

# Programming with Types

Run-time type  
analysis and the  
foundations of  
program reflection

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# Reflection

- A style of programming that supports the *run-time discovery* of program information.
  - “What does this code do?”
  - “How is this data structured?”
- Running program provides information about itself.
  - self-descriptive computation.
  - self-descriptive data.

# Applications of reflection

- **Runtime systems:** garbage collection, serialization, structural equality, cloning, hashing, checkpointing, dynamic loading
- **Code monitoring tools:** debuggers, profilers
- **Component frameworks:** software composition tools, code browsers
- **Adaptation:** stub generators, proxies
- **Algorithms:** iterators, visitor patterns, pattern matching, unification

# Primitive notions of reflection

- What is the fundamental enabling mechanism to support reflection?
  - **Run-time examination of type or class.**
- **Not** dynamic dispatch in OO languages.
  - Have to declare an instance for every new class declared. Easy but tedious.
  - Simple apps hard-wired in Java.
- **Not** instanceof operator in OO languages.
  - It requires a closed world.
    - Need to know the name of the class a priori.
    - Need to know what that name means.

# Structural Reflection

- Need to know about the **structure** of the data to implement these operations once and for all.
- Java Reflection API
  - Classes to describe the type structure of Java Class, Field, Method, Array,...
  - Methods to provide access to these classes at run time: Object.getClass, Class.getFields, Field.getType ...

```
String serialize( Object o ) {
    String result = "[";
    Fields[] f = o.getClass().getFields();
    for ( int i=0; i<f.length; i++ ) {
        Class fc = f[i].getType();
        if ( fc.isPrimitive() ) {
            if ( fc == Integer.TYPE ) {
                result += serializeInt((Integer) f[i].get( o ) );
            } else if ( fc == Boolean.TYPE ) {
                result += serializeBoolean((Boolean) f[i].get( o ) );
            } else if ...
        } else { result += serialize( f[i].get( o ) ); }
    }
    return result + "]" ;
}
```

# Not integrated with type system

- Can't catch bugs statically.

```
if ( fc == Integer.TYPE )  
    result += serializeBoolean( (Boolean) f[i].get( o ) );
```

- Need redundant tests of type information.

```
if ( fc == Integer.TYPE )  
    result += serializeInt( (Integer) f[i].get( o ) );
```

- All objects must have attached type information.

```
o.getClass();  
(Integer)o;
```

# Separating types from data

- Implementation must store type information with each data value.
  - Necessary for `getClass` and `runtime casts`.
- Can't express the run-time behavior of type information.
  - Hinders optimization in typed low-level languages.
- Prevents type abstraction in high-level languages.
  - Impossible to hide the implementation of an abstract data-type.
  - Necessary for modularity and representation independence.

# Foundational study of reflection

- It is not clear how to smoothly integrate these dynamic mechanisms into a statically typed language.
- An ideal framework...
  - Must be connected with the type system.
  - Must be able to express optimizations.
  - Must allow type abstraction.
  - Must extend to advanced type systems.

# My Work

- Examination of the foundational mechanisms for reflection.
  - Done in the context of typed lambda calculi
- Contributions in this area:
  - An accurate connection between run-time type information and types [Crary, Weirich, Morrisett 98].
  - A core reflection language with the flexibility to describe a variety of type systems [Crary & Weirich 99].
  - An encoding of these languages into a language without specialized reflection mechanisms [Weirich 01].
  - An extension of reflection that encompasses type constructors and quantified types [Weirich 02].

# Formalizing reflection

- A standard typed lambda calculus plus an abstract datatype (ADT) to represent type information.

$\tau ::= \text{int} \mid \text{string} \mid \tau_1 \rightarrow \tau_2 \mid \tau_1 \text{ ' } \tau_2 \mid \text{any} \mid \text{rep}$   
 $e ::= 0 \mid 1 \mid \text{"foo"} \mid \dots \mid x \mid \lambda x:\tau. e \mid e_1 (e_2) \mid \langle e_1, e_2 \rangle \mid e.1 \mid e.2$

$(\tau) e \mid \text{typeof}(e)$   
 $\text{Rint} \mid \text{Rstring}$   
 $\text{Rarrow}(e_1, e_2) \mid \text{Rpair}(e_1, e_2)$   
 $\text{tcase } e \text{ of}$   
 $\text{Rint} ) \dots$   
 $\text{Rstring} ) \dots$   
 $\text{Rarrow}(x, y) ) \dots$   
 $\text{Rpair}(x, y) ) \dots$

Some way to hide the

A convenient way to get the type of a value

and a checked cast to recover it

# Comparison with Java Reflection

## Idealized Language

- any
- rep
- Rint
- Rstring
- typeof(e)
- $(\tau)e$

## Java Reflection API

- Object
- Class/Field/Method
- Integer.TYPE
- String.getClass();
- e.getClass();
- *(classname)e*

# Serialization

serialize has type: `any → string`

`serialize (x) =`

`tcase ( typeof(x) ) of`

`Rint ) int2string( (int) x )`

`Rstring ) “\“” + (string) x + “\””`

`Rpair(w,z) )`

`“(“ + serialize( (any'any) x.1 ) + “,”`

`+ serialize( (any'any) x.2 ) + “)”`

`Rarrow(w,z) ) “<function>”`

# Serialize without typeof

New type of serialize : rep ' any → string

**serialize (xrep, x ) =**

**tcase ( xrep ) of**

**Rint                   ) int2string( (int) x )**

**Rstring               ) “\“” + (string) x + “\””**

**Rpair(w,z)        )**

**“(“ + serialize( w, (any'any) x.1 ) + “,”**

**+ serialize( z, (any'any) x.2 ) + “)”**

**Rarrow(w,z) ) “<function>”**

# Accurate reflection

- Connect types and their representations.
- A term has the type  $\text{rep}(\tau)$  if it represents  $\tau$ .

$\text{Rint} : \text{rep}(\text{int})$

$\text{Rstring} : \text{rep}(\text{string})$

$\text{Rpair}(e1, e2) : \text{rep}(\tau1 \text{ ' } \tau2)$  ( if  $e1 : \text{rep}(\tau1)$  and  $e2 : \text{rep}(\tau2)$  )

$\text{Rarrow}(e1, e2) : \text{rep}(\tau1 \rightarrow \tau2)$  ( if  $e1 : \text{rep}(\tau1)$  and  $e2 : \text{rep}(\tau2)$  )

- Type variables express the connection.
  - $x : \alpha, y : \text{rep}(\alpha)$

[Crary, Weirich, Morrisett 98]

# Type Analysis

- The analysis term *refines* the type information.

**tcase (x : rep( $\alpha$ )) of**

**Rint                    ) ...  $\alpha$  is int**

**Rstring                 ) ...  $\alpha$  is string**

**Rpair(e1, e2)         ) ...  $\alpha$  is a pair type**

**Rarrow(e1,e2)        ) ...  $\alpha$  is a function type**

# Serialize without casts

- `serialize` has type :  $\delta\alpha. \text{rep}(\alpha) ' \alpha \rightarrow \text{string}$

`serialize (x:rep( $\alpha$ ), y: $\alpha$ ) =`

`tcase x of`

`Rint            ) int2string(y)`

`Rstring        ) “\“” + y + “\””`

`Rpair(w,z)    ) “(” + serialize(w,y.1) + “,”  
                  + serialize(z, y.2) + “)”`

`Rarrow(w,z)   ) “<function>”`

# Benefits of this approach

- Can express low-level operation.
  - Rep types used to add dynamic loading to Typed Assembly Language (TAL).  
[Hicks, Weirich, Crary 2000]
- Can optimize use of analysis.
  - **foo (x:array  $\alpha$ , y:rep( $\alpha$ )) = tcase y of ...**
- Preserves type abstraction.
  - can't determine  $\alpha$  without **rep( $\alpha$ )**

# Scaling to more expressivity

- Current type systems are *much* more sophisticated.
  - Objects/Classes [Java, C++, C#, OCaml, ... ]
  - First-class polymorphic/abstract types [Haskell, Cyclone, Vault, CLU, ... ]
  - Higher-order type constructors [ML, Haskell, ...]
  - Region types [Cyclone, Vault, Tofte&Talpin, Gay&Aiken, ...]
  - Security types [JIF, MLIF, PCC, CCured, Cqual, Walker, ...]
  - Bounding time/space usage [Crary&Weirich]
  - Using resources correctly [Igarashi & Kobayashi, ... ]
  - Dependent types [Cayenne, Xi, Shao et al., ...]
- Scaling structural type analysis to these systems in this framework is a challenge.

## But we want to...

- These type systems are getting very good at describing the **behavior** of programs.
  - The goal of advanced type systems is to verify expressive program properties.
- Analyzing these types at run-time provides a foundation for *Behavioral Reflection*.
  - *Example*: if the type system tracks the running time of each method, a real-time scheduler may use this information.

# Rest of Talk

- I will talk about how to extend type analysis to advanced type systems.
- Two crucial issues:
  - Type constructors
  - Types with binding structure
- These constructs are *foundational* to many current type systems.



# Serialization

**serialize**[ $\alpha$ ] ( $x:\alpha$ ) =

**tcase**  $\alpha$  of

**int** ) **int2string**( $x$ )

**string**) “\” +  $x$  + “\””

$\beta$  '  $\gamma$  ) “(” + **serialize**[ $\beta$ ]( $x.1$ ) + “,”

+ **serialize**[ $\gamma$ ]( $x.2$ ) + “)”

$\beta \rightarrow \gamma$  ) “<function>”

# Type constructors

- Types indexed by other types.
- Useful to describe parameterized data structures.
  - **head** : $\delta\alpha. \text{list } \alpha \rightarrow \alpha$
  - **tail** : $\delta\alpha. \text{list } \alpha \rightarrow \text{list } \alpha$
  - **add** : $\delta\alpha. (\alpha' \text{ list } \alpha) \rightarrow \text{list } \alpha$
- Don't have to cast the type of elements removed from data structures.

# Type functions

- Type constructors are functions from types to types.
- Expressed in the type syntax like lambda-calculus functions.

$$\tau ::= \dots \mid \lambda\alpha . \tau \mid \tau_1 \tau_2 \mid \alpha$$

- *Example:*

$$\mathbf{Quad} = \lambda\alpha. (\alpha' \alpha)' (\alpha' \alpha)$$

- Static language for reasoning about the relationship between types.

# Types with binding structure

- Parametric polymorphism hides the types of inputs to functions.

$\delta\alpha. \text{rep}(\alpha) ' \alpha \rightarrow \text{string}$

- *Other examples:*
  - Existential types ( $\exists\alpha. \tau$ ) hide the actual type of stored data.
  - Recursive types ( $\mu\alpha. \tau$ ) describe data structures that may refer to themselves (such as lists).
  - Self quantifiers ( $\text{self } \alpha. \tau$ ) encode objects.

# Problems with these types

- tcase is based on the fact that the closed, simple types are inductive.

$$\tau ::= \text{int} \mid \text{string} \mid \tau_1 \rightarrow \tau_2 \mid \tau_1 \mid \tau_2$$

- Analysis is an *iteration* over the type structure.
- With quantified types, the structure is not so simple.

$$\tau ::= \dots \mid \forall \alpha. \tau \mid \alpha$$

# Example

tcase  $\alpha$  of  
int ) ...  
string ) ...

$\beta \rightarrow \gamma$  ) ...

$\beta' \gamma$  ) ...

$\delta\alpha.??$  ) ...

Here  $\beta$  and  $\gamma$  are bound to the subcomponents of the type, so they may be analyzed.

Can't abstract the body of the type here, because of free occurrences of  $\alpha$ .

# Higher-order abstract syntax

- Use type constructors to represent polymorphic types.

$\delta \alpha . \alpha \rightarrow \alpha$  vs.  $\delta(\lambda \alpha . \alpha \rightarrow \alpha)$

- In branch for  $\delta$ , we can abstract that constructor.

**tcase**  $\delta(\lambda \alpha . \alpha \rightarrow \alpha)$  of

**int**    ) ...

**$\beta \rightarrow \gamma$**  ) ...

**$\delta\delta$**     ) ... //  $\delta$  is bound to  $(\lambda \alpha . \alpha \rightarrow \alpha)$

- Have to apply  $\delta$  to some type in order to analyze it. This works well for some examples.

[Pfenning&Elliot][Trifonov et al.]

## But not for all

`serializeType[ $\alpha$ ] =`

`tcase  $\alpha$  of`

`int ) “int”`

`$\beta$  '  $\gamma$  ) “(“ + serializeType[ $\beta$ ] + “ * ”  
+ serializeType[ $\gamma$ ] + “)”`

`$\beta \rightarrow \gamma$  ) “(“ + serializeType[ $\beta$ ] + “ -> ”  
+ serializeType[ $\gamma$ ] + “)”`

`$\delta\beta$  ) ???`

# Two solutions with one stone

If we can analyze type constructors in a principled way, then we can analyze quantified types in a principled way.

# Type equivalence

- For type checking, we must be able to determine when two types are semantically equal.
  - to call a function we must make sure that its argument has the right type.
- *Reference algorithm*: fully apply all type functions inside the two types and compare the results.

$$(\lambda \alpha. \alpha ' \alpha) (\text{int}) =? (\lambda \beta. \beta ' \text{int}) (\text{int})$$
$$\text{int}' \text{int} =? \text{int}' \text{int}$$

# Constraint on type analysis

- When we analyze this type language we *must* respect type equivalence.

**`tcase [(\lambda\alpha. \alpha ' int) int]...`**

must produce the same result as

**`tcase [ int ' int ]...`**

- Type functions, applications, and variables must be “transparent” to analysis.
- Otherwise, execution of program depends on implementation of type checker.

# Generic/Polytypic programming

- Provides a general way to generate operations over parameterized data-structures.
  - [Moggi & Jay][Jansson & Juering][Hinze]
  - Example: **gmap**<list> applies a function  $f$  to all of the  $\alpha$ 's in **list**  $\alpha$ .
  - This is a *compile-time* specialization. No type information is analyzed at run-time.
- A polytypic definition must also respect type equality.
  - $\text{foo} < (\lambda\alpha. \alpha' \text{ int}) \text{ int} > = \text{foo} < \text{int}' \text{ int} >$

## Basic idea

- Create an *interpretation* of the type language with the term language.
  - Map type functions to term functions.
  - Map type variables to term variables.
  - Map type applications to term applications.
  - Map type constants to (almost) anything.
- We can use this idea at run-time to analyze type constructors and quantified types.

# Type Language

$t ::= \alpha$

|  $\lambda\alpha. \tau$

|  $\tau_1 \tau_2$

| **int** | **string**

|  $\rightarrow$  |  $'$  |  $\delta$

- variable
- function
- application
- constants

- The type **int ' int** is the constant **'** applied to **int** twice.
- The type  **$\delta\alpha . \alpha \rightarrow\alpha$**  is the constant  **$\delta$**  applied to the type constructor  **$(\lambda\alpha . \alpha \rightarrow\alpha)$** .

# Interpreter

Instead of `tcase`, define analysis term:

$$\text{tinterp}[\eta] \tau$$

- To interpret this language we need an environment to keep track of the variables.
- This environment will also have mappings for all of the constants.

# Operational semantics of tinterp

- Type constants are retrieved from the environment

$\text{tinterp}[\eta] \text{ int} \rightarrow \eta(\text{int})$

$\text{tinterp}[\eta] \text{ string} \rightarrow \eta(\text{string})$

$\text{tinterp}[\eta] \rightarrow \rightarrow \eta(\rightarrow)$

$\text{tinterp}[\eta] ' \rightarrow \eta(')$

$\text{tinterp}[\eta] 8 \rightarrow \eta(8)$

- Type variables are retrieved from the environment

$\text{tinterp}[\eta] \alpha \rightarrow \eta(\alpha)$

# Type functions

- Type functions are mapped to term functions.
- When we reach a type function, we add a new mapping to the environment.

$\text{tinterp}[\eta] (\lambda\alpha.\tau) \rightarrow$   
 $\lambda x. \text{tinterp}[\underbrace{\eta + \{\alpha\}x}] (\tau)$

Execution extends  
environment, mapping  $\alpha$  to  $x$ .

# Application

- Type application is interpreted as term application

$\text{tinterp}[\eta] (\tau_1 \tau_2)$

$\rightarrow (\text{tinterp}[\eta] \tau_1) (\text{tinterp}[\eta] \tau_2)$

The interpretation of  $\tau_1$  is a function

# Example

`serializeType[τ] = tinterp [η] τ`

where  $\eta = \{$

`int`     ) `“int”`

`string` ) `“string”`

`'`       ) `λ x:string. λ y:string.`  
          `“(" + x + “*” + y + “)”`

`→`      ) `λ x:string. λ y:string.`  
          `“(" + x + “->” + y + “)”`

`8`      ) `λ x:string→string.`  
          `let v = gensym () in`  
          `“(all ” + v + “.” + (x v) + “)”`

`}`

# Example execution

`serializeType[int'int]`

→ `(tinterp[η] `) (tinterp[η] int) (tinterp[η] int)`

→ `(λ x:string. λ y:string. "(" + x + "*" + y + ")")  
 (tinterp[η] int) (tinterp[η] int)`

→ `(λ x:string. λ y:string. "(" + x + "*" + y + ")")  
 "int" "int"`

→ `"(" + "int" + "*" + "int" + ")"`

→ `"(int*int)"`

# Example

`serializeType[τ] = tinterp [η] τ`

where  $\eta = \{$

`int`     ) `“int”`

`string` ) `“string”`

`'`       ) `λ x:string. λ y:string.`  
          `“(" + x + “*” + y + “)”`

`→`      ) `λ x:string. λ y:string.`  
          `“(" + x + “->” + y + “)”`

`8`      ) `λ x:string→string.`  
          `let v = gensym () in`  
          `“(all ” + v + “.” + (x v) + “)”`

`}`

# Not the whole story

- More complicated examples require a generalization of this framework.
  - Must allow the type of each mapping in the environment to depend on the analyzed type.
  - Requires maintenance of additional type substitutions to do so in a type-safe way.
  - This language is type sound.
- Details appear in:

Stephanie Weirich. Higher-Order Intensional Type Analysis. In *European Symposium on Programming (ESOP '02)*.

# Conclusion

- Reflection is analyzing the structure of abstract types.
- Branching on type structure doesn't scale well to sophisticated and expressive type systems.
- A better solution is to interpret the compile-time language at run-time.

# Future work

- Type-based reflection
  - Reconciliation of structural and name-based analysis.
- Multi-level programming
  - Extensible programming languages.
  - Domain-specific languages.
- Program verification
  - Sophisticated type systems allow the representation and verification of many program properties.

