

Equivalence

- Brute Force:
 - Generate all strings of length |state|
 - (for larger FSM = the one with the most states)
 - Feed to both FSMs with these strings
- Observe any differences?How many such strings?
- |Alphabet|states

enn ESE 535 Spring 2011 -- DeHon

Smarter

- Create composite FSM
 - Start with both FSMs
 - Connect common inputs together (Feed both FSMs)
 - XOR together outputs of two FSMs
 - Xor's will be 1 if they disagree, 0 otherwise
- Ask if the new machine ever generate a 1 on an xor output (signal disagreement)

8

- Any 1 is a proof of non-equivalence
- Never produce a 1 \rightarrow equivalent

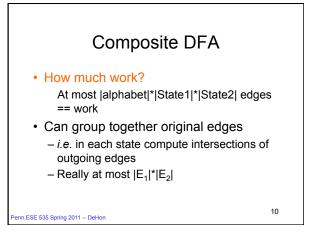
enn ESE 535 Spring 2011 -- DeHon

7

9

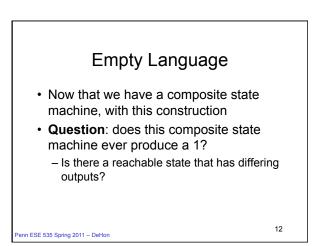
Creating Composite FSM

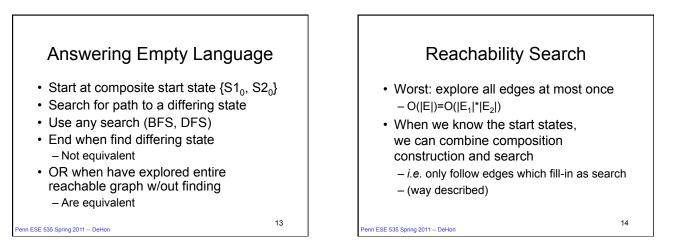
- Assume know start state for each FSM
- + Each state in composite is labeled by the pair $\{S1_i,\,S2_j\}$
- How many such states?
 - Compare to number of strings of length #states?
- Start in {S1₀, S2₀}
- For each symbol *a*, create a new edge:
 T(a,{S1₀, S2₀})→ {S1ᵢ, S2ᵢ}
 - If $T_1(a, S1_0) \rightarrow S1_i$ and $T_2(a, S2_0) \rightarrow S2_i$
- Repeat for each composite state reached ESE 535 Spring 2011 - DeHon

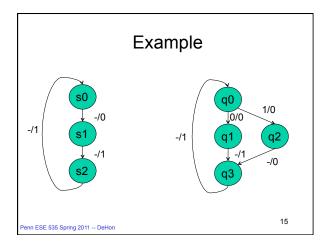


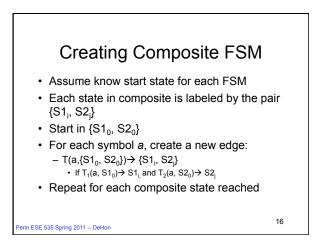
Non-Equivalence

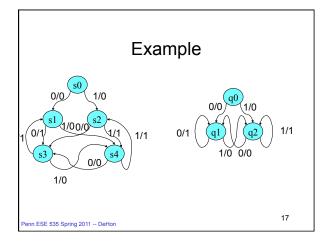
- State {S1_i, S2_j} demonstrates nonequivalence iff
 - {S1_i, S2_i} reachable
 - On some input, State S1, and S2, produce different outputs
- If S1_i and S2_j have the same outputs for all composite states, it is impossible to distinguish the machines
 - They are equivalent
- A **reachable** state with differing outputs - Implies the machines are not identical 11 Penn ESE 55 Spring 2011 - DeHon

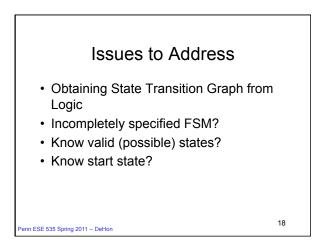


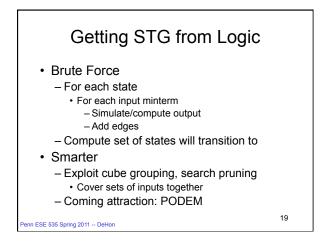












reachable

Penn ESE 535 Spring 2011 -- DeHor

Incomplete State Specification · Add edge for unspecified transition to - Single, new, terminal state · Reachability of this state may indicate problem - Actually, if both transition to this new state for same cases Might say are equivalent · Just need to distinguish one machine in this

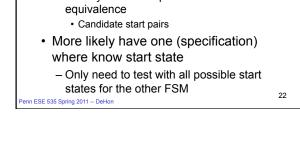
20

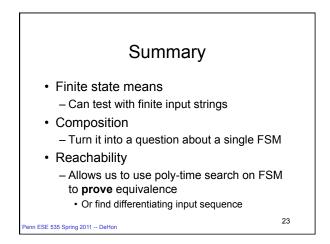
state and other not

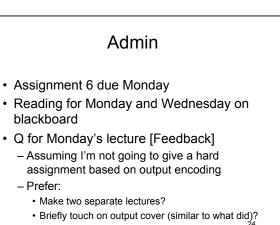
Valid States Start State? • Worst-case: · Composite state construction and reachability further show what's - Try verifying for all possible start state pairs - Identify start state pairs that lead to equivalence · So, end up finding set of valid states · Candidate start pairs - Not all possible states from state bits · More likely have one (specification) where know start state

nn ESE 535 Spring 2011 -- DeHon

21







enn ESE 535 Spring 2011 -- DeHon

Big Ideas	
 Equivalence Same observable behavior Internal implementation irrelevant Number/organization of states, encoding of state bit Exploit structure Finite DFA necessity of reconvergent paths Structured Search – group together cubes Limit to valid/reachable states Proving invariants vs. empirical verification 	3
renn ESE 535 Spring 2011 DeHon	25