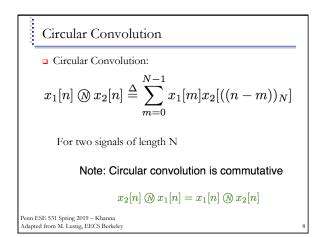
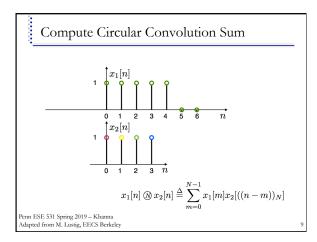
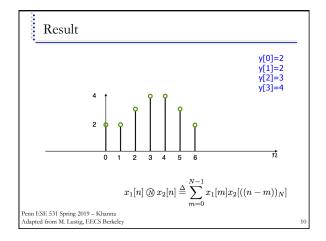


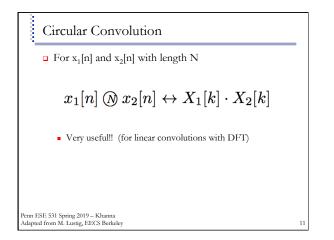
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Discrete Fourier Series			Discrete Fourier Transform		
Property	N-periodic sequence N-periodic DFS		Property	N-point sequence	N-point DFT
	$\widetilde{x}[n]$ $\widetilde{x}_1[n], \widetilde{x}_2[n]$	$\overline{X}[k]$ $\overline{X}_1[k], \overline{X}_1[k]$		x[n] $x_1[n], x_2[n]$	$X[k] = X_1[k], X_2[k]$
Linearity	$a\widetilde{x}_1[n] + b\widetilde{x}_2[n]$	$a\widetilde{X}_1[k] + b\widetilde{X}_2[k]$	Linearity	$ax_1[n] + bx_2[n]$	$aX_1[k] + bX_2[k]$
Duality	$\widetilde{X}[n]$	$N \bar{x}[-k]$	Duality	X[n]	$N x[((-k))_N]$
Time Shift	$\tilde{x}[n-m]$	$W^{ln}_{X}\widetilde{X}[k]$	Circular Time Shift	$x[((n-m))_{\times}]$	$W_N^{loc}X[k]$
Frequency Shift	$W_N^{-ic} \bar{x}[a]$	$\widetilde{X}[k-l]$	Circular Frequency Shift	$W_{\chi}^{\to h}x[n]$	$X[((k-l))_N]$
Periodic Convolution	$\sum_{n=0}^{N-1}\widetilde{x}_1[m]\widetilde{x}_2[n-m]$	$\widetilde{X}_1[k]\widetilde{X}_2[k]$	Circular Convolution	$\sum_{m=0}^{N-1} x_1[m] x_2[((n-m))_N]$	$X_1[k]X_2[k]$
Multiplication	$\widetilde{x}_1[n]\widetilde{x}_2[n]$	$\frac{1}{N}\sum_{l=0}^{N-1} \widetilde{X}_1[l]\widetilde{X}_2[k-l]$	Multiplication	$x_1[n]x_2[n]$	$\frac{1}{N}\sum_{i=0}^{N-1} X_i[t]X_2[((k-t))_N]$
Complex Conjugation	$\overline{x}^*[n]$	$\overline{X}^*[-k]$	Complex Conjugation	$x^*[n]$	$X^{*}[((-k))_{N}]$

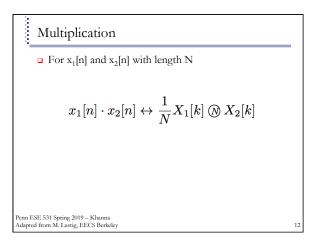
110	perues	Continu	.eu)		
Time- Reversal and Complex Conjugation	$\overline{x}^*[-n]$	$\tilde{X}^*[k]$	Time- Reversal and Complex Conjugation	$x^*[((-n))_{\times}]$	$X^*[k]$
Real Part	$Re{\hat{x}[n]}$	$\widetilde{X}_{ep}[k] \!=\! \frac{1}{2} \left(\widetilde{X}[k] \!+\! \widetilde{X}^*[\!-\!k] \right)$	Real Part	Re[x[n]]	$\boldsymbol{X}_{op}[k] = \frac{1}{2} \left(\boldsymbol{X}[k] + \boldsymbol{X}^*[((-k))_N] \right)$
Imaginary Part	$j \operatorname{Im}\{\tilde{x}[n]\}$	$\widetilde{X}_{op}[k] \!=\! \frac{1}{2} \left(\widetilde{X}[k] \!-\! \widetilde{X}^*[-k] \right)$	Imaginary Part	/ Im{x[n]}	$X_{op}[k] = \frac{1}{2} \left(X[k] - X^*[((-k))_N] \right)$
Even Part	$\widetilde{x}_{o}[n] = \frac{1}{2} \left(\widetilde{x}[n] + \widetilde{x}^*[-n] \right)$	$Re{[\bar{X}[k]]}$	Even Part	$x_{ip}[n] = \frac{1}{2} \left(x[n] + x^* [((-n))_{ij}] \right)$	$\operatorname{Re}\{X[k]\}$
Odd Part	$\widetilde{x}_{op}[n] = \frac{1}{2} \left(\widetilde{x}[n] - \widetilde{x}^*[-n] \right)$	$/ \operatorname{Im} \{ \tilde{X}[k] \}$	Odd Part	$x_{ip}[n] = \frac{1}{2} \left\{ x[n] - x^* \left[((-n))_x \right] \right\}$	$/Im{X[k]}$
Symmetry for Real Sequence	$\tilde{x}[u] = \tilde{x}^*[u]$	$\begin{split} \widetilde{X}[k] &= \widetilde{X}^*[-k] \\ \begin{cases} \operatorname{Re}[\widetilde{X}[k]] &= \operatorname{Re}[\widetilde{X}[-k]] \\ \operatorname{Im}[\widetilde{X}[k]] &= -\operatorname{Im}[\widetilde{X}[-k]] \\ \end{cases} \\ \begin{cases} \widetilde{X}[k]] &= -\widetilde{X}[-k] \\ \angle \widetilde{X}[k] &= -\angle \widetilde{X}[-k] \end{cases} \end{split}$	Symmetry for Real Sequence	$x[n] = x^{+}[n]$	$\begin{split} & \boldsymbol{\chi}[k] = \boldsymbol{\chi}^* [((-k))_{\boldsymbol{\chi}}] \\ & \left[\begin{array}{c} \operatorname{Re} \{\boldsymbol{\chi}[k] = \operatorname{Re} \{\boldsymbol{\chi}[((-k))_{\boldsymbol{\chi}}]\} \\ \operatorname{Im} \{\boldsymbol{\chi}[k] = -\operatorname{Im} \{\boldsymbol{\chi}[((-k))_{\boldsymbol{\chi}}]\} \\ \end{array} \right] \\ & \left[\begin{array}{c} \boldsymbol{\chi}[k] = -\operatorname{Im} \{\boldsymbol{\chi}[((-k))_{\boldsymbol{\chi}}] \\ \\ \boldsymbol{\zeta} \boldsymbol{\chi}[k] = -\boldsymbol{\zeta} \boldsymbol{\chi}[((-k))_{\boldsymbol{\chi}}] \end{array} \right] \end{split} \end{split} $
Parseval's Identity	$\sum_{n=0}^{N-1} \bar{x}_{n}[n] \bar{x}_{1}^{*}[n] - \frac{1}{N} \sum_{k=0}^{N-1} \bar{x}_{n}[k] \bar{x}_{1}^{*}[k]$ $\sum_{n=0}^{N-1} [\bar{x}[n]]^{2} - \frac{1}{N} \sum_{k=0}^{N-1} [\bar{x}[k]]^{2}$		Parseval's Identity	$\sum_{a=4}^{N-1} x_a [w] x_2^* [a] - \frac{1}{N} \sum_{s=6}^{N-1} X_s [k] X_2^* [k]$ $\sum_{s=6}^{N-1} [x_a^* [a]]^2 - \frac{1}{N} \sum_{s=6}^{N-1} X_s [k]^2$	

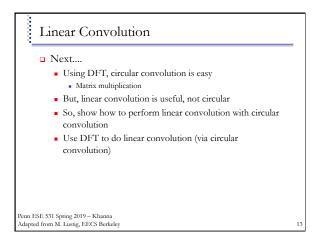


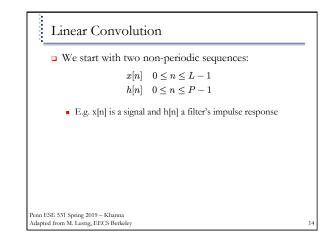


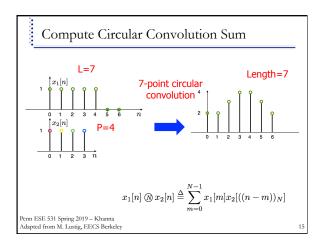


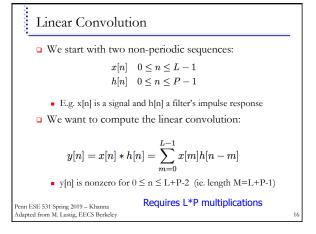


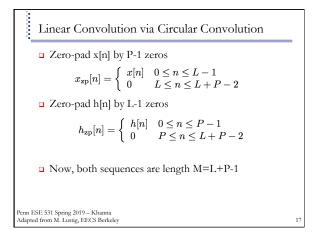


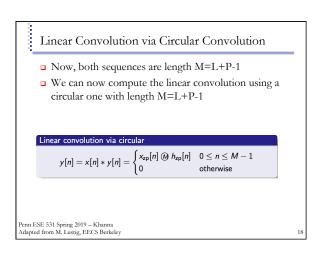


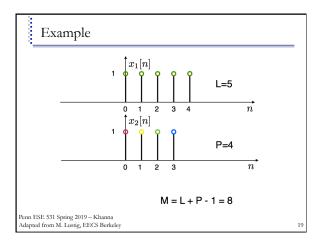


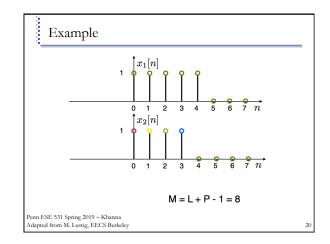


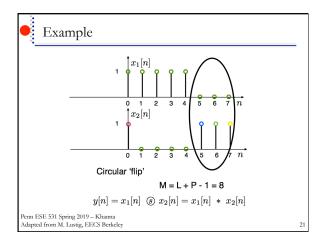


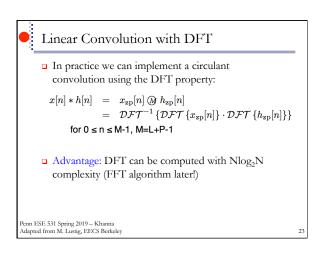


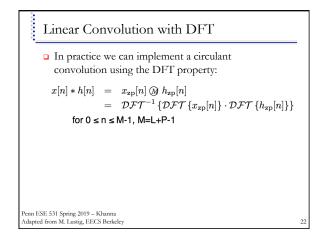


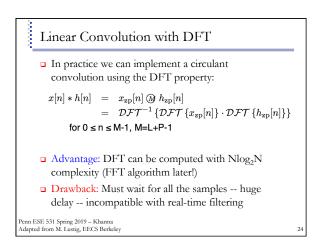


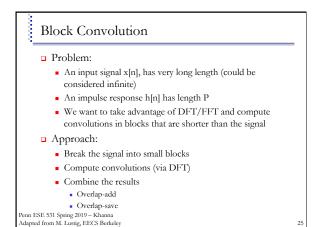


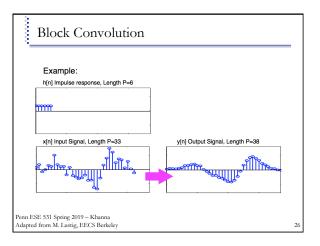


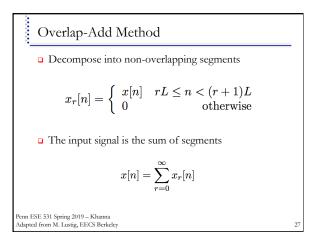


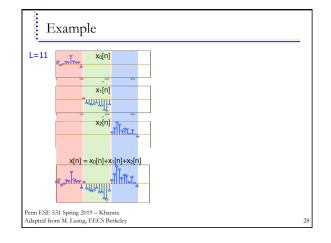


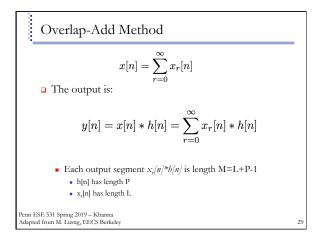


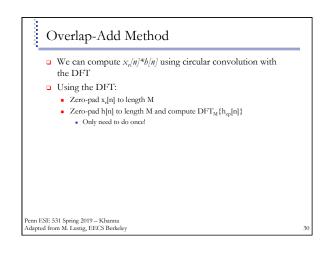


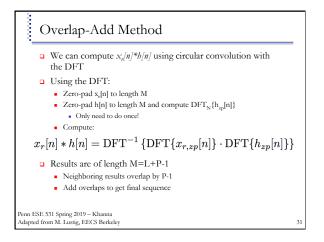


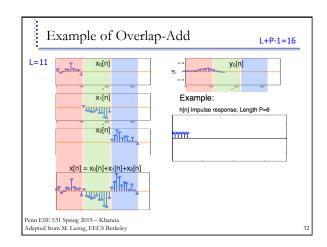


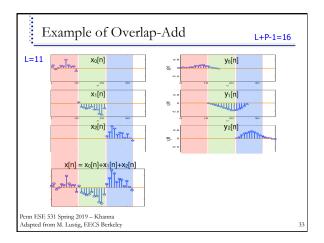


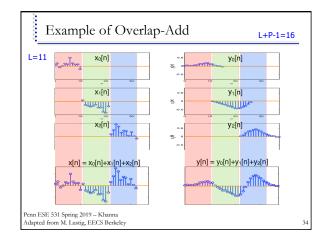


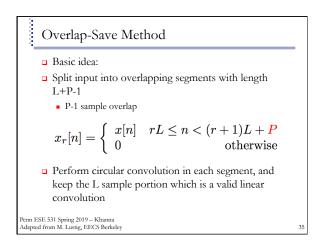


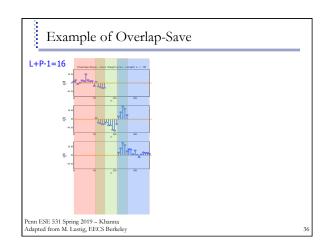


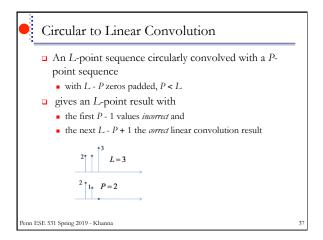


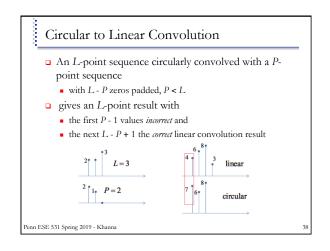


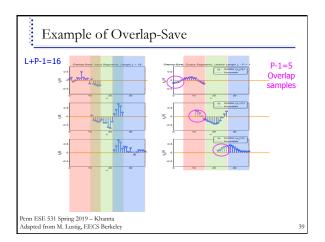


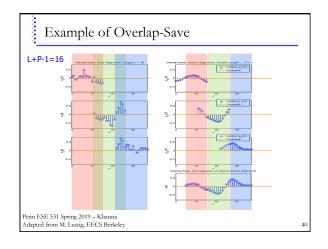


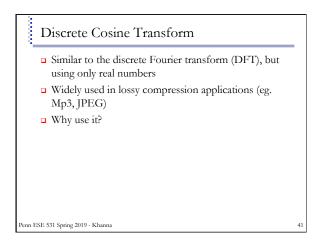


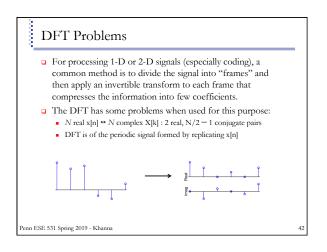


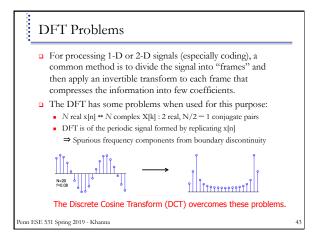


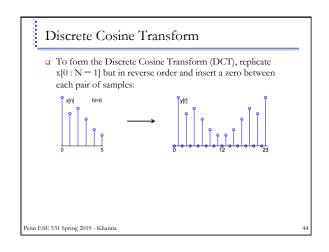


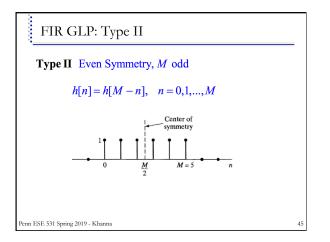


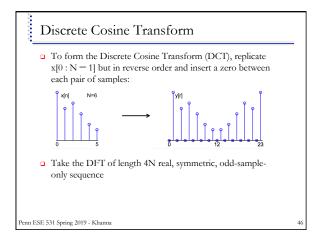


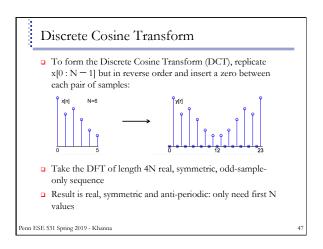


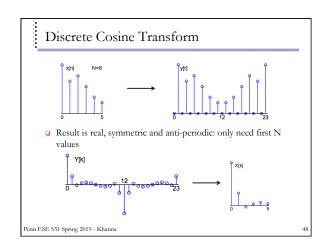


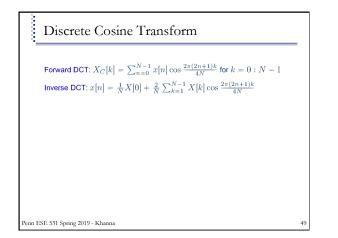


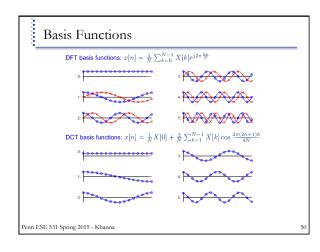












 $\frac{m}{N}$

 $f \neq \frac{m}{N}$

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