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Solving Optimization Problems

general optimization problem

very difficult to solve

 $\bullet\,$ methods involve some compromise, $\mathit{e.g.},$ very long computation time, or not always finding the solution

exceptions: certain problem classes can be solved efficiently and reliably

- least-squares problems
- linear programming problems
- convex optimization problems

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amples

folio optimization

- ariables: amounts invested in different assets
- onstraints: budget, max./min. investment per asset, minimum return
- bjective: overall risk or return variance

ce sizing in electronic circuits

- ariables: device widths and lengths
- onstraints: manufacturing limits, timing requirements, maximum area
- bjective: power consumption
- fitting
- ariables: model parameters
- onstraints: prior information, parameter limits
- bjective: measure of misfit or prediction error

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Least-Squares Optimization

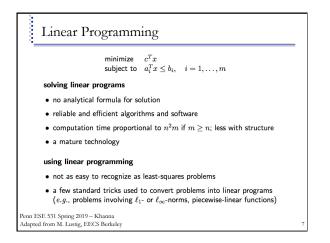
minimize $||Ax - b||_2^2$

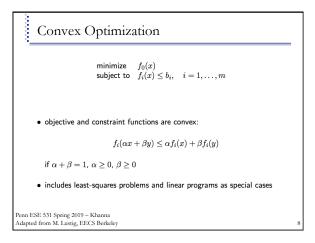
- solving least-squares problems
- analytical solution: $x^{\star} = (A^T A)^{-1} A^T b$
- reliable and efficient algorithms and software
- computation time proportional to n^2k ($A \in \mathbf{R}^{k imes n}$); less if structured
- a mature technology

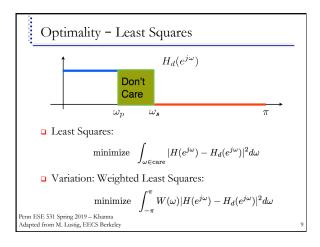
using least-squares

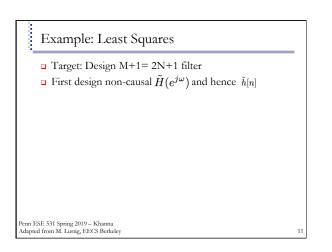
- · least-squares problems are easy to recognize
- a few standard techniques increase flexibility (e.g., including weights, adding regularization terms)

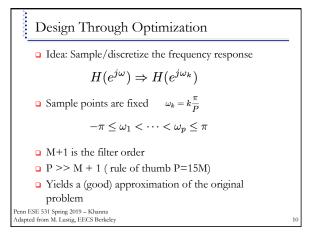
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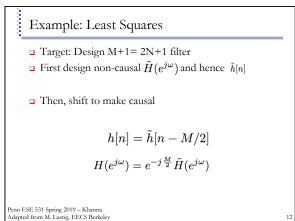


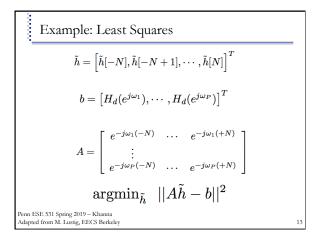


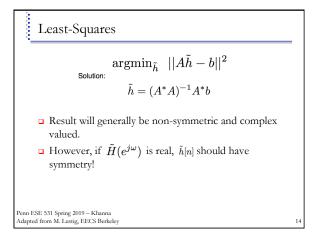


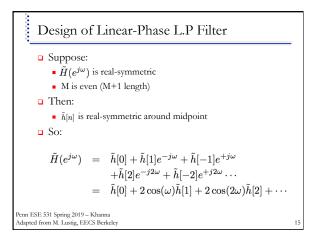


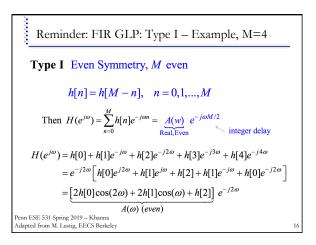


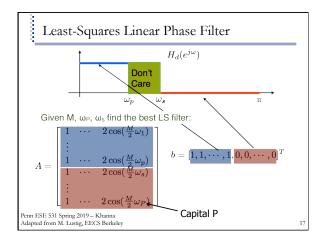


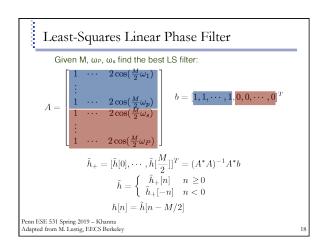


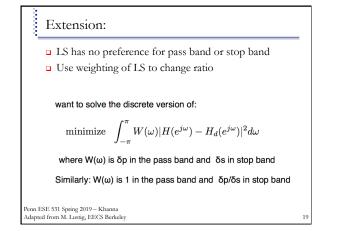


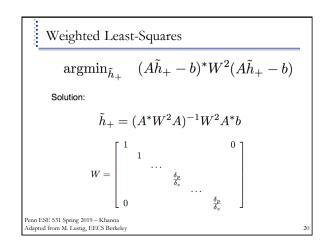












Parks-McClellan

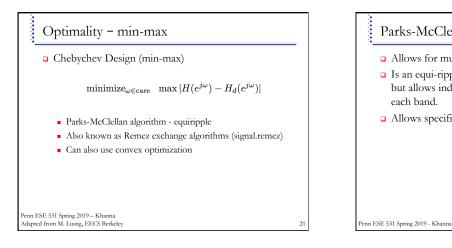
each band.

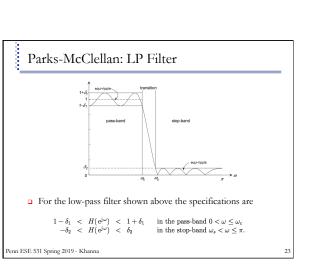
□ Allows for multiple pass- and stop-bands.

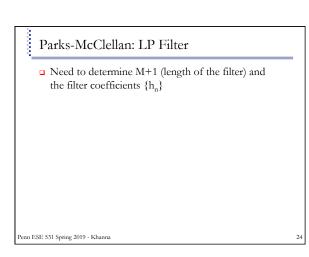
Allows specification of the band edges.

□ Is an equi-ripple design in the pass- and stop-bands,

but allows independent weighting of the ripple in







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Parks-McClellan: LP Filter
Reformulate

$$A_e(e^{j\omega}) = h_e[0] + \sum_{n=1}^{L} 2h_e[n] \cos(\omega n).$$

To fitting a polynomial
 $A_e(e^{j\omega}) = \sum_{k=0}^{L} a_k (\cos \omega)^k,$
 $A_e(e^{j\omega}) = P(x)|_{x=\cos\omega}, \qquad P(x) = \sum_{k=0}^{L} a_k x^k.$
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