























| Dee | montion | Continu | (h. a | | |
|---|--|--|---|---|--|
| Pro | perues (| Continu | ea) | | |
| | | | | | |
| Time- Reversal and Complex Conjugation | $\bar{x}^*[-n]$ | $\tilde{X}^*[k]$ | Time- Reversal and Complex Conjugation | $x'[((-n))_x]$ | X'[k] |
| Real Part | $\operatorname{Re}\{\hat{x}[n]\}$ | $\widetilde{X}_{cp}[k] = \frac{1}{2} \left(\widetilde{X}[k] + \widetilde{X}^*[-k] \right)$ | Real Part | Re[x[n]] | $\boldsymbol{X}_{\sigma}[k] \!=\! \frac{1}{2} \left(\boldsymbol{X}[k] \!+\! \boldsymbol{X}^*[((-k))_{\boldsymbol{X}}] \right)$ |
| Imaginary Part | $j \operatorname{Im}\{\tilde{x}[n]\}$ | $\widetilde{X}_{op}[k] = \frac{1}{2} \left(\widetilde{X}[k] - \widetilde{X}^*[-k] \right)$ | Imaginary Part | $j \ln\{s[n]\}$ | $X_{op}[k] = \frac{1}{2} \left(X[k] - X^*[((-k))_N] \right)$ |
| Even Part | $\widetilde{x}_{o}[n] = \frac{1}{2} \left(\widetilde{x}[n] + \widetilde{x}^*[-n] \right)$ | $Re{\overline{X}[k]}$ | Even Part | $x_{ip}[n] = \frac{1}{2} \left(x[n] + x^* [((-n))_N] \right)$ | $\operatorname{Re}\{X[k]\}$ |
| Odd Part | $\widetilde{x}_{op}[n] = \frac{1}{2} \left(\widetilde{x}[n] - \widetilde{x}^*[-n] \right)$ | $/ Im \{ \tilde{X}[k] \}$ | Odd Part | $x_{ip}[n] = \frac{1}{2} \Big(x[n] - x^* \big[((-n))_X \big] \Big)$ | $/\operatorname{Im}\{X[k]\}$ |
| Symmetry for Real Sequence | $\tilde{x}[u] = \tilde{x}^*[u]$ | $\begin{split} \widetilde{X}[k] &= \widetilde{X}^*[-k] \\ \left\{ \begin{array}{l} \operatorname{Re}[\widetilde{X}[k]] &= \operatorname{Re}[\widetilde{X}[-k]] \\ \operatorname{Im}[\widetilde{X}[k]] &= -\operatorname{Im}[\widetilde{X}[-k]] \\ \\ \left[\begin{array}{l} \widetilde{X}[k] &= \widetilde{X}[-k] \\ \\ \widetilde{X}[k] &= -\widetilde{X}[-k] \end{array} \right] \\ \end{array} \right. \end{split}$ | Symmetry for Real Sequence | $x[n] = x^*[n]$ | $\begin{split} & \boldsymbol{\chi}[k] = \boldsymbol{\chi}^* [((-k))_{\boldsymbol{\chi}}] \\ & \left[\begin{array}{c} \operatorname{Re} \{\boldsymbol{\chi}[k]\} = \operatorname{Re} \{\boldsymbol{\chi}[((-k))_{\boldsymbol{\chi}}]\} \\ \operatorname{Im} \{\boldsymbol{\chi}[k]\} = -\operatorname{Im} \{\boldsymbol{\chi}[((-k))_{\boldsymbol{\chi}}\}\} \\ & \left[\begin{array}{c} \boldsymbol{\chi}[k] = -\operatorname{Im} \{\boldsymbol{\chi}[((-k))_{\boldsymbol{\chi}}\} \\ \\ \boldsymbol{\zeta} \{k\} = -\boldsymbol{\zeta} \boldsymbol{\chi}[((-k))_{\boldsymbol{\chi}}] \end{array} \right] \end{split} \right] \end{split} $ |
| Parseval's Identity | $\begin{split} \sum_{n=0}^{N-1} \widetilde{X}_n [n] \widetilde{Y}_1^r[n] &= \frac{1}{N} \sum_{k=0}^{N-1} \widetilde{X}_n[k] \widetilde{X}_1^r[k] \\ \\ \sum_{n=0}^{N-1} [\widetilde{x}[n]]^2 &= \frac{1}{N} \sum_{k=0}^{N-1} [\widetilde{X}[k]]^2 \end{split}$ | | Parseval's Identity | $\sum_{a=0}^{N-1} x_a [w] w_2^*[a] = \frac{1}{N} \sum_{a=0}^{N-1} X_a [k] X_2^*[k]$ $\sum_{a=0}^{N-1} x[a] ^2 = \frac{1}{N} \sum_{a=0}^{N-1} X[k] ^2$ | |



























Linear Convolution

• We start with two non-periodic sequences:

 $x[n] \quad 0 \le n \le L - 1$

 $h[n] \quad 0 \le n \le P - 1$

E.g. x[n] is a signal and h[n] a filter's impulse response





















































