ESE535:
Electronic Design Automation
Day 9: February 20, 2008
Partitioning
(Intro, KLFM)
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## Motivation (1)

- Divide-and-conquer
- trivial case: decomposition
- smaller problems easier to solve
- net win, if super linear
- Part(n) $+2 \times T(n / 2)<T(n)$
- problems with sparse connections or interactions
- Exploit structure
- limited cutsize is a common structural property
- random graphs would not have as small cuts


## Today

- Partitioning
- why important
- practical attack
- variations and issues


## Motivation (2)

- Cut size (bandwidth) can determine area
- Minimizing cuts
- minimize interconnect requirements
- increases signal locality
- Chip (board) partitioning
- minimize IO
- Direct basis for placement


## Bisection Bandwidth

- Partition design into two equal size halves
- Minimize wires (nets) with ends in both halves
- Number of wires crossing is bisection bandwidth
- lower bw = more locality


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## Interconnect Area

- Bisection is lowerbound on IC width
- Apply wire dominated
- (recursively)

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$$
\begin{aligned}
& \text { metal wires } \\
& \text { crossing }
\end{aligned}
$$

$$
\begin{aligned}
& \text { crossing } \\
& \text { middle of chip }
\end{aligned}
$$

## Classic Partitioning Problem

- Given: netlist of interconnect cells
- Partition into two (roughly) equal halves (A,B)
- minimize the number of nets shared by halves
- "Roughly Equal"
- balance condition: $(0.5-\delta) \mathrm{N} \leq|\mathrm{A}| \leq(0.5+\delta) \mathrm{N}$


## KL FM Partitioning Heuristic

- Greedy, iterative
- pick cell that decreases cut and move it
- repeat
- small amount of non-greediness:
- look past moves that make locally worse
- randomization


## Efficiency

Tricks to make efficient:

- Expend little (O(1)) work picking move candidate
- Update costs on move cheaply [O(1)]
- Efficient data structure
- update costs cheap
- cheap to find next move


## Balanced Partitioning

- NP-complete for general graphs
- [ND17: Minimum Cut into Bounded Sets, Garey and Johnson]
- Reduce SIMPLE MAX CUT
- Reduce MAXIMUM 2-SAT to SMC
- Unbalanced partitioning poly time
- Many heuristics/attacks
- Repeat until no updates
- Start with all cells free
- Repeat until no cells free
- Move cell with largest gain (balance allows)
- Update costs of neighbors
- Lock cell in place (record current cost)
- Pick least cost point in previous sequence and use as next starting position
- Repeat for different random starting pointso Penn ESE535 Spring 2008 -- DeHon


## Ordering and Cheap Update

- Keep track of Net gain on node == delta net crossings to move a node
- cut cost after move = cost - gain
- Calculate node gain as $\Sigma$ net gains for all nets at that node
- Each node involved in several nets
- Sort nodes by gain


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## FM Cell Gains

Gain = Delta in number of nets crossing between partitions
= Sum of net deltas for nets on the node


Composability of Net Gains


## FM Recompute Cell Gain

- For each net, keep track of number of cells in each partition [F(net), $T$ (net)]
- Move update:(for each net on moved cell)
- if $\mathrm{T}($ net $)==0$, increment gain on F side of net
- (think -1 $=>0$ )
- if $T$ (net) $==1$, decrement gain on $T$ side of net
- (think $1=>0$ )



## After move node?

- Update cost
- Newcost=cost-gain
- Also need to update gains
- on all nets attached to moved node
- but moves are nodes, so push to
- all nodes affected by those nets


## FM Recompute Cell Gain

- For each net, keep track of number of cells in each partition [F(net), $T$ (net)]
- Move update:(for each net on moved cell)
- if $T$ (net) $==0$, increment gain on $F$ side of net -(think -1 $=>0$ )



## FM Recompute Cell Gain

- Move update:(for each net on moved cell)
- if $T$ (net) $==0$, increment gain on $F$ side of net
- if $T$ (net)==1, decrement gain on $T$ side of net
- decrement $F$ (net), increment $T$ (net)




## FM Recompute Cell Gain

- Move update:(for each net on moved cell)
- if $T$ (net) $==0$, increment gain on $F$ side of net
- if $T$ (net) $==1$, decrement gain on $T$ side of net
- decrement $F(n e t)$, increment $T$ (net)
- if $F(n e t)==1$, increment gain on $F$ cell



## FM Recompute Cell Gain

- Move update:(for each net on moved cell)
- if $T$ (net) $==0$, increment gain on $F$ side of net
- if $T(n e t)==1$, decrement gain on $T$ side of net
- decrement $F$ (net), increment $T$ (net)
- if $F($ net $)==1$, increment gain on $F$ cell
- if $F($ net $)==0$, decrement gain on all cells $(T)$


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FM Recompute (example)


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FM Optimization Sequence



## FM Running Time?

- Randomly partition into two halves
- Repeat until no updates
- Start with all cells free
- Repeat until no cells free
- Move cell with largest gain
- Update costs of neighbors
- Lock cell in place (record current cost)
- Pick least cost point in previous sequence and use as next starting position
- Repeat for different random starting pointş Penn ESE535 Spring 2008 -- DeHon


## FM Running Time

- Claim: small number of passes (constant?) to converge
- Small (constant?) number of random starts
- N cell updates each round (swap)
- Updates K + fanout work (avg. fanout K) - assume K-LUTs
- Maintain ordered list O(1) per move - every io move up/down by 1
- Running time: $\mathrm{O}\left(\mathrm{K}^{2} \mathrm{~N}\right)$
- Algorithm significant for its speed (more than quality)


## Weaknesses?

- Local, incremental moves only - hard to move clusters - no lookahead
- Looks only at local structure



## Clustering

- Group together several leaf cells into cluster
- Run partition on clusters
- Uncluster (keep partitions) - iteratively
- Run partition again
- using prior result as starting point
- instead of random start


## Improving FM

- Clustering
- Technology mapping
- Initial partitions
- Runs
- Partition size freedom
- Replication

Following comparisons from Hauck and Boriello '96
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## Clustering Benefits

- Catch local connectivity which FM might miss
- moving one element at a time, hard to see move whole connected groups across partition
- Faster (smaller N)
- METIS -- fastest research partitioner exploits heavily
- FM work better w/ larger nodes (???)


## How Cluster?

- Random
- cheap, some benefits for speed
- Greedy "connectivity"
- examine in random order
- cluster to most highly connected
- 30\% better cut, 16\% faster than random
- Spectral (next time)
- look for clusters in placement
- (ratio-cut like)
- Brute-force connectivity (can be $\mathrm{O}\left(\mathrm{N}^{2}\right)$ )


## Initial Partitions?

- Random
- Pick Random node for one side
- start imbalanced
- run FM from there
- Pick random node and Breadth-first search to fill one half
- Pick random node and Depth-first search to fill half
- Start with Spectral partition



## LUT Mapped?

- Better to partition before LUT mapping.
- When IO limited


Today: maybe a case for crude placement before LUT mapping? --- something to explore. ${ }_{38}$

## Initial Partitions

- If run several times
- pure random tends to win out
- more freedom / variety of starts
- more variation from run to run
- others trapped in local minima
- 2-10\%
- 10-18\%
- $20<20 \%$ (2\% better than 10)
- 50 ( $4 \%$ better than 10 )
- ...but?
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## Unbalanced Partitions



Small/large is benchmark size not small/large partition IO.
Following comparisons from Hauck and Boriello '96 Penn ESE535 Spring 2008 -- DeHon

## Replication

- $5 \% \rightarrow 38 \%$ cut size reduction
- $50 \% \rightarrow 50+\%$ cut size reduction


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## Unbalanced Cuts

- Increasing slack in partitions



## Replication

- Trade some additional logic area for smaller cut size
- Net win if wire dominated


Replication data from: Enos, Hauck, Sarrafzadeh '97

## What Bisection doesn't tell us

- Bisection bandwidth purely geometrical
- No constraint for delay
- I.e. a partition may leave critical path weaving between halves

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- Minimizing bisection
- good for area
- oblivious to delay/critical path


## Partitioning Summary

- Decompose problem
- Find locality
- NP-complete problem
- linear heuristic (KLFM)
- many ways to tweak
- Hauck/Boriello, Karypis
- even better with replication
- only address cut size, not critical path delay


## Today's Big Ideas:

- Divide-and-Conquer
- Exploit Structure
- Look for sparsity/locality of interaction
- Techniques:
- greedy
- incremental improvement
- randomness avoid bad cases, local minima
- incremental cost updates (time cost)
- efficient data structures

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