## ESE532: System-on-a-Chip Architecture

Day 2: September 4, 2019 Analysis, Metrics, and Bottlenecks

Work Preclass Lecture start 10:35am

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## Today: Analysis

- How do we quickly estimate what's possible?
  - Before (with less effort than) developing a complete solution
- · How should we attack the problem?
  - Achieve the performance, energy goals?
- When we don't like the performance we're getting, how do we understand it?
- · Where should we spend our time?

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## Today: Analysis

- Throughput
- Latency
- Bottleneck
- · Computation as a Graph, Sequence
- Critical Path
- Resource Bound
- 90/10 Rule (time permitting)

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## Message for Day

- Identify the Bottleneck
  - May be in compute, I/O, memory, data movement
- · Focus and reduce/remove bottleneck
  - More efficient use of resources
  - More resources
- Repeat

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## Latency vs. Throughput

- Latency: Delay from inputs to output(s)
- Throughput: Rate at which can produce new set of outputs
  - (alternately, can introduce new set of inputs)

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# Preclass Washer/Dryer Example

• 10 shirt capacity



- 1 Washer Takes 30 minutes
- 1 Dryer Takes 60 minutes
- How long to do one load of wash?
   → Wash latency
  - a. . <del>.</del> . .
- · Cleaning Throughput?



60m

## Pipeline Concurrency



- · Break up the computation graph into stages
  - Allowing us to
    - reuse resources for new inputs (data),
    - while older data is still working its way through the graph
      - -Before it has exited graph
  - Throughput > (1/Latency)
- · Relate liquid in pipe
  - Doesn't wait for first drop of liquid to exit far end of pipe before accepting second drop

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# Escalator Williams Source: https://commons.wikimedia.org/wiki/File:Tanforan\_Target\_escalator\_1.JPG 8

## **Escalator**



- · Moves 2 ft/second
- Assume for simplicity one person can step on escalator each second
- Escalator travels 30 feet (vertical and horizontal)
- · Latency of escalator trip?
- Throughput of escalator: people/hour?

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## **Bottleneck**

What is the rate limiting item?
 Resource, computation, ....

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# Preclass Washer/Dryer Example

- 1 Washer Takes 30 minutes
  - Isolated throughput 20 shirts/hour
- 1 Dryer Takes 60 minutes
  - Isolated throughput 10 shirts/hour
- Where is bottleneck in our cleaning system?



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# Preclass Washer/Dryer Example

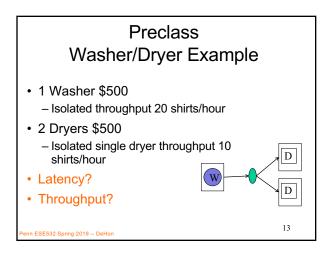
• 1 Washer \$500

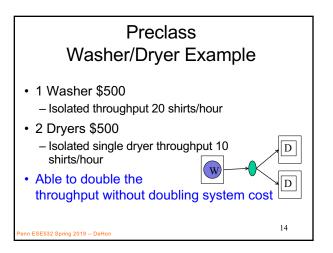


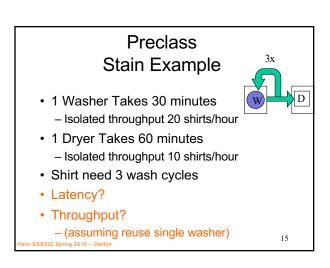
- Isolated throughput 20 shirts/hour
- 1 Dryer \$500
  - Isolated throughput 10 shirts/hour
- How do we increase throughput with \$500 investment

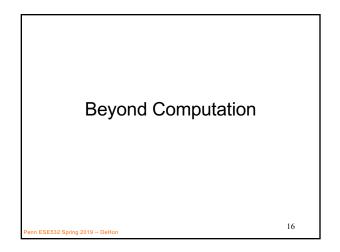


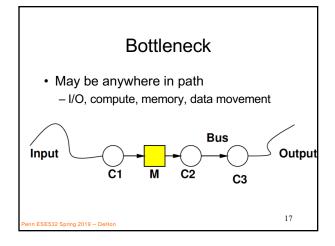
60m

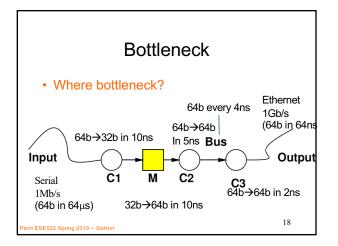


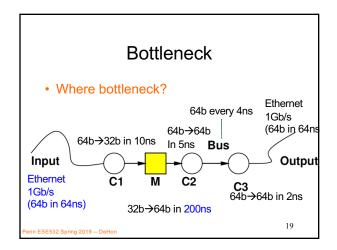


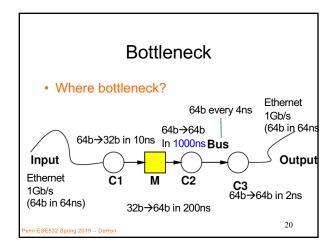












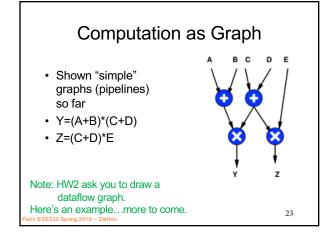
## Feasibility / Limits

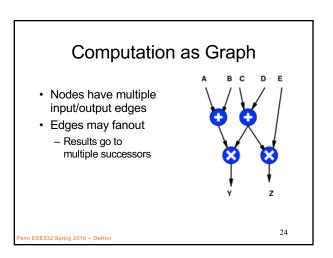
- First things to understand
   Obvious limits in system?
- · Impossible?
- Which aspects will demand efficient mapping?
- · Where might there be spare capacity

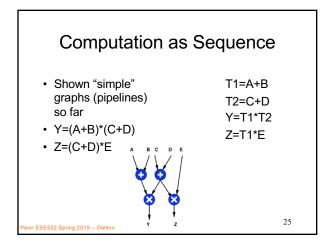
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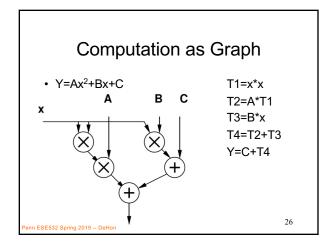
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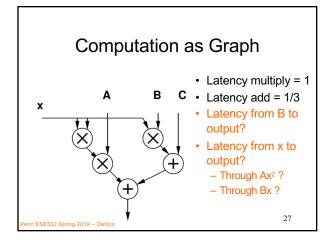
# Generalizing (to more general task graphs)







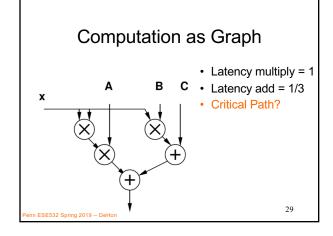


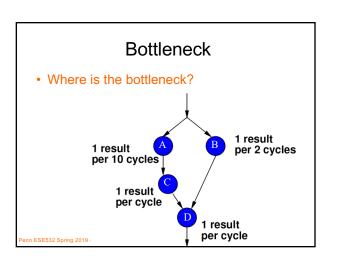


## Delay in Graphs

- **Observe:** There are multiple paths from inputs to outputs
- Need to complete all of them to produce outputs
- · Limited by longest path
- Critical path: longest path in the graph

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## Time and Space

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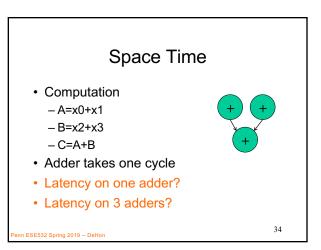
## **Space**

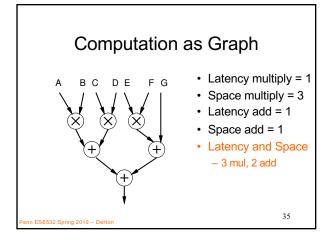
- "Space" is an abstract term for physical resources
  - On VLSI chip: Area mm<sup>2</sup> of silicon
  - On our FPGA: # of LUTs used
  - More abstractly: # of Adders, multipliers
  - Laundry example
    - \$\$ to spend on laundry equipment
    - Physical space (sq. ft) in laundry room

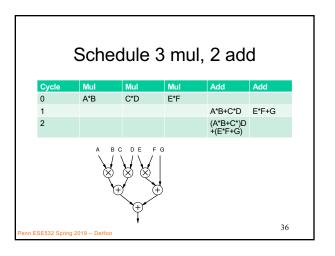
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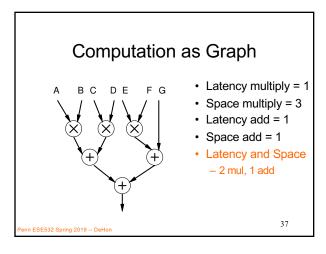
32

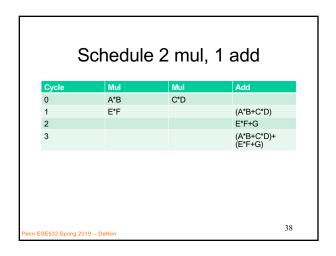
# Space-Time In general, we can spend resources to reduce time Increase throughput Three wash stain removal case

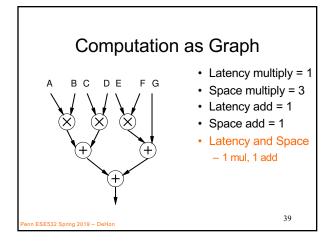


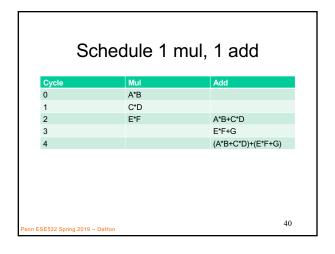


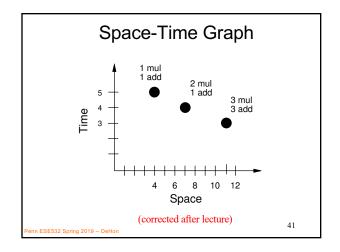


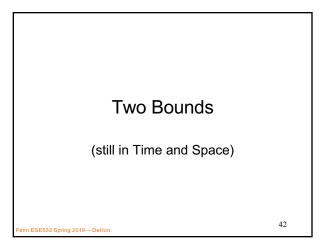












### Problem

- Coming up with an exact time count can be hard (human/computer time consuming)
  - Technically a hard problem
    - NP-Complete: no known non-exponential solution
- Requires reasoning about structure of graph
- Would be nice to have a quick (easy) answer on what is feasible
  - ...and what is not feasible → impossible.

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### **Bounds**

- · Establish the feasible range
  - Must be larger than LB
  - Must be smaller than UB
  - Solution will be between LB and UB
  - $-LB \le ActualTime \le UB$
- · Bounds in sports
  - Ball landing in-bounds or out-of bounds

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### Bounds

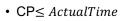
- · Quick lower bounds (LB) can estimate
  - $-LB \leq ActualTime$
- Two:
  - CP: Critical Path
    - · Sometimes call it "Latency Bound"
  - RB: Resource Capacity Bound
    - Sometimes call it "Throughput Bound" or "Compute Bound"

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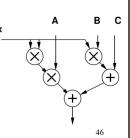
## Critical Path Lower Bound

- · Critical path assuming infinite resources
- Certainly cannot finish x any faster than that



• Ignores resource limits

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## Resource Capacity Lower Bound

- Sum up all capacity required per resource: TotalOps = ∑ Ops
  - E.g. number of multiplications, additions, memory lookups
- Divide by total resource (for type)
  - E.g., number of multipliers, adders, memory ports
  - $\textit{RB} = [\textit{TotalOps/Operators}] \leq \textit{ActualTime}$
- · Lower bound on compute
  - (best can do is pack all use densely)

- Ignores data dependency constraints 47

## Multiple Resource Types

- $RB = Max([TotalOps_1/Operators_1],$   $[TotalOps_2/Operators_2],$  $...) \leq ActualTime$
- Combine Critical Path Lower Bound  $Max(CP, \lceil TotalOps_1/Operators_1 \rceil, \lceil TotalOps_2/Operators_2 \rceil, \dots) \leq ActualTime$

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## For Single Resource Type

- (and no communication time...)
- · Can use to get upper bound:
- $ActualTime \leq CP + RB$
- · Together:
- $Max(CP, RB) \le ActualTime \le CP + RB$

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## Washer-Dryer Bounds

· Task: wash & dry 30 shirts

• Washer: 10 shirts/30 min.

• Dryer: 10 shirts/60 min.

· 2 Washers, 2 Dryers

• W-->D CP=90 minutes

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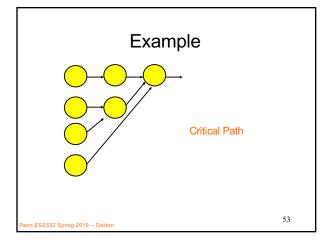
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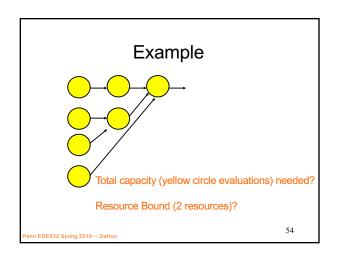
## Washer-Dryer Bounds

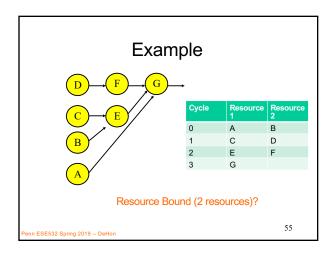
- Task: wash & dry 30 shirts CP=90 min
- · Washer: 10 shirts/30 min.
- Dryer: 10 shirts/60 min.
- 2 Washers, 2 Dryers
- · Washer Bound:
  - WB= [30 shirts/2 washers×10 shirts/washer] × 30 min = 60 min
- Dryer
  - $-DB=[(30 \text{ shirts/2 dryers} \times 10 \text{ }$
- shirts/dryer)]× 60 min = 120 minutes

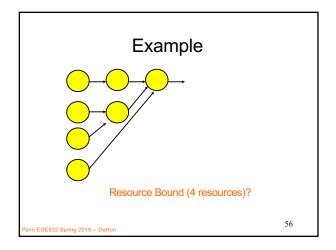
## Washer-Dryer Bounds

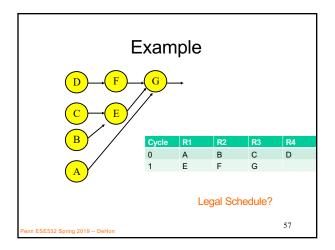
- Task: wash & dry 30 shirts CP=90 min
- Washer: 10 shirts/30 min.
- Dryer: 10 shirts/60 min.
- 2 Washers, 2 Dryers RB=120 min
- $Max(90,60,120)=120 \le TaskTime$
- TaskTime: 150
  - 0 start 2 washes
  - 30 start 2 dryers; start 1 wash
  - 90 finish 2 dryers; start last dryer load
- 150 finish last dryer load







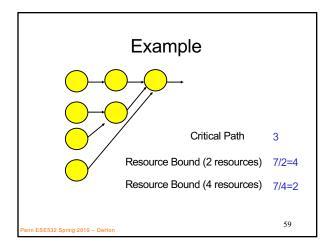




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  - $-RB = [TotalOps/Operators] \le ActualTime$
- · Lower bound on compute
  - (best can do is pack all use densely)
- Ignores data dependency constraints

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## 90/10 Rule (of Thumb)

- · Observation that code is not used uniformly
- 90% of the time is spent in 10% of the code
- Knuth: 50% of the time in 2% of the code
- Implications
  - There will typically be a bottleneck
  - We don't need to optimize everything
  - We don't need to uniformly replicate space to achieve speedup
  - Not everything needs to be accelerated

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# Big Ideas

- · Identify the Bottleneck
  - May be in compute, I/O, memory ,data movement
- Focus and reduce/remove bottleneck
  - More efficient use of resources
  - More resources

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## Admin

- Reading for Day 3 on web
- HW1 due Friday
- HW2 out
  - Partner assignment (see canvas)
- Remember feedback

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