# University of Pennsylvania Department of Electrical and System Engineering Digital Audio Basics 

- Exam ends at 5:50PM; begin as instructed (target 4:35PM)
- Do not open exam until instructed to begin exam.
- Problems weighted as shown.
- Calculators allowed.
- Closed book $=$ No text or notes allowed.
- Provided reference materials on next to last page.
- Show work for partial credit consideration.
- Unless otherwise noted, answers to two significant figures are sufficient.
- Sign Code of Academic Integrity statement (see last page for code).

I certify that I have complied with the University of Pennsylvania's Code of Academic Integrity in completing this exam.

## Name:

| 1 |  |  |  |  | 2 | 3 |  |  | 4 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| a | b | c | d | e |  | a | b | c | a | b | c | d |
| 3 | 3 | 3 | 3 | 3 | 15 | 5 | 3 | 2 | 2.5 | 2.5 | 2.5 | 2.5 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 5 |  | 6 | 7 |  | 8 |  |  |  | Tot | tal |
| a | b | c | d |  |  | a | b | c |  |  |  |  |
| 2 | 3 | 3 | 2 | 15 | 10 | 3 | 3 | 9 |  |  | 10 |  |
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1. Cat hearing ranges from 45 Hz to 64 KHz . Consider performing sound capture for cats.
(a) What is the minimum sample rate you should use to capture the full range of frequencies the cat can hear?
(b) What is the minimum period between samples at this rate?
(c) How many Bytes will it take to encode a 3-minute, single-channel (mono) "cat" song with 16b PCM samples?
(d) Given that human hearing goes to 22 KHz , how much more PCM data is required for a "cat" song than a human song? (State as a ratio.)
(e) Staying with PCM audio, how could you compress the cat song to guarantee to achieve the same data rate (bits/second) as human PCM audio? Is this lossy or lossless compression?
2. Consider the following sampling cases, complete the table entries.

3. While the cat can hear up to 64 KHz , it likely has similar critical band limitations to humans. Consider the hypothetical band structure shown on the facing page, and make the simplifying assumption that we only need to represent the strongest 4 frequencies in each band over a 25 ms time window to 4 Hz resolution. Assume 16b amplitude quantization for each frequency. Let's determine efficient frequency-band representations for discernable cat audio.
(a) Exploiting this structure, what do you store for each 25 ms window and how many bits does this require?
(b) How much compression does this achieve over the PCM samples for the same 25 ms window? (State as a ratio.)
(c) What kind of compression is this (lossless or lossy) and why?

Hypothetical cat auditory critical bands:

| Band Number | Low | High |
| ---: | ---: | ---: |
| 1 | 45 | 100 |
| 2 | 100 | 200 |
| 3 | 200 | 300 |
| 4 | 300 | 400 |
| 5 | 400 | 500 |
| 6 | 500 | 600 |
| 7 | 600 | 800 |
| 8 | 800 | 1200 |
| 9 | 1200 | 1500 |
| 10 | 1500 | 2000 |
| 11 | 2000 | 2500 |
| 12 | 2500 | 3000 |
| 13 | 3000 | 4000 |
| 14 | 4000 | 5000 |
| 15 | 5000 | 6000 |
| 16 | 7000 | 8500 |
| 17 | 8500 | 10000 |
| 18 | 10000 | 12000 |
| 19 | 12000 | 15000 |
| 20 | 15000 | 18000 |
| 21 | 18000 | 22000 |
| 22 | 22000 | 25000 |
| 23 | 25000 | 30000 |
| 24 | 30000 | 35000 |
| 25 | 35000 | 42000 |
| 26 | 42000 | 46000 |
| 27 | 46000 | 50000 |
| 28 | 50000 | 56000 |
| 29 | 56000 | 60000 |
| 30 | 60000 | 64000 |

While the cat auditory range to $64,000 \mathrm{~Hz}$ is real. This auditory band structure is a synthetic construct generated just for this problem and likely does not represent reality.
4. Consider the following set of sounds that occur simultaneously. Identify which sounds a human is likely to hear and explain why or why not. (read through all 4 sounds before starting your answers.)
(a) Soft $(25 \mathrm{~dB})$ cat purrs at 150 Hz
(b) Loud ( 80 dB ) mechanical squeek at 30 KHz
(c) Moderate $(60 \mathrm{~dB})$ child yelling at 2200 Hz
(d) Soft $(30 \mathrm{~dB})$ cat meow at 2100 Hz
5. Consider the following Claude Shannon quote:

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Thus we may have knowledge of the past but cannot control it;
we may control the future but have no knowledge of it.
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Including spaces and punctuation, the quote has 116 total symbols (and 26 unique symbols).
(a) If we give every symbol the same number of bits, how many bits do we need to encode each symbol?
(b) For a variable length symbol encoding, which symbol should get the fewest bits? (and why?)
(c) For a variable length symbol encoding, which symbol could get the most bits? (and why?)
(d) Is variable length symbol encoding a lossy or lossless compression scheme? (why?)
6. Given a signal with 3 frequencies, 250 Hz (amplitude $1 / 2$ ), 1400 Hz (amplitude $1 / 4$ ), and 8000 Hz (amplitude 1), that can be represented as sine waves starting at $t=0$, what is the amplitude of the temporal waveform at each of the following time points?

| Time | Amplitude |
| ---: | ---: |
| 0.02 ms |  |
| 1.00 ms |  |
| 2.37 ms |  |

7. A curious engineer with several cats would like to know what her cats hear (are they reacting to sounds she cannot hear? do they talk to each other above the range of her hearing?) Making the same assumptions about cat hearing from Problems 1 and 3, describe how she could build a cat-sound translator that converts the full range of cat-audible sounds into human-audible sounds.
8. Audio forensics (think Sherlock Holmes, CSI) may not find conventional MP3 encodings as useful as standard Compact-Disc (44KHz sample rate) PCM encodings or even analog recordings. [Assume the analog recording is a perfect capture of the original continuous sound waveform at the point of the recording microphone.]
(a) Of the three, which would capture a high pitched sound (e.g. 30KHz)? For each, why or why not?
i. MP3 encoded
ii. PCM encoded with 44 KHz samples, anti-alias input filtering
iii. analog recording
(b) Of the three, which might be able to recover a whispered conversation happening further from the microphone than a loud conversation? For each, why or why not?
i. MP3 encoded
ii. PCM encoded with 44 KHz samples, anti-alias input filtering
iii. analog recording
(c) Assuming you are willing to store information at a variable data rate (unlike MP3s), want to preserve any potential signal up to 120 KHz , but also want to minimize bits used (equivalently, maximize the time period you can store on 1TB of storage), describe a sampling, transformation, compression, and storage strategy.

Human auditory critical bands:

| Band Number | Low | High |
| ---: | ---: | ---: |
| 1 | 20 | 100 |
| 2 | 100 | 200 |
| 3 | 200 | 300 |
| 4 | 300 | 400 |
| 5 | 400 | 510 |
| 6 | 510 | 630 |
| 7 | 630 | 720 |
| 8 | 720 | 920 |
| 9 | 920 | 1080 |
| 10 | 1080 | 1370 |
| 11 | 1270 | 1480 |
| 12 | 1480 | 1720 |
| 13 | 1720 | 2000 |
| 14 | 2000 | 2320 |
| 15 | 2320 | 2700 |
| 16 | 2700 | 3150 |
| 17 | 3150 | 3700 |
| 18 | 3700 | 4400 |
| 19 | 4400 | 5300 |
| 20 | 5300 | 6400 |
| 21 | 6400 | 7700 |
| 22 | 7700 | 9500 |
| 23 | 9500 | 12000 |
| 24 | 12000 | 15500 |
|  |  |  |

## Code of Academic Integrity

Since the University is an academic community, its fundamental purpose is the pursuit of knowledge. Essential to the success of this educational mission is a commitment to the principles of academic integrity. Every member of the University community is responsible for upholding the highest standards of honesty at all times. Students, as members of the community, are also responsible for adhering to the principles and spirit of the following Code of Academic Integrity.*

Academic Dishonesty Definitions
Activities that have the effect or intention of interfering with education, pursuit of knowledge, or fair evaluation of a students performance are prohibited. Examples of such activities include but are not limited to the following definitions:
A. Cheating Using or attempting to use unauthorized assistance, material, or study aids in examinations or other academic work or preventing, or attempting to prevent, another from using authorized assistance, material, or study aids. Example: using a cheat sheet in a quiz or exam, altering a graded exam and resubmitting it for a better grade, etc.
B. Plagiarism Using the ideas, data, or language of another without specific or proper acknowledgment. Example: copying another persons paper, article, or computer work and submitting it for an assignment, cloning someone elses ideas without attribution, failing to use quotation marks where appropriate, etc.
C. Fabrication Submitting contrived or altered information in any academic exercise. Example: making up data for an experiment, fudging data, citing nonexistent articles, contriving sources, etc.
D. Multiple Submissions Multiple submissions: submitting, without prior permission, any work submitted to fulfill another academic requirement.
E. Misrepresentation of academic records Misrepresentation of academic records: misrepresenting or tampering with or attempting to tamper with any portion of a students transcripts or academic record, either before or after coming to the University of Pennsylvania. Example: forging a change of grade slip, tampering with computer records, falsifying academic information on ones resume, etc.
F. Facilitating Academic Dishonesty Knowingly helping or attempting to help another violate any provision of the Code. Example: working together on a take-home exam, etc.
G. Unfair Advantage Attempting to gain unauthorized advantage over fellow students in an academic exercise. Example: gaining or providing unauthorized access to examination materials, obstructing or interfering with another students efforts in an academic exercise, lying about a need for an extension for an exam or paper, continuing to write even when time is up during an exam, destroying or keeping library materials for ones own use., etc.

* If a student is unsure whether his action(s) constitute a violation of the Code of Academic Integrity, then it is that students responsibility to consult with the instructor to clarify any ambiguities.

