

ESE535: Electronic Design Automation

Day 15: March 13, 2013
High Level Synthesis II
Dataflow Graph Sharing

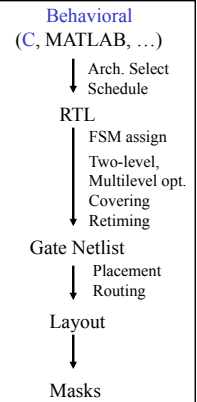


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Today

Sharing

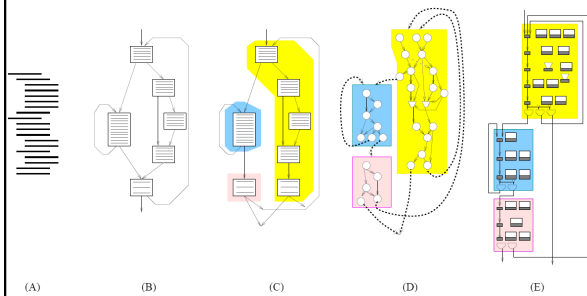
- Dataflow subgraph
 - Pattern identification
 - Pattern selection



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Flow Review



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Additional Concerns?

What are we still not satisfied with?

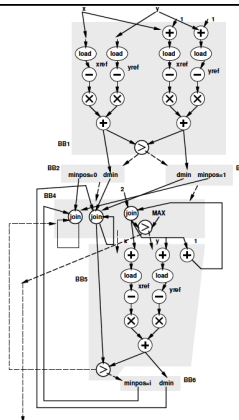
- Parallelism in hyperblock
 - Especially if memory sequentialized
 - Disambiguate memories?
 - Allow multiple memory banks?
- Only one hyperblock active at a time
 - Share hardware between blocks?
- Data only used from one side of mux
 - Share hardware between sides?
- Most logic in hyperblock idle?
 - Couldn't we pipeline execution?

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Preclass

- Common subgraphs?
- How would we like to share?
 - If trying to avoid slowdown
 - If willing to make area-time tradeoffs?



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Subgraph Sharing

- Can potentially share identical subgraphs
- Can share similar subgraphs

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Evaluating Subgraph Sharing

- What do we have to do to share subgraphs?
- When is it worthwhile?
 - How big does graph need to be?
 - How much overhead to share?

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Example

- Muxes on inputs to an adder
 - Probably bigger than just having two adders
 - $2(A_{mux}) + A_{add} > 2(A_{add})$
- Muxes on input to multiplier
 - Probably smaller than two multipliers
 - $2(A_{mux} + A_{mpy}) < 2(A_{mpy})$

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Extreme Case

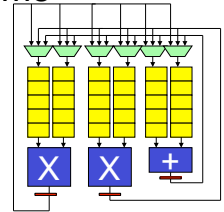
- If ignored multiplexing overhead, what would we get?

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VLIW Extreme

- Sketch
 - Each basic block requires a set of operators to achieve minimum path length
 - Union sets over all basic blocks
 - Build VLIW with that operator set
- Why unsatisfying?



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Favorable Subgraphs

- Particularly beneficial when I/O into subgraph small
 - Overhead for muxing proportional to inputs

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Approach

- Find candidate, reusable subgraphs
- Select a cover set of subgraphs
- Assign original graph to subgraphs
 - Assess benefits of sharing
- Patch together subgraphs with control and multiplexing

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Find Subgraphs

- How might we find the set of candidate subgraphs?

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Finding Subgraphs

- Keep set of subgraphs of size k
- Create subgraphs of size $k+1$ from subgraphs of size k
 - By adding a neighboring node
 - Maybe several such expansions for each k -subgraph
- Careful: can end up with exponential subgraphs

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Optimization

- Canonicalize subgraphs so recognize when encounter same subgraph again
 - Keep set of subgraphs small

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Optimization

- Compute candidate graph patterns during subgraph generation
 - Each subgraph may become a candidate
 - Keep track of subgraphs that might match with candidate subgraphs
 - As add subgraph, compare it with candidate patterns and add to list if “close” enough
 - At end of a given graph size, prune out patterns with too few potential matches

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Close enough?

- **Conceptually:** not too expensive to use the candidate pattern
- **Concretely:** compute a distance metric between graph and pattern
 - Minimum cost of edits to morph one graph into another
 - E.g. relabel nodes, remove nodes
 - Want to capture potential cost of adding muxes and control

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Algorithm 1 HPR Algorithm
1:  $\mathbb{P}$        $\rightarrow$  set of discovered patterns
2:  $S_k$       $\rightarrow$  set of size  $k$  subgraph
3:  $INST(\mathbb{P})$   $\rightarrow$  instances of a pattern  $P$ 
4:  $l_{dist}$     $\rightarrow$  edit distance limit
5:  $l_{count}$    $\rightarrow$  frequency limit
6:
7: travel all DFGs, add size 1 patterns and instances to  $\mathbb{P}$  and  $S_1$ 
8: for  $k \leftarrow 2, N$  do
9:   for all  $s_k \in S_k$  do
10:    adding a neighbor to expand  $s_k$  to  $s_{k+1}$ 
11:    if  $s_k$  is the primary subgraph of  $s_{k+1}$  and convex then
12:      calculate  $CV(s_{k+1})$ 
13:      get list of patterns  $P_i$  s.t.  $\|CV(P_i) - CV(s_{k+1})\|_1 \leq 4 * l_{dist}$  using LSH
14:      calculate edit distance of  $s_{k+1}$  with each  $P_i$ 
15:      if  $d(P_i, s_{k+1}) < l_{dist}$  then
16:        add  $s_{k+1}$  to  $INST(P_i)$ 
17:      else
18:        create a new pattern based on  $s_{k+1}$ , add to  $\mathbb{P}$ 
19:      end if
20:      add  $s_{k+1}$  to  $S_{k+1}$ 
21:    end if
22:  end for
23:  for all new pattern  $P_i \in \mathbb{P}$  do
24:    if  $|INST(P_i)| < l_{count}$  &&  $size(P_i) \leq (k+1 - l_{dist})$  then
25:      remove  $P_i$  from  $\mathbb{P}$ 
26:      remove  $INST(P_i)$  from  $S_{k+1}$ 
27:    end if
28:  end for
29: end for
  
```

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[Cong & Jiang / FPGA 2008]

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Cover Subgraphs

- What's our goal?

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Cover Goal

- Minimize area

$$\sum_P A(p) + \sum_{BB} A_{use}(p \in P)$$

- Minimum added latency
 - Delay of BB covered by p in P

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Cover Subgraph

- Given a proposed set of pattern graphs, how can we cover?

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Cover Subgraph

- How many sets if we explored them all?

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Greedy Cover Subgraph

- How might we cover greedily?

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Greedy Cover Subgraph

- Select most beneficial pattern
- Assign it to the stuff it covers
 - Add logic to share accommodate
 - Remove those as things that need to be covered
- Repeat until all covered or no benefit

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Most Beneficial Pattern

- How would we define pattern benefit?

Beneficial Pattern

- Area

$$\frac{N * (mux(io) + mux(internal)) + area(P)}{N * mux(io) + area(P)}$$

- Latency

$$\frac{|P|}{latency(P)}$$

Pattern and Graph Statistics

Size	#Subgraph	#Pattern	#Inst	#Calc
2	62	3	62	0.96
3	108	12	108	1.08
4	195	20	161	1.48
5	366	26	248	1.49
6	701	35	404	1.9
7	1357	58	579	2.6
8	2533	76	714	3.18
9	4517	86	762	3.82
10	7800	94	793	4.43
11	13112	101	668	7.04
12	21365	73	348	7.89
13	33316	32	87	5.03
14	49040	3	6	1.7

Big Ideas:

- Sharing
- Estimation
- Techniques
 - Graph Matching
 - Covering
 - Greedy

Admin

- Assignment 5a due Monday
- Reading for Monday online