









CNF

- · Conjunctive Normal Form
- · Logical AND of a set of clauses - Product of sums
- Clauses: logical OR of a set of literals
- · Literal: a variable or its complement
- E.g.

(A+B+/C)*(/B+D)*(C+/A+/E)

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CNF · Conjunctive Normal Form · Logical AND of a set of clauses · To be satisfied: - Every clause must be made true • (A+B+/C)*(/B+D)*(C+/A+/E) -If know D=false → B must be false

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Avoiding Clause Visits

- Idea: watch only 2 variables in each clause
- Only care about final set of next to last variable
- If set other k-2, won't force an implication

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- When set one of these (and everything else set)
 - Then we have an implication

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Davis-Putnam w/ Learning

while (true) {
 if (!decide()) // no unassigned vars
 return(satisfiable);
 while (!bcp()) { // constraint propagation
 analyzeConflicts(); // learning
 if (!resolveConflict()) // backtrack
 return(not satisfiable);
 }
}

}

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Implication Graph
As perform bcp propagation

When set variable, insert back link to previous variable set forcing this variable set
Graph captures what this implication depends upon

When encounter a conflict

Identify what variable values caused













Clause Tradeoff

- Adding clauses facilitates implications
 Increases pruning
 - Must make less decisions
- Adding clauses increases size of clause database
 - Increases memory
 - Could add exponential clauses
 - Forces more work to push implications

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Learned Clauses

- Runtime = Decisions * ImplicationTime
 Decisions decreasing
 - Implication Time increasing
- Starting from 0 learned clauses,
 Net decrease in runtime
- Eventually, Implication Time too large and slows down
- · Optimum with limited number of learned clauses

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