### ESE535: **Electronic Design Automation**

Day 9: February 20, 2008 Partitioning (Intro, KLFM)

ESE535 Spring 2008 -- DeHo



### Today

- · Partitioning
  - why important
  - practical attack
  - variations and issues

### Motivation (1)

- Divide-and-conquer
  - trivial case: decomposition
  - smaller problems easier to solve
    - net win, if super linear
    - Part(n) +  $2 \times T(n/2) < T(n)$
  - problems with sparse connections or interactions
  - Exploit structure
    - limited cutsize is a common structural property
    - random graphs would **not** have as small cuts

### Motivation (2)

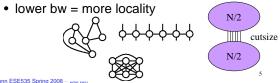
- · Cut size (bandwidth) can determine area
- · Minimizing cuts
  - minimize interconnect requirements
  - increases signal locality
- · Chip (board) partitioning
  - minimize IO
- · Direct basis for placement

nn ESE535 Spring 2008 -- DeHon

### **Bisection Bandwidth**

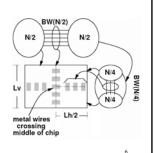
- Partition design into two equal size halves
- Minimize wires (nets) with ends in both halves
- Number of wires crossing is bisection bandwidth

• lower bw = more locality



### Interconnect Area

- · Bisection is lowerbound on IC width
  - Apply wire dominated
- · (recursively)



enn ESE535 Spring 2008 -- DeHon

### Classic Partitioning Problem

- Given: netlist of interconnect cells
- Partition into two (roughly) equal halves (A,B)
- minimize the number of nets shared by halves
- · "Roughly Equal"
  - balance condition:  $(0.5-\delta)N \le |A| \le (0.5+\delta)N$

Penn ESE535 Spring 2008 -- DeHor

### **Balanced Partitioning**

- · NP-complete for general graphs
  - [ND17: Minimum Cut into Bounded Sets, Garey and Johnson]
  - Reduce SIMPLE MAX CUT
  - Reduce MAXIMUM 2-SAT to SMC
  - Unbalanced partitioning poly time
- Many heuristics/attacks

Penn ESE535 Spring 2008 -- DeHon

### KL FM Partitioning Heuristic

- · Greedy, iterative
  - pick cell that decreases cut and move it
  - repeat
- · small amount of non-greediness:
  - look past moves that make locally worse
  - randomization

Penn ESE535 Spring 2008 -- DeHor

### Fiduccia-Mattheyses (Kernighan-Lin refinement)

- Start with two halves (random split?)
- · Repeat until no updates
  - Start with all cells free
  - Repeat until no cells free
    - Move cell with largest gain (balance allows)
    - Update costs of neighbors
    - Lock cell in place (record current cost)
  - Pick least cost point in previous sequence and use as next starting position
- Repeat for different random starting points,

  Penn ESESS Spring 2008 Delton

### Efficiency

Tricks to make efficient:

- Expend little (O(1)) work picking move candidate
- Update costs on move cheaply [O(1)]
- · Efficient data structure
  - update costs cheap
  - cheap to find next move

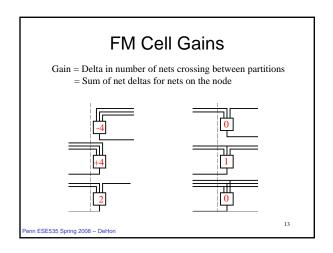
Penn ESE535 Spring 2008 -- DeHon

### Ordering and Cheap Update

- Keep track of Net gain on node == delta net crossings to move a node
  - cut cost after move = cost gain
- Calculate node gain as Σ net gains for all nets at that node
  - Each node involved in several nets
- · Sort nodes by gain



Penn ESE535 Spring 2008 -- DeHon



### After move node?

- · Update cost
  - Newcost=cost-gain
- · Also need to update gains
  - on all nets attached to moved node
  - but moves are nodes, so push to
    - all nodes affected by those nets

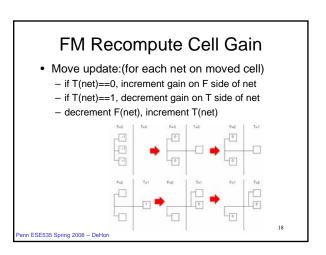
Penn ESE535 Spring 2008 -- DeHon

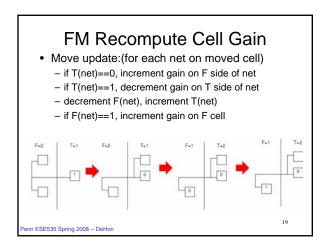
14

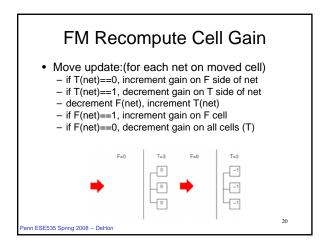
# Composability of Net Gains -1+1-0-1 = -1 Penn ESE535 Spring 2008 -- DeHon

# FM Recompute Cell Gain • For each net, keep track of number of cells in each partition [F(net), T(net)] • Move update:(for each net on moved cell) - if T(net)==0, increment gain on F side of net • (think -1 => 0)

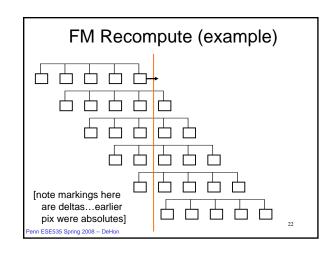
# FM Recompute Cell Gain • For each net, keep track of number of cells in each partition [F(net), T(net)] • Move update:(for each net on moved cell) - if T(net)==0, increment gain on F side of net • (think -1 ⇒ 0) - if T(net)==1, decrement gain on T side of net • (think 1=>0) F=2 T=1 F=2 T=1 F=2 T=1 T=1 F=2 T=1 T=1

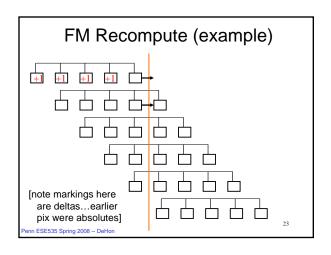


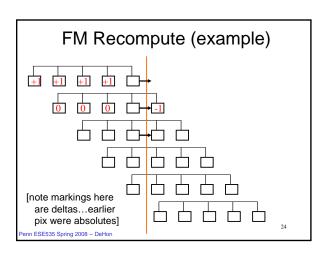


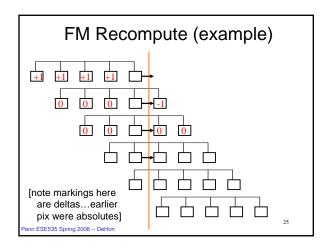


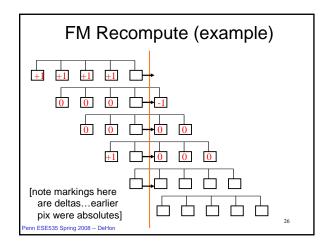
# FM Recompute Cell Gain • For each net, keep track of number of cells in each partition [F(net), T(net)] • Move update:(for each net on moved cell) - if T(net)==0, increment gain on F side of net • (think ·1 ⇒ 0) - if T(net)==1, decrement gain on T side of net • (think 1=>0) - decrement F(net), increment T(net) - if F(net)==1, increment gain on F cell - if F(net)==0, decrement gain on all cells (T)

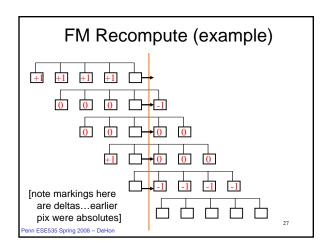


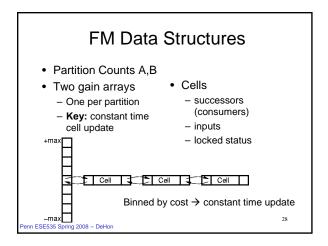


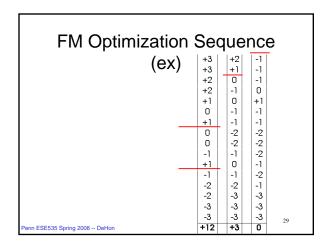












### FM Running Time?

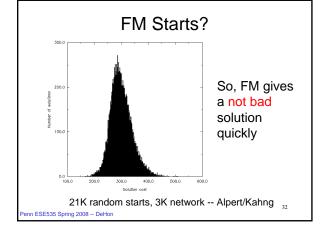
- · Randomly partition into two halves
- · Repeat until no updates
  - Start with all cells free
  - Repeat until no cells free
    - · Move cell with largest gain
    - Update costs of neighbors
    - · Lock cell in place (record current cost)
  - Pick least cost point in previous sequence and use as next starting position
- Repeat for different random starting points

Penn ESE535 Spring 2008 -- DeHon

### **FM Running Time**

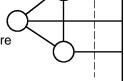
- Claim: small number of passes (constant?) to converge
- Small (constant?) number of random starts
- N cell updates each round (swap)
- Updates K + fanout work (avg. fanout K)
   assume K-LUTs
- Maintain ordered list O(1) per move
  - every io move up/down by 1
- Running time: O(K<sup>2</sup>N)
  - Algorithm significant for its speed (more than quality)

Penn ESE535 Spring 2008 -- DeHon



### Weaknesses? • Local, incremental moves only

- hard to move clusters
- no lookahead
- · Looks only at local structure



31

enn ESE535 Spring 2008 -- DeHon

### Improving FM

- Clustering
- · Technology mapping
- · Initial partitions
- Runs
- · Partition size freedom
- Replication

Following comparisons from Hauck and Boriello '96

Penn ESE535 Spring 2008 -- DeHo

### Clustering

- Group together several leaf cells into cluster
- Run partition on clusters
- Uncluster (keep partitions)
  - iteratively
- · Run partition again
  - using prior result as starting point
    - instead of random start

Penn ESE535 Spring 2008 -- DeHon

35

### **Clustering Benefits**

- Catch local connectivity which FM might miss
  - moving one element at a time, hard to see move whole connected groups across partition
- Faster (smaller N)
  - METIS -- fastest research partitioner exploits heavily
  - FM work better w/ larger nodes (???)

Penn ESE535 Spring 2008 -- DeHon

36

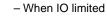
### How Cluster?

- Random
  - cheap, some benefits for speed
- · Greedy "connectivity"
  - examine in random order
  - cluster to most highly connected
  - 30% better cut, 16% faster than random
- Spectral (next time)
  - look for clusters in placement
  - (ratio-cut like)
- Brute-force connectivity (can be O(N2))

Penn ESE535 Spring 2008 -- DeHon

### **LUT Mapped?**

• Better to partition before LUT mapping.







**Today:** maybe a case for crude placement before LUT mapping? --- something to explore.

Penn ESE535 Spring 2008 -- DeHon

### **Initial Partitions?**

- Random
- · Pick Random node for one side
  - start imbalanced
  - run FM from there
- Pick random node and Breadth-first search to fill one half
- Pick random node and Depth-first search to fill half
- Start with Spectral partition

Penn ESE535 Spring 2008 -- DeHon

### **Initial Partitions**

- If run several times
  - pure random tends to win out
  - more freedom / variety of starts
  - more variation from run to run
  - others trapped in local minima

Penn ESE535 Spring 2008 -- DeHon

40

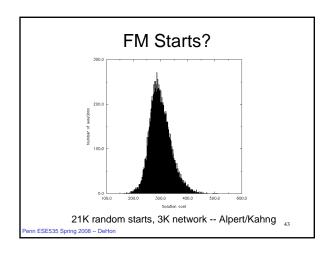
### 

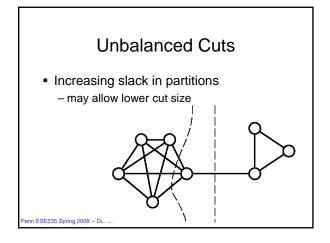
### Number of Runs

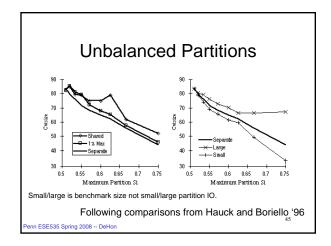
- 2 10%
- 10 18%
- 20 <20% (2% better than 10)
- 50 (4% better than 10)
- ...but?

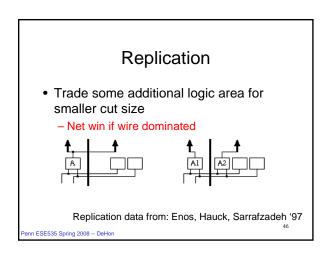
Penn ESE535 Spring 2008 -- DeHon

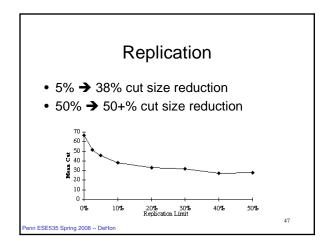
42



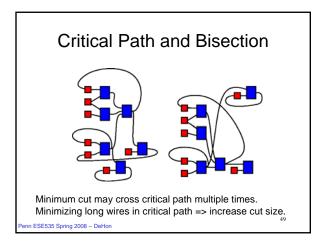








# What Bisection doesn't tell us • Bisection bandwidth purely geometrical • No constraint for delay – I.e. a partition may leave critical path weaving between halves



### So...

- · Minimizing bisection
  - good for area
  - oblivious to delay/critical path

Penn ESE535 Spring 2008 -- DeHon

Spring 2008 -- DeHop

### **Partitioning Summary**

- · Decompose problem
- · Find locality
- NP-complete problem
- linear heuristic (KLFM)
- many ways to tweak
  - Hauck/Boriello, Karypis
- · even better with replication
- only address cut size, not critical path delay

enn ESE535 Spring 2008 -- DeHon

51

### Admin

- Assignment 3
  - Start early
  - Select a time on Friday to meet?
- No class Monday (2/25)
  - Next class Wednesday

Penn ESE535 Spring 2008 -- DeHon

52

### Today's Big Ideas:

- Divide-and-Conquer
- Exploit Structure
  - Look for sparsity/locality of interaction
- Techniques:
  - greedy
  - incremental improvement
  - randomness avoid bad cases, local minima
  - incremental cost updates (time cost)
  - efficient data structures

Penn ESE535 Spring 2008 -- DeHon

53