



Example 2:

A sequence $x = \{x[n], n = 0, 1, ..., N - 1\}$ is given; let $X(e^{j\omega})$ be its DTFT.

(a) Suppose N = 10. You want to evaluate both X(e^{i2x7/l2}) and X(e^{i2x3/8}). The only computation you can perform is one DFT, on any one input sequence of your choice. Can you find the desired DTFT values? (Show your analysis and explain clearly.)

Penn ESE 531 Spring 2017 - Khanna

Example 2: A sequence $x = \{x[n], n = 0, 1, ..., N - 1\}$ is given; let $X(e^{j\omega})$ be its DTFT. (a) Suppose N = 10. You want to evaluate both $X(e^{j2\pi^{7/12}})$ and $X(e^{j2\pi^{3/8}})$. The only computation you can perform is one DFT, on any one input sequence of your choice.

Can you find the desired DTFT values? (Show your analysis and explain clearly.)
(b) Suppose N is large. You want to obtain X(e^{iw}) at the following 2M frequencies:

 $\omega = \frac{2\pi}{M}m, \ m = 0, 1, ..., M - 1$ and $\omega = \frac{2\pi}{M}m + \frac{2\pi}{N}, \ m = 0, 1, ..., M - 1.$

Here $M = 2^{\mu} \ll N = 2^{\nu}$

A standard radix-2 FFT algorithm is available. You may execute the FFT algorithm once or more than once, and multiplications and additions outside of the FFT are allowed, if necessary.

You want to get the 2M DTFT values with as few *total multiplications* as possible (*including those in the FFT*). Give explicitly the best method you can find for this, with an estimate of the *total number of multiplications* needed in terms of M and N.

Penn ESE 531 Spring 2017 - Khanna

Example 2:

A sequence $x = \{x[n], n = 0, 1, ..., N - 1\}$ is given; let $X(e^{j\omega})$ be its DTFT.

(a) Suppose N = 10. You want to evaluate both X(e^{i/2x7/12}) and X(e^{i/2x3/8}). The only computation you can perform is one DFT, on any one input sequence of your choice. Can you find the desired DTFT values? (Show your analysis and explain clearly.)

(b) Suppose N is large. You want to obtain
$$X(e^{j\omega})$$
 at the following 2M frequencies:
 $\omega = \frac{2\pi}{M}m, \ m = 0, 1, ..., M-1$ and $\omega = \frac{2\pi}{M}m + \frac{2\pi}{N}, \ m = 0, 1, ..., M-1.$

Here
$$M = 2^{\mu} \ll N = 2^{\nu}$$

A standard radix-2 FFT algorithm is available. You may execute the FFT algorithm once or more than once, and multiplications and additions outside of the FFT are allowed, if necessary.

You want to get the 2M DTFT values with as few total multiplications as possible (including those in the FFT). Give explicitly the best method you can find for this, with an estimate of the total number of multiplications needed in terms of M and N. Does your result change if extra multiplications outside of FFTs are not allowed?

Penn ESE 531 Spring 2017 - Khanna





























































35



- Devised a way to randomly sample 20% of the Nyquist required samples and still detect the tremor frequencies within 100mHz
 - Requires post processing to randomly sample!

Implementing Compressive Sampling

- Devised a way to randomly sample 20% of the Nyquist required samples and still detect the tremor frequencies within 100mHz
 - Requires post processing to randomly sample!
- Implement hardware on chip to "choose" samples in real time
 - Only write to memory the "chosen" samples
 - Design random-like sequence generator
 - Only convert the "chosen" samplesDesign low energy ADC

ł

Big Ideas

Compressive Sampling

- Integrated sensing/sampling, compression and processing
- Based on sparsity and incoherency

