

ESE150 Spring 2022

**ESE**

Lecture #11 – Psychoacoustic Model/Compression/MP3

**ESE 150 – DIGITAL AUDIO BASICS**

Based on slides © 2009–2022 DeHon, Koditschek  
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**FIRST MP3 PLAYER**

- × **MpMan -- 1998**
- × **SaeHan Information Systems**
  - + South Korea
- × **32MB of Flash memory**

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**FLASH SCALING**

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**FLASH SCALING**

Transistor Count Trends

Sources: Intel, SIA, Wikichip, IC Insights

<https://www.icinsights.com/news/bulletins/Transistor-Count-Trends-Continue-To-Track-With-Moores-Law/>

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**PCM AND CD AUDIO**

- × **PCM – Pulse Code Modulation**
  - + CD-Quality Audio – state-of-the-art 1990s
    - Filtering/Sampling/Quantizing/Encoding using ADC
    - DAC/Reconstruction Filter
  - + CD Quality Digital Audio uses PCM (uncompressed, lots of storage!)
    - 44,100 samples per second, each sample 16-bits
    - 1 sec. of music:  $44,100 \times 16\text{bits} = 705,600 \text{ bits or } 86 \text{ kB}$
    - 60 seconds of music:  $705,600 \times 60 = 42,336,000 \text{ bits} = 5167 \text{ kB} = 5 \text{ MB}$
    - 3 minute song:  $42,336,000 \times 3 = 127,008,000 \text{ bits} = 15 \text{ MB}!$
    - You want it in stereo???  $15 \text{ MB} \times 2 = 30 \text{ MB}!$  (no compression!)

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**OBSERVE**

- × **If we kept the CD Audio encoding format**
  - + Could hold **one** song on the 1998 MpMan
  - + (maybe 2 on the 64MB version)
- × **For solid-state audio to be viable**
  - + Needed more compact encoding for music

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## FIRST MP3 PLAYER

- × **MpMan -- 1998**
- × **SaeHan Information Systems**
  - + South Korea
- × **32MB of Flash memory**
- × **Held 6 songs (MP3)**
- × **(12 on 64MB version)**
- × **3 years before Apple iPod**
  - + October 2001
  - + Initially hard disk
- × **Diamond Rio later 1998**



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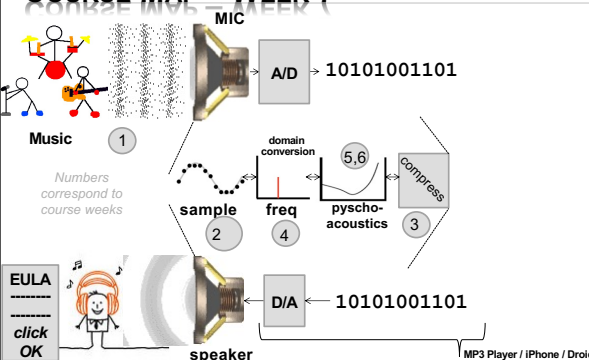
## LECTURE TOPICS

- × **Teaser**
- × **Where are we?**
- × **Preclass**
- × **How do we take advantage of psychoacoustics in MP3**  
Achieve this 6—12x reduction from CD Audio
  - + Review Tricks
  - + Formulate Optimization
  - + Adaptation (next Friday)
- × **Next Lab**
- × **References**

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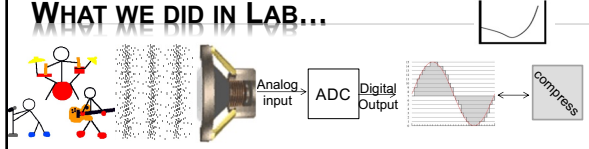
## COURSE MAP – WEEK 7



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## WHAT WE DID IN LAB...



- × **Week 1: Converted Sound to analog voltage signal**
  - a "pressure wave" that changes air molecules w/ respect to time
  - a "voltage wave" that changes amplitude w/ respect to time
- × **Week 2: Sampled voltage, then quantized it to digital sig.**
  - **Sample:** Break up independent variable, take discrete 'samples'
  - **Quantize:** Break up dependent variable into n-levels (need 2<sup>n</sup> bits to digitize)
- × **Week 3: Compress digital signal**
  - Use even less bits without using sound quality!
- × **Week 4: Before we compress...**
  - Put our 'digital' data into another form...BEFORE we compress...less stuff to compress!
- × **Week 5: Psychoacoustics**
  - Measured limits of human hearing; measured masking

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## COMPARE TO LAB

- × **Lab 6**
  - + Capture spirit of reducing frequencies
  - + Simplified – only taking loudest fraction in each band
    - Rather than being rigorous about masking
    - Or trying to hit some fixed rate
- × **Lecture 11 & 12 (this week)**
  - + Help understand more what real MP3 encoding looks like
  - + Thinking about fixed rate
    - And adaptation for variable rate encoding from Huffman
  - + Formulating masking more explicitly
    - But still simplistic
  - + Illustrating Optimization Approaches

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## PRECLASS

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## PRECLASS

- × 4 critical bands
- × 10 frequencies
- × 16b amplitude
- × **Preclass 1: Bits to represent (no further encode)?**

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## PRECLASS

- × 4 critical bands
- × 10 frequencies
- × 16b amplitude
- × 107b encoding budget
- × **Preclass 2: amplitude quantization necessary to achieve budget?**
- × **Preclass 3: frequencies (reduced sampling rate) can keep to achieve budget?**

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## PRECLASS

- × 4 critical bands
- × 10 frequencies
- × 16b amplitude
- × 107b encoding budget
- × **Preclass 4**
  - + Bits to represent which frequency?
  - + Bits to encode (frequency, amplitude) pair?
  - + Number of (frequency, amplitude) pairs fit within budget?

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## PRECLASS

- × 4 critical bands
- × 10 frequencies
- × 16b amplitude
- × 107b encoding budget
- × **Preclass 5**
  - + Which frequencies do we keep?

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## PRECLASS

- × 4 critical bands
- × 10 frequencies
- × 16b amplitude
- × 107b encoding budget
- × **Preclass 6: which likely to sound best?**
  - + Amplitude quantization
  - + Frequency quantization (reduce sampling rate)
  - + Frequency selection based on masking

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## TRICKS FOR COMPRESSION

- × **Quantization**
- × **Sampling Rate / Frequency Quantization**
- × **Critical Band Masking**
  - + Selective frequency dropping

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# BACKGROUND

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## THE MPEG-1 STANDARD

- × **ISO (International Standards Organization)**
  - + Looking for ways to reduce transmission requirements for digital video and audio (low bandwidth transmission of digital media)
  - + 1988 – establishes a sub-committee of ISO:
    - × Moving Picture Experts Group (MPEG)
    - × Goal: Develop common standard for coding/compressing audio/video
      - × To reduce size of data to transmit without sacrificing quality
      - × Fraunhofer Institute and German University of Erlangen
        - × Lots of basic research in Digital Audio Broadcast, tapped to be MPEG
  - + Result: 1992: Finalized Standard called: MPEG-1 (Phase I)
    - × 3 Parts: Audio/Video/System
    - × Audio component: defined 3 layers: 1, 2, 3
      - × Increasing levels of compression and complexity
      - × **MPEG-1, layer 3 achieves 12:1 compression ratio! (for short MP3)**

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## THE MPEG-1 STANDARD

- × **MPEG-1, (3) Layers for Audio Coding:**

|              | Coding          | Ratio | Required bitrate |
|--------------|-----------------|-------|------------------|
| Complexity ↓ | PCM CD Quality  | 1:1   | 1.4 Mbps         |
|              | Layer I         | 4:1   | 384 kbps         |
|              | Layer II        | 8:1   | 192 kbps         |
|              | Layer III (MP3) | 12:1  | 128 kbps         |

- × **Why is PCM CD Quality 1.4 Mbps?**
  - + Recall: 1 sec. of music:  $44,100 \times 16\text{bits} = 705,600$  bits
  - + Don't forget stereo (R/L):  $2 \times 706,600 = 1,413,200$  (1.4Mbs)
    - × Defines bandwidth requirements of network
  - + Notice: 128 kbps was just about double modem speed in 1992
    - × Enables transmission of audio (MP3) via modem!

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## BIG PICTURE: WHY CARE

- × **MP3 shows**
  - + We can reduce bits needed to adequately represent music by 12x over PCM samples
- × **1998**
  - + Necessary to make MP3 player viable at all on 32MB Flash memory
    - × Small, affordable by masses
  - + Also meant lower bandwidth to stream
- × **2006**
  - + Necessary to make Spotify streaming viable
- × **2021**
  - + With 64GB phones, maybe not essential for music on iPhone, but...

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## BIG PICTURE: WHY CARE

- × **Networks / Internet bandwidth / Cell capacity**
  - + Allows us to reduce bandwidth needed for audio
  - + Alternative is
    - × Building out more wires and capacity
    - × Fewer cell calls supported simultaneously in a region
  - + Being efficient with bits
    - × Reduces physical investment needed in wires
- × **Same ideas enable video**
  - + Viable to store (many) hours of video on phone/tablet
    - × Of increasing resolution: HD, 4K...
  - + Viable to stream video into homes
  - + Zoom, Netflix, AppleTV, ... all enabled by compression

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Part 2

## OPTIMIZING ENCODING

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## KNOBS WE CAN TURN

- × Amplitude quantization
- × Frequency quantization
- × Frequencies kept (per critical band)
  - + Too soft
  - + Masked
- × ...and can perform lossless compression

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## BANDS VARY IN IMPORTANCE

- × Not equally sensitive across bands
- × If quantize bands differently, where want finer resolution?
- × Where tolerate more quantization?

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## KNOBS WE CAN TURN

- × Amplitude quantization
  - + Per band
- × Frequency quantization
  - + Per band?
- × Frequencies kept (per critical band)
  - + Per band
- × ...and can perform lossless compression

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## OPPORTUNITIES/CHALLENGES

- × Trying to hit fixed bit rate, what challenge does lossless compression impose?
  - + Encounter many common frequencies, amplitudes?
  - + Encounter many uncommon frequencies, amplitudes?
  - + Hint: what did we see in Lab 3 for time samples?

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## OPPORTUNITIES/CHALLENGES

- × What challenge/opportunities might these band spectra represent?

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## SUGGEST

- × May want to do something smarter than
  - + Allocating fixed number of frequencies per band
  - + Allocating fixed quantization to a band
- × Like to adapt our encoding to the data
  - + If more Huffman compressible, we get more frequencies
  - + If fewer frequencies suffice for one band,
    - × Allow more frequencies for another
    - × ...or allocate less quantization

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### OPTIMIZATION PROBLEM

- How fit in the resource constraints (128Kb/s) while maximizing goodness (sound quality)?

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### REMINDER: A WINDOW OPERATION

- In the example below, we traverse the signal but only look at 64 samples at a time

MP3: 26ms frames or 1,144 sample window  
(sepwww.stanford.edu/oldsep/hale/FftLab.html)

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### OPTIMIZATION PROBLEM

- How fit in the resource constraints (128Kb/s) while maximizing goodness (sound quality)?
  - + 128K/s \* 0.026 s = 3408 bits per 26ms frame
  - + 3408/2 = 1704 per stereo channel

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### OPTIMIZATION PROBLEM

- How fit in the resource constraints (128Kb/s) while maximizing goodness (sound quality)?
  - + 128K/s \* 0.026 s = 3408 bits per 26ms frame
  - + 3408/2 = 1704 per stereo channel
- Optimization problems central to engineering

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### OPTIMIZATION PROBLEM

- How fit in the resource constraints (128Kb/s = 3048 bits/frame) while maximizing goodness (sound quality)?
- Quantify bits used  $\sum_{bands} \sum_{f \in freqs} Bits(f)$
- Quantify goodness  $\sum_{f \in freqs} Error(f) \times W(f)$

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### QUANTIFYING BIT COST

- Simple, fixed sample: Frequencies \* Bits/freq
- Fixed frequencies per Band:
  - + Bands \* (Frequencies/Band) \* Bits/freq
- Variable Frequencies per Band:  $\sum_{b \in bands} frequencies(b) \times (bits/freq)$
- Variable Frequencies and quantization per Band:  $\sum_{b \in bands} frequencies(b) \times bit(b)$
- Huffman means different bits/frequency  $\sum_{bands} \sum_{f \in freqs} Bits(f)$

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## GOODNESS/SOUND QUALITY

- × **Error(Amp) = |Orig Amplitude – Encoded|**
  - + Whole OrigAmplitude if dropped
  - + |Orig Amplitude-Quantize(OrigAmplitude,bits)| if quantized
- × **W(freq)**
  - + 0 if below hearing threshold
  - + 0 if masked
  - + Value between 0 and 5 if partially masked in critical band
    - × More critical bands, higher
  - + Really depend on what already encoded

$$\sum_{f \in freqs} Error(f) \times W(f)$$

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## OPTIMIZATION PROBLEM

- × **How fit in the resource constraints (128Kb/s) while maximizing goodness (sound quality)?**
- × **Quantify bits used:**

$$\sum_{bands} \sum_{f \in freqs} Bits(f)$$
  - + Cannot exceed 128Kb/s
  - + = 3,408 b / 26ms frame
- × **Quantify goodness: minimize**

$$\sum_{f \in freqs} Error(f) \times W(f)$$

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## PROBLEM FORMULATION

- × **How fit in the resource constraints (128Kb/s) while maximizing goodness (sound quality)?**
- × **Quantify bits used:**

$$\sum_{bands} \sum_{f \in freqs} Bits(f)$$
  - + Cannot exceed 128Kb/s
  - + = 3,408 b / 26ms frame
- × **Quantify goodness: minimize**

$$\sum_{f \in freqs} Error(f) \times W(f)$$

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## FORMULATION VS. SOLUTION

- × **Formulation – goal – formally what want to achieve**
  - + Today's focus
- × **Solution – how go about solving it**
  - + How achieve (minimize) constraints (costs) in formulation
  - + More on Wednesday

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## MOVES

- × **Select a frequency to encode**
  - + Main example today
- × **Assign more bits to a band for quantization**

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(as time permits)

## APPROACH

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### APPROACH

- Start with nothing
- Start with bitbudget

$$\sum_{bands} \sum_{f \in freqs} Bits(f)$$

$$\sum_{f \in freqs} Error(f) \times W(f)$$

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### EXAMPLE WEIGHT FUNCTION W(F)

- $W(f) = CBWeight * Mask$
- Mask = 0 if MaxAmp-FreqAmp > 3
- Mask = 1 otherwise

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### APPROACH

- Start with nothing
- Start with bitbudget

$$\sum_{bands} \sum_{f \in freqs} Bits(f)$$

$$\sum_{f \in freqs} Error(f) \times W(f)$$

|          |        |        |        |        |    |
|----------|--------|--------|--------|--------|----|
|          | Band 0 | Band 1 | Band 2 | Band 3 |    |
| sum      | 14     | 13     | 13     | 6      | 41 |
| weight   | 3      | 5      | 5      | 3      | 18 |
| weighted | 42     | 65     | 65     | 18     |    |

Bits = 0  
Error = 190

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### APPROACH

- Start with nothing
- Start with bitbudget
- While(bitbudget > 0)
  - Identify Largest Error component:  $Error(freq) \times W(freq)$
  - What do to reduce error?

$$\sum_{bands} \sum_{f \in freqs} Bits(f)$$

$$\sum_{f \in freqs} Error(f) \times W(f)$$

|          |        |        |        |        |    |
|----------|--------|--------|--------|--------|----|
|          | Band 0 | Band 1 | Band 2 | Band 3 |    |
| sum      | 11     | 8      | 2      | 11     | 41 |
| weight   | 3      | 5      | 5      | 3      | 18 |
| weighted | 33     | 40     | 10     | 33     |    |

Bits = 0  
Error = 190

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### APPROACH

- Start with nothing
- Start with bitbudget

$$\sum_{bands} \sum_{f \in freqs} Bits(f)$$

$$\sum_{f \in freqs} Error(f) \times W(f)$$

|          |        |        |        |        |    |
|----------|--------|--------|--------|--------|----|
|          | Band 0 | Band 1 | Band 2 | Band 3 |    |
| sum      | 11     | 8      | 2      | 11     | 41 |
| weight   | 3      | 5      | 5      | 3      | 18 |
| weighted | 33     | 40     | 10     | 33     |    |

Assume 8 levels  
Bits = 3+6=9  
Error = 125

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### APPROACH

- Start with nothing
- Start with bitbudget
- While(bitbudget > 0)
  - Identify Largest Error component:  $Error(freq) \times W(freq)$
  - What do to reduce error?

$$\sum_{bands} \sum_{f \in freqs} Bits(f)$$

$$\sum_{f \in freqs} Error(f) \times W(f)$$

|          |        |        |        |        |    |
|----------|--------|--------|--------|--------|----|
|          | Band 0 | Band 1 | Band 2 | Band 3 |    |
| sum      | 11     | 8      | 2      | 11     | 41 |
| weight   | 3      | 5      | 5      | 3      | 18 |
| weighted | 33     | 40     | 10     | 33     |    |

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