ESE5320: System-on-a-Chip Architecture

Day 21: November 10, 2025
Verification 2

Today

- Assertions (Part 1)
- Proving correctness (Part 2)
  - FSM Equivalence
- Timing and Testing (Part 3)

Message

- If you don't test it, it doesn't work.
- Testing can only prove the presence of bugs, not the absence.
  - Full verification strategy is more than testing.
- Valuable to decompose testing
  - Functionality
  - Functionality at performance

Assertions

Assertion

- Properties expect/demand to hold
- Predicate (Boolean expression) that must be true
- Add to code
  - Can uses variables in code to write expression
- Example: `assert(num<100);`
- Invariant
  - Expect/demand this property to always hold
  - Never vary → never not be true

Equivalence with Reference as Assertion

- Match of test and golden reference is a heavy-weight example of an assertion

- r=fimpl(in);
- assert (r==fgolden(in));

Assertion as Invariant

- May express a property that must hold without expressing how to compute it.
  - Different than just a simpler way to compute

```
int res[2];
res=divide(n,d);
assert(res[QUOTIENT]*d+res[REMAINDER]==n);
```


Lightweight

- Typically, lighter weight (less computation) than full equivalence check
- Typically, less complete than full check
- Allows continuum expression

Preclass 1

What property needs to hold on `l`?

Note: divide: s/l

```
s=packetsum(p);
l=packetlen(p);
res=divide(s,l);
```


Check a Requirement

```
s=packetsum(p);
l=packetlen(p);
assert(l!=0);
res=divide(s,l);
```


Preclass 2

What must be true of `my_array[loc]` after call?

```
int findloc(int target, int *a, int limit);
.
.
.
int loc;

loc=findloc(my_target,my_array,MY_ARRAY_LEN);
// property on my_array[loc] should hold here?
.
.
.
```


Merge using Streams

Day 13

- Merging two sorted list is a streaming operation
- int aptr; int bptr;
- astream.read(ain); bstream.read(bin)
- For (i=0;i<MCNT;i++)

  If ((aptr<ACNT) && (bptr<BCNT))

  If (ain>bin)

  { ostream.write(ain); aptr++; astream.read(ain);}

  Else

  { ostream.write(bin) bptr++; bstream.read(bin);}

  Else // copy over remaining from astream/bstream

Merge Requirement

- Require: astream, bstream sorted
- int aptr; int bptr;
- astream.read(ain); bstream.read(bin)
- For (i=0;i<MCNT;i++)

```
If ((aptr<ACNT) && (bptr<BCNT))
  If (ain>bin)
   { ostream.write(ain); aptr++; astream.read(ain);}
  Else
   { ostream.write(bin) bptr++; bstream.read(bin);}
Else // copy over remaining from astream/bstream
```

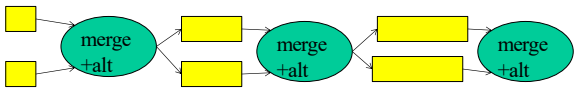

Merge Requirement

- Require: astream, bstream sorted
- Int ptr; int bptr;
- astream.read(ain); bstream.read(bin)
- For (i=0;i<MCNT;i++)

```
If ((aptr<ACNT) && (bptr<BCNT))
  If (ain>bin)
   { ostream.write(ain); aptr++;
     int prev_ain=ain;  astream.read(ain);
     assert(prev_ain>=ain);
  }
```


Merge with Order Assertion

- When composed
  - Every downstream merger checks work of predecessor



Merge Requirement

- Require: astream, bstream sorted
- Requirement that input be sorted is good
  - And not hard to check
- Not comprehensive
  - Weaker than saying output is a sorted version of input
- What errors would it allow?

What do with Assertions?

- Include logic during testing (verification)
- Omit once tested
  - Compiler/library/macros (#define) omit code
  - Keep in source code
- Maybe even synthesize to gate logic for FPGA testing
- When assertion fail
  - Count
  - Break program for debugging (dump core)

Assertion Roles

- Specification (maybe partial)
  - May address state that doesn't exist in gold reference
- Documentation
  - This is what I expect to be true
    - Needs to remain true as modify in the future
- Defensive programming
  - Catch violation of input requirements
- Catch unexpected events, inputs
- Early failure detection
- Validate that something isn't happening

Assertion Discipline

- Worthwhile discipline
  - Consider and document input/usage requirements
  - Consider and document properties that must always hold
- Good to write those down
  - As precisely as possible
- Good to check assumptions hold

Equivalence Proof

FSM

Part 2

Prove Equivalence

- Testing is a subset of Verification
- Testing can only prove the presence of bugs, not the absence.
- Depends on picking an adequate set of tests
- Can we guarantee that all behaviors are the correct? Same as reference? Seen all possible behaviors?

Idea

- Reason about all behaviors
  - Response to all possible inputs
- Try to find if there is *any* way to reach disagreement with specification
- Or can prove that they always agree
- Still demands specification
  - …but we can also relax that with assertions

Testing with Reference Specification

Day 20

Validate the design by testing it:

- Create a set of test inputs
- Apply test inputs
  - To implementation under test
  - To reference specification
- Collect response outputs
- Check if outputs match

Formal Equivalence with Reference Specification

Validate the design by proving equivalence between:

- implementation under consideration
- reference specification

Testing FSM Equivalence

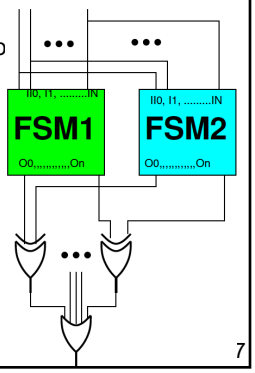
- Exhaustive:
  - Generate all strings of length |state|
    - (for larger FSM = the one with the most states)
  - Feed to both FSMs with these strings
  - Observe any differences?
- How many such strings?
  - (N binary input bits to FSM, S states)
  - 2^{N*S}

FSM Equivalence

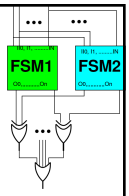
- Illustrate with concrete model of FSM equivalence
  - Is some implementation FSM
  - Equivalent to reference FSM

Compare

- Start with golden model setup
  - Run both and compare output
- Create composite FSM
  - Start with both FSMs
  - Connect common inputs together (Feed both FSMs)
  - XOR together outputs of two FSMs
    - Xor's will be 1 if they disagree, 0 otherwise

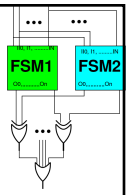


Compare



- Create composite FSM
  - Start with both FSMs
  - Connect common inputs together (Feed both FSMs)
  - XOR together outputs of two FSMs
    - Xor's will be 1 if they disagree, 0 otherwise
- Ask if the new machine ever generate a 1 on an xor output (signal disagreement)
  - Any 1 is a proof of non-equivalence
  - Never produce a 1 → equivalent

Creating Composite FSM



- Assume know start state for each FSM
- Each state in composite is labeled by the pair $\{S1_i, S2_j\}$
  - How many such states?
- Start in $\{S1_0, S2_0\}$
- For each input *a*, create a new edge:
  - $T(a,\{S1_0, S2_0\}) \rightarrow \{S1_i, S2_j\}$
    - If $T_1(a, S1_0) \rightarrow S1_i$ and $T_2(a, S2_0) \rightarrow S2_j$
- Repeat for each composite state reached

Composite FSM

- How much work?
- Hint:
  - Maximum number of composite states (state pairs)
  - Maximum number of edges from each state pair?
  - Work per edge?

Composite FSM

- Work
  At most $|2^N|*|State1|*|State2|$ edges == work
- Can group together original edges
  - *i.e.* in each state compute intersections of outgoing edges
  - Really at most $|E_1|*|E_2|$
    - |E| = # edges in FSM

Non-Equivalence

- State $\{S1_i, S2_j\}$ demonstrates non-equivalence iff
  - $\{S1_i, S2_j\}$ reachable
  - On some input, State $S1_i$ and $S2_j$ produce different outputs
- If $S1_i$ and $S2_j$ have the same outputs for all composite states, it is impossible to distinguish the machines
  - They are equivalent
- A **reachable** state with differing outputs
  - Implies the machines are not identical

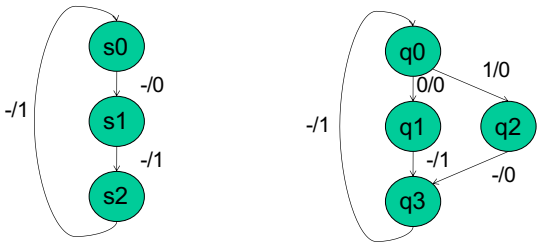
Answering Reachability

- Start at composite start state $\{S1_0, S2_0\}$
- Search for path to a differing state
- Use any search
  - Breadth-First Search, Depth-First Search
- End when find differing state
  - Not equivalent
- OR when have explored entire reachable graph without finding
  - Are equivalent

Reachability Search

- Worst: explore all edges at most once
  - $O(|E|)=O(|E_1|*|E_2|)$
- Can combine composition construction and search
  - *i.e.* only follow edges which fill-in as search
  - (way described)

Preclass 3



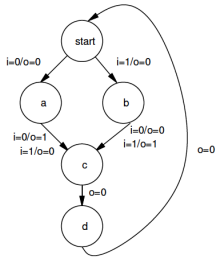
- Means don't-care. Can read as (0 or 1) here.

Creating Composite FSM

- Assume know start state for each FSM
- Each state in composite is labeled by the pair $\{S1_i, S2_j\}$
- Start in $\{S1_0, S2_0\}$
- For each symbol *a*, create a new edge:
  - $T(a,\{S1_0, S2_0\}) \rightarrow \{S1_i, S2_j\}$
    - If $T_1(a, S1_0) \rightarrow S1_i$ and $T_2(a, S2_0) \rightarrow S2_j$
    - Check that both state machines produce same outputs on input symbol *a*
- Repeat for each composite state reached

Preclass 4

i	State	NextState	o
0	S0	S1	0
1	S0	S2	0
0	S1	S3	1
1	S1	S4	0
0	S2	S4	0
1	S2	S4	1
-	S3	S5	0
-	S4	S5	0
-	S5	S0	0



FSM → Model Checking

- FSM case simple – only deal with states
- More general, need to deal with
  - operators (add, multiply, divide)
  - Wide word registers in datapath
    - Cause state exponential in register bits
- Tricks
  - Treat operators symbolically
    - Separate operator verification from control verif.
  - Abstract out operator width
- Similar flavor of case-based search
  - Conditionals need to be evaluated symbolically

Assertion Failure Reachability

- Can use with assertions
- Is assertion failure reachable?
  - Can identify a path (a sequence of inputs) that leads to an assertion failure?

Formal Equivalence Checking

- Rich set of work on formal models for equivalence
  - Challenges and innovations to making search tractable
  - Used with processor validation
- Common versions
  - Model Checking (2007 Turing Award)
  - Bounded Model Checking

Timing

Part 3

Issues

- Cycle-by-cycle specification can be overspecified
- Golden Reference Specification not run at target speed

Tokens

- Use data presence to indicate when producing a value
- Only compare corresponding outputs
  - Only store present outputs from computations, since that's all comparing
- Relevant non-Real-Time
- Examples?
  - (not want to match cycle-by-cycle)

Timing

- Record timestamp from implementation
- Allow reference specification to specify its time stamps
  - "Model this as taking one cycle"
  - Or requirements on its timestamps
    - This must occur before cycle 63
    - This must occur between cycle 60 and 65
- Compare values and times
- More relevant Real Time
- Example Real Time where exact cycle not matter?

Challenge

- Cannot record at full implementation rate
  - Inadequate bandwidth to
    - Store off to disk
    - Get out of chip
- Cannot record all the data you might want to compare at full rate

At Speed Testing

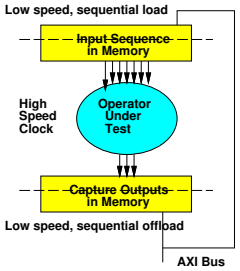
- Compiled assertions might help
  - Perform the check at full rate so don't need to record
- Capture bursts to on-chip memory
  - Higher bandwidth
  - …but limited capacity, so cannot operate continuously

Bursts to Memory

- Run in bursts
- Repeat
  - Enable computation
  - Run at full rate storing to memory buffer
  - Stall computation
  - Offload memory buffer at (lower) available bandwidth
  - (possibly check against golden model)

Generalize

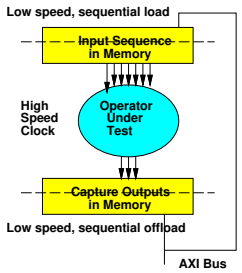
- Generalize to input and output
- Feed from memories
- Compute full rate
- Write into memory



- Can run at high rate for number of cycles can store inputs and outputs

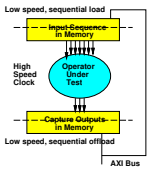
Generalize

- Generalize to input and output
- Feed from memories
- Compute full rate
- Write into memory



- What might this fail to test?

Burst Testing



- Issue
  - May only see high speed for computation/interactions that occur within a burst period
  - May miss interaction at burst boundaries
- Mitigation
  - Rerun with multiple burst boundary offsets
  - So all interactions occur within some burst
  - Decorrelate interaction and burst boundary

Timing Validation

- Doesn't need to be all testing either
- Static Timing Analysis to determine viable clock frequency
  - As Vivado is providing for you
- Cycle estimates as get from Vivado
  - II, to evaluate a function
- Worst-Case Execution Time for software

Decompose Verification

Breaks into two pieces:

1. Does it function correctly?
2. What speed does it operate it?
   - Does it continue to work correctly at that speed?

Learn More

- CIS6730 – Computer Aided Verification
- CIS5410 – includes verification for real-time system properties
- CIS5000 – Software Foundations
  - Has mechanized proofs, proof checkers

Big Ideas

- Assertions valuable
  - Reason about requirements and invariants
  - Explicitly validate
- Formally validate equivalence when possible
- Valuable to decompose testing
  - Functionality
  - Functionality at performance
- …we can extend techniques to address timing and support at-speed tests

Admin

- Feedback
- No class on Wednesday
  - Work on project
- Reading for Monday on Canvas
- P3 due Friday
- P4 out