

ESE534 Computer Organization

Day 8: February 10, 2010
Energy, Power, Reliability



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Today

- Energy Tradeoffs?
- Voltage limits and leakage?
- Variations
- Transients
- Thermodynamics meets Information Theory (brief, if we get to it)

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At Issue

- Many now argue **power** will be the ultimate scaling limit
 - (not lithography, costs, ...)
- Proliferation of portable and handheld devices
 - ...battery size and life biggest issues
- Cooling, energy costs may dominate cost of electronics
 - Even server room applications

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Preclass 1

- 1GHz case
 - Voltage?
 - Energy per Operation?
 - Power required for 2 processors?
- 2GHz case
 - Voltage?
 - Energy per Operation?
 - Power required for 1 processor?

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Energy and Delay

$$E = \frac{1}{2} CV^2$$

$$\tau_{gd} = Q/I = (CV)/I$$

$$I_{d,sat} = (\mu C_{OX}/2)(W/L)(V_{gs} - V_{TH})^2$$

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Tradeoff

- $E \approx V^2$
- $\tau_{gd} \approx 1/V$
- $I_{d,sat} \propto (V_{gs} - V_{TH})^2$
- We can trade speed for energy
- $E \times (\tau_{gd})^2 \approx \text{constant}$

$$E = \frac{1}{2} CV^2$$

$$T_{gd} = (CV)/I$$

$$I_{d,sat} \propto (V_{gs} - V_{TH})^2$$

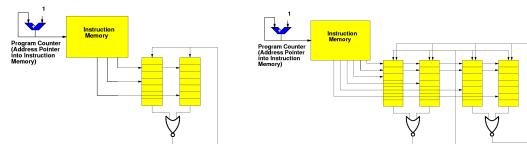
Martin et al. *Power-Aware Computing*, Kluwer 2001
<http://caltechcstr.library.caltech.edu/308/>

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Parallelism

- We have Area-Time tradeoffs
- Compensate slowdown with additional parallelism



- ...trade Area for Energy → Architectural Option

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Question

- How far can this go?
- What limits us?

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Challenge: Power

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Origin of Power Challenge

- Limited capacity to remove heat
 - ~100W/cm² force air
 - 1-10W/cm² ambient
- Transistors per chip grow at Moore's Law rate = $(1/F)^2$
- Energy/transistor must decrease at this rate to keep constant power density
- $E/tr \propto CV^2$
 - ...but V scaling more slowly than F

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Energy per Operation

$$E = \frac{1}{2}CV^2$$

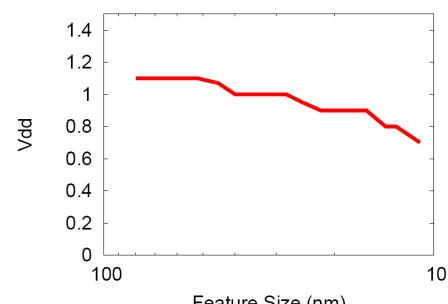
$$C_{\text{total}} = \# \text{ transistors} \times C_{\text{tr}}$$

C_{tr} scales (down) as F
transistors scales as F^{-2}
...ok if V scales as F...

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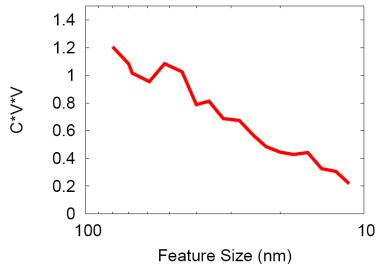
ITRS Vdd Scaling: V Scaling more slowly than F



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CV² scaling from ITRS: More slowly than (1/F)²

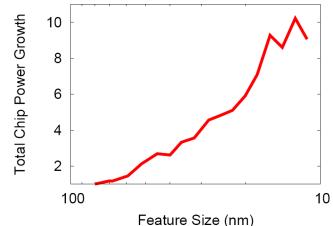


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Origin of Power Challenge

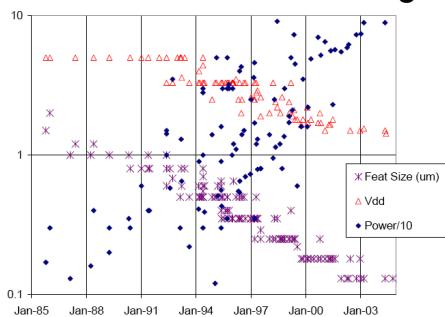
- Transistors per chip grow at Moore's Law rate = $(1/F)^2$
- Energy/tr must decrease at this rate to keep constant
- $E/tr \propto CV^2$



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Historical Power Scaling



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[Horowitz et al. / IEDM 2005]

Impact

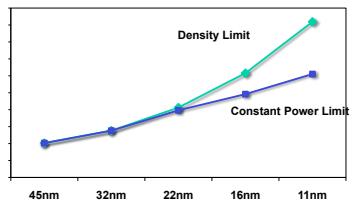
- Can already place more transistors on a chip than we can afford to turn on.
- Power potential challenge/limiter for all future chips.

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Impact

Power Limits Integration



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Source: Carter/Intel

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How far can we reduce voltage?

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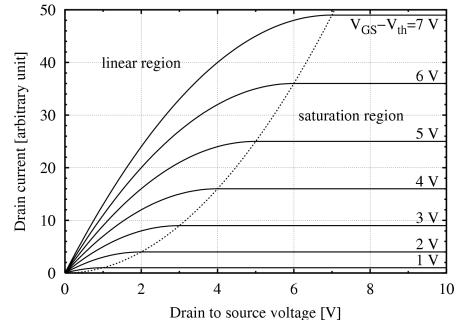
Limits

- Ability to turn off the transistor
- Noise
- Parameter Variations

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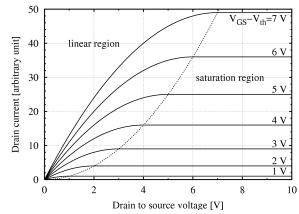
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MOSFET Conduction



From: http://en.wikipedia.org/wiki/File:IVsV_mosfet.png 20

Transistor Conduction



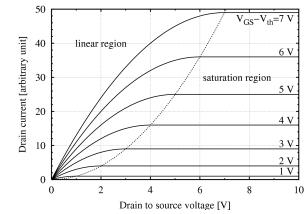
- Three regions
 - Subthreshold ($V_{gs} < V_{TH}$)
 - Linear ($V_{gs} > V_{TH}$) and ($V_{ds} < (V_{gs} - V_{TH})$)
 - Saturation ($V_{gs} > V_{TH}$) and ($V_{ds} > (V_{gs} - V_{TH})$)

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Saturation Region

- Saturation Region
- $(V_{gs} > V_{TH})$
- $(V_{ds} > (V_{gs} - V_{TH}))$



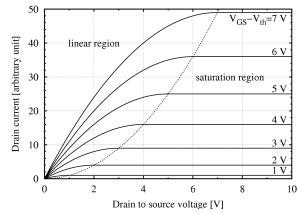
$$I_{d,sat} = (\mu C_{OX}/2)(W/L)(V_{gs} - V_{TH})^2$$

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Linear Region

- $(V_{gs} > V_{TH})$
- $(V_{ds} < (V_{gs} - V_{TH}))$



$$I_{d,lin} = (\mu C_{OX})(W/L)(V_{gs} - V_{TH})V_{ds} - (V_{ds})^2/2$$

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Subthreshold Region

- $(V_{gs} < V_{TH})$

$$I_{sub} = I_{VT} \times 10^{((V_{gs} - V_{TH})/S)}$$

$$S = (\ln(10))\eta kT / e$$

[Frank, IBM J. R&D v46n2/3p235]

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Operating a Transistor

- Concerned about I_{on} and I_{off}
- I_{on} drive current for charging
 - Determines speed: $T_{gd} = CV/I$
- I_{off} leakage current
 - Determines leakage power
 - $E_{leak} = V \times I_{leak} \times T_{cycle}$

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Leakage

- To avoid leakage want I_{off} very small

• Switch V from 0 to V_{dd}

• V_{gs} in off state is 0 $\rightarrow V_{gs} < V_{TH}$

$$I_{sub} = I_{VT} \times 10^{((V_{gs} - V_{TH})/S)}$$

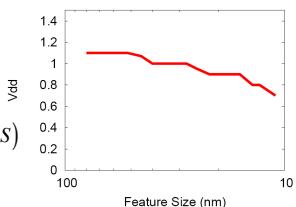
$$I_{off} = I_{VT} \times 10^{-(V_{TH}/S)}$$

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Leakage

$$I_{off} = I_{VT} \times 10^{-(V_{TH}/S)}$$



- S≈90mV for single gate
- S≈70mV for double gate
- 4 orders of magnitude $I_{VT}/I_{off} \rightarrow V_{TH} > 280mV$

Leakage limits V_{TH} in turn limits V_{dd}

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Preclass 2

- $E = E_{sw} + E_{leak}$
- $E_{leak} = V \times I_{leak} \times T_{cycle}$
- $E_{sw} \propto CV_2$
- $I_{sub} = I_{VT} \times 10^{((V_{gs} - V_{TH})/S)}$
- $I_{chip-leak} = N_{devices} \times I_{leak}$

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How maximize I_{on}/I_{off} ?

- Maximize I_{on}/I_{off} – for given V_{dd} ? $E_{sw} \propto CV_2$
- Get to pick V_{TH} , V_{dd}

$$I_{d,sat} = (\mu C_{OX}/2)(W/L)(V_{gs} - V_{TH})^2$$

$$I_{d,lin} = (\mu C_{OX})(W/L)(V_{gs} - V_{TH})V_{ds} - (V_{ds})^2/2$$

$$I_{sub} = I_{VT} \times 10^{((V_{gs} - V_{TH})/S)}$$

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Preclass 2

- $E_{leak}(V)$?
- $T_{cycle}(V)$?

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In Class

- Assign calculations
- Collect results

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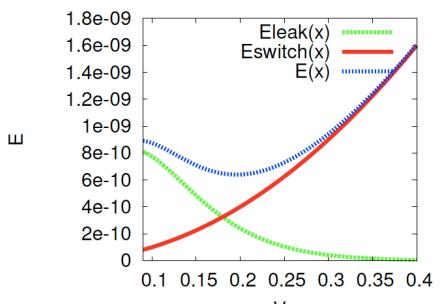
Values

V	T(v)	Esw(V)	Eleak(V)	E(V)
0.36	3.6E-09	1.296E-09	1.296E-11	1.30896E-09
0.27	0.000000027	7.29E-10	7.29E-11	8.019E-10
0.24	5.17064E-08	5.76E-10	1.24095E-10	7.00095E-10
0.21	9.74734E-08	4.41E-10	2.04694E-10	6.45694E-10
0.205	1.08137E-07	4.2025E-10	2.21682E-10	6.41932E-10
0.2	1.19897E-07	4E-10	2.39794E-10	6.39794E-10
0.19	1.4711E-07	3.61E-10	2.79509E-10	6.40509E-10
0.18	0.00000018	3.24E-10	3.24E-10	6.48E-10
0.15	3.23165E-07	2.25E-10	4.84748E-10	7.09748E-10
0.12	5.56991E-07	1.44E-10	6.68389E-10	8.12389E-10
0.09	0.0000009	8.1E-11	8.1E-10	8.91E-10

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Graph for In Class



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Impact

- Subthreshold slope prevents us from scaling voltage down arbitrarily.
- Induces a minimum operating energy.

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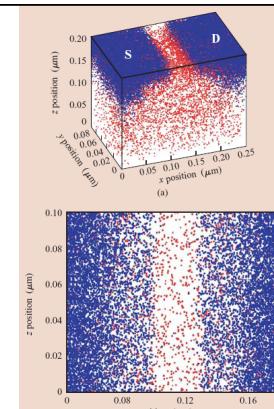
Challenge: Variation

(This section was a little rushed)

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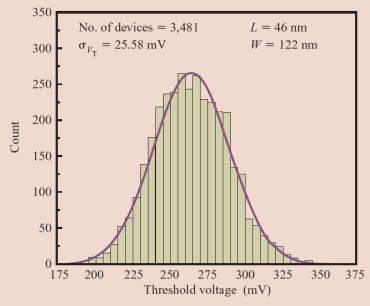
Statistical Dopant Count and Placement



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[Bernstein et al, IBM JRD 2006]

V_{th} Variability @ 65nm



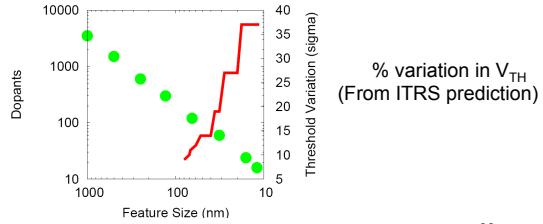
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[Bernstein et al, IBM JRD 2006]

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Variation

- Fewer dopants, atoms → increasing Variation
- How do we deal with variation?



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Impact of Variation?

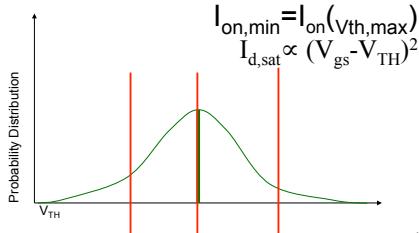
- Higher V_{TH} ?
 - Not drive as strongly
 - $I_{d,sat} \propto (V_{gs} - V_{TH})^2$
- Lower V_{TH} ?
 - Not turn off as well → leaks more
$$I_{off} = I_{VT} \times 10^{-(V_{TH}/S)}$$

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Variation

- Margin for expected variation
- Must assume V_{TH} can be any value in range



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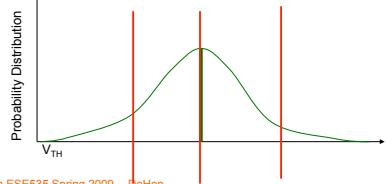
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Margining

- Must raise V_{dd} to accommodate worst-case value
- → increase energy

$$I_{on,min} = I_{on}(V_{th,max})$$

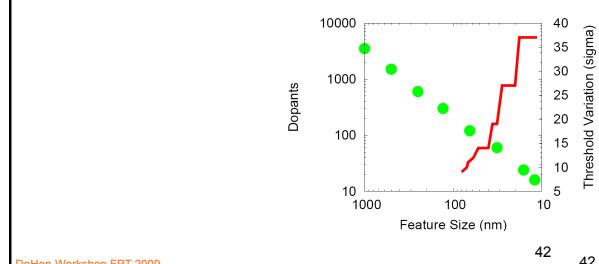
$$I_{d,sat} \propto (V_{gs} - V_{TH})^2$$



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Variation

- Increasing variation forces higher voltages
 - On top of our leakage limits



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Variations

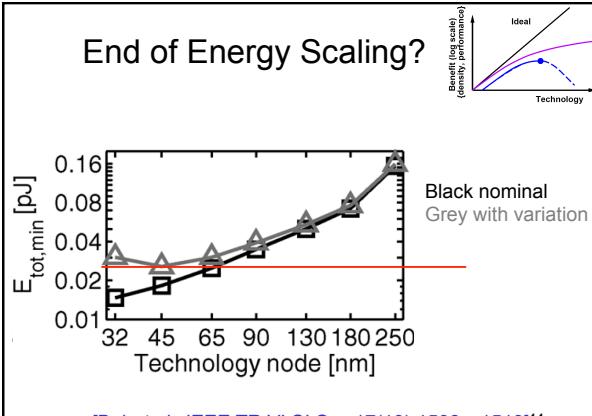
- Margins growing due to increasing variation
- Margined value may be worse than older technology?



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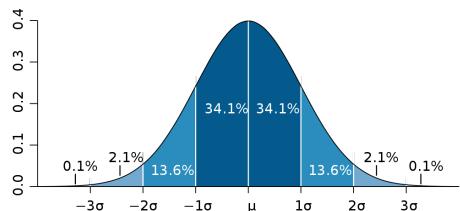
End of Energy Scaling?



[Bol et al., IEEE TR VLSI Sys 17(10):1508—1519]⁴⁴

Chips Growing

- Larger chips → sample further out on distribution curve



From: http://en.wikipedia.org/wiki/File:Standard_deviation_diagram.svg

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Lecture Ended Here

(Didn't really cover material in transient and thermodynamics sections)

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Challenge Transients

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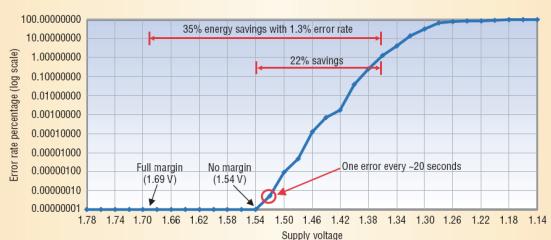
Transient Sources

- Effects
 - Thermal noise
 - Timing
 - Ionizing particles
 - α particle 10^5 to 10^6 electrons
 - Calculated gates with 15–30 electrons last time
 - Even if CMOS restores, takes time

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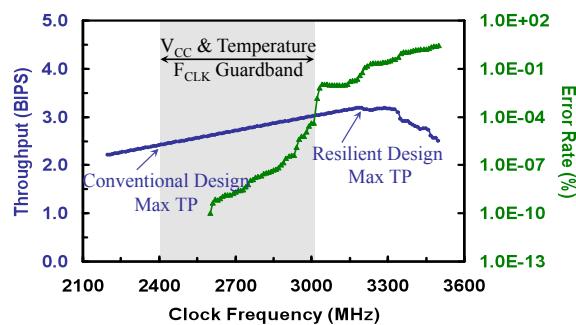
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Voltage and Error Rate



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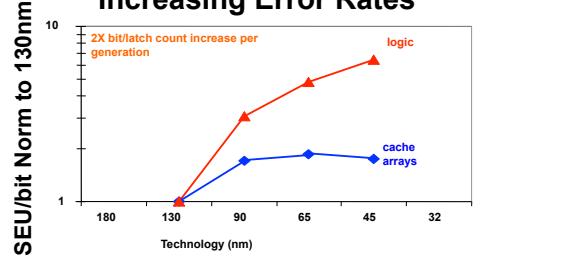
Errors versus Frequency



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Scaling and Error Rates

Increasing Error Rates



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Source: Carter/Intel

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Power and Reliability

- Intersection is the challenge
- Push V_{dd} in opposite directions
- Both reach inflection points
 - From doesn't matter
 - To major concern

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Thermodynamics

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Lower Bound?

- Reducing entropy costs energy
- Single bit gate output
 - Set from previous value to 0 or 1
 - Reduce state space by factor of 2
 - Entropy: $\Delta S = k \times \ln(\text{before}/\text{after}) = k \times \ln 2$
 - Energy = $T \Delta S = kT \times \ln 2$
- Naively: setting a bit costs at least $kT \times \ln 2$

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Numbers (ITRS 2005)

- $kT \times \ln(2) = 2.87 \times 10^{-21} J$ (at R.T. K=300)

Year in Production	2014	2015	2016	2017	2018	2019	2020
DRAM ½ Pitch (nm) (contacted)	28	25	22	20	18	16	14
MPU/ASIC Metal 1 (M1) ½ Pitch (nm) (contacted)	28	25	22	20	18	16	14
MPU/Physical Gate Length (nm)	11	10	9	8	7	6	6
L_p Physical gate length for LOP (nm) [1]	14	13	11	10	9	8	7
V_{dd} Power Supply Voltage (V) [6]	0.6	0.6	0.5	0.5	0.5	0.5	0.5
$C_{g\text{ total}}$ Total gate capacitance for calculation of CVT [14]							
Extended Planar Bulk (F/μm)							
UTB FD (F/μm)	5.83E-16	5.44E-16	5.09E-16				
DG (F/μm)	6.43E-16	6.14E-16	5.59E-16	5.24E-16	4.82E-16	4.41E-16	4.00E-16

W/L=3 \Rightarrow W=21nm=0.021μm $C \approx 8 \times 10^{-18} F \approx 10^{-17} F$

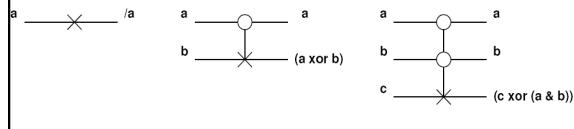
Table 41d

$$E_{op} = CV^2 = 2.5 \times 10^{-18} F \quad 55$$

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Three Reversible Primitives



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Universal Primitives

- These primitives
 - Are universal
 - Are all reversible
- If keep all the intermediates they produce
 - Discard no information
 - Can run computation in reverse

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Thermodynamics

- In theory, at least, thermodynamics does not demand that we dissipate any energy (power) in order to compute.

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Admin

- Assignment grades, feedback on blackboard for HW1 and HW2
- Class Wed.
- No class next Monday (2/22)

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Big Ideas

- Can trade time for energy
 - ...area for energy
- Noise and leakage limit voltage scaling
- Power major limiter going forward
 - Can put more transistors on a chip than can switch
- **Continued scaling demands**
 - Deal with noisier components
 - High variation and high transient upsets
- Thermodynamically admissible to compute without dissipating energy