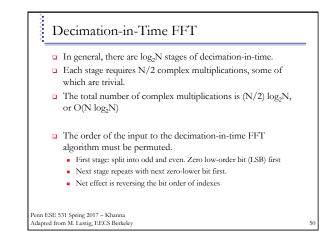


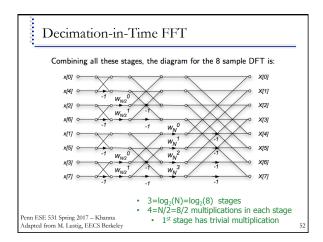
Decimation-in-Time FFT

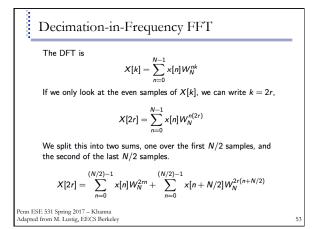
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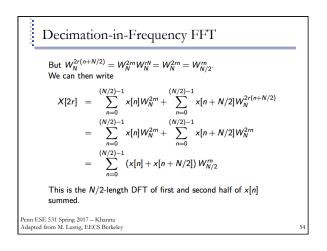
- □ In general, there are log₂N stages of decimation-in-time.
- Each stage requires N/2 complex multiplications, some of which are trivial.
- \square The total number of complex multiplications is $(N/2) \log_2 \! N,$ or $\mathrm{O}(N \log_2 \! N)$



Decimation-in-Time FFT					
This is illustrated in the following table for $N = 8$.					
	Decimal	Binary	Bit-Reversed Binary	Bit-Reversed Decimal	
	0	000	000	0	
	1	001	100	4	
	2	010	010	2	
	3	011	110	6	
	4	100	001	1	
	5	101	101	5	
	6	110	011	3	
	7	111	111	7	
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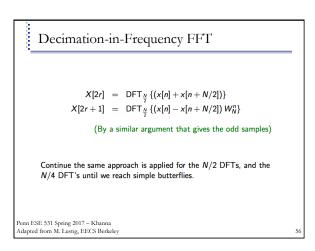


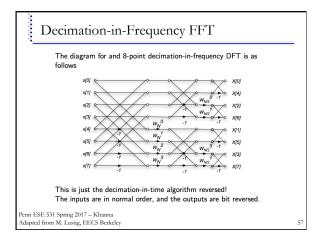


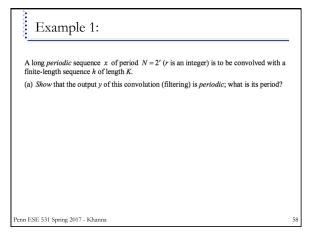
Decimation-in-Frequency FFT

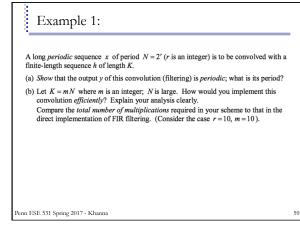
$$X[2r] = DFT_{\frac{N}{2}} \{(x[n] + x[n + N/2])\}$$
 $X[2r + 1] = DFT_{\frac{N}{2}} \{(x[n] - x[n + N/2]) W_N^n\}$

 (By a similar argument that gives the odd samples)









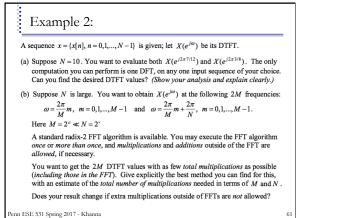
Example 2:

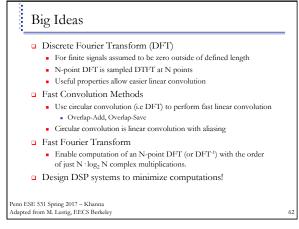
-

A sequence $x = \{x[n], n = 0, 1, ..., N - 1\}$ is given; let $X(e^{j\omega})$ be its DTFT.

(a) Suppose N = 10. You want to evaluate both X(e^{i2π/l2}) and X(e^{i2π/l2}). The only computation you can perform is one DFT, on any one input sequence of your choice. Can you find the desired DTFT values? (Show your analysis and explain clearly.)

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Admin Project Due 4/25 Penn ESE 531 Spring 2017 – Khana Adapted from M. Lustig, EECS Berkeley 63