

Signal Processing Trends

- □ Traditional DSP → sample first, ask questions later
- □ Explosion in sensor technology/ubiquity has caused two trends:
 - Physical capabilities of hardware are being stressed, increasing speed/resolution becoming expensive
 - gigahertz+ analog-to-digital conversion
 - accelerated MRI
 - industrial imaging
 - Deluge of data
 - camera arrays and networks, multi-view target databases, streaming video...

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- □ Compressive Sensing → sample smarter, not faster

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Compressive Sensing/Sampling Standard approach • First collect, then compress Throw away unnecessary data Compression Penn ESE 531 Spring 2019 – Khanna Adapted from M. Lustig, EECS Berkeley

Compressive Sensing

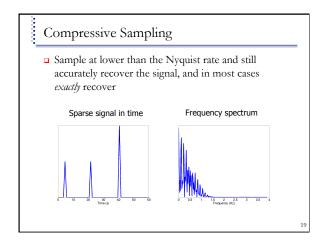
- □ Shannon/Nyquist theorem is pessimistic
 - 2×bandwidth is the worst-case sampling rate holds uniformly for any bandlimited data
 - sparsity/compressibility is irrelevant
 - Shannon sampling based on a linear model, compression based on a nonlinear model
- Compressive sensing
 - new sampling theory that leverages compressibility
 - key roles played by new uncertainty principles and randomness

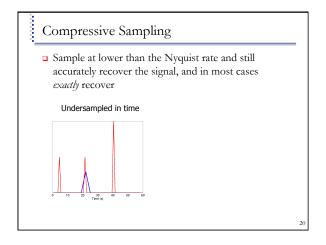
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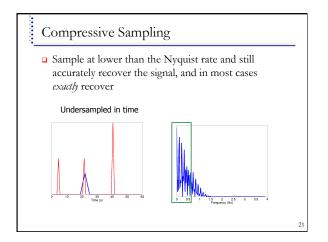
Sensing to Data data compression sensor Penn ESE 531 Spring 2019 - Khanna

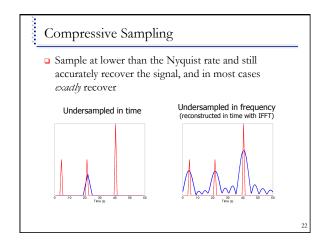
Compressive Sampling

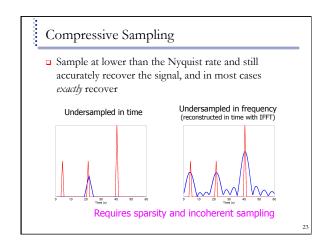
 Sample at lower than the Nyquist rate and still accurately recover the signal, and in most cases exactly recover

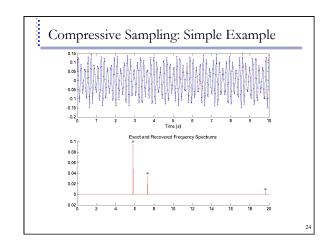


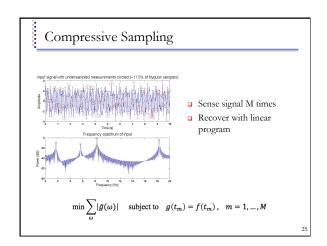


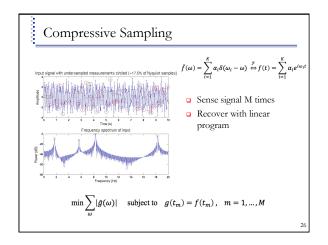


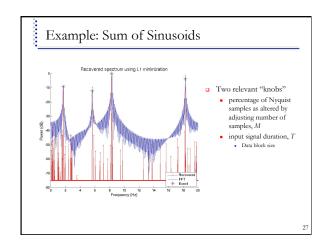


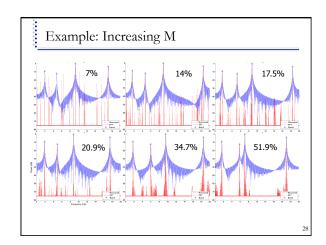


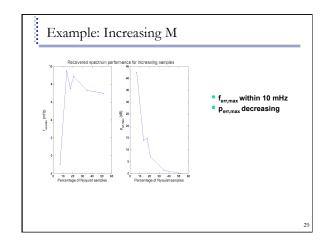


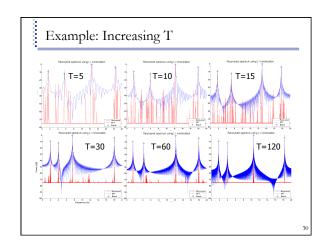


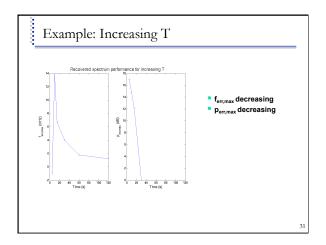


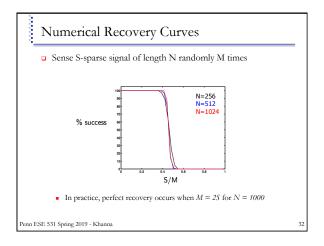












A Non-Linear Sampling Theorem

- □ Exact Recovery Theorem (Candès, R, Tao, 2004):
 - Select M sample locations $\{t_m\}$ "at random" with

 $M \ge \operatorname{Const} \cdot S \log N$

□ Take time-domain samples (measurements)

$$y_m = x_0(t_m)$$

□ Solve

 $\min_{x} \|\hat{x}\|_{\ell_1}$ subject to $x(t_m) = y_m, \ m = 1, \dots, M$

□ Solution is exactly recovered signal with extremely high probability

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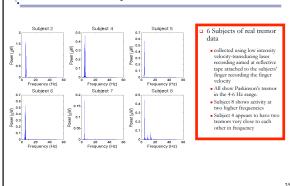
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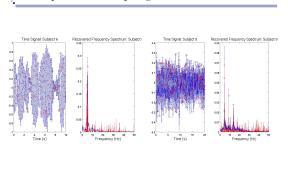
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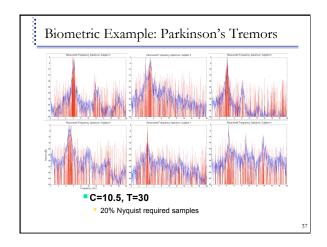
 $M > C \cdot \mu^2(\Phi, \Psi) \cdot S \cdot \log N$

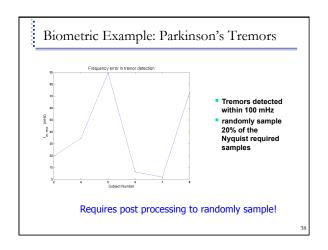
Biometric Example: Parkinson's Tremors



Compressive Sampling: Real Data







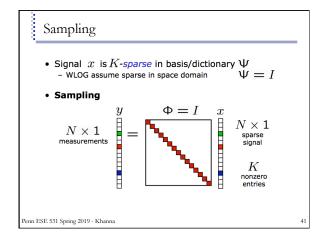
Implementing Compressive Sampling

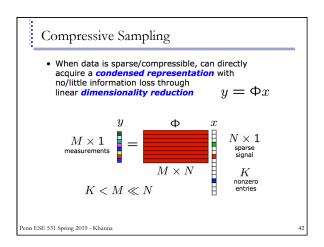
- Devised a way to randomly sample 20% of the Nyquist required samples and still detect the tremor frequencies within 100mHz
 - Requires post processing to randomly sample!
- Implement hardware on chip to "choose" samples in real time
 - Only write to memory the "chosen" samples
 - Design random-like sequence generator
 - Only convert the "chosen" samples
 - Design low energy ADC

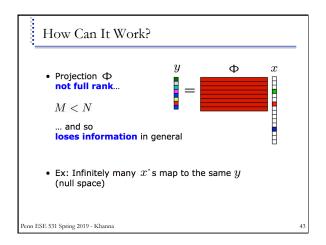
CS Theory

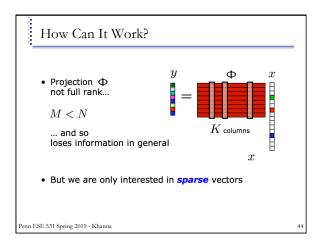
Why does is work?

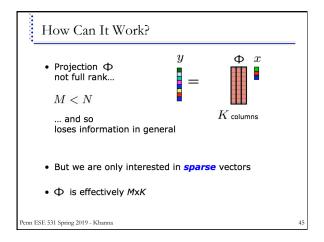
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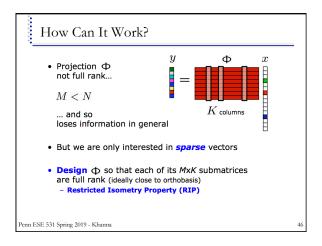


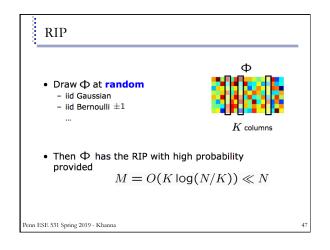


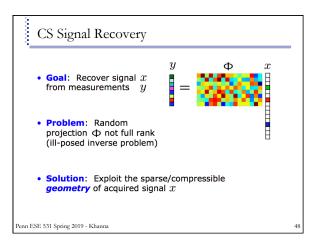


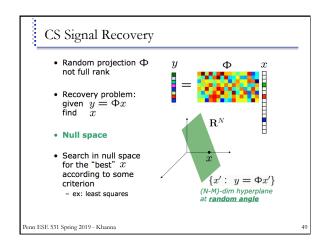


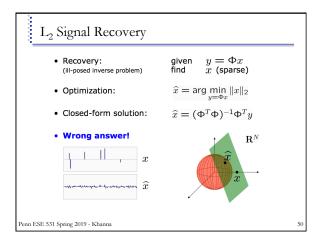


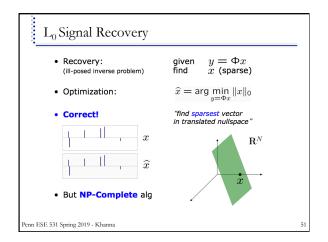


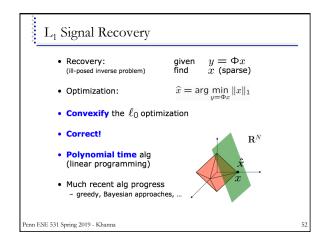


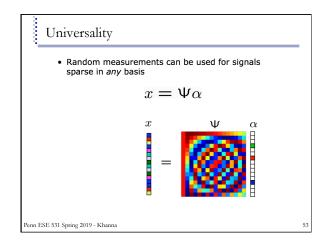


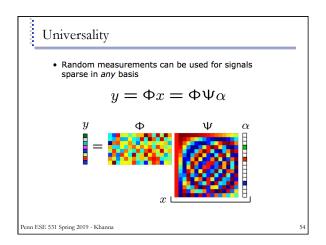




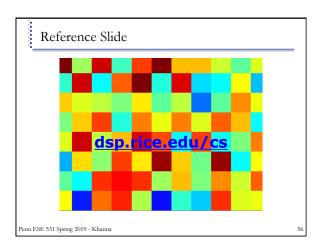








Universality • Random measurements can be used for signals sparse in any basis $y = \Phi x = \Phi \Psi \alpha = \Phi' \alpha$ $y = \Phi' \qquad \alpha \qquad N \times 1$ sparse coefficient vector Vector



Big Ideas

Compressive Sampling
Integrated sensing/sampling, compression and processing
Based on sparsity and incoherency

Admin

Final Project due - Apr 30th

TA advice - "The report takes time. Leave time for it."

No late accepted. Turn into Canvas on time.

Last day of TA office hours - Apr 30th

Piazza still available

Last day of Tania office hours - May 8th

Final Exam Review Session - May 10th (time TBD)

Watch Piazza for details

Final Exam - May 13th

Final Exam Admin

Final – 5/13

Location Levine 101

Starts at exactly 3:00pm, ends at exactly 5:00pm (120 minutes)

Cumulative – covers entire course

Except data converters, noise shaping (lec 12), adaptive filters (lec 23), wavelet transform (lec 25), and compressive sampling (lec 26)

Closed book

Data/Equation sheet provided by me

2.8.5x11 two-sided cheat sheets allowed

Calculators allowed, no smart phones

Old exams posted

TA Review session on 5/10, Time and Place TBD

Watch Piazza for details