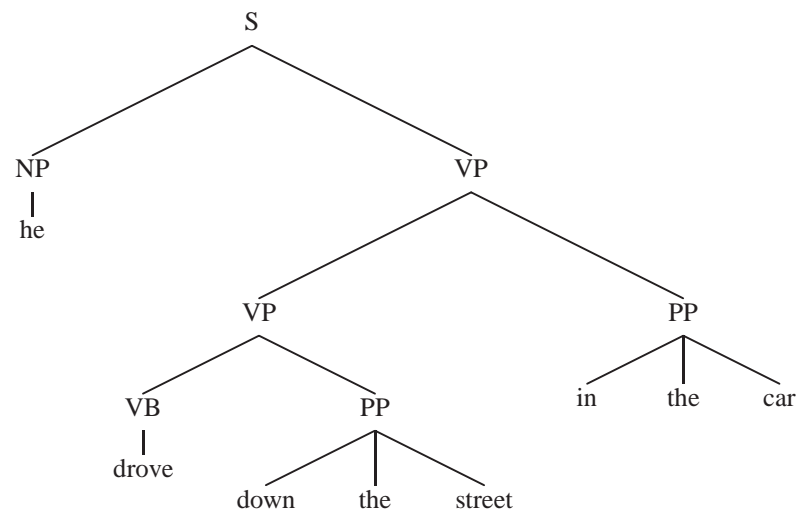
$VP \rightarrow VP PP$

$VP \rightarrow VB PP$

$VB \rightarrow drove$

$PP \rightarrow down\ the\ street$

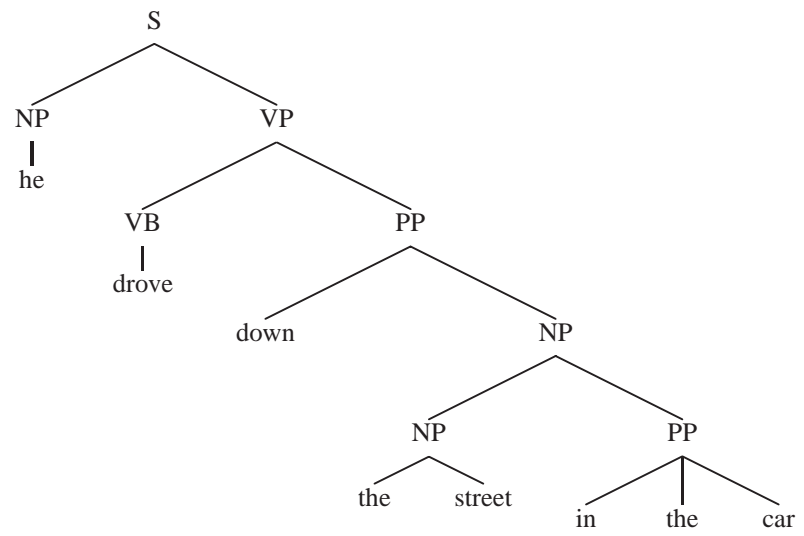
$PP \rightarrow in\ the\ car$



DERIVATION

S

RULES USED



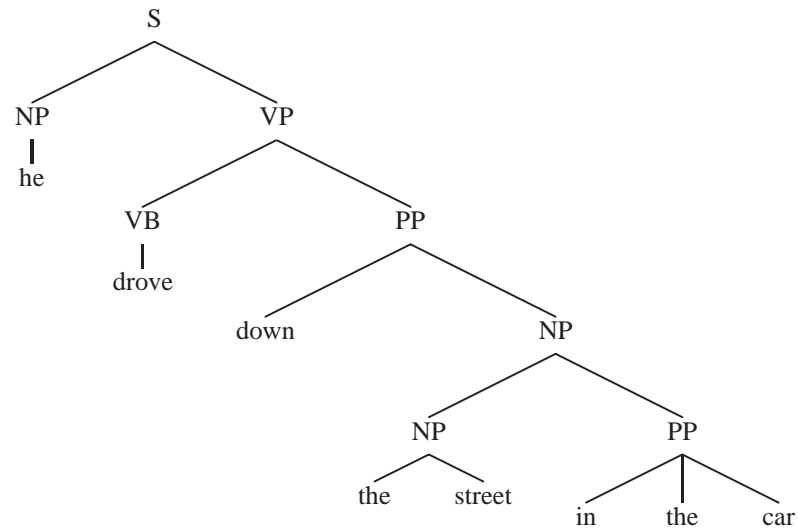
DERIVATION

S

NP VP

RULES USED

$S \rightarrow NP VP$



DERIVATION

S

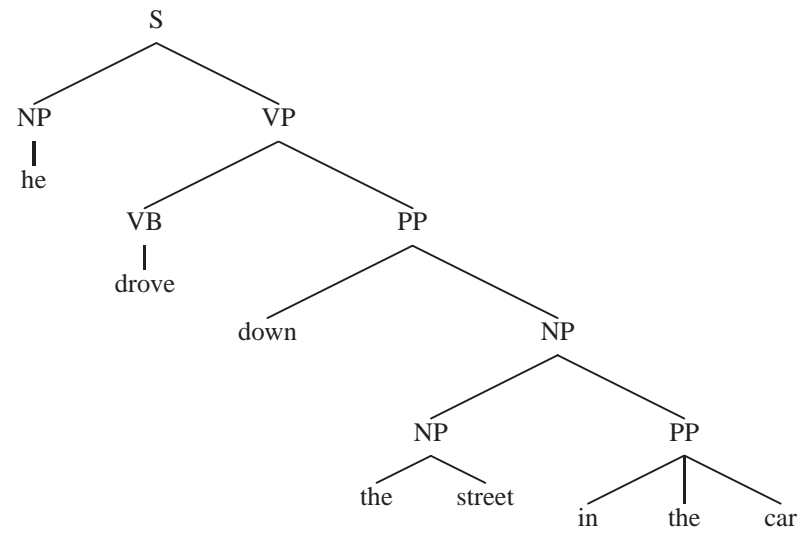
NP VP

he VP

RULES USED

$S \rightarrow NP VP$

$NP \rightarrow he$



DERIVATION

S

NP VP

he VP

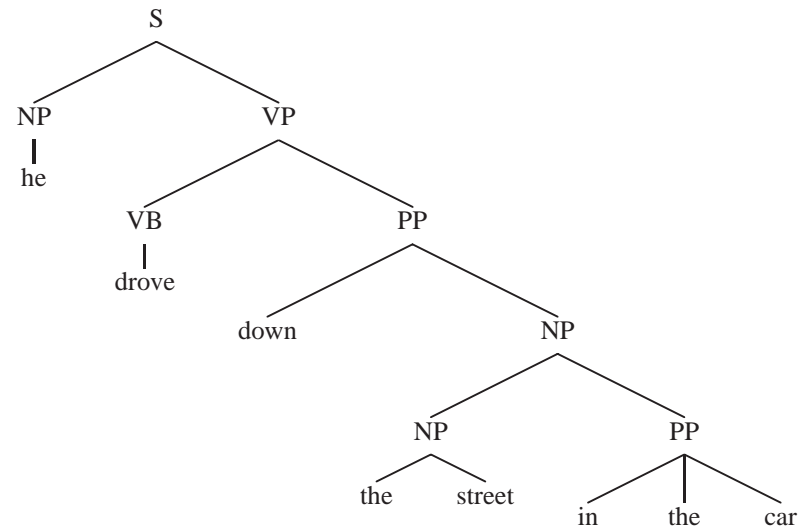
he VB PP

RULES USED

$S \rightarrow NP VP$

$NP \rightarrow he$

$VP \rightarrow VB PP$



DERIVATION

S

NP VP

he VP

he VB PP

he drove PP

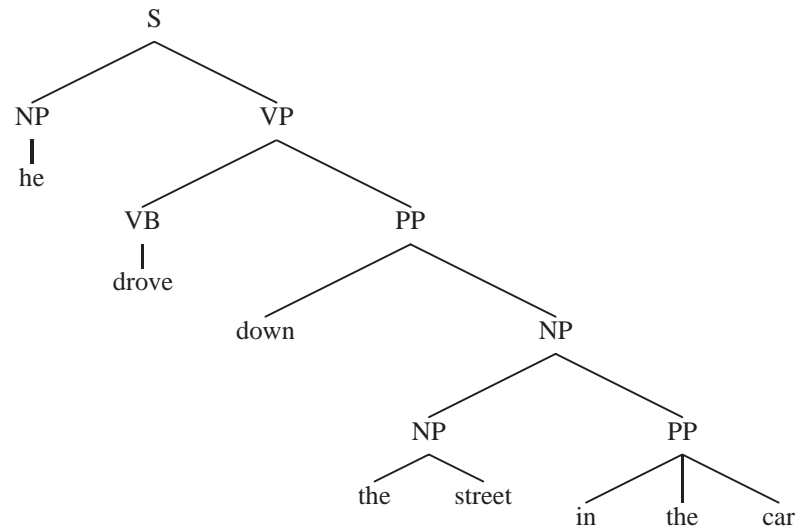
RULES USED

$S \rightarrow NP VP$

$NP \rightarrow he$

$VP \rightarrow VB PP$

$VB \rightarrow drove$



DERIVATION

S

NP VP

he VP

he VB PP

he drove PP

he drove down NP

RULES USED

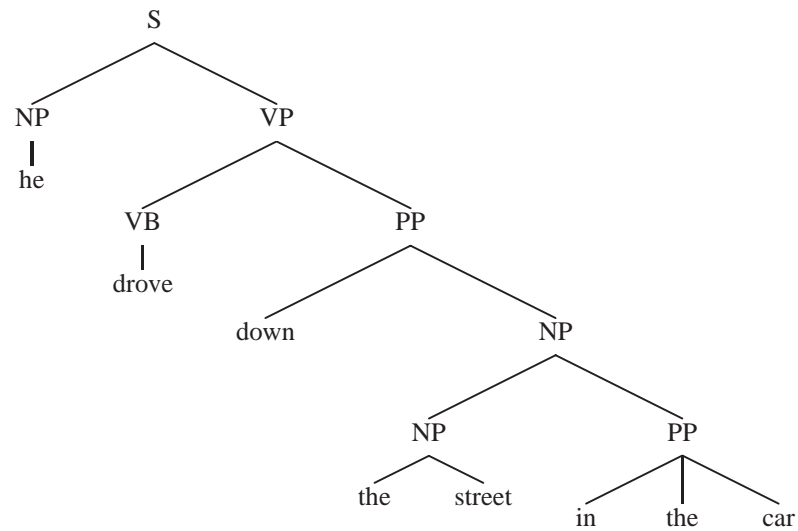
$S \rightarrow NP VP$

$NP \rightarrow he$

$VP \rightarrow VB PP$

$VB \rightarrow drove$

$PP \rightarrow down NP$



DERIVATION

S

NP VP

he VP

he VB PP

he drove PP

he drove down NP

he drove down NP PP

RULES USED

$S \rightarrow NP VP$

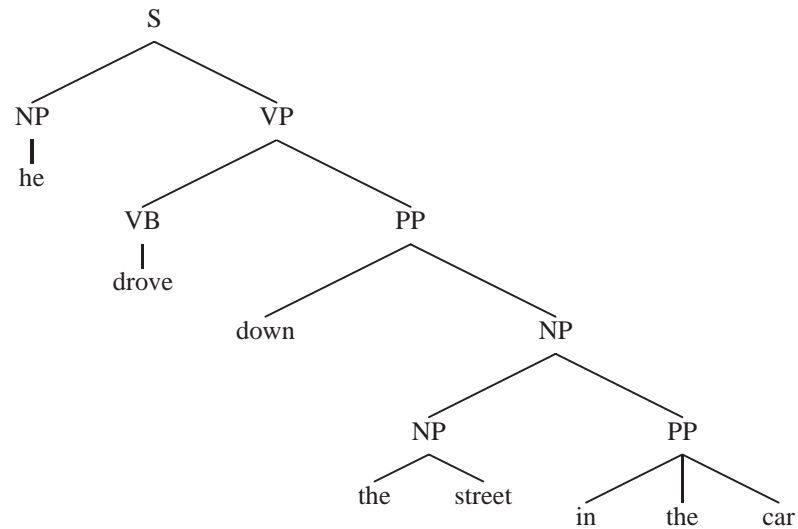
$NP \rightarrow he$

$VP \rightarrow VB PP$

$VB \rightarrow drove$

$PP \rightarrow down NP$

$NP \rightarrow NP PP$



DERIVATION

S

NP VP

he VP

he VB PP

he drove PP

he drove down NP

he drove down NP PP

he drove down the street PP

RULES USED

$S \rightarrow NP VP$

$NP \rightarrow he$

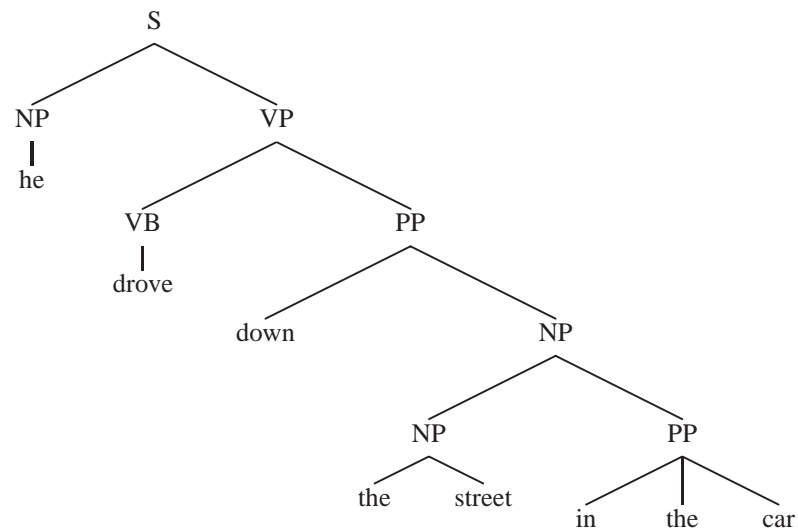
$VP \rightarrow VB PP$

$VB \rightarrow drove$

$PP \rightarrow down NP$

$NP \rightarrow NP PP$

$NP \rightarrow the street$



DERIVATION

S

NP VP

he VP

he VB PP

he drove PP

he drove down NP

he drove down NP PP

he drove down the street PP

he drove down the street in the car

RULES USED

$S \rightarrow NP VP$

$NP \rightarrow he$

$VP \rightarrow VB PP$

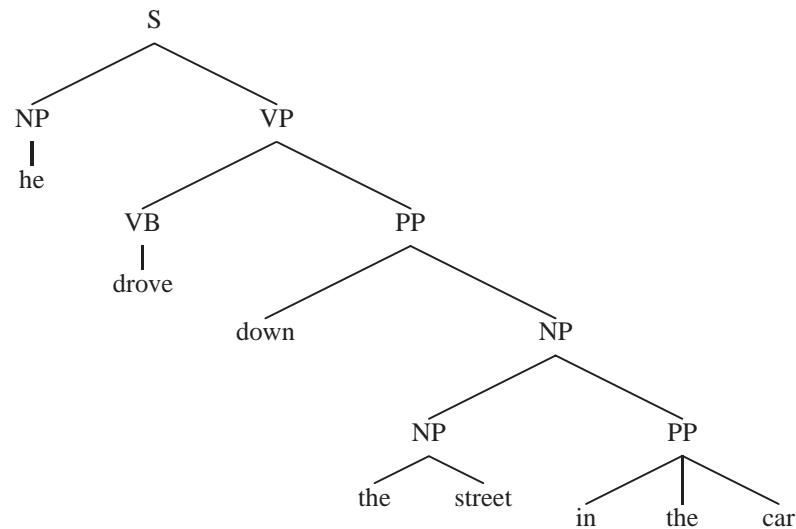
$VB \rightarrow drove$

$PP \rightarrow down NP$

$NP \rightarrow NP PP$

$NP \rightarrow the\ street$

$PP \rightarrow in\ the\ car$



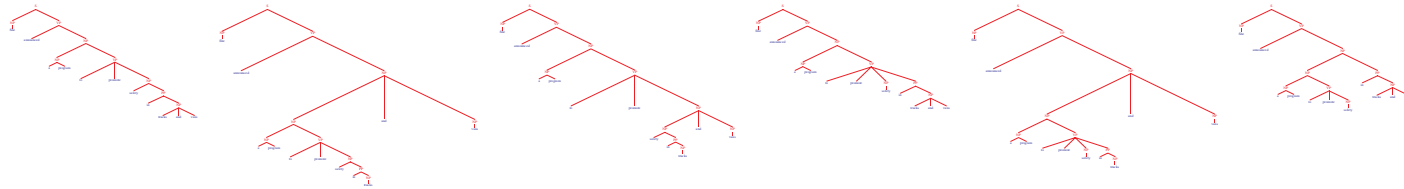
The Problem with Parsing: Ambiguity

INPUT:

She announced a program to promote safety in trucks and vans



POSSIBLE OUTPUTS:



And there are more...

A Brief Overview of English Syntax

Parts of Speech:

- Nouns

(Tags from the *Brown corpus*)

NN = singular noun e.g., man, dog, park

NNS = plural noun e.g., telescopes, houses, buildings

NNP = proper noun e.g., Smith, Gates, IBM

- Determiners

DT = determiner e.g., the, a, some, every

- Adjectives

JJ = adjective e.g., red, green, large, idealistic

A Fragment of a Noun Phrase Grammar

\bar{N}	\Rightarrow	NN		NN	\Rightarrow	box
\bar{N}	\Rightarrow	NN	\bar{N}	NN	\Rightarrow	car
\bar{N}	\Rightarrow	JJ	\bar{N}	NN	\Rightarrow	mechanic
\bar{N}	\Rightarrow	\bar{N}	\bar{N}	NN	\Rightarrow	pigeon
NP	\Rightarrow	DT	\bar{N}			
				DT	\Rightarrow	the
				DT	\Rightarrow	a
				JJ	\Rightarrow	fast
				JJ	\Rightarrow	metal
				JJ	\Rightarrow	idealistic
				JJ	\Rightarrow	clay

Generates:

a box, the box, the metal box, the fast car mechanic, . . .

Prepositions, and Prepositional Phrases

- Prepositions

IN = preposition e.g., of, in, out, beside, as

An Extended Grammar

\bar{N}	\Rightarrow	NN			\Rightarrow	JJ	\Rightarrow	fast
\bar{N}	\Rightarrow	NN	\bar{N}		\Rightarrow	JJ	\Rightarrow	metal
\bar{N}	\Rightarrow	JJ	\bar{N}		\Rightarrow	JJ	\Rightarrow	idealistic
\bar{N}	\Rightarrow	\bar{N}	\bar{N}		\Rightarrow	JJ	\Rightarrow	clay
NP	\Rightarrow	DT	\bar{N}		\Rightarrow	NN	\Rightarrow	box
PP	\Rightarrow	IN	NP		\Rightarrow	NN	\Rightarrow	car
\bar{N}	\Rightarrow	\bar{N}	PP		\Rightarrow	NN	\Rightarrow	mechanic
					\Rightarrow	NN	\Rightarrow	pigeon
					\Rightarrow	DT	\Rightarrow	the
					\Rightarrow	DT	\Rightarrow	a
					\Rightarrow	IN	\Rightarrow	in
					\Rightarrow	IN	\Rightarrow	under
					\Rightarrow	IN	\Rightarrow	of
					\Rightarrow	IN	\Rightarrow	on
					\Rightarrow	IN	\Rightarrow	with
					\Rightarrow	IN	\Rightarrow	as

Generates:

in a box, under the box, the fast car mechanic under the pigeon in the box, ...

Verbs, Verb Phrases, and Sentences

- Basic Verb Types

Vi = Intransitive verb e.g., sleeps, walks, laughs

Vt = Transitive verb e.g., sees, saw, likes

Vd = Ditransitive verb e.g., gave

- Basic VP Rules

VP → Vi

VP → Vt NP

VP → Vd NP NP

- Basic S Rule

S → NP VP

Examples of VP:

sleeps, walks, likes the mechanic, gave the mechanic the fast car,
gave the fast car mechanic the pigeon in the box, . . .

Examples of S:

the man sleeps, the dog walks, the dog likes the mechanic, the dog in the box gave the mechanic the fast car, . . .

PPs Modifying Verb Phrases

A new rule:

VP \rightarrow VP PP

New examples of VP:

sleeps in the car, walks like the mechanic, gave the mechanic the fast car on Tuesday, . . .

Complementizers, and SBARs

- Complementizers

COMP = complementizer e.g., that

- SBAR

SBAR → COMP S

Examples:

that the man sleeps, that the mechanic saw the dog . . .

More Verbs

- New Verb Types

V[5] e.g., said, reported

V[6] e.g., told, informed

V[7] e.g., bet

- New VP Rules

VP → V[5] SBAR

VP → V[6] NP SBAR

VP → V[7] NP NP SBAR

Examples of New VPs:

said that the man sleeps

told the dog that the mechanic likes the pigeon

bet the pigeon \$50 that the mechanic owns a fast car

Coordination

- A New Part-of-Speech:

CC = Coordinator e.g., and, or, but

- New Rules

NP → NP CC NP

\bar{N} → \bar{N} CC \bar{N}

VP → VP CC VP

S → S CC S

SBAR → SBAR CC SBAR

Sources of Ambiguity

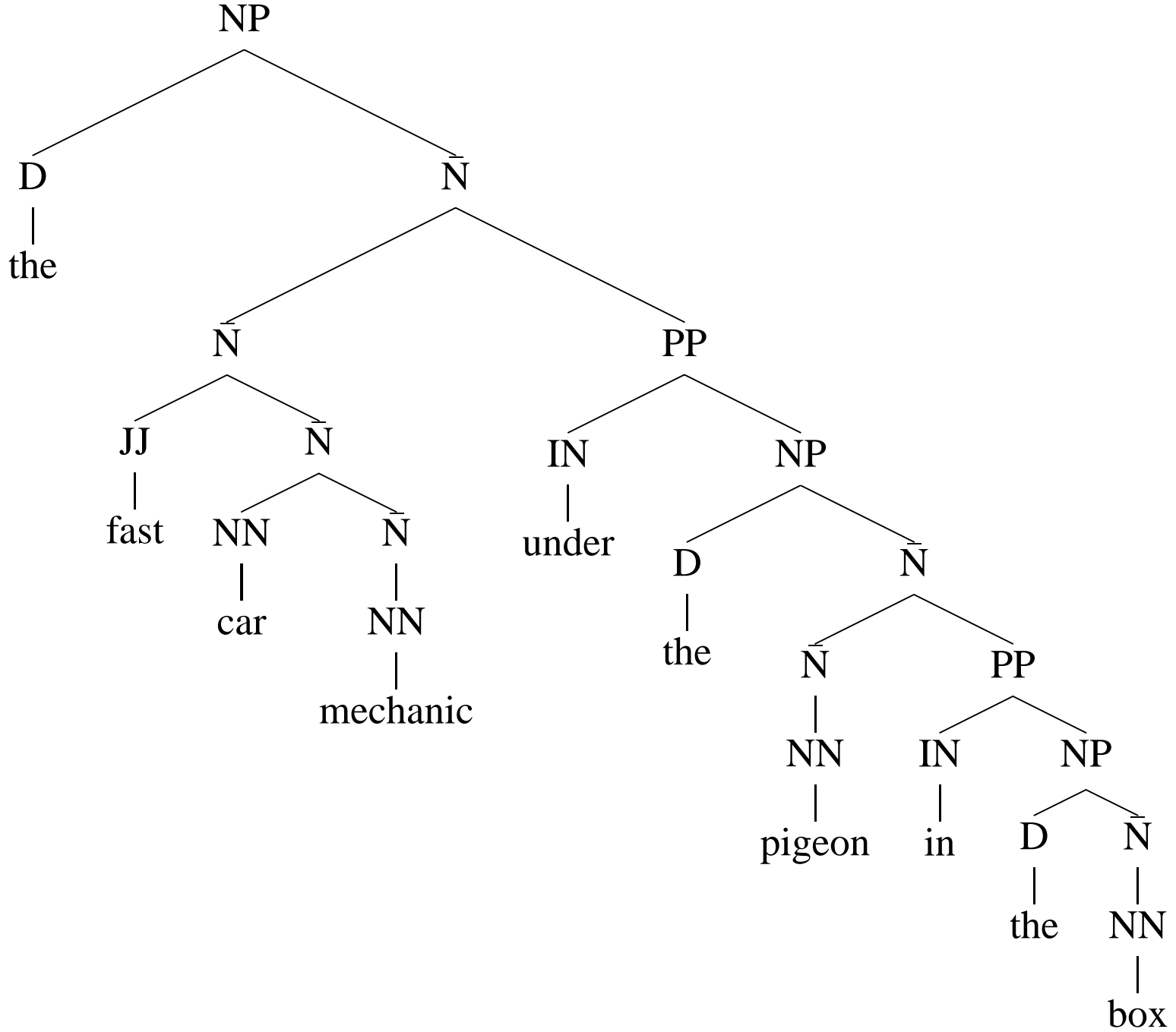
- Part-of-Speech ambiguity

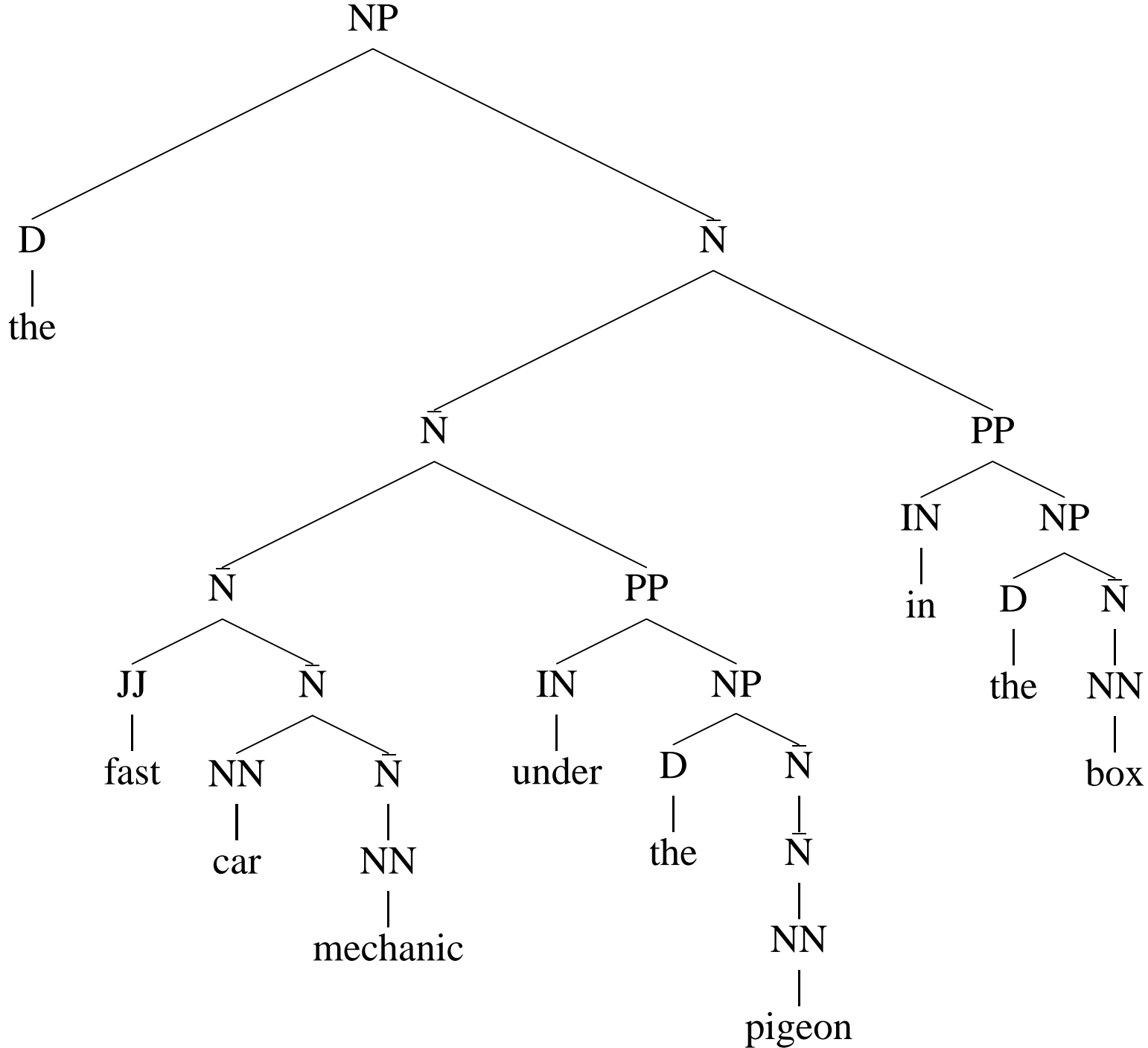
NNS → walks

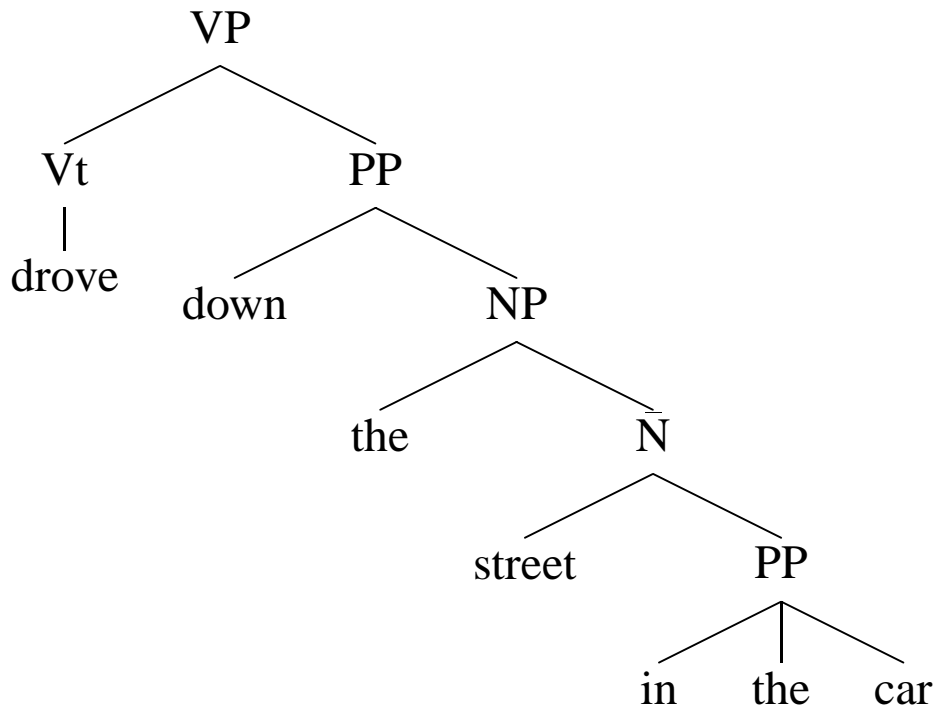
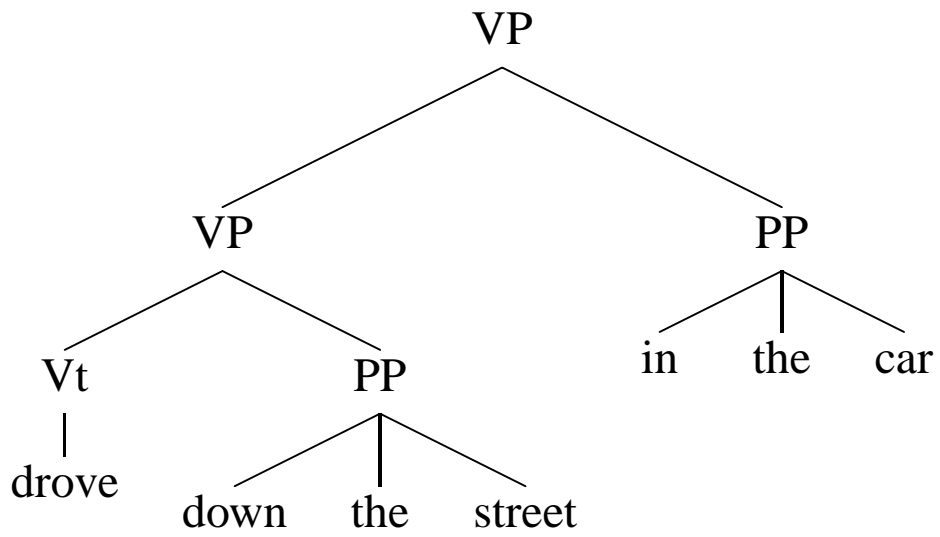
Vi → walks

- Prepositional Phrase Attachment

the fast car mechanic under the pigeon in the box

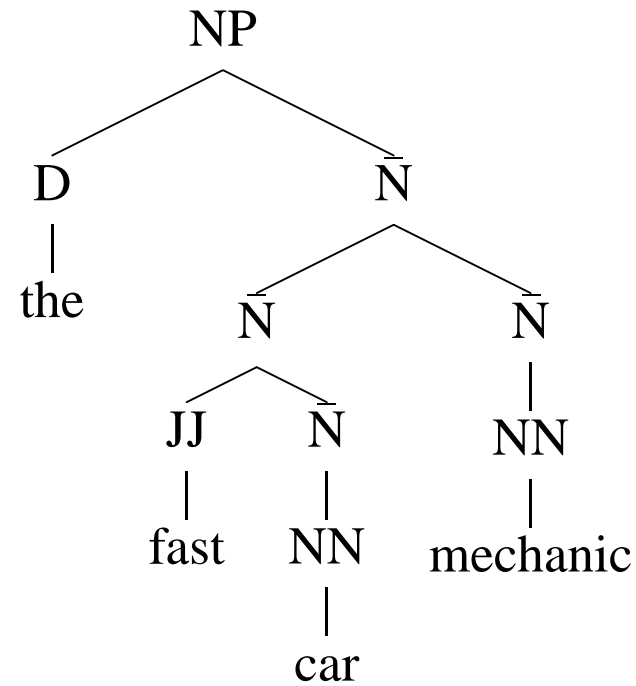
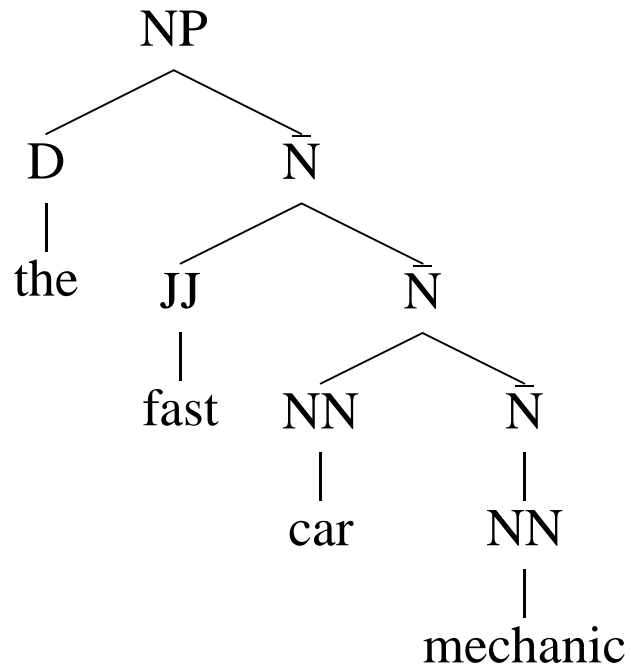






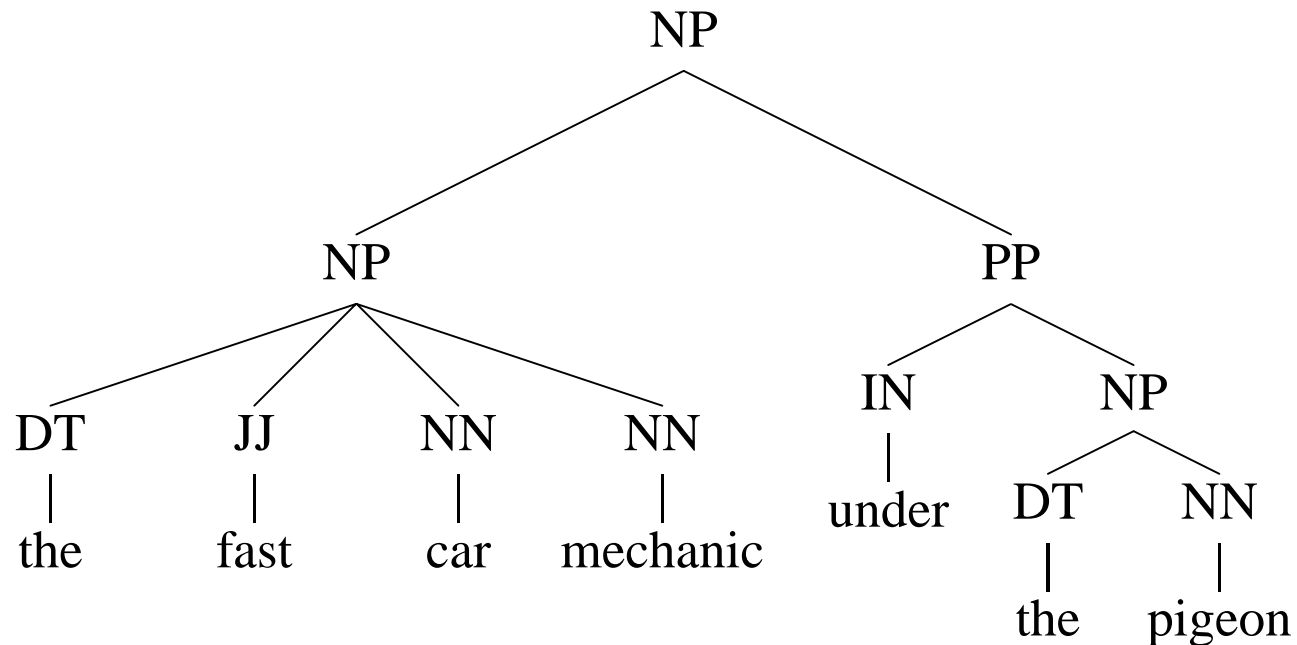
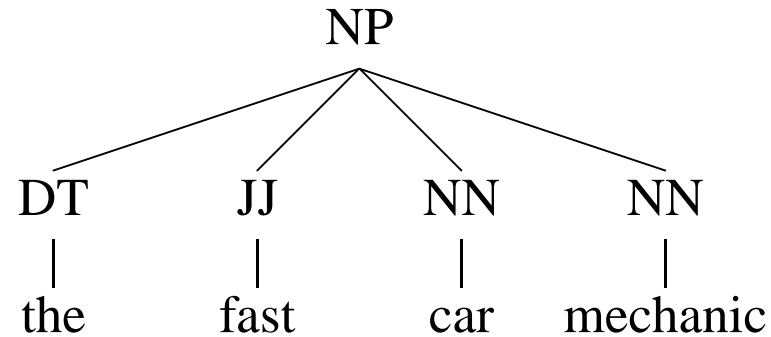
Sources of Ambiguity: Noun Premodifiers

- Noun premodifiers:



A Funny Thing about the Penn Treebank

Leaves NP premodifier structure flat, or underspecified:



A Probabilistic Context-Free Grammar

S	⇒	NP	VP	1.0
VP	⇒	Vi		0.4
VP	⇒	Vt	NP	0.4
VP	⇒	VP	PP	0.2
NP	⇒	DT	NN	0.3
NP	⇒	NP	PP	0.7
PP	⇒	P	NP	1.0

Vi	⇒	sleeps	1.0
Vt	⇒	saw	1.0
NN	⇒	man	0.7
NN	⇒	woman	0.2
NN	⇒	telescope	0.1
DT	⇒	the	1.0
IN	⇒	with	0.5
IN	⇒	in	0.5

- Probability of a tree with rules $\alpha_i \rightarrow \beta_i$ is $\prod_i P(\alpha_i \rightarrow \beta_i | \alpha_i)$

DERIVATION

S

RULES USED

PROBABILITY

DERIVATION

S

NP VP

RULES USED

$S \rightarrow NP VP$

PROBABILITY

1.0

DERIVATION

S

NP VP

DT N VP

RULES USED

$S \rightarrow NP VP$

$NP \rightarrow DT N$

PROBABILITY

1.0

0.3

DERIVATION

S

NP VP

DT N VP

the N VP

RULES USED

$S \rightarrow NP VP$

$NP \rightarrow DT N$

$DT \rightarrow \text{the}$

PROBABILITY

1.0

0.3

1.0

DERIVATION

S

NP VP

DT N VP

the N VP

the dog VP

RULES USED

$S \rightarrow NP VP$

$NP \rightarrow DT N$

$DT \rightarrow \text{the}$

$N \rightarrow \text{dog}$

PROBABILITY

1.0

0.3

1.0

0.1

DERIVATION

S

NP VP

DT N VP

the N VP

the dog VP

the dog VB

RULES USED

$S \rightarrow NP VP$

$NP \rightarrow DT N$

$DT \rightarrow the$

$N \rightarrow dog$

$VP \rightarrow VB$

PROBABILITY

1.0

0.3

1.0

0.1

0.4

DERIVATION	RULES USED	PROBABILITY
S	$S \rightarrow NP VP$	1.0
NP VP	$NP \rightarrow DT N$	0.3
DT N VP	$DT \rightarrow \text{the}$	1.0
the N VP	$N \rightarrow \text{dog}$	0.1
the dog VP	$VP \rightarrow VB$	0.4
the dog VB	$VB \rightarrow \text{laughs}$	0.5
the dog laughs		

$$\text{TOTAL PROBABILITY} = 1.0 \times 0.3 \times 1.0 \times 0.1 \times 0.4 \times 0.5$$

Properties of PCFGs

- Assigns a probability to each *left-most derivation*, or parse-tree, allowed by the underlying CFG
- Say we have a sentence S , set of derivations for that sentence is $\mathcal{T}(S)$. Then a PCFG assigns a probability to each member of $\mathcal{T}(S)$. i.e., *we now have a ranking in order of probability.*
- The probability of a string S is

$$\sum_{T \in \mathcal{T}(S)} P(T, S)$$

Deriving a PCFG from a Corpus

- Given a set of example trees, the underlying CFG can simply be **all rules seen in the corpus**

- Maximum Likelihood estimates:

$$P_{ML}(\alpha \rightarrow \beta \mid \alpha) = \frac{\text{Count}(\alpha \rightarrow \beta)}{\text{Count}(\alpha)}$$

where the counts are taken from a training set of example trees.

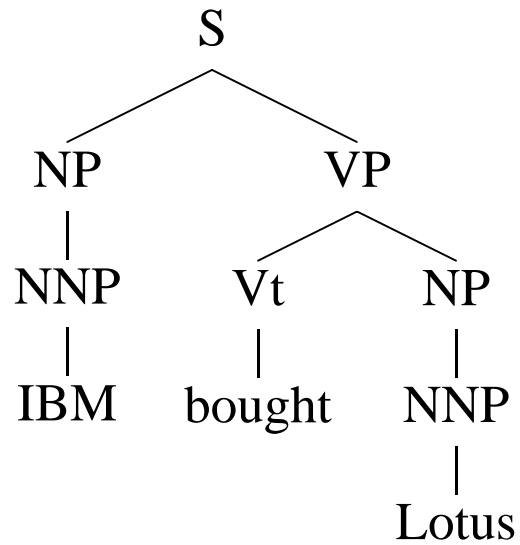
- **If the training data is generated by a PCFG**, then as the training data size goes to infinity, the maximum-likelihood PCFG will converge to the same distribution as the “true” PCFG.

Overview

- An introduction to the parsing problem
- Context free grammars
- A brief(!) sketch of the syntax of English
- Examples of ambiguous structures
- PCFGs, their formal properties, and useful algorithms
- Weaknesses of PCFGs

Weaknesses of PCFGs

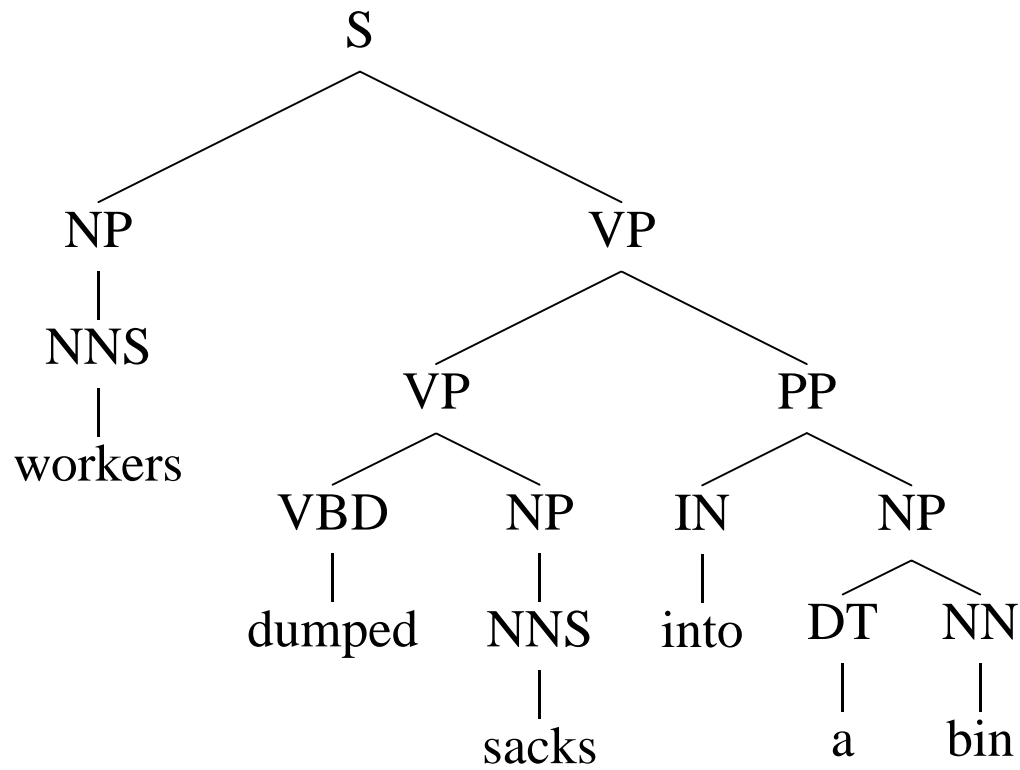
- Lack of sensitivity to lexical information
- Lack of sensitivity to structural frequencies



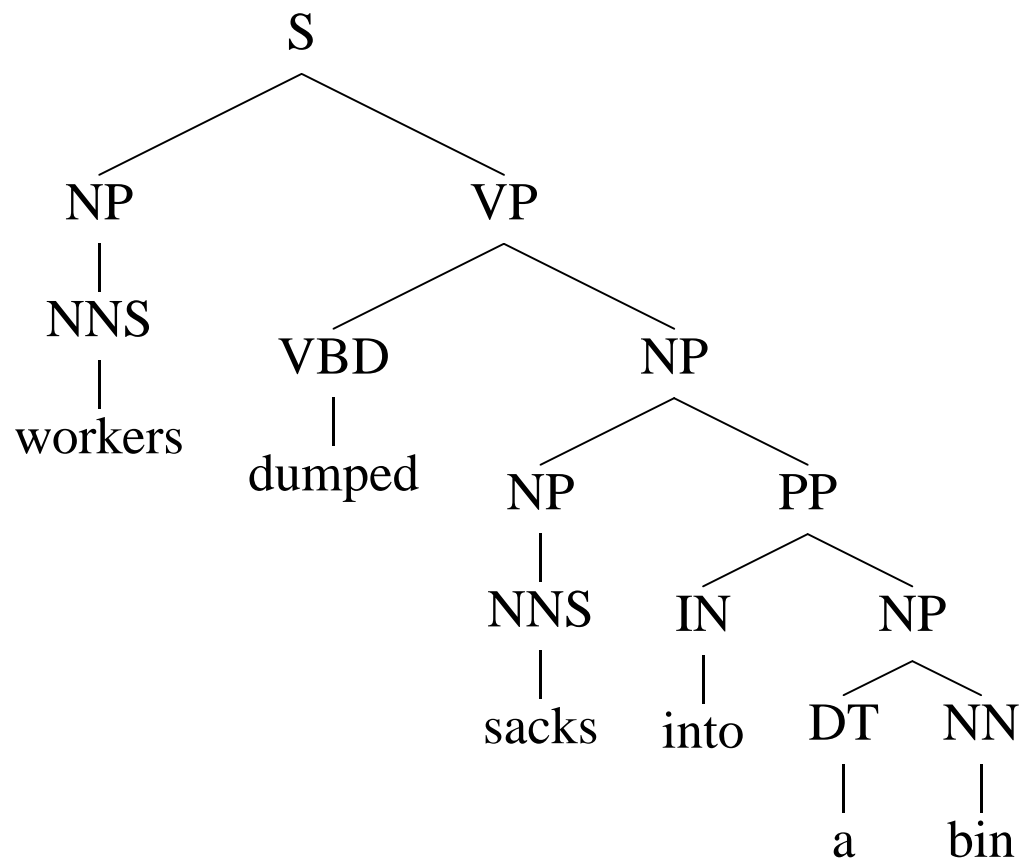
$$\begin{aligned}
 \text{PROB} = & P(S \rightarrow \text{NP VP} \mid S) && \times P(\text{NNP} \rightarrow \textit{IBM} \mid \text{NNP}) \\
 & \times P(\text{VP} \rightarrow \text{V NP} \mid \text{VP}) && \times P(\text{Vt} \rightarrow \textit{bought} \mid \text{Vt}) \\
 & \times P(\text{NP} \rightarrow \text{NNP} \mid \text{NP}) && \times P(\text{NNP} \rightarrow \textit{Lotus} \mid \text{NNP}) \\
 & \times P(\text{NP} \rightarrow \text{NNP} \mid \text{NP})
 \end{aligned}$$

Another Case of PP Attachment Ambiguity

(a)



(b)



(a)

Rules
S → NP VP
NP → NNS
VP → VP PP
VP → VBD NP
NP → NNS
PP → IN NP
NP → DT NN
NNS → workers
VBD → dumped
NNS → sacks
IN → into
DT → a
NN → bin

(b)

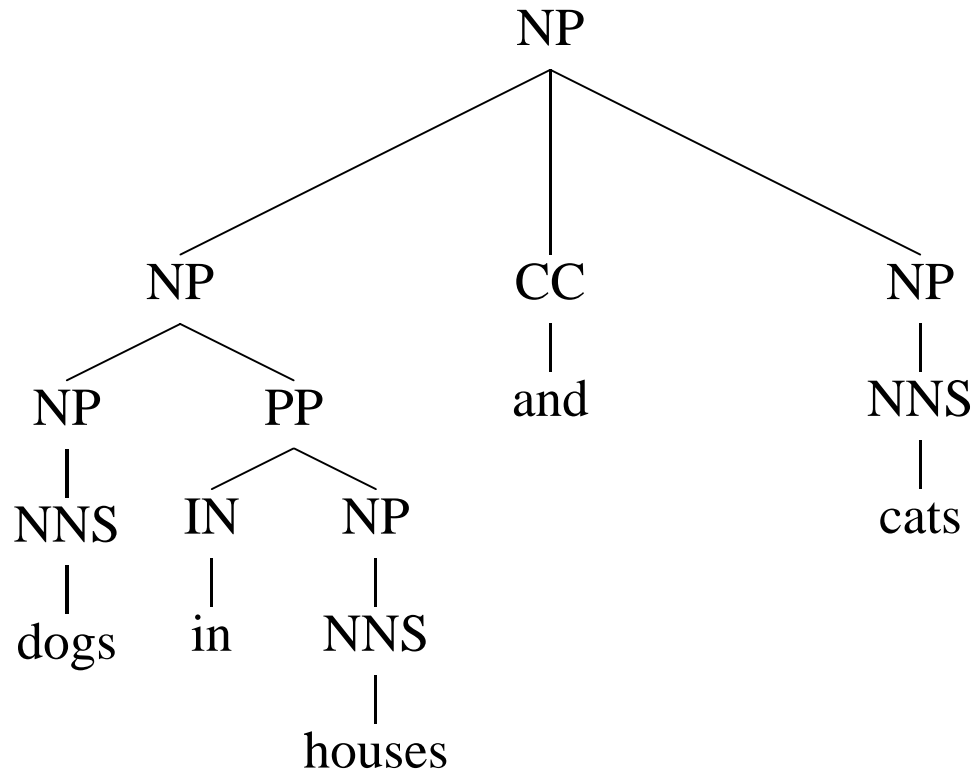
Rules
S → NP VP
NP → NNS
NP → NP PP
VP → VBD NP
NP → NNS
PP → IN NP
NP → DT NN
NNS → workers
VBD → dumped
NNS → sacks
IN → into
DT → a
NN → bin

If $P(\text{NP} \rightarrow \text{NP PP} \mid \text{NP}) > P(\text{VP} \rightarrow \text{VP PP} \mid \text{VP})$ then (b) is more probable, else (a) is more probable.

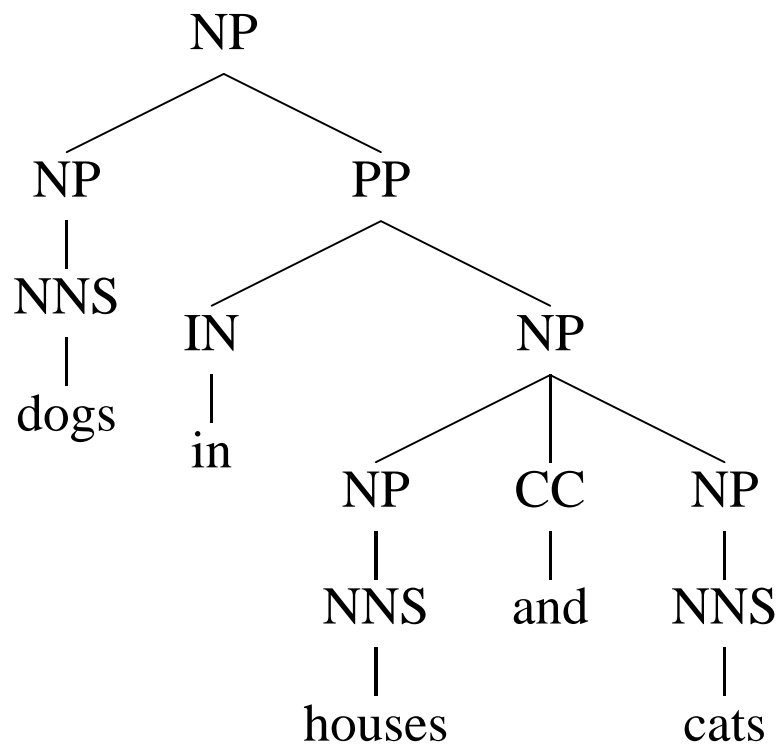
Attachment decision is completely independent of the words

A Case of Coordination Ambiguity

(a)



(b)



(a)

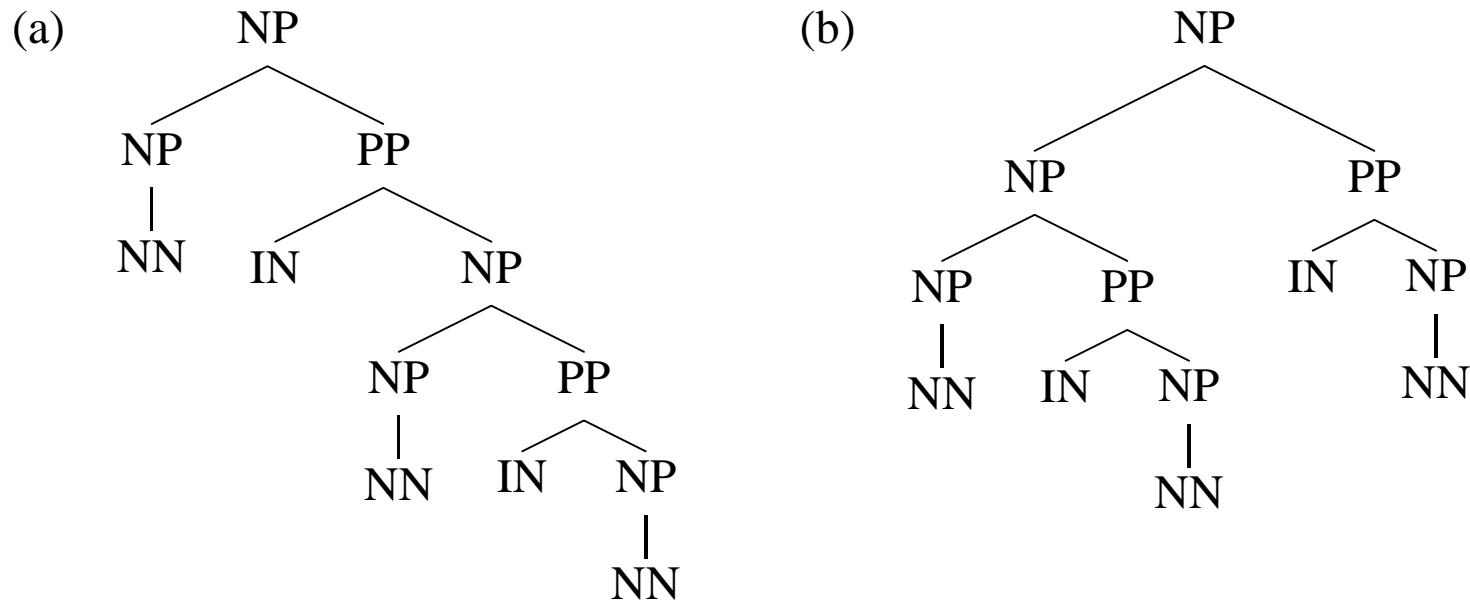
Rules
NP → NP CC NP
NP → NP PP
NP → NNS
PP → IN NP
NP → NNS
NP → NNS
NNS → dogs
IN → in
NNS → houses
CC → and
NNS → cats

(b)

Rules
NP → NP CC NP
NP → NP PP
NP → NNS
PP → IN NP
NP → NNS
NP → NNS
NNS → dogs
IN → in
NNS → houses
CC → and
NNS → cats

Here the two parses have identical rules, and therefore have identical probability under any assignment of PCFG rule probabilities

Structural Preferences: Close Attachment



- Example: [president of a company in Africa](#)
- Both parses have the same rules, therefore receive same probability under a PCFG
- “Close attachment” (structure (a)) is twice as likely in Wall Street Journal text.

Heads in Context-Free Rules

Add annotations specifying the “**head**” of each rule:

S	⇒	NP	VP
VP	⇒	Vi	
VP	⇒	Vt	NP
VP	⇒	VP	PP
NP	⇒	DT	NN
NP	⇒	NP	PP
PP	⇒	IN	NP

Vi	⇒	sleeps
Vt	⇒	saw
NN	⇒	man
NN	⇒	woman
NN	⇒	telescope
DT	⇒	the
IN	⇒	with
IN	⇒	in

Note: S=sentence, VP=verb phrase, NP=noun phrase, PP=prepositional phrase, DT=determiner, Vi=intransitive verb, Vt=transitive verb, NN=noun, IN=preposition

More about Heads

- Each context-free rule has one “special” child that is the head of the rule. e.g.,

S	⇒	NP	VP	(VP is the head)	
VP	⇒	Vt	NP	(Vt is the head)	
NP	⇒	DT	NN	NN	(NN is the head)

- A core idea in linguistics
(X-bar Theory, Head-Driven Phrase Structure Grammar)
- Some intuitions:
 - The central sub-constituent of each rule.
 - The semantic predicate in each rule.

Rules which Recover Heads: An Example of rules for NPs

If the rule contains NN, NNS, or NNP:

Choose the rightmost NN, NNS, or NNP

Else If the rule contains an NP: Choose the leftmost NP

Else If the rule contains a JJ: Choose the rightmost JJ

Else If the rule contains a CD: Choose the rightmost CD

Else Choose the rightmost child

e.g.,

NP	⇒	DT	NNP	NN
NP	⇒	DT	NN	NNP
NP	⇒	NP	PP	
NP	⇒	DT	JJ	
NP	⇒	DT		

Rules which Recover Heads: An Example of rules for VPs

If the rule contains Vi or Vt: Choose the leftmost Vi or Vt

Else If the rule contains an VP: Choose the leftmost VP

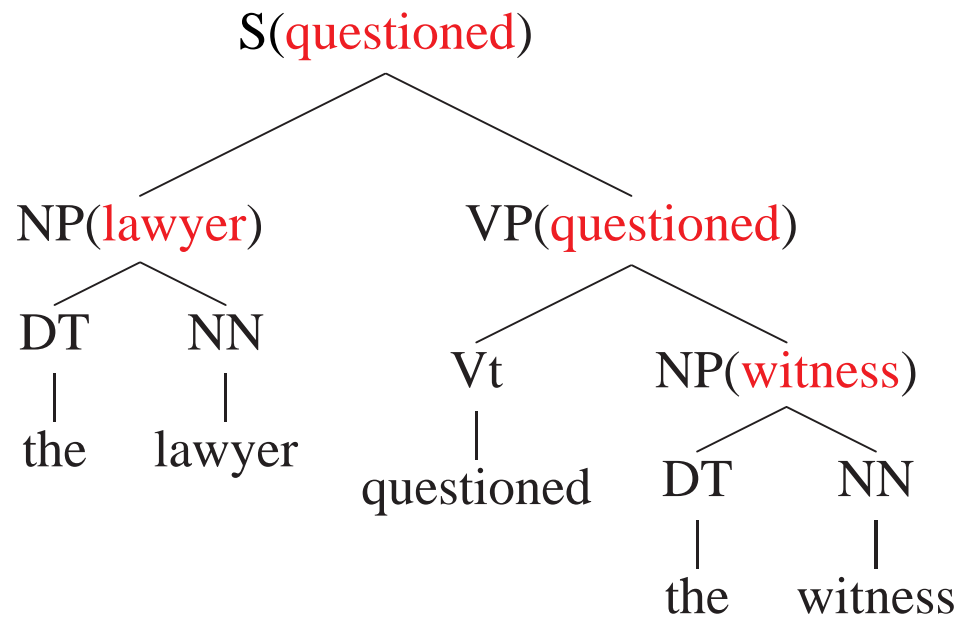
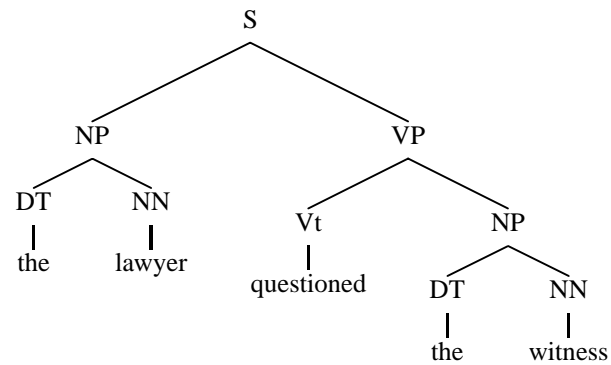
Else Choose the leftmost child

e.g.,

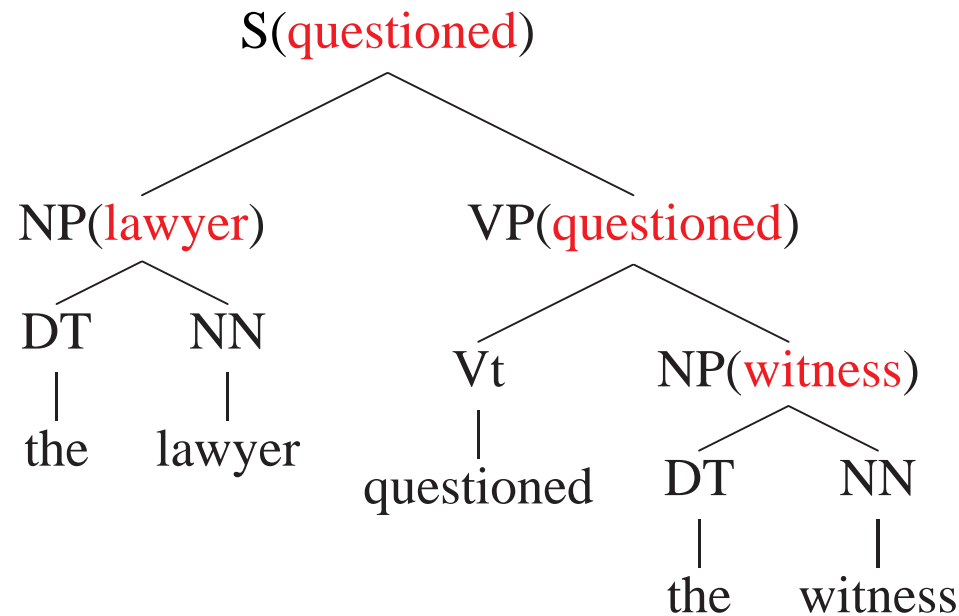
VP \Rightarrow Vt NP

VP \Rightarrow VP PP

Adding Headwords to Trees



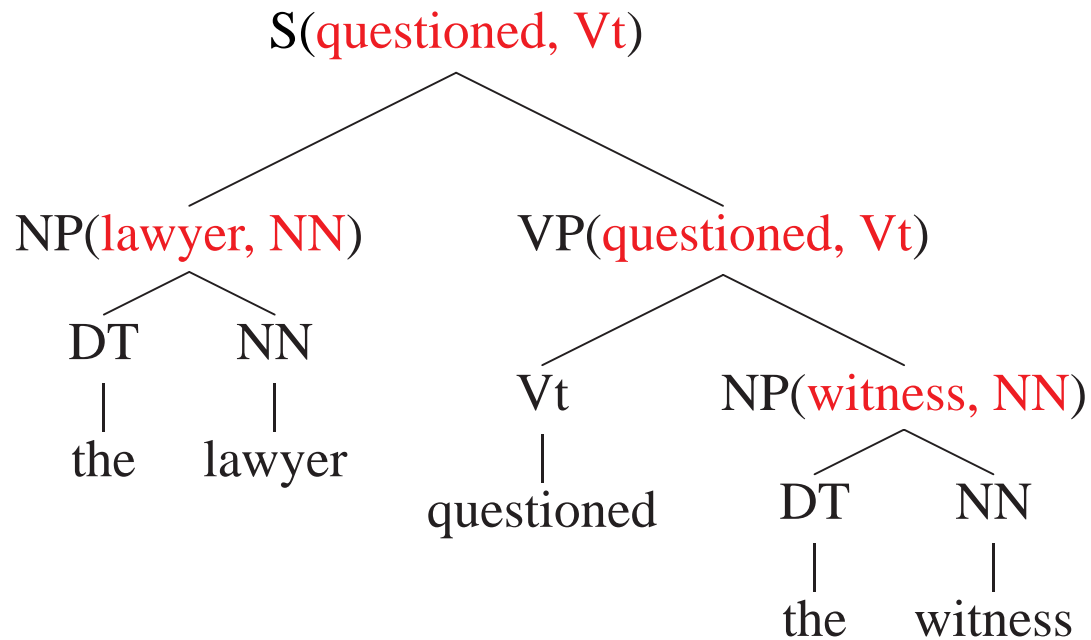
Adding Headwords to Trees



- A constituent receives its **headword** from its **head child**.

S	⇒	NP	VP	(S receives headword from VP)
VP	⇒	Vt	NP	(VP receives headword from Vt)
NP	⇒	DT	NN	(NP receives headword from NN)

Adding Headtags to Trees



-
- Also propagate **part-of-speech tags** up the trees (We'll see soon why this is useful!)

A Bottom-Up Chart Parser

- The main difference between top-down and bottom-up parser is the way the grammar rules are used
- The basic operation in bottom-up parsing is to take a sequence of symbols and match it to the right-hand side of the rules
 - rewrite a word by its possible lexical categories
 - replace a sequence of symbols that matches the right-hand side of the grammar rule by its left-hand side symbol
 - use a chart structure to keep track of the partial results, so that the work need not be reduplicated

A Bottom-Up Chart Parser (The Algorithm)

To add a constituent C from position p_1 to p_2 :

1. Insert C into the chart from position p_1 to p_2 .
2. For any active arc of the form $X \rightarrow X_1 \dots \circ C \dots X_n$ from position p_0 to p_1 , add a new active arc $X \rightarrow X_1 \dots C \circ \dots X_n$ from position p_0 to p_2 .
3. For any active arc of the form $X \rightarrow X_1 \dots X_n \circ C$ from position p_0 to p_1 , then add a new constituent of type X from p_0 to p_2 to the agenda.

Figure 3.10 The arc extension algorithm

Do until there is no input left:

1. If the agenda is empty, look up the interpretations for the next word in the input and add them to the agenda.
2. Select a constituent from the agenda (let's call it constituent C from position p_1 to p_2).
3. For each rule in the grammar of form $X \rightarrow C X_1 \dots X_n$, add an active arc of form $X \rightarrow \circ C X_1 \dots X_n$ from position p_1 to p_2 .
4. Add C to the chart using the arc extension algorithm above.

Figure 3.11 A bottom-up chart parsing algorithm

A Bottom-Up Chart Parser (An Example) 1/5

- Let's consider the sentence to be parsed:
 - ₁ *The* ₂ *large* ₃ *can* ₄ *can* ₅ *hold* ₆ *the* ₇ *water* ₈
- Lexicon:
 - the: ART
 - large: ADJ
 - can: N, AUX, V
 - hold: N, V
 - water: N, V
- Grammar:

1. $S \rightarrow NP VP$
2. $NP \rightarrow ART ADJ N$
3. $NP \rightarrow ART N$
4. $NP \rightarrow ADJ N$
5. $VP \rightarrow AUX VP$
6. $VP \rightarrow V NP$

A Bottom-Up Chart Parser (An Example) 2/5

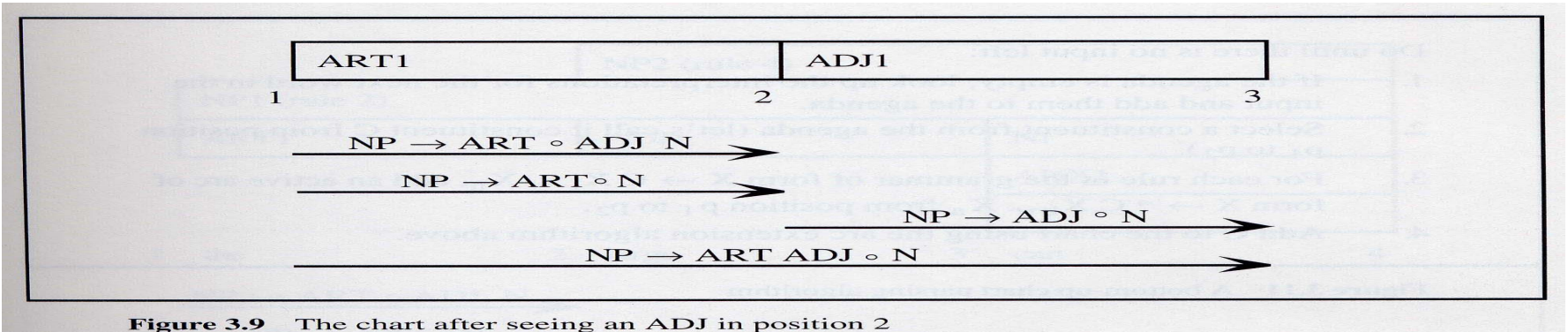


Figure 3.9 The chart after seeing an ADJ in position 2

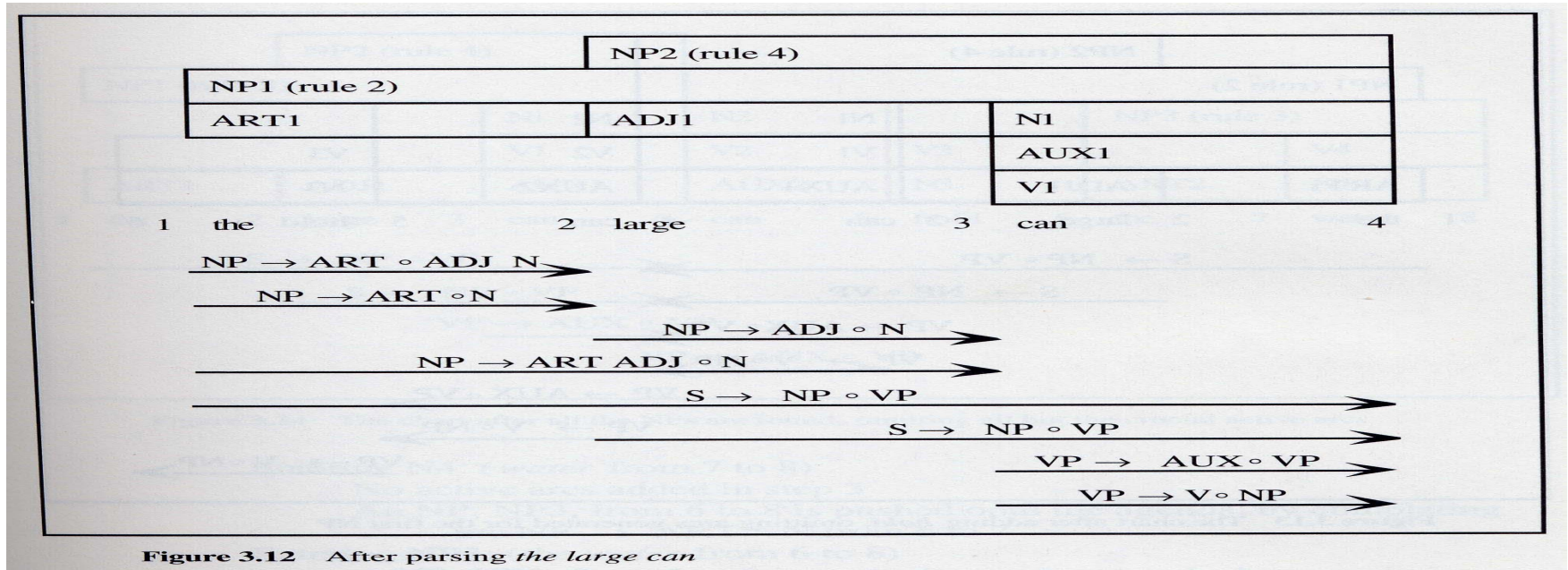


Figure 3.12 After parsing *the large can*

A Bottom-Up Chart Parser (An Example) 3/5

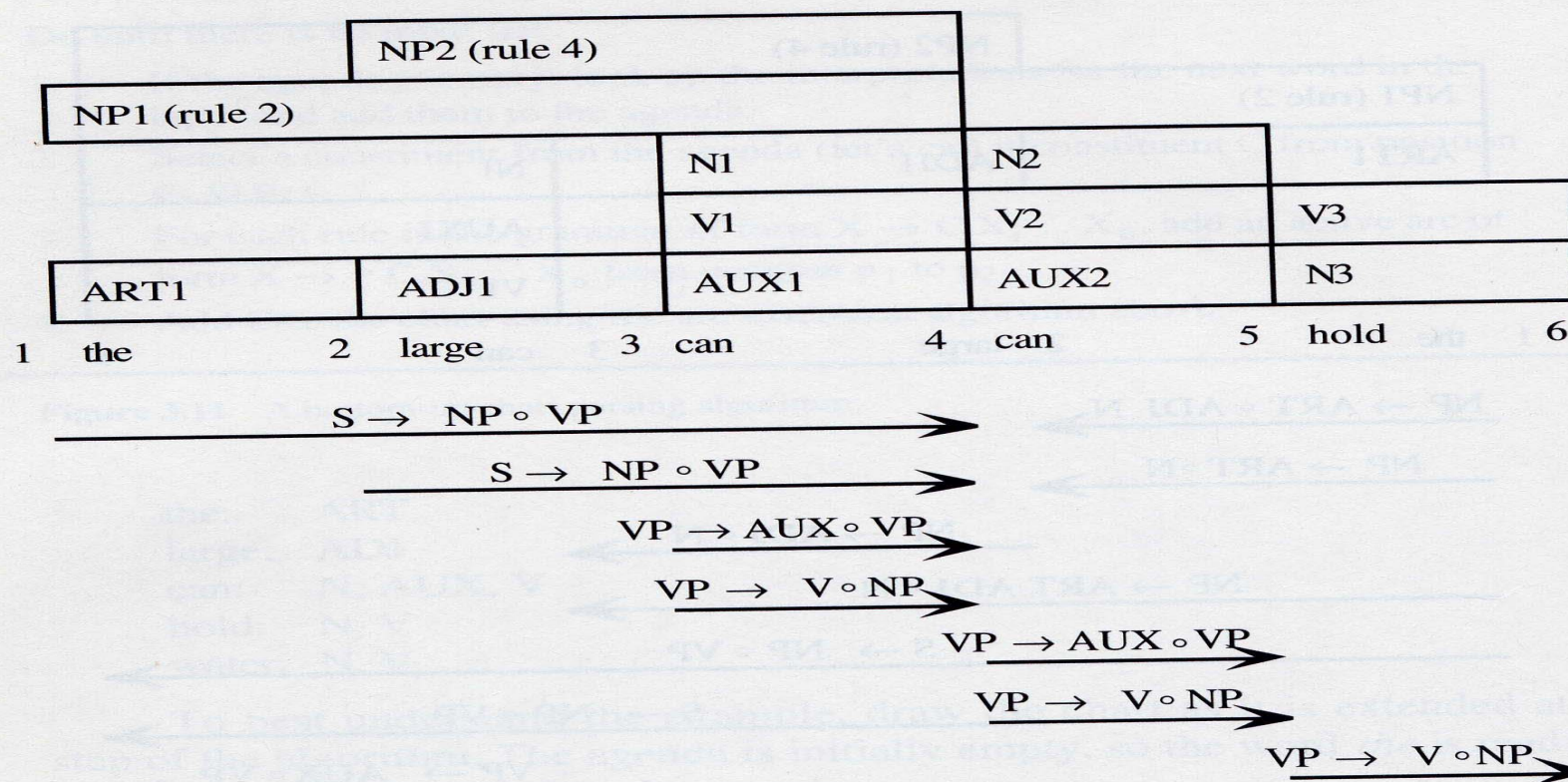


Figure 3.13 The chart after adding *hold*, omitting arcs generated for the first NP

A Bottom-Up Chart Parser (An Example) 4/5

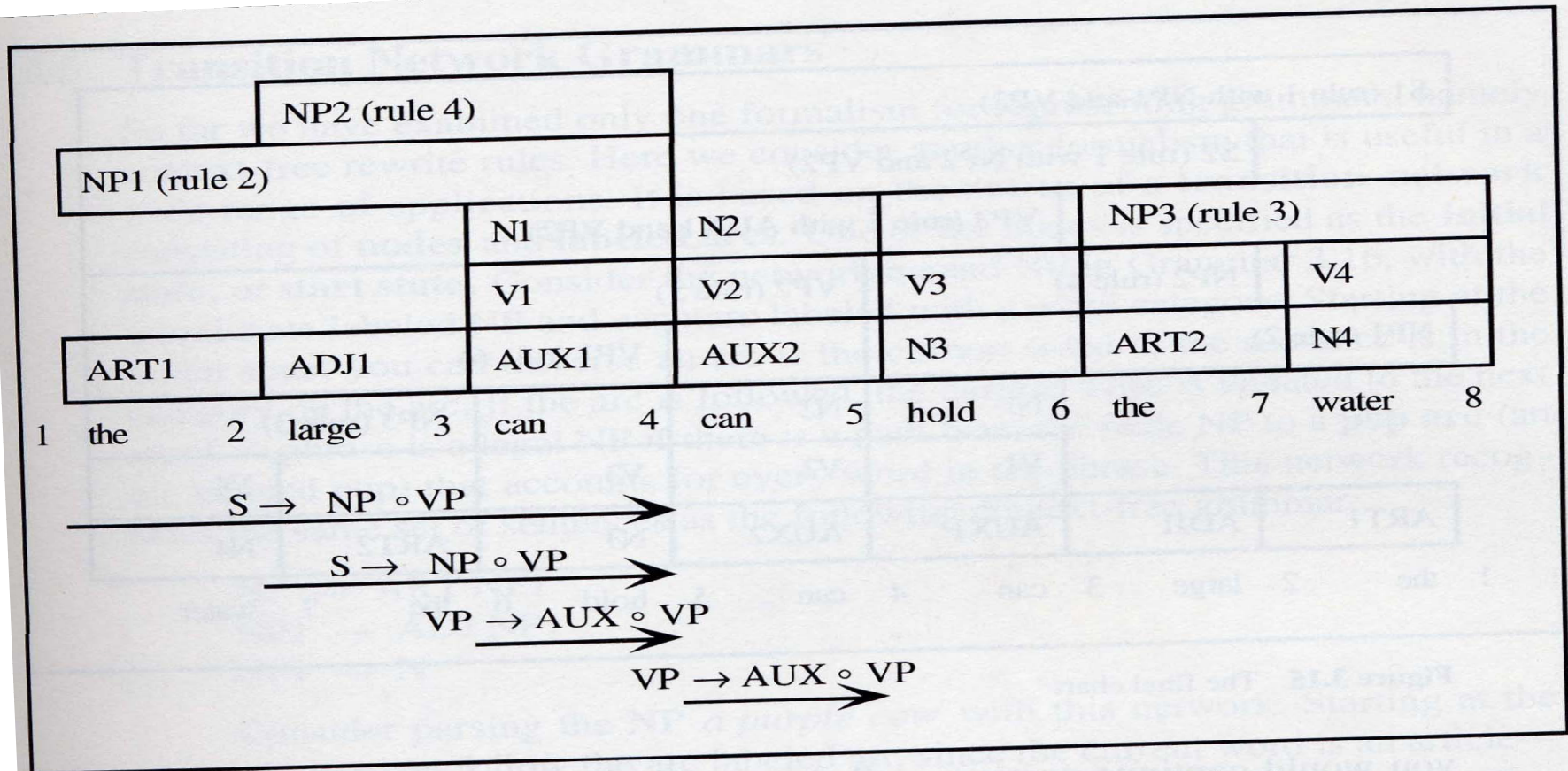


Figure 3.14 The chart after all the NPs are found, omitting all but the crucial active arcs

A Bottom-Up Chart Parser (An Example) 5/5

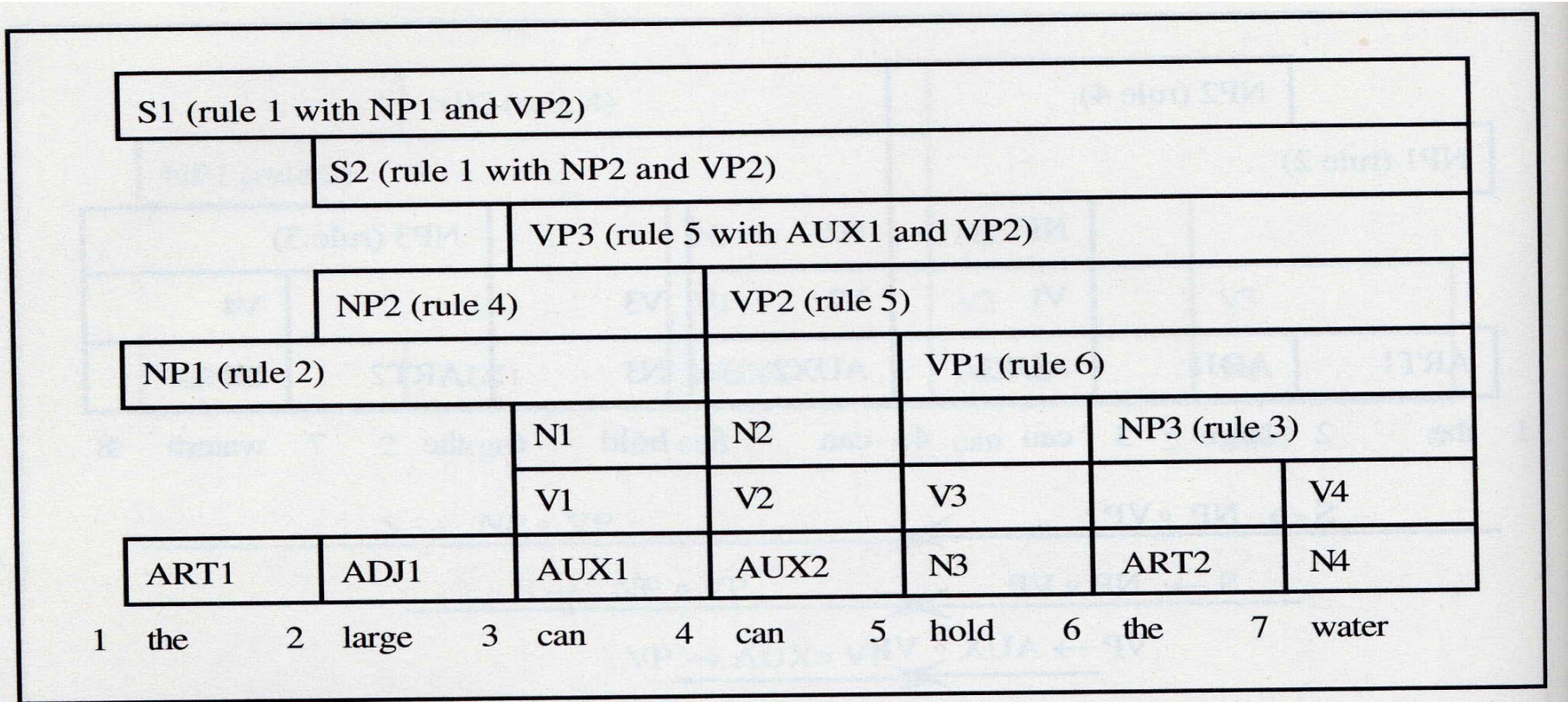


Figure 3.15 The final chart

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